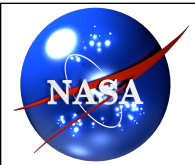


SDP Modal Identification

- Using the methods of Lai and Bhavnani (1975) an analytic estimate of the system modes for a spacecraft consisting of a base-body and four radial (symmetrically deployed) booms.
- McGee, Shankar, and Kemp, "Analysis of Spinning Spacecraft with Wire Booms Part 2: Out of Plane Dynamics and Maneuvers", AIAA 2009



SDP Modal Identification

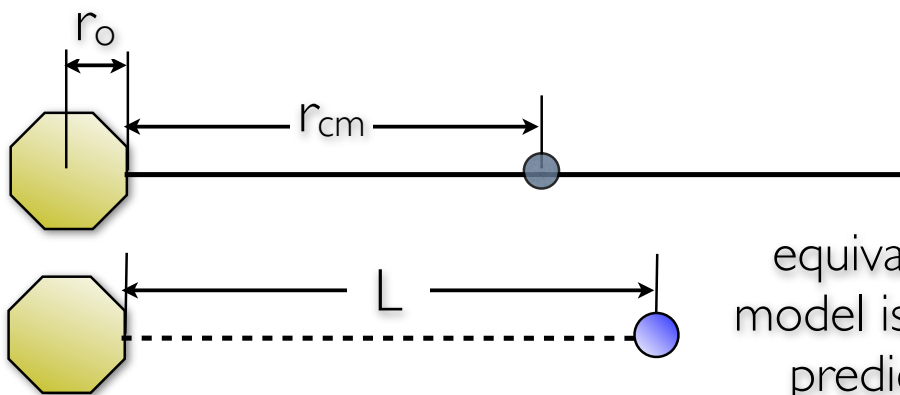
Pure Uncoupled “Crab” Mode

$$\omega_4 = \omega_s \sqrt{\frac{r_o}{L}}$$

r_o is the radius to boom attach point

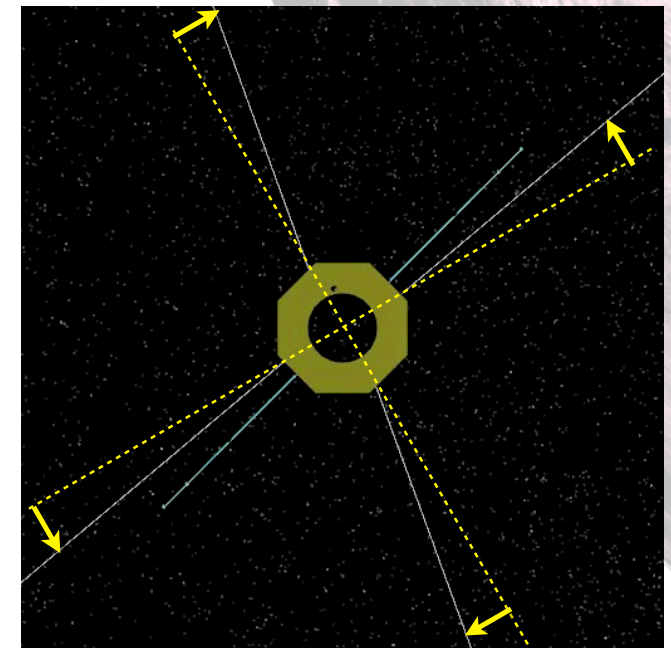
L is the “effective” length of the boom

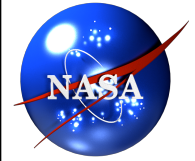
$$L = \sqrt{\frac{I_{cm} + mr_{cm}^2}{m}} = 42.875 \text{ kg-m}^2$$



equivalent point mass
model is used for analytic
prediction (not sim)

Spin Plane Motion





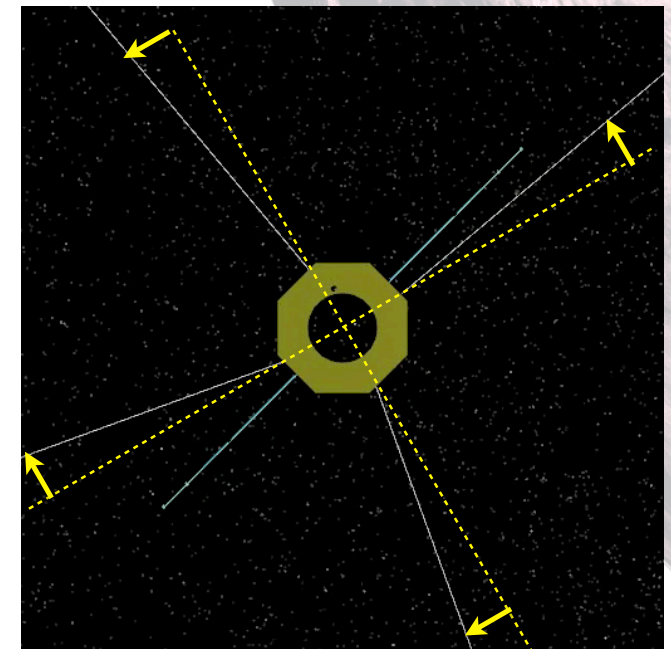
SDP Modal Identification

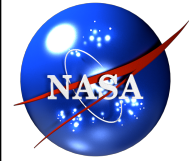
Uncoupled “Flex” Mode with Translation

$$\omega_{5,6} \simeq \omega_s \sqrt{\frac{r_o}{L} \left(1 + \frac{m}{M} \cdot \frac{L + r_o}{r_o} \right)}$$

r_o is the radius to boom attach point
 L is the “effective” length of the boom
 m is the mass of the boom
 M is the mass of the base body
 ω_s is the spin rate

Spin Plane Motion





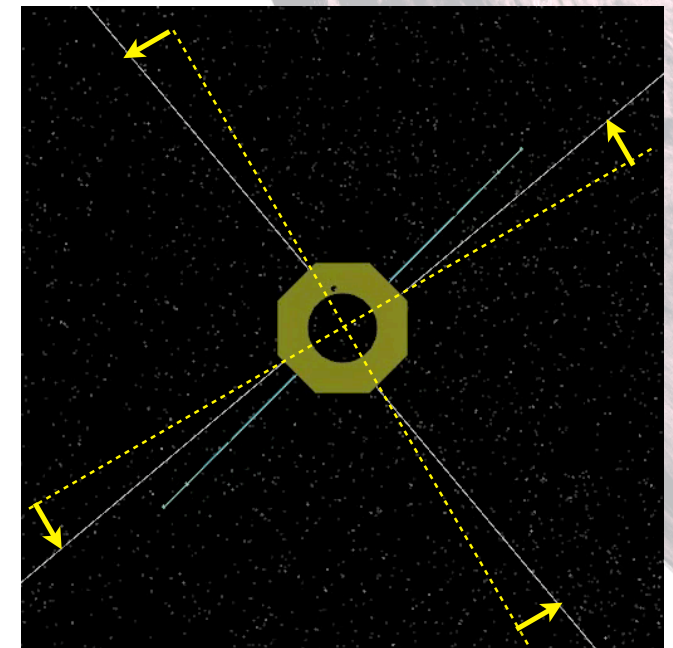
SDP Modal Identification

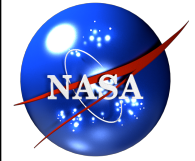
Coupled “Twist” Mode

$$\omega_7 = \omega_s \sqrt{\frac{r_o}{L} \cdot \frac{I_s + 4m(r_o + L)^2}{I_s}}$$

r_o is the radius to boom attach point
 L is the “effective” length of the boom
 I_s is the spin-axis inertia of the base
 m is the mass of the boom
 ω_s is the spin rate

Spin Plane Motion





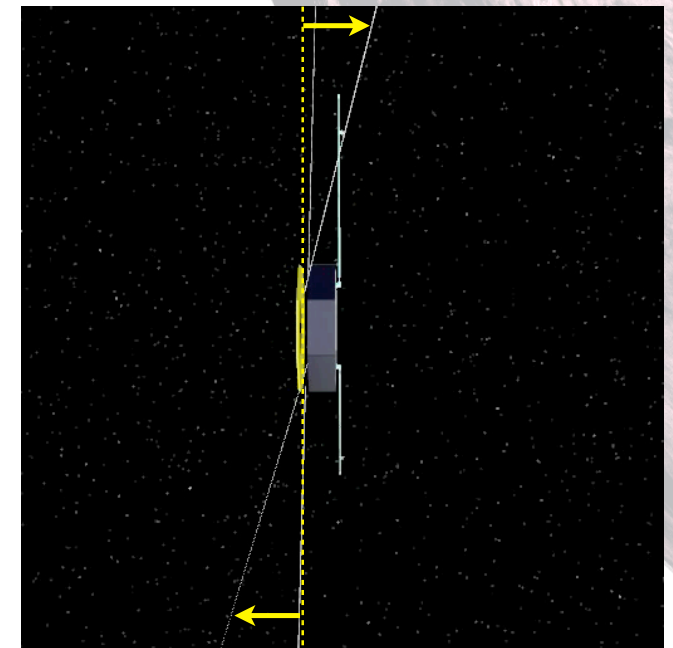
SDP Modal Identification

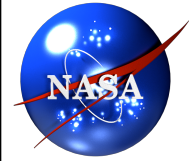
Coupled “Twist” Mode

Out-of-Plane Motion

$$\omega_{11,12} = \omega_s \sqrt{\frac{L + r_o}{L} \cdot \frac{I_t + 2m(r_o + L)^2}{I_t}}$$

r_o is the radius to boom attach point
 L is the “effective” length of the boom
 I_t is the transverse inertia of the base
 ω_s is the spin rate





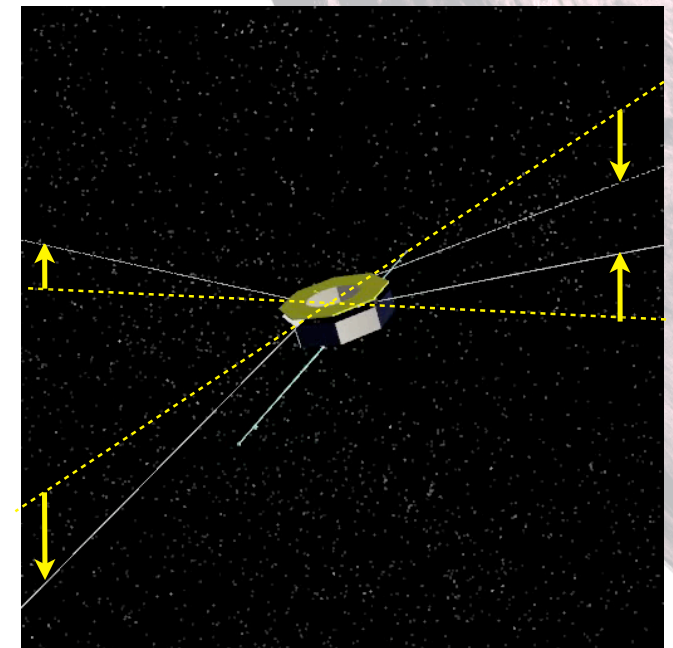
SDP Modal Identification

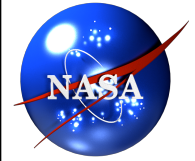
Coupled “Saddle” Mode

$$\omega_{13} = \omega_s \sqrt{\frac{L + r_o}{L}}$$

r_o is the radius to boom attach point
 L is the “effective” length of the boom
 ω_s is the spin rate

Out-of-Plane Motion





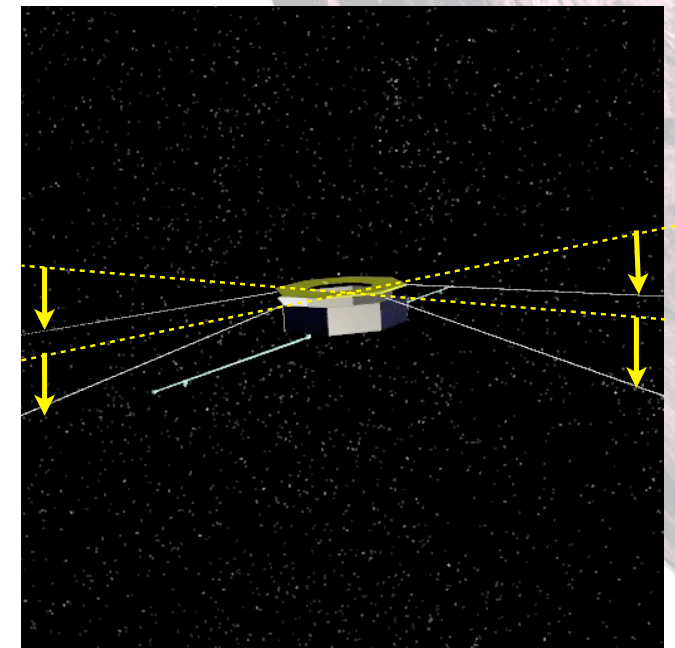
SDP Modal Identification

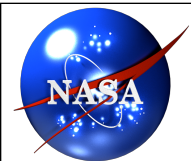
Coupled “Jellyfish” Mode

$$\omega_{14} = \omega_s \sqrt{\frac{L + r_o}{L} \frac{M + 4m}{M}}$$

r_o is the radius to boom attach point
 L is the “effective” length of the boom
 m is the mass of the boom
 M is the mass of the base body
 ω_s is the spin rate

Out-of-Plane Motion





SDP Modal Identification

Frequency Summary

for Fully Deployed Configuration

| Mode Designations | | | Predicted* | | Simulated* | | Error |
|---|------------|----------------------|------------|--------|------------|--------|-------|
| Name | Spin Plane | Id | Hz | sec | Hz | sec | % |
| Uncoupled (Crab) | In | ω_4 | 0.00983 | 101.73 | 0.00995 | 100.50 | 1.21 |
| Uncoupled + Translation (Flex) | In | ω_5, ω_6 | 0.00996 | 100.40 | 0.01007 | 99.30 | 1.09 |
| Coupled (Twist) | In | ω_7 | 0.01787 | 55.96 | 0.01813 | 55.16 | 1.43 |
| Uncoupled (Saddle) | Out | ω_{13} | 0.05096 | 19.62 | 0.05096 | 19.62 | 0.00 |
| Jellyfish | Out | ω_{14} | 0.05100 | 19.61 | 0.05103 | 19.60 | 0.06 |
| Mutual Precession | Shape | - | 0.05237 | 19.09 | 0.05103 | 19.60 | 2.63 |
| Boom Nutation | Shape | - | 0.05066 | 19.74 | 0.05103 | 19.60 | 0.73 |
| Hub Nutation | Shape | - | 0.02202 | 45.41 | 0.01990 | 50.25 | 10.65 |
| * Base-body includes Mag Boom+ADP+Fuel (40% fill) rigid approximation | | | | | | | |