

INF 551 – Spring 2018

Quiz 2: Storage systems (10 points), 10 minutes

Consider a hard drive with the following characteristics:

Number of cylinders	512
Number of heads	8
Number of sectors per track	256
Size of sector	4KB
Number of sectors per block	1
(Maximum) bandwidth	100MB/s
Rotational speed	7,200RPM
Maximum seek time	15ms

- a) [2 points] What is the capacity of the hard drive?

$$\begin{aligned} \text{Capacity} &= \# \text{cylinders} * \# \text{heads} * \# \text{sector per track} * \text{size of sector} \\ &= 512 * 8 * 256 * 4 \text{ KB} = 2^9 * 2^3 * 2^8 * 2^2 * 2^{10} \text{ Bytes} \\ &= 2^{32} \text{ Bytes} = 4 \text{ GB} \end{aligned}$$

- b) [4 points] How much does it take to access 100 blocks **randomly** located on the disk? What is the actual bandwidth for this workload?

Random access: For each block

$$T_{\text{seek}} = \text{Average seek time} = 1/3 * \text{Maximum seek time} = 5 \text{ ms}$$

$$\begin{aligned} T_{\text{rotation}} &= \frac{1}{2} \text{ rotation} * \text{Full rotation time} \\ &= \frac{1}{2} \text{ rotation} * (60000 \text{ ms per minute}) / (7200 \text{ Rotations per minute}) \\ &= \frac{1}{2} \text{ rotation} * 8.33 \text{ ms / rotation} \\ &= 4.17 \text{ ms} \end{aligned}$$

$$T_{\text{transfer}} = 4 \text{ KB} / (100 \text{ MB/s}) = 4 \text{ KB} / (100 \text{ KB/ms}) = 0.04 \text{ ms}$$

$$T = (T_{\text{seek}} + T_{\text{rotation}} + T_{\text{transfer}}) * \# \text{blocks} = 9.21 * 100 = 921 \text{ ms}$$

$$\begin{aligned} \text{Actual bandwidth} &= 100 \text{ blocks} * 4 \text{ KB/sector} * 1 \text{ sector/block} / 921 \text{ ms} \\ &= 400/921 \text{ KB/ms} = 0.43 \text{ KB/ms} = 0.43 \text{ MB/s} \end{aligned}$$

- c) [4 points] How much does it take to access 100 blocks **sequentially** located on the disk? What is the actual bandwidth for this workload?

Sequential access:

For the full process:

$$T_{\text{seek}} = 5 \text{ ms}$$

$$T_{\text{rotation}} = 4.17 \text{ ms}$$

For each block:

$$T_{\text{transfer}} = 0.04 \text{ ms}$$

$$\begin{aligned} T &= T_{\text{seek}} + T_{\text{rotation}} + T_{\text{transfer}} * \# \text{blocks} \\ &= 5 + 4.17 + 0.04 * 100 \\ &= 13.17 \text{ ms} \end{aligned}$$

$$\text{Actual bandwidth} = 400/13.17 \text{ KB/ms} = 30.37 \text{ KB/ms} = 30.37 \text{ MB/s}$$