

Computational Physics - WS 2015/16  
Lecture on 18th Nov 2015

# Homework #3 - sample solution

## Statistics, random numbers, references

```
#include <iostream>
#include <cstdlib>
```

```
using namespace std;
```

```
void randomize(double* const, const int);
void stat(double&, double&, const double* const, const int);
```

```
int main(void){
```

```
    double mean = 0,    var = 0;
    int      N     = 100;
    double p[N];
```

```
    randomize(p, N);
    stat(mean, var, p, N);
```

```
    cout << "Mean value : " << mean << endl;
    cout << "Variance   : " << var  << endl;
```

```
    return 0;
```

```
}
```

```
void randomize(double* const p, const int N){
```

```
    for(int i = 0; i < N; i++)
        p[i] = double(rand()) / RAND_MAX;
```

```
}
```

```
void stat(double& mean, double& var, const double* const p, const
int N){
```

```
    for(int i = 0; i < N; i++)
        mean += p[i];
    mean /= N;
```

```
    for(int i = 0; i < N; i++)
        var += (p[i]-mean)*(p[i]-mean);
    var /= N;
```

```
}
```

```
#include <ctime>
```

sometimes not necessary to  
include, depends on compiler

```
srand(time(NULL));
```

Output:

```
Mean value : 0.549589
Variance   : 0.0850506
```

## const

- We often have variables which store a value that should never change. These values can be protected from change using the const statement

```
double area(const double r, const double PI){  
    return r*r*PI;  
}  
  
int main(){  
    const double PI = 3.14159265;  
    const double PI2 = 2*PI;  
    double r;  
  
    cout << "r = "; cin >> r;  
    const double u = PI2*r;  
  
    cout << "circumference = " << u << ",\t area = " << area(r,PI) << endl;  
}
```

- Use const wherever possible to minimize the risk of changing a variable unintentionally
- Const also allows the compiler to optimize code generation

## const

- Using const together with pointers we have to distinguish two cases:
  - ▶ The pointer points to a variable which is constant,
  - ▶ The pointer itself is constant and can not be altered, it always points to the same place, but the value at this place may change
- A `const double*` is a pointer which always points to a `const double`
- A `double* const` is a pointer which points to always the same double, but the value of the double may be altered
- It is possible to combine both to `const double* const`, which is a constant pointer that always points to the same constant double...

## const

```
void f(const double* x, double* const y){  
    // *x = 1; // error: assignment of read-only location  
    *y = 3;  
  
    const double q = 2;  
    x = &q;  
  
    double g=2;  
    // y = &g; // error: assignment of read-only parameter 'y'  
}  
  
int main(){  
    const double pi = 3.141;  
    const double e = 2.714;  
    double d=2;  
  
    // double* p = &pi; // invalid conversion from 'const double*' to 'double*'  
  
    const double* pp = &pi;  
    // *pp = 1; // error: assignment of read-only location  
  
    f(pp, &d);  
  
    const double* const ppp = &pi;  
    // ppp = &e; // assignment of read-only variable 'ppp'  
}
```

## Dynamic arrays

- Often we need arrays for which the size is only known at runtime, then we need to dynamically reserve memory to store the array.
- To obtain a chunk of memory of the correct size, we need the new command
- `new double[n]` will return a double pointer to a chunk of memory large enough to hold n doubles

```
#include <iostream>

using namespace std;

int main(){
    const int N = 10;
    double p[N]; //static allocation,
                //size known in advance

    int n;
    cout << "n = "; cin >> n;

    double* pn = new double[n]; //dynamic allocation

    for(int i=0; i<n; i++) pn[i] = 0;

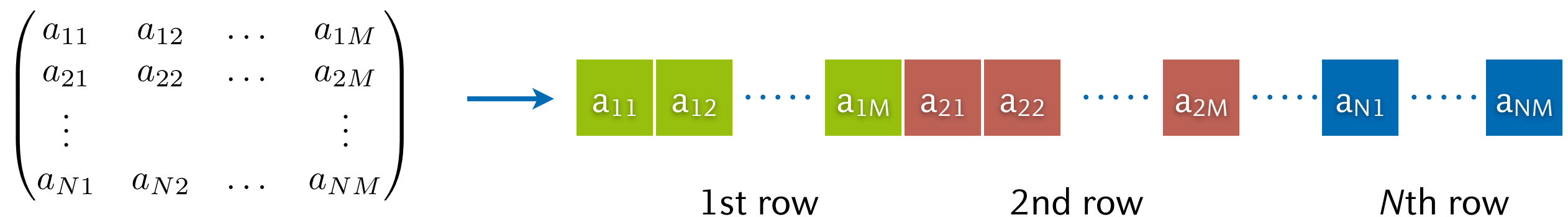
    delete[] pn; //free up memory
}
```

## Dynamic arrays

- For every new statement we need the according delete statement
- If we reserve memory just for a single variable  
`double* d = new double;`  
we only need to free this single memory slot via  
`delete d;`
- When we reserve memory for an array of data  
`double *d = new double[n];`  
we need to free the whole memory block via  
`delete d[];`
- When you forget to free memory again, this may lead to a crash of your program
- Always check programs for memory leaks (e.g. using Valgrind) and take memory leaks seriously!

## Multi-dimensional arrays

- Static allocation is easy:  
`double p[100][20];`  
`p[99][19] = 10;`
- When we pass a multi-dimensional, statically allocated array to a function we have to write the size of all dimensions but the first into the function header:  
`void f(double p[][20]);`
- How is the data stored in memory?
  - ▶ C++ uses row-major format (Fortran column-major!)





## Multi-dimensional arrays

- For us the more interesting case is a dynamically allocated multi-dimensional array.  
**There is no such thing in C++.**
- We could mimic the syntax `a[i][j]` for dynamic allocation of memory for a  $N \times M$  matrix by dynamically allocating memory for  $N$  double pointers. Each double pointer would then be assigned via `new` to a 1D double array of length  $M$ .
  - ▶ This provides intuitive indexing, but we can not guarantee all double arrays to lie in a contiguous memory block  $\Rightarrow$  this is bad for performance
- We need to map a 2D array onto a 1D array on our own
- Assume we want to store a Matrix of  $N_y \times N_x$  double values.
  - ▶ Allocate an array of length  $N = N_y * N_x$
  - ▶ Entry  $(i,j)$  of the Matrix is located at index  $k = (i-1)*N_x + j - 1$  of the array  
(assuming all entries in one row of the matrix are stored sequentially - row-major order)
- Writing code that makes extensive use of Matrices becomes very cumbersome this way...  
We will need a much easier way to access these entries.

## Multi-dimensional arrays

```
#include <iostream>

using namespace std;

int idx(const int, const int, const int, const int);

int main(void){
    int N, M, n, m;
    double* p;

    cout << "Enter matrix dim N (#columns)" << endl;
    cin >> N;
    cout << "Enter matrix dim M (#rows)" << endl;
    cin >> M;

    p = new double[N*M]; // allocate memory

    cout << "which idx should be set to 5?" << endl;
    cin >> n;
    cin >> m;

    p[idx(n,m,N,M)] = 5.0;

    cout << "p(" << n << ", " << m << ") = " << p[idx(n,m,N,M)] << endl;

    delete[] p; // free memory
    return 0;
}

int idx(const int n, const int m, const int N, const int M){
    if ((n-1 < N) && (m-1 < M) && (n > 0) && (m > 0)) // control validity
        return (n-1)+(m-1)*N;
    else
        cout << "Error! n = " << n << ", m = " << m << " is not valid" << endl;
        exit(1); // end program if not valid
}
```

In this example we have  
column-major (free choice!)  
and indices start at (1,1) and  
end at (N,M)

## Strings

- Sometimes we want to give a string to a function in order to specify e.g. the filename

```
#include <iostream>
#include <string>
#include <fstream>

using namespace std;

void print_f(string);    // print-to-file function
void print_c(string);    // print-to-console function

int main(void){

    string word = "placeholder";

    print_f(word);
    print_c(word);

    return 0;
}

void print_f(string word){
    ofstream out(word.c_str());    // attention: out needs a char pointer
    out << "word of the day is " << word << endl;
    out.close();
}

void print_c(string word){
    cout << "word of the day is " << word << endl;
    cout << "word of the day is " << word.c_str() << endl; // cout can handle both
}
```

Output:

word of the day is placeholder  
word of the day is placeholder  
+ the file „placeholder“ which includes  
word of the day is placeholder

## Stringstreams

- Sometimes we want to append characters to a preexisting string, e.g. for labeling multiple output files

```
#include <string>
#include <fstream>
#include <sstream>

using namespace std;

void print_f(string);

int main(void){

    int N = 5;
    string word = "placeholder";
    stringstream s;
    for (int i = 0; i < N; i++){
        s.str("");
        s << word << "_" << i << ".txt";
        print_f(s.str());
    }

    return 0;
}

void print_f(string word){
    ofstream out(word.c_str()); // make a char pointer out of the string
    out << "useful content" << endl;
    out.close();
}
```

Output:

the files „placeholder\_0.txt“  
„placeholder\_1.txt“  
„placeholder\_2.txt“  
„placeholder\_3.txt“  
„placeholder\_4.txt“  
including „useful content“

## Ifstreams

- reading data via input file stream object (*ifstream*)

output: p[0] = 0.245  
p[1] = 0.632  
p[2] = 0.123  
p[3] = 0.741  
p[4] = 0.953

Array contained in file „data“:

0.1	0.245
0.2	0.632
0.3	0.123
0.4	0.741
0.5	0.953

We want to store the second column into an array

```
#include <fstream>
#include <string>
#include <iostream>

using namespace std;

void reading(double* const, const int, const string);

int main(void){
    const int N = 5;
    const string filename = "data";
    double* p = new double[N];

    reading(p, N, filename);

    for (int i = 0; i < N; i++){
        cout << "p[" << i << "] = " << p[i] << endl;
    }

    delete[] p;

    return 0;
}

void reading(double* const p, const int N, const string fname){
    ifstream in(fname.c_str());    // create input file stream
    double temp;                  // temp variable
    for (int i = 0; i < N; i++){
        in >> temp;                // row major reading
        in >> p[i];                // every 2nd entry is what we store
    }
    in.close();                   // close input file stream
}
```

## Typedef

- Typedef allows us to introduce our own datatypes

```
#include <complex>
using namespace std;

typedef int* intp;
typedef complex<double> cmplx;

int main(void)
{
    int* nx,ny; //Only nx is a pointer,
               //ny is a regular int

    int *NX, *NY; //Both are pointers to int

    intp MX, MY; // Both are pointers to int

    cmplx c; // c is a double precision complex number

    cmplx* cp= new cmplx[*MX]; //cp is a pointer
                               //to an array of length
                               //*MX
}
```

## Structs

- Structs are data structures that are made up from several components. Each component may have another datatype.
- Example: When we study the motion of a particle due to some force, we will need the values  $v_x$ ,  $v_y$ ,  $v_z$ ,  $x$ ,  $y$ ,  $z$ . Maybe we will need additional values like mass  $m$ , charge  $q$ , ...
  - ▶ Structs allow to summarize these under the same name
- Structs are defined as

```
struct{  
    component1;  
    component2;  
};
```

  - ▶ Don't forget the finalizing semi-colon!
- Any datatype we know can become component of a struct

## Structs

- Once a struct is defined it can be used like any other datatype

```
#include <cmath>
#include <iostream>

using namespace std;

//-----
struct particle{
    int n;
    double x,y,z;
    double vx,vy,vz;
    double q,m;
};

//-----
//-----
int main(){
    particle p1;

    p1.x = 0.0; p1.y = 0.5; p1.z=0;
    p1.vx = 1.0; p1.vz = 0.2;
    p1.m = 1836; p1.q = -1;

    return 0;
}
```



## Accessing members via pointers to structs

- If we have a pointer to a struct, access to the struct members is provided only by the -> operator
- No explicit de-referencing is necessary

```
#include <iostream>
using namespace std;
//-----
struct particle{
    int n;
    double x,y,z;
    double vx,vy,vz;
    double q,m;
};
//-----
int main(){
    particle p1;
    particle* pp = &p1;

    p1.x = 0.0; p1.y = 0.5; p1.z=0;
    p1.vx = 1.0; p1.vz = 0.2;
    p1.m = 1836; p1.q = -1;

    // pp.x = 1; // Will not work since pp is a pointer
    pp->x = 1;
    pp->y = 1;

    cout << "x = " << p1.x << ",\t y =" << p1.y << endl;
    return 0;
}
```