

#### A General-Purpose Multi-body, Multi-spacecraft Simulation

Eric Stoneking 2014

#### What kind of a name is 42?

- 42 is a tongue-in-cheek reference to the "answer to Life, the Universe, and Everything", as proclaimed by Douglas Adams in his Hitchhiker's Guide to the Galaxy stories
  - The first book is spent seeking this answer, which had taken a special computer and millions of years to compute. But by the time they had it, nobody knew what the question was anymore.
  - The next two books are spent seeking the question, which turns out to be: "What do you get when you multiply six by nine?"
- The reader may draw a number of lessons from this story...

## So what is it really?

- A simulation of spacecraft attitude and orbital dynamics and control
- Intended for use from concept studies through ops
  - Rapid prototyping makes it useful for MDL studies
  - Environment models support actuator sizing, performance studies
  - High-fidelity dynamics handle multi-body, flexible-body spacecraft
  - Portability (Mac, linux, Windows) minimizes infrastructure requirements
  - Clean interface aids progression from flight software "model" to dropping in actual flight software
  - Visualization aids situational awareness from concept to operations
- Designed to be powerful, but easy to get started

#### **Offshoots**

- 42 is the rootstock. Copies are spawned, evolve to suit the needs of a project
  - GLAST: GncSim (FSW Validation), GlastCam (Visualization)
  - MMS: 42 (Boom/Spin/Thruster Dynamics)
  - LRO: LroCam (Visualization)
  - LDCM: LDCM-Cam (Visualization)
  - SSMO: SatCam, SSUP (Visualization)
  - Scott Starin's Heliophysics thing (Formation Flying)
  - FACET (Formation Flying)
  - WFIRST: WiFi (Flexible Modes, Slew Control)
  - LADEE: 42 (Actuator Sizing)
  - OSIRIS-REX: 42 (Touch-and-Go Maneuver Independent Sim)
  - MDL Studies: 42 (Actuator Sizing, Visualization)

#### **Features**

- Multiple spacecraft, anywhere in the solar system
  - Two-body, three-body orbit dynamics (with seamless transition between)
  - One sun, nine planets, 45 major moons
  - Minor bodies (comets and asteroids) added as needed
    - RQ36, Eros, Itokawa, Wirtanen, etc
- Multi-body spacecraft
  - Tree topology
  - Kane's dynamics formulation
  - Each body may be rigid or flexible
  - Flexible parameters taken (by m-file script) from Nastran output (.f06 file)
  - Joints may have any combination of rotational and translational degrees of freedom

#### **More Features**

- Supports precision formation flying
  - Several S/C may be tied to a common reference orbit
    - Used by FACET, Stellar Imager studies
  - Encke's method or Euler-Hill equations used to propagate relative orbit states
    - Precision maintained by judicious partitioning of dynamics
      - Add big things to big things, small things to small things
- Clean FSW interface facilitates FSW validation
  - Used by GLAST project for independent validation of vendor's (autocoded) GNC flight software

# 42 Software Overview Architecture, Interfaces with Matlab

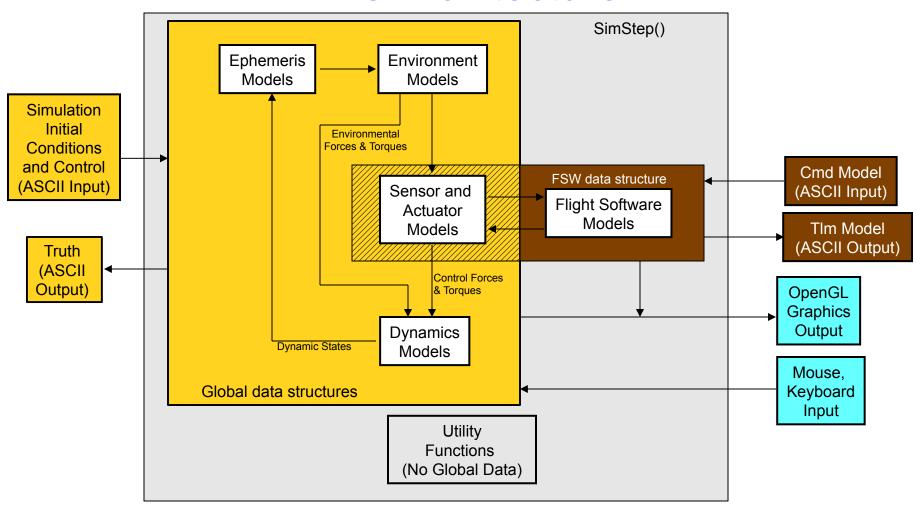
## 42 is Written in C for Speed, Portability

- The C language has a well-deserved reputation for giving you enough rope to hang yourself. Like any sharp tool, some care in handling is needed.
- If it weren't fast, powerful, portable, ubiquitous, and free, we wouldn't put up with it.
- The good news is, you can get a quick prototype running in 42 with zero C coding
  - Use "prototype FSW", command script
- The next steps are to add your own sensor, FSW, and actuator models
  - Simple existing models show where to insert yours
  - Global data structures make needed signals easy to find
  - Choose your level of fidelity and difficulty: n00b -> l33t
- You can get into the guts of the environment and dynamics if you want to, but you probably won't ever need to

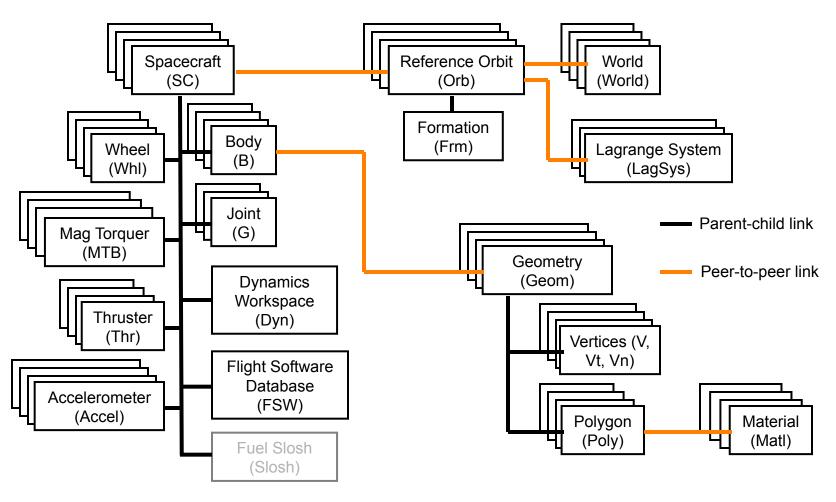
## **Command Script**

- The command script allows changing configuration (sim, FSW, or GUI) in the course of a sim run, from an ASCII input file.
- Good for rapid prototyping
- Inject sensor or actuator failures
- Model ground commands
- Script graphics for movie generation

#### 42's Architecture



#### Global Data Structure Relationships



## The Three Layers of Code

- 42 uses three "layers" of code:
  - Low-level toolkit functions:
    - Everything comes in and goes out through arguments and return value
    - No global variables
    - Segregated into \*kit.c files (mathkit.c, dcmkit.c, etc)
  - Top-level frame outline:
    - Follows outline, does minimal math/logic itself
    - Access to all global variables
  - Mid-level workhorse functions
    - Most likely to be tailored to a particular need
    - Access to global variables

## Toolkit Code Example

## Top-level Code Example

```
ReportProgress();
ManageFlags();
/* Read and Interpret Command Script File */
CmdInterpreter();
/* Update Dynamics to next Timestep */
for(Isc=0;Isc<Nsc;Isc++) {</pre>
   if (SC[Isc].Exists) Dynamics(&SC[Isc]);
OrbitMotion():
SimComplete = AdvanceTime();
/* Update SC Bounding Boxes occasionally */
ManageBoundingBoxes():
Ephemerides(); /* Sun, Moon, Planets, Spacecraft, Useful Auxiliary Frames */
for(Isc=0;Isc<Nsc;Isc++) {</pre>
   S = \&SC[Isc];
   if (S->Exists) {
      Environment(S); /* Magnetic Field, Atmospheric Density */
      Perturbations(S); /* Environmental Forces and Torques */
      Sensors(S);
      FlightSoftWare(S);
      Actuators(S);
      PartitionForces(S): /* Orbit-affecting and "internal" */
  }
Report(); /* File Output */
```

## Mid-level Code Example

```
/* Find Attitude Command */
FindCLN(FSW->PosN,FSW->VelN,CRN,wln);
C2Q(CRN,qrn);
MxV(CRN,FSW->svn,svr);
/* Form Error Signals */
QxQT(FSW->qbn,qrn,qbr);
RECTIFYQ(qbr);
/* PD Control */
for(i=0;i<3;i++) {
   FSW->Tcmd[i] = -FSW->Kr[i]*FSW->wbn[i]-FSW->Kp[i]*(2.0*qbr[i]);
   FSW->Twhlcmd[i] = -FSW->Tcmd[i];
/* Momentum Management */
for(i=0;i<3;i++) {
   Herr[i]=FSW->Hw[i]-FSW->Hwcmd[i];
VxV(Herr,FSW->bvb,HxB);
for(i=0;i<3;i++) FSW->Mmtbcmd[i] = FSW->Kunl*HxB[i];
```

#### Interfaces to Matlab

- 42 generates ASCII output files, which may be loaded into Matlab (or whatever) for post-processing and plotting
- Using Matlab's mcc utility, m-files may be translated into C, and compiled and linked into 42
  - As done by FACET

#### Matlab + 42 = Monte Carlo

- 42 can be called from within Matlab using the system command
- Use Matlab as the MC executive
  - Generate initial conditions, parameters
  - Write to 42's input files
  - Run 42
  - Process and save data
  - Repeat
- Use 42 as the high-speed, high-fidelity component

#### Matlab/42 Example

```
for Irun=1:Nrun,
   % Compute initial attitude
   CRN = TRIAD(tvn(Irun,:), svn, [0 0 1], [1 0 0]);
   qrn = C2Q(CRN);
   % Write target to file
   Outdata = [TrqRA(Irun) TrqDec(Irun)];
   save -ascii ./MOMBIAS/TargetRaDec.inp Outdata
   % Write initial attitude to file
   line = sprintf('%f %f %f %f ! Quaternion\n', qrn(1),qrn(2),qrn(3),qrn(4));
   OverwriteLineInFile('./MOMBIAS/GLAST.inp',21,line);
   % Run 42 for three days.
   system('./42 MOMBIAS');
   % Record pointing histogram.
   load ./MOMBIAS/AngleToGo.42
   [HistCount(Irun,:), HistAng(Irun,:)] = hist(AngleToGo, 20);
end
```

#### 42 Walkthrough Models, Terminology, Input Files

#### **Environment Models**

- Planetary Ephemerides
  - From Meeus, "Astronomical Algorithms"
  - Good enough for GNC validation, not intended for mission planning
    - Use GMAT or ODTBX for that
- Gravity Models have coefficients up to 18th order and degree
  - Earth: EGM96
  - Mars: GMM-2B
  - Luna: GLGM2
- Planetary Magnetic Field Models
  - IGRF up to 10th order (Earth only)
  - Tilted offset dipole field
- Earth Atmospheric Density Models
  - MSIS-86 (thanks to John Downing)
  - Jacchia-Roberts Atmospheric Density Model (NASA SP-8021)
- Simple exponential Mars atmosphere density model
  - New models easily incorporated as the state of the art advances

## **Dynamics Models**

- Full nonlinear "6DOF" (actually N-DOF) dynamics
- Attitude Dynamics
  - One or many bodies
    - Tree topology (no kinematic loops)
  - Each body may be rigid or flexible
  - Joints may combine rotational and translational DOFs
    - May be gimballed or spherical
  - Slosh may be modeled as a pendulum (lo-fi, quick to implement and run)
    - 42 may run concurrently with Star-CCM CFD software for hi-fi slosh
  - Wheels embedded in Body[0]
  - Torques from actuators, aerodynamic drag, gravity-gradient, solar radiation pressure, joint torques

#### Orbit Dynamics

- Two- or three-body orbits
- Encke or Euler-Hill (Clohessy-Wiltshire) for relative orbit motion (good for formation flying, prox ops)
- Forces from actuators, aerodynamic drag, non-spherical gravity, third-body gravity, solar radiation pressure

  42: A General-Purpose Multi-body.

Multi-spacecraft Simulation

## Reference Frames are Important!

- In any dynamics problem beyond the spinning top, a systematic approach to reference frames and the relationships between them is vital
- For 42, we define several fundamental reference frames, and notational conventions to keep quaternions and direction cosines sorted out

## Reference Frames (1 of 2)

- Heliocentric Ecliptic (H)
  - Planet positions expressed in this frame
- Each world has an inertial (N) and rotating (W) frame
  - For Earth, N = ECI (True of date), W = ECEF
  - N is the bedrock for orbits, S/C attitude dynamics
  - Full Disclosure: Although True-of-Date <-> J2000 conversions are provided, the distinction is not always rigorously made
    - Star vectors provided in J2000 (from Skymap), converted to H
    - Planet ephemerides are assumed given in true-of-date H
    - Transformation from N to W is simple rotation, implying N is True-of-Date

## Reference Frames (2 of 2)

- Each reference orbit has a reference point R
  - For two-body orbit, R moves on Keplerian orbit
  - For three-body orbit, R propagates under influence of both attracting centers (as point masses)
  - S/C orbit perturbations integrated with respect to R
- Associated with each R is a LVLH frame (L) and a formation frame (F)
  - F is useful for formation-flying scenarios
  - F may be offset from R, may be fixed in N or L
- Each spacecraft has one or more Body (B) frames and one LVLH frame (L)
  - L(3) points to nadir, L(2) points to negative orbit normal
  - SC.L is distinct from Orb.L, since SC may be offset from R

#### Notation for Quaternions, DCMs

 The rotation from frame A to frame B may be described by the direction cosine matrix

$$^{B}C_{ij}^{A}=\hat{b}_{i}\cdot\hat{a}_{j}$$

 Given the components of a vector in A, its components in B may be found by the multiplication

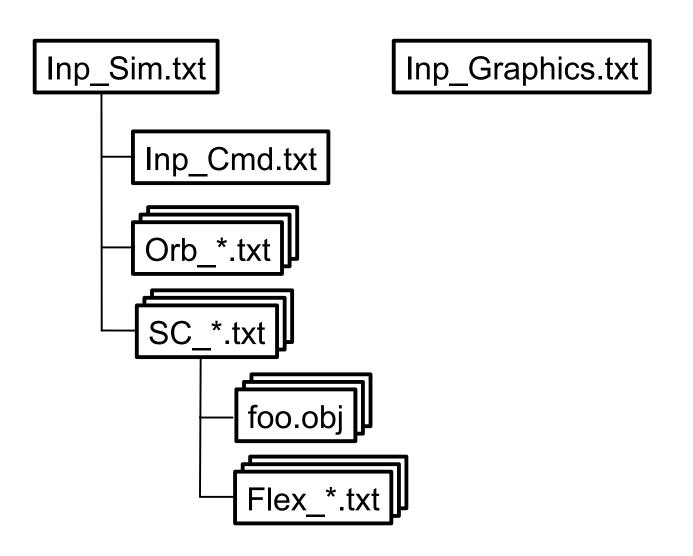
$$^{B}v=^{B}C^{AA}v$$

- In C, we write the DCM as CBA to preserve order of superscripts, eg
   MxV(CBA, va, vb)
- Quaternions are another way to describe rotations. We use a parallel notation:

These and similar conventions promote concise, unambiguous code

## Input File Overview

## Input File Hierarchy



## Top-level Input File (Slide 1 of 3)

```
FASTER THAN REAL
                           Time Mode (FASTER THAN REAL, REAL TIME,...)
20000.0
          0.1
                         ! Sim Duration, Step Size [sec]
10.0
                         ! File Output Interval [sec]
                         ! Graphics Front End?
TRUE
                         ! Command Script File Name
Inp Cmd.txt
******************* Reference Orbits *****************
                         ! Number of Reference Orbits
4
     Orb EOS.txt
                  ! Input file name for Orb 0
TRUE
                  ! Input file name for Orb 1
TRUE
     Orb ISS.txt
                  ! Input file name for Orb 2
TRUE
     Orb FGST.txt
                           Input file name for Orb 3
TRUE
     Orb Eros.txt
                        Spacecraft
                                ******
                           Number of Spacecraft
TRUE 0 SC LDCM.txt
                         ! Existence, RefOrb, Input file for SC 0
TRUE
   1 SC ISS.txt
                       ! Existence, RefOrb, Input file for SC 1
                     ! Existence, RefOrb, Input file for SC 2
TRUE
   1 SC Dragon.txt
TRUE 2 SC FGST.txt
                        ! Existence, RefOrb, Input file for SC 3
TRUE
   3 SC IonCruiser.txt
                         ! Existence, RefOrb, Input file for SC 4
```

## Top-level Input File (Slide 2 of 3)

```
****** Environment
                                         *********
06 28 2011
                               ! Date (Month, Day, Year)
16 45 00.00
                               ! Greenwich Mean Time (Hr, Min, Sec)
0.0
                                 Time Offset (sec)
USER DEFINED
                                 Solar Flux, AP values (TWOSIGMA KP, NOMINAL ...)
                                 If USER DEFINED, enter desired F10.7 value
230.0
                                 If USER DEFINED, enter desired AP value
100.0
                                 Magfield (NONE, DIPOLE, IGRF)
IGRF
                                IGRF Degree and Order (<=10)
                               ! Earth Gravity Model N and M (<=18)
                                 Mars Gravity Model N and M (<=18)
                                 Luna Gravity Model N and M (<=18)
                                Aerodynamic Forces & Torques
TRUE
                               ! Gravity Gradient Torques
FALSE
                                Solar Pressure Forces & Torques
FALSE
FALSE
                              ! Gravity Perturbation Forces
FALSE
                               ! Passive Joint Torques
FALSE
                               ! Thruster Plume Forces & Torques
                               ! Output Environmental Torques to Files
FALSE
```

## Top-level Input File (Slide 3 of 3)

```
*************** Celestial Bodies of Interest **************
TRUE
                              Mercury
TRUE
                              Venus
TRUE
                            ! Earth and Luna
TRUE
                            ! Mars and its moons
TRUE
                            ! Jupiter and its moons
TRUE
                            ! Saturn and its moons
TRUE
                            ! Uranus and its moons
TRUE
                            ! Neptune and its moons
TRUE
                            ! Pluto and its moons
TRUE
                            ! Asteroids and Comets
******* Lagrange Point Systems of Interest ************
                            ! Earth-Moon
FALSE
TRUE
                              Sun-Earth
FALSE
                              Sun-Jupiter
5
                                       ! Number of Ground Stations
TRUE EARTH -77.0 37.0
                      "GSFC"
                                       ! Exists, World, Lng, Lat, Label
TRUE EARTH -155.6 19.0 "South Point"
                                       ! Exists, World, Lng, Lat, Label
TRUE EARTH 115.4 -29.0 "Dongara"
                                       ! Exists, World, Lng, Lat, Label
TRUE EARTH -71.0 -33.0 "Santiago"
                                       ! Exists, World, Lng, Lat, Label
                      "Moon Base Alpha" ! Exists, World, Lng, Lat, Label
TRUE LUNA 45.0 45.0
```

## Reference Orbit Definition (1 of 2)

```
<><<<< > 42: Orbit Description File
                                         >>>>>>>>>>
Low Earth Orbit
                         Description
CENTRAL WORLD
                         Orbit Type (CENTRAL, THREE BODY), Center Type (WORLD, MINORBODY)
Orbit Center
EARTH
                         Use Keplerian elements (KEP) or (RV)
KEP
                         Use Peri/Apoapsis (PA) or min alt/ecc (AE)
PA
                       ! Periapsis & Apoapsis Altitude, km
400.0
      400.0
200.0 2.0
                       ! Min Altitude (km), Eccentricity
0.0
                       ! Inclination (deg)
0.0
                       ! Right Ascension of Ascending Node (deg)
0.0
                       ! Argument of Periapsis (deg)
180.0
                         True Anomaly (deg)
                       ! RV Initial Position (km)
0.0 0.0 0.0
0.0 0.0 0.0
                         RV Initial Velocity (km/sec)
```

## Reference Orbit Definition (2 of 2)

```
SUNEARTH
                           ! Lagrange system
LAGDOF MODES
                              Propagate using LAGDOF MODES or LAGDOF COWELL
                              Initialize with MODES or XYZ
MODES
L2
                             Libration point (L1, L2, L3, L4, L5)
                              XY Semi-major axis, km
800000.0
                              Initial XY Phase, deg
45.0
                              Sense (CW, CCW), viewed from +Z
CW
0.0
                              Second XY Mode Semi-major Axis, km (L4, L5 only)
                              Second XY Mode Initial Phase, deg (L4, L5 only)
0.0
CW
                              Sense (CW, CCW), viewed from +Z (L4, L5 only)
                              Z Semi-axis, km
400000.0
60.0
                              Initial Z Phase, deg
1.05 0.5 0.0
                              Initial X, Y, Z (Non-dimensional)
                              Initial Xdot, Ydot, Zdot (Non-dimensional)
0.0 0.0 0.0
*************** Formation Frame Parameters ******************
                              Formation Frame Fixed in [NL]
L
0.0 0.0 0.0 123
                           ! Euler Angles (deg) and Sequence
                           ! Formation Origin expressed in [NL]
Т.
0.0 0.0 0.0
                           ! Formation Origin wrt Ref Orbit (m)
```

#### Example Spacecraft Input File (1 of 4)

```
<><<<<<< >42: Spacecraft Description File
                                          >>>>>>>>>>
SpaceX Dragon
                        ! Description
"Dragon"
                        ! Label
GenScSpriteAlpha.ppm
                        ! Sprite File Name
PROTOTYPE FSW
                        ! Flight Software Identifier
! Orbit Prop FIXED, EULER HILL, or ENCKE
ENCKE
                        ! Pos of CM or ORIGIN, wrt F
CM
-200.0 0.0 100.0
                        ! Pos wrt Formation (m), expressed in F
0.0 0.0 0.0
                        ! Vel wrt Formation (m/s), expressed in F
NAN
                        ! Ang Vel wrt [NL], Att [QA] wrt [NLF]
0.01
    0.02
                        ! Ang Vel (deg/sec)
            0.03
0.0
     0.0
           0.0
                        ! Quaternion
                1.0
     0.0
           0.0
                        ! Angles (deg) & Euler Sequence
0.0
                123
*******
                       ! Rotation STEADY, KIN JOINT, or DYN JOINT
DYN JOINT
TRUE
                        ! Assume constant mass properties
FALSE
                        ! Passive Joint Forces and Torques Enabled
FALSE
                        ! Compute Constraint Forces and Torques
                        ! Mass Props referenced to REFPT CM or REFPT JOINT
REFPT CM
                        ! Flex Active
FALSE
FALSE
                        ! Include 2nd Order Flex Terms
2.0
                        ! Drag Coefficient
```

## Example Spacecraft Input File (2 of 4)

```
**************************
! Number of Bodies
200.0
                 ! Mass
100.0 200.0 300.0
                 ! Moments of Inertia (kg-m^2)
0.0 0.0 0.0
                 ! Products of Inertia (xy,xz,yz)
0.0 0.0 0.0
                 ! Location of mass center, m
IonCruiser.obj
                 ! Geometry Input File Name
                 ! Flex File Name
NONE
```

#### Example Spacecraft Input File (3 of 4)

```
*****************************
*************************
       (Number of Joints is Number of Bodies minus one)
! Inner, outer body indices
0 1
   213
                       ! RotDOF, Seq, GIMBAL or SPHERICAL
       GIMBAL
   123
                       ! TrnDOF, Seq
FALSE FALSE FALSE
                       ! RotDOF Locked
                       ! TrnDOF Locked
FALSE FALSE FALSE
0.0
     0.0
          0.0
                       ! Initial Angles [deg]
     0.0
                       ! Initial Rates, deg/sec
0.0
           0.0
0.0
     0.0
          0.0
                       ! Initial Displacements [m]
                       ! Initial Displacement Rates, m/sec
0.0
     0.0
           0.0
                       ! Bi to Gi Static Angles [deg] & Seg
0.0
    0.0 0.0 312
    0.0 0.0 312
                       ! Go to Bo Static Angles [deg] & Seq
0.0
    0.0 0.0
                       ! Position wrt inner body origin, m
0.0
0.0
    0.0 0.0
                       ! Position wrt outer body origin, m
0.0
    0.0 0.0
                       ! Rot Passive Spring Coefficients (Nm/rad)
                       ! Rot Passive Damping Coefficients (Nms/rad)
0.0
    0.0 0.0
                       ! Trn Passive Spring Coefficients (N/m)
0.0
    0.0 0.0
0.0
    0.0 0.0
                       ! Trn Passive Damping Coefficients (Ns/m)
```

#### Example Spacecraft Input File (4 of 4)

```
************************ Wheel Parameters *******************
                     ! Number of wheels
0.0
                     ! Initial Momentum, N-m-sec
1.0 0.0 0.0
                    ! Wheel Axis Components, [X, Y, Z]
                     ! Max Torque (N-m), Momentum (N-m-sec)
0.14 50.0
0.012
                     ! Wheel Rotor Inertia, kq-m^2
! Number of MTBs
----- MTB 0 -----
180.0
                     ! Saturation (A-m^2)
1.0 0.0 0.0
                     ! MTB Axis Components, [X, Y, Z]
************************* Thruster Parameters *******************
                     ! Number of Thrusters
----- Thr O ------
                    ! Thrust Force (N)
1.0
-1.0 0.0 0.0
                    ! Thrust Axis
1.0 1.0 1.0
                    ! Location in BO, m
************************** CMG Parameters *********************
                     ! Number of CMGs
! CMG DOF (typically 1 or 2)
                 ! Initial Gimbal Angles [deg] and Seg
0.0 0.0 0.0 123
0.0 0.0 0.0
                    ! Initial Gimbal Angle Rates, deg/sec
-90.0 0.0 -54.74 123 ! Static Mounting Angles [deg] and Seg
0.12
                    ! Rotor Inertia, kg-m^2
75.0
                     ! Momentum, Nms
1.0 0.0 0.0
                     ! Max Gimbal Angle Rates, deg/sec
```

#### **Geometry Definition**

- Geometry uses Wavefront "Object" format
  - ASCII, human-readable
  - Can hand-generate models in theory
  - In practice, you'll want mechanical help
- I use Wings3D solid modeling software
  - Free, multi-platform
- 42 can support myriad-polygon models, limited mainly by your patience
  - I get impatient at about 10,000 polys
- Note that aerodynamic and solar-pressure force and torque computations use these models
  - Interior polygons, self-shadowing are error sources

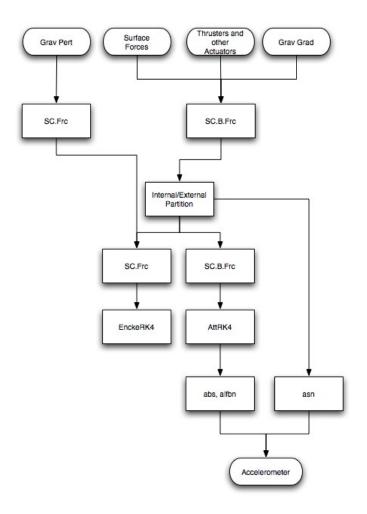
```
# Exported from Wings 3D 0.99.00b
mtllib Altair.mtl
o cylinder9
#12 vertices, 8 faces
v 2.11050391 1.21850000 -1.80666667
v 2.11050391 -1.21850000 -1.80666667
[...]
vn 0.0000000e+0 9.1113913e-17 1.00000000
vn 0.50000000 0.86602540 0.0000000e+0
[...]
g cylinder9_SHINY_WHITE
usemtl SHINY_WHITE
f 1//1 6//16 5//13 4//10 3//7 2//4
f 1//2 7//20 12//35 6//17
[...]
```

Excerpt from Altair.obj

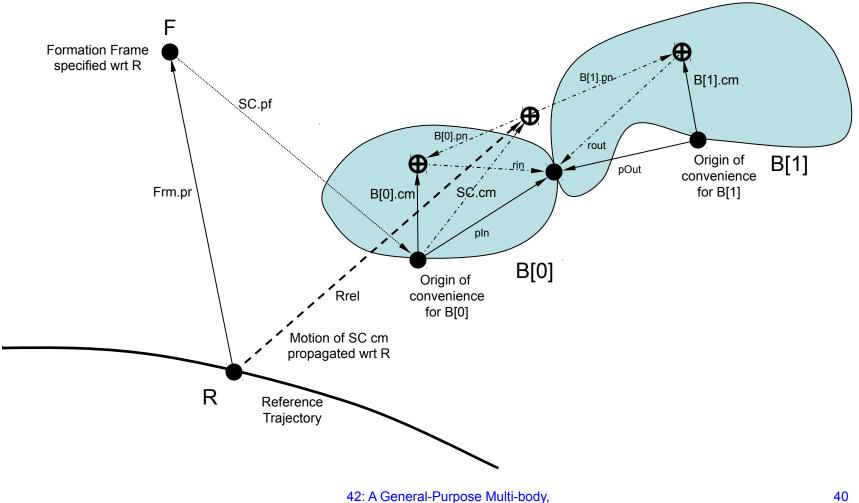
## Reference Slides

#### Force Flow

- Careful accounting needed to decouple orbit and attitude equations of motion
- Accelerometer model also requires careful accounting



## **Bookkeeping of Translational States**



Multi-spacecraft Simulation

## Geometry for Surface Forces

