BEARscc: Using spike-ins to assess single cell cluster robustness

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1 Introduction

1.1 Scope

Single-cell transcriptome sequencing data are subject to substantial technical variation and batch effects that can confound the classification of cellular sub-types. Unfortunately, current clustering algorithms do not account for this uncertainty. To address this shortcoming, we have developed a noise perturbation algorithm called **BEARscc** that is designed to determine the extent to which classifications by existing clustering algorithms are robust to observed technical variation.

BEARscc makes use of spike-in measurements to model technical variance as a function of gene expression and technical dropout effects on lowly expressed genes. In our benchmarks, we found that BEARscc accurately models read count fluctuations and drop-out effects across transcripts with diverse expression levels. Applying our approach to publicly available single-cell transcriptome data of mouse brain and intestine, we have demonstrated that BEARscc identified cells that cluster consistently, irrespective of technical variation. For more details, see the manuscript on bioRxiv.

1.2 Installation

It is our hope that BEARscc will shortly be available on Bioconductor. For now, installing BEARscc is easy. You can download a source package here. You can then use `install.packages`, but give it the location of the downloaded file:

```
install.packages('../inst/BEARscc_0.99.0.tar.gz', repos = NULL, type="source")
library("BEARscc")
```

1.3 Citation

BEARscc and its associated manuscript are currently under review for publication at a peer-reviewed journal. For now please cite the bioRxiv pre-print:

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2 Tutorial

2.1 Overview

BEARscc relies upon spike-in count measurements in single-cell transcriptome experiments to estimate experimental noise and produce simulated technical replicates to provide a quantitative understanding of the robustness of proposed single cell cluster labels to experimental noise. In principal, the algorithm is compatible with any clustering algorithm. The following should provide users with a comprehensive tutorial of the use and utlity of BEARscc as a tool for vetting single cell clusters with respect to experimental noise.

Before getting started, we need to sort some data and dependencies.

First, we are using the excellent `data.table` library here, which can be easily installed by typing:

```
install.packages('data.table')
```

Next, BEARscc is equipped with a set of sample data for the purpose of testing functions, examples in help files, and this nifty tutorial. We can load `data.table` and access the data provided with the package as follows:

```
library('data.table')
data("BEARscc_examples")
```

The loaded file `BEARscc_examples` is equipped with separate `data.frame` objects including ERCC spike-in observations (`ERCC.counts.df`), endogenous count observations (`data.counts.df`), and the expected or actual spike-in concentrations.

In the event we were working with a seperate set of data, the spike-in concentrations `data.frame` can be computed from the factory concentrations and the relevant dilution protocol utilized in the experiment. Counts tables would need to be mapped and counted with preferred software, and the spike-in control counts (ERCC or otherwise) would need to be seperated from the endogenous counts into two distinct `data.frame` objects.

For now we can have a look at the first few lines and columns of each of the loaded files:

```
head(ERCC.counts.df[,1:2])
#>           WTCHG_217386_229230 WTCHG_217386_249229
#> ERCC-00002                 629                 803
#> ERCC-00003                  13                  27
#> ERCC-00004                  61                  49
#> ERCC-00009                 183                 202
#> ERCC-00013                   0                   0
#> ERCC-00019                   0                   0

head(data.counts.df[,1:2])
#>                 WTCHG_217386_229230 WTCHG_217386_249229
#> ENSG00000000003                   0                   0
#> ENSG00000000419                   0                   0
#> ENSG00000000457                   0                   1
#> ENSG00000000460                   1                  37
#> ENSG00000000938                   0                   0
#> ENSG00000000971                   0                   0

head(ERCC.meta.df)
#>              Transcripts
#> ERCC-00002 3.011070e+02
#> ERCC-00003 1.881919e+01
#> ERCC-00004 1.505535e+02
#> ERCC-00009 1.881919e+01
```

```
#> ERCC-00012 2.297264e-03
#> ERCC-00013 1.837812e-02
```

2.2   Building the noise model

We will now estimate the single-cell noise present in the experiment using spike-in controls. In this tutorial, we rely upon a subsample of artificial control data found in `BEARscc_examples`; however, users are encouraged to work through the tutorial with their own single cell data provided some form of spike-ins were included in the experiment. Building the noise models with BEARscc is relatively straightforward with `estimate_noiseparameters()`. We simply provide the function with the previously discussed. spike-in (ERCCs here) known concentrations, endogenous count measurements, and spike-in counts measurement `data.frame` objects. Although `estimate_noiseparameters()` speed is invariant to data size, it does take a couple of minutes to estimate noise with a reasonably granular `alpha_granularity` parameter, so please be patient when running the following code.

```
results <- estimate_noiseparameters(ERCC.counts.df,
                                    data.counts.df,
                                    ERCC.meta.df,
                                    granularity=30,
                                    write.noise.model=FALSE,
                                    model_view=c("Observed","Optimized"))
#> [1] "Fitting parameter alpha to establish ERCC-derived noise model."
#> [1] "Estimating error for ERCCs with alpha = 0"
#> [1] "Estimating error for ERCCs with alpha = 0.05"
#> [1] "Estimating error for ERCCs with alpha = 0.1"
#> [1] "Estimating error for ERCCs with alpha = 0.2"
#> [1] "Estimating error for ERCCs with alpha = 0.25"
#> [1] "Estimating error for ERCCs with alpha = 0.35"
#> [1] "Estimating error for ERCCs with alpha = 0.4"
#> [1] "Estimating error for ERCCs with alpha = 0.45"
#> [1] "Estimating error for ERCCs with alpha = 0.5"
#> [1] "Estimating error for ERCCs with alpha = 0.55"
#> [1] "Estimating error for ERCCs with alpha = 0.65"
#> [1] "Estimating error for ERCCs with alpha = 0.7"
#> [1] "Estimating error for ERCCs with alpha = 0.75"
#> [1] "Estimating error for ERCCs with alpha = 0.8"
#> [1] "Estimating error for ERCCs with alpha = 0.9"
#> [1] "Estimating error for ERCCs with alpha = 0.95"
#> [1] "Estimating error for ERCCs with alpha = 1"
```

Several options exist for `estimate_noiseparameters()`.   These are fully documented in the help page `?estimate_noiseparameters`. Some of the more important options for the user are listed below

- 'granularity' determines the number of bins for comparison of the quality of fit between the mixed-model and observed data for each alpha. This should be set lower for small datasets and higher for datasets with more observations
- 'write.noise.model=TRUE' outputs two tab-delimited files containing the dropout effects and noise model parameters; this allows users to apply the noise generation on a seperate high compute node.
- 'plot=TRUE' will plot all linear fits and individual ERCCs distributions across samples
- 'file="./Rplot"' determines the root name for all plots, which write to the current working directory unless a path is contained in the root name.

2.3   Simulating technical replicates

Following estimation of noise, the parameters computed are then used to generate a simulate a technical replicate. Here we will simulate replicates on our local computer, but frequently users will want to utilize the methods described in Section 2.4.

```
    sim_replicates <- create_noiseinjected_counts(results, n=3)
#> [1] "Creating a noise-injected counts matrix: 1."
#> [1] "Creating a noise-injected counts matrix: 2."
#> [1] "Creating a noise-injected counts matrix: 3."
```

Recall that `results` is the list object we recently generated with the function `estimate_noiseparameters()` and note that the variable `n` is the desired number of simulated technical replicates. The resulting object is a list, where each element is a simulated technical replicate, and one element is the original counts matrix.

2.4   Simulation of replicates for larger datasets

For larger datasets it is recommended that the user set `write.noise.model=TRUE` and copy the written bayesian drop-out and noise estimate files with the observed counts table to a high performance computing environment. For example, we would run:

```
results <- estimate_noiseparameters(ERCC.counts.df,
                                    data.counts.df,
                                    ERCC.meta.df,
                                    granularity=30,
                                    write.noise.model=TRUE,
                                    file="noise_estimation",
                                    model_view=c("Observed","Optimized"))
```

Furthermore, the script `HPC_generate_noise_matrices` contains `create_noiseinjected_counts()` functions that are adapted to a parallel environment along with suggested code, which is commented out for user-modification. The script generates seperate noise-injected counts files, which can be loaded into R as a list or re-clustered seperately in a high performance compute environment.

2.5   Forming a noise consensus

After generating noise-injected counts tables, these should be re-clustered using the clustering method applied to the original dataset. For simplicity, here we use hierarchical clustering on a euclidean distance metric to identify two clusters. In our experience, some published clustering algorithms are sensitive to cell order, so we suggest scrambling the order of cells for each noise iteration as we do below in the function, `recluster()`.

To quickly recluster a list, we define a reclustering function:

```
recluster <- function(x) {
    x <- data.frame(x, row.names = "GENE_ID")
    scramble <- sample(colnames(x), size=length(colnames(x)), replace=FALSE)
    x <- x[,scramble]
    clust <- hclust(dist(t(x),method="euclidean"),method="complete")
    clust <- cutree(clust,2)
    data.frame(clust)
}
```

We then apply the function `recluster()` to all noise-injected counts matrices and the original counts matrix and manipulate the list into a `data.frame`.

```
cluster.list<-lapply(noisy_counts.list, `recluster`)
clusters.df<-do.call("cbind", cluster.list)
colnames(clusters.df)<-names(cluster.list)
```

If running clustering algorithms on a seperate high performance cluster, the user should retrieve labels and format as a `data.frame` of cluster labels, where the last column must be the original cluster labels derived from the observed count data. As an example, examine the file, example/example_clusters.tsv.

Using the cluster labels file as described above, we can generate a noise consensus matrix using:

```
noise_consensus <- compute_consensus(clusters.df)
```

Using the `aheatmap()` function in the `NMF` library, the consensus matrix result of 30 iterations of BEARscc on the provided example data will look this:

To reproduce the plot run:

```
library("NMF")
aheatmap(noise_consensus, breaks=0.5)
```

2.6   Evaluating the noise consensus

In order to interpret the noise consensus, we have defined three cluster (and analagous cell) metrics. Stabilty indicates the propensity for a putative cluster to contain the same cells across noise-injected counts matrices. Promiscuity indicates a tendency for cells in a putative cluster to associate with other clusters across noise-injected counts matrices. Score represents the promiscuity substracted from the stability.

We have found it useful to identify the optimal number of clusters in terms of resiliance to noise by examining these metrics by cutting hierarchical clustering dendograms of the noise consensus and comparing the results to the original clustering labels. To do this create a vector containing each number of clusters one wishes to examine (the function automatically determines the results for the dataset as a single cluster) and then cluster the consensus with `cluster_consensus()`:

```
vector <- seq(from=2, to=5, by=1)
BEARscc_clusts.df <- cluster_consensus(noise_consensus,vector)
```

We add the original clustering to the `data.frame`:

```
BEARscc_clusts.df <- cbind(BEARscc_clusts.df,
    Original=clusters.df$Original_counts)
```

2.6.1   Understanding robustness at the cluster level

Compute cluster metrics by running the command:

```
cluster_scores.dt <- report_cluster_metrics(BEARscc_clusts.df,
    noise_consensus, plot=TRUE, file="example")
```

The output is a melted `data.table` that displays the name of each cluster, the size of each cluster, the metric (score, Promiscuity, Stability), the value of each metric for the respective cluster and clustering, the clustering in question (1,2,...,Original), whether the cluster consists of only one cell, and finally the mean of each metric across all clusters in a clustering.

An example of the resulting plot for 3 noise-injected perturbations is provided for the user's reference: example/example_cluster_scores.pdf. It is evident from the plot that one cluster is optimal and outperforms the original clustering which bifurcated this set of purely technical data into 2 clusters.

2.6.2 Using BEARscc to inform cluster number, k, choice

While BEARscc certainly does not claim to provide a definitive solution to the question concerning the number of clusters, we provide what we believe to be a useful perspective on the matter. Specifically, we have found that

2.6.3 Understanding robustness at the sample level

Likewise, the cell metrics may be computed using:

```
cell_scores.dt <- report_cell_metrics(BEARscc_clusts.df, noise_consensus)
```

The output is a melted `data.table` that displays the name of each cluster to which the cell belongs, the cell label, the size of each cluster, the metric (score, Promiscuity, Stability), the value for each metric, and finally the clustering in question (1,2,...,Original).

These results can be plotted to visualize cells in the context of different clusterings using `ggplot2`.

3   Algorithm and theory

In order to simulate technical replicates, BEARscc first builds a statistical model of expression variance and drop-out frequency, which is dependent only on observed gene expression. The parameters of this model are estimated from spike-in counts. Expression-dependent variance is approximated by fitting read counts of each spike-in transcript across cells to a mixture model comprised of a Poisson and negative binomial distribution (Section 3.1.1). The drop-out model (Section 3.1.2) in BEARscc has two distinct parts: the *drop-out injection distribution* models the likelihood that a given transcript concentration will result in a drop-out, and the *drop-out recovery distribution* models the likelihood that an observed drop-out resulted from a given transcript concentration. The drop-out injection distribution is taken to be the observed drop-out rate in spike-in controls as a function of actual spike-in transcript concentration. This distribution is then used to estimate the drop-out recovery distribution density via Bayes' theorem and a an empirically informed set of priors and assumptions. Briefly, BEARscc utilizes the drop-out injection distribution and the number of observed zeroes for each endogenous gene to infer a gene-specific probability distribution describing the likelihood that an observed drop-out should in fact have been some non-zero value, given the drop-out rate of the endogenous gene. This entire process is facilitated by the function, `estimate_noiseparameters()`.

In the second step, BEARscc generates simulated technical replicates by applying the models described in the first step (Section 3.2). For every observed count in the range of values where drop-outs occurred amongst the spike-in transcripts, BEARscc uses the drop-out injection distribution from Step 1 to determine whether to convert the count to zero. For observations where the count is zero, the drop-out recovery distribution is used to estimate a new value, given the overall drop-out frequency for the gene (Section 3.2). Next, BEARscc substitutes all values larger than zero with a value generated from the derived model of expression variability, parameterized to the observed count for that gene. This procedure can then be repeated any number of times to generate a collection of simulated technical replicates. This step is carried out by `create_noiseinjected_counts()`.

In the third step, the simulated technical replicates are then re-clustered, using exactly the same method as for the observed data; this re-clustering for each simulated technical replicate is described as an *association matrix* where each element indicates whether two cells share a cluster identity (1) or cluster apart from each other (0). The association matrices for each simulated technical replicate are averaged to form a noise consensus matrix that can be easily interpreted (Section 3.3). This is accomplished with the function `compute_consensus()`. Each element of the noise consensus matrix represents the fraction of simulated technical replicates that, upon applying the clustering method of choice, resulted in two cells clustering together (the *association frequency*). Then, the functions `report_cell_metrics()` and `report_cluster_metrics()` may be used to explore and quantitate the noise consensus matrix at the cell sample and cluster levels, respectively.

3.1   Noise estimation

As mentioned previously, BEARscc uses spike-ins to estimate the noise of the experiment for the purpose of producing simulated technical replicates. BEARscc models overall technical variation with a mixture-model (Section 3.1.1) and inferred drop-out effects (Section 3.1.2) independently using the spike-in observations. However, a single function in BEARscc `estimate_noiseparameters()` accomplishes this task.

3.1.1   Estimating transcript variation

Technical variance is modeled in BEARsccby fitting a single parameter mixture model, $Z(c)$, to the spike-ins' observed count distributions. The noise model is fit independently for each spike-in transcript and subsequently regressed onto spike-in mean expression to define a generalized noise model. This is accomplished in three steps:

1. Define a mixture model composed of *poisson* and *negative binomial* random variables:
$$Z \sim (1 - \alpha) * Pois(\mu) + \alpha * NBin(\mu, \sigma) \tag{1}$$

2. Empirically fit the parameter, α_i, in a spike-in specific mixture-model, Z_i, to the observed distribution of counts for each ERCC spike-in transcript, i, where μ_i and σ_i are the observed mean and variance of the given spike-in. The parameter, α_i, is chosen such that the error between the observed and mixture-model is minimized.

3. Generalize the mixture-model by regressing α_i parameters and the observed variance, σ_i, onto the observed spike-in mean expression, μ_i. Thus the mixture model describing the noise observed in ERCC transcripts is defined solely by μ, which is treated as the count transformation parameter, c, in the generation of simulated technical replicates .

In step 2, a mixture model distribution is defined for each spike-in, i: $Z_i(\alpha_i, \mu_i, \sigma_i) \sim (1-\alpha_i)*Pois(\mu_i)+\alpha_i*NBin(\mu_i, \sigma_i)$. The distribution, Z_i, is fit to the observed counts of the respective spike-in, where α_i is an empirically fitted parameter, such that the α_i minimizes the difference between the observed count distribution of the spike-in and the respective fitted model, Z_i. Specifically, for each spike-in transcript, μ_i and σ_i are taken to be the mean and standard deviation, respectively, of the observed counts for spike-in transcript, i. Then, α_i is computed by empirical parameter optimization; α_i is taken to be the $\alpha_{i,j}$ in the mixture-model, $Z_{i,j}(\alpha_{i,j}, \mu_i, \sigma_i) \sim (1 - \alpha_{i,j}) * Pois(\mu_i) + \alpha_{i,j} * NBin(\mu_i, \sigma_i)$, found to have the least absolute total difference between the observed count density and the density of the fitted model, Z_i. In the case of ties, the minimum $\alpha_{i,j}$ is chosen.

In step 3, $\alpha(c)$ is then defined with a linear fit, $\alpha_i = \alpha*log2(\mu_i)+b$. $\sigma(c)$ was similarly defined, $log2(\sigma_i) = \alpha*log2(\mu_i)+b$. In this way, the observed distribution of counts in spike-in transcripts defines the single parameter mixture-model, $Z(c)$, used to transform counts during generation of simulated technical replicates:

$$Z(c) \sim (1 - \alpha(c)) * Pois(c) + \alpha(c) * NBin(c, \sigma(c)) \tag{2}$$

During technical replicate simulation, the parameter c is set to the observed count value, a, and the transformed count in the simulated replicate was determined by sampling a single value from $Z(c = a)$.

3.1.2 Defining the drop-out models

A model of the drop-outs is developed by BEARscc in order to inform the permutation of zeros during noise injection. The observed zeros in spike-in transcripts as a function of actual transcript concentration and Bayes' theorem are used to define two models: the *drop-out injection distribution* and the *drop-out recovery distribution*.

The drop-out injection distribution is described by $Prob(X = 0|Y = y)$, where X is the distribution of observed counts and Y is the distribution of actual transcript counts; the density is computed by regressing the fraction of zeros observed in each sample, D_i, for a given spike-in, i, onto the expected number spike-in molecules in the sample, y_i, e.g. $D = a*y+b$. Then, D describes the density of zero-observations conditioned on actual transcript number, y, or $Prob(X = 0|Y = y)$. Notably, each gene was treated with an identical density distribution for drop-out injection.

In contrast, the density of the drop-out recovery distribution, $Prob(Y_j = y|X_j = 0)$, is specific to each gene, j, where X_j is the distribution of the observed counts and Y_j is the distribution of actual transcript counts for a given gene. The gene-specific drop-out recovery distribution is inferred from drop-out injection distribution using Bayes' theorem and a prior. This is accomplished in 3 steps:

1. For the purpose of applying Bayes' theorem, the gene-specific distribution, $Prob(X_j = 0|Y_j = y)$, is taken to be the the the drop-out injection density for all genes, j.
2. The probability that a specific transcript count is present in the sample, $Prob(Y_j = y)$, is a necessary, but empirically unknowable prior. Therefore, the prior was defined using the law of total probability, an assumption of uniformity, and the probability that a zero was observed in a given gene, $Prob(X_j = 0)$. The probability, $Prob(X_j = 0)$, is taken to be the fraction of observations that are zero for a given gene. BEARscc does this in order to better inform the density estimation of the gene-specific drop-out recovery distribution.
3. The drop-out recovery distribution density is then computed by applying Bayes' theorem:

$$Prob(Y_j = y|X_j = 0) = \frac{Prob(X_j = 0|Y_j = y) * Prob(Y_j = y)}{Prob(X_j = 0)}, \tag{3}$$

In the second step, the law of total probability, an assumption of uniformity, and the fraction of zero observations in a given gene are leveraged to define the prior, $Prob(Y_j = y)$. First, a threshold of expected number of transcripts, k in Y, is chosen such that k was the maximum value for which the drop-out injection density was non-zero. Next, uniformity is assumed for all expected number of transcript values, y greater than zero and less than or equal to k; that is $Prob(Y_j = y)$ is defined to be some constant probability, n. Furthermore, $Prob(Y_j = y)$ is defined to be 0 for all $y > k$. In order to

inform $Prob(Y_j = y)$ empirically, $Prob(Y_j = 0)$ and n are derived by imposing the law of total probability (Equation 4) and unity (Equation 5) yielding a system of equations:

$$Prob(X_j = 0) = \Sigma_{y=0}^{k-1}(Prob(X_j = 0|Y_j = y) * Prob(Y_j = y)) \tag{4}$$

$$\Sigma_{y=0}^{k-1}Prob(Y_j = y) = Prob(Y_j = 0) + (k - 1) * n = 1 \tag{5}$$

The probability that a zero is observed given there are no transcripts in the sample, $Prob(X_j = 0|Y_j = 0)$, is assumed to be 1. With the preceding assumption, solving for $Prob(Y_j = 0)$ and n give:

$$n = \frac{1 - Prob(Y_j = 0)}{k - 1} \tag{6}$$

$$Prob(Y_j = 0) = \frac{Prob(X_j = 0) - \frac{1}{k-1} * \Sigma_{y=1}^{k-1}(Prob(X_j = 0|Y_j = y))}{(1 - \frac{1}{k-1} * \Sigma_{y=1}^{k-1}(Prob(X_j = 0|Y_j = y))} \tag{7}$$

\

In this way, $Prob(Y_j = 0)$ is defined by (Equation 6) for y in Y_j less than or equal to k and greater than zero, and defined by (Equation 7) for y in Y_j equal to zero. For y in Y_j greater than k, the prior $Prob(Y_j = y)$ is defined to be equal to zero.

In the third step, the previously computed prior, $Prob(Y_j = y)$, the fraction of zero observations in a given gene, $Prob(X_j = 0)$, and the drop-out injection distribution, $Prob(X_j = 0|Y_j = y)$, are utilized to estimate, with Bayes's theorem, the density of the drop-out recovery distribution, $Prob(Y_j = y|X_j = 0)$. During the generation of simulated technical replicates for zero observations and count observations less than or equal to k, values are sampled from the drop-out recovery and injection distributions as described in the pseudocode of the BEARscc algorithm for simulating technical replicates.

3.2 Simulating technical replicates

Simulated technical replicates were generated from the noise mixture-model and two drop-out models. For each gene, the count value of each sample is systematically transformed using the mixture-model, $Z(c)$, and the drop-out injection, $Prob(X = 0|Y = y)$, and recovery, $Prob(Y_j = y|X_j = 0)$, distributions in order to generate simulated technical replicates as indicated by the following pseudocode:

```
FOR EACH gene, $j$
    FOR EACH count, $c$
        IF $c=0$
                $n \leftarrow SAMPLE$ one count, y, from $Prob(Y_j=y | X_j=0)$
                IF $n=0$
                    $c \leftarrow 0$
            ELSE
                    $c \leftarrow SAMPLE$ one count from $Z(n)$
            ENDIF
        ELSE
            IF $c\leq k$
                    $dropout \leftarrow TRUE$ with probability, $Prob(X=0 | Y=k)$
                    IF $dropout=TRUE$
                      $c \leftarrow 0$
                    ELSE
                        $c \leftarrow SAMPLE$ one count from $Z(c)$
```

```
                    ENDIF
                ELSE
                    $c \leftarrow SAMPLE$ one count from $Z(c)$
                ENDIF
            ENDIF
            RETURN $c$
        DONE
DONE
```

4 List of functions

4.1 `estimate_noiseparameters()`

4.1.1 Description

Estimates the drop-out model and technical variance from spike-ins present in the sample.

For greater detail, please see help file `?estimate_noiseparameters()`.

4.1.2 Usage

```
data(BEARscc_examples)
estimated_noise <- estimate_noiseparameters(ERCC.counts.df,
                                data.counts.df,
                                ERCC.meta.df,
                                granularity=30,
                                alpha_granularity=0.25,
                                write.noise.model=FALSE)
estimated_noise
```

4.1.3 Output

The resulting output of `estimate_noiseparameters()` is a long list, which is enumerated in the function's package help page.

4.1.4 Note

The above usage is for execution of `create_noiseinjected_counts` on a local machine. To save results as files for us of `prepare_probabilities` on high performance computing environment, then use:

```
estimate_noiseparameters(ERCC.counts.df,
                                data.counts.df,
                                ERCC.meta.df,
                                granularity=30,
                                write.noise.model=TRUE,
                                alpha_granularity=0.25,
                                file="noise_estimation",
                                model_view=c("Observed","Optimized"))
```

4.2 `create_noiseinjected_counts()`

4.2.1 Description

Computes BEARscc simulated technical replicates from the previously estimated noise parameters computed with the function `estimate_noise_parameters()`.

For greater detail, please see help file `?create_noiseinjected_counts()`.

4.2.2   Usage

```
data(analysis_examples)
sim_replicates<-create_noiseinjected_counts(estimated_noise, n=3)
sim_replicates
```

4.2.3   Output

The resulting object is a list of counts data, where each element of the list is a `data.frame` of the counts representing a BEARscc simulated technical replicate. For further details refer to the function help page.

4.2.4   Note

This function is the in-package analog of the high-performance computing function,`prepare_probabilities`.

4.3   `prepare_probabilities()`

4.3.1   Description

The high-performance computing function analog to `create_noiseinjected_counts()`.

4.3.2   Usage

Please refere to section 2.4.

4.3.3   Output

The resulting objects would normally be output to a tab-delimited file, where each file results from a `data.frame` of the counts representing a BEARscc simulated technical replicate.

4.3.4   Note

This function has no help file, but is referred to in the section 2.4 of this document on simulating for larger datasets.

4.4   `compute_consensus()`

4.4.1   Description

Computes the consensus matrix using a `data.frame` of cluster labels across different BEARscc simulated technical replicates.The consensus matrix is is a visual and quantitaive representation of the clustering variation on a cell-by-cell level created by using cluster labels to compute the number of times any given pair of cells associates in the same cluster; this forms the 'noise consensus matrix'. Each element of this matrix represents the fraction of simulated technical replicates in which two cells cluster together (the 'association frequency'), after using a clustering method of the user's choice to generate a data.frame of clustering labels. This consensus matrix may be used to compute BEARscc metrics at both the cluster and cell level.

For greater detail, please see help file `?compute_consensus()`.

4.4.2 Usage

```
data("analysis_examples")
noise_consensus <- compute_consensus(clusters.df)
noise_consensus
```

4.4.3 Output

When the number of samples are *n*, then the noise consensus resulting from this function is an *n* x *n* matrix describing the fraction of simulated technical replicates in which each cell of the experiment associates with another cell.

4.5 cluster_consensus()

4.5.1 Description

This function will perform hierarchical clustering on the noise consensus matrix allowing the user to investigate the appropriate number of clusters, *k*, considering the noise within the experiment. Frequently one will want to assess multiple possible cluster number situations at once. In this case it is recommended that one use a `lapply` in conjunction with a vector of all biologically reasonable cluster numbers to fulfill the task of attempting to identify the optimal cluster number.

For greater detail, please see help file `?cluster_consensus()`.

4.5.2 Usage

```
data(analysis_examples)
vector <- seq(from=2, to=5, by=1)
BEARscc_clusts.df <- cluster_consensus(consensus_matrix=noise_consensus,
    vector)
BEARscc_clusts.df
```

4.5.3 Output

The output is a vector of cluster labels based on hierarchical clustering of the noise consensus. In the event that a vector is supplied for number of clusters in conjunction with `lapply`, then the output is a data.frame of the cluster labels for each of the various number of clusters deemed biologically reasonable by the user.

4.6 report_cell_metrics()

4.6.1 Description

To quantitatively evaluate the results, three metrics are calculated from the noise consensus matrix: 'stability' is the average frequency with which a cell within a cluster associates with other cells within the same cluster across simulated replicates; 'promiscuity' measures the average association frequency of a cell within a cluster with the *n* cells outside of the cluster with the strongest association with the cell in question; and 'score' is the difference between 'stability' and 'promiscuity'. Importantly, 'score' reflects the overall "robustness" of a given cell's assignment to a user-provided cluster label with respect to technical variance. Together these metrics provide a quantitative measure of the extent to which cluster labels provided by the user are invariant across simulated technical replicates.

For greater detail, please see help file `?report_cell_metrics()`.

4.6.2 Usage

```
data(analysis_examples)
cell_scores.dt <- report_cell_metrics(BEARscc_clusts.df, noise_consensus)
cell_scores.dt
```

4.6.3 Output

A melted `data.table` describing the BEARscc metrics for each cell, where the columns are enumerated in the help file.

4.7 `report_cluster_metrics()`

4.7.1 Description

To quantitatively evaluate the results, three metrics are calculated from the noise consensus matrix: 'stability' is the average frequency with which cells within a cluster associate with each other across simulated replicates; 'promiscuity' measures the association frequency between cells within a cluster and those outside of it; and 'score' is the difference between 'stability' and 'promiscuity'. Importantly, 'score' reflects the overall "robustness" of a cluster to technical variance. Together these metrics provide a quantitative measure of the extent to which cluster labels provided by the user are invariant across simulated technical replicates.

For greater detail, please see help file `?report_cluster_metrics()`.

4.7.2 Usage

```
data(analysis_examples)
cluster_scores.dt <- report_cluster_metrics(BEARscc_clusts.df,noise_consensus,
    plot=TRUE, file="example")
cluster_scores.dt
```

4.7.3 Output

A melted `data.table` describing the BEARscc metrics for each cluster, where the columns are enumerated in the help file.

5   Example data

Within the package there are data subsampled from single cell sequencing protocol applied to water samples containing ERCC spike-ins (blanks) and dilute RNA from brain whole tissue (brain) discussed at length in in a manuscript on bioRxiv

5.1   BEARscc_examples

5.1.1   Description

A toy dataset for applying BEARscc functions as described in the README on https://bitbucket.org/bsblabludwig/bearscc.git. These data are a subset of observations made by Drs. Michael White and Richard Owen in the Xin Lu Lab. Samples were sequenced by the Wellcome Trust Center for Genomics, Oxford, UK. These data are available in full with GEO accession number, GSE95155.

For greater detail, please see help file ?BEARscc_examples.

5.1.2   Usage

```
data("BEARscc_examples")
```

5.2   analysis_examples

5.2.1   Description

BEARscc downstream example objects: The analysis_examples Rdata object contains downstream data objects for use in various help pages for dynamic execution resulting from running tutorial in README and vignette on BEARscc_examples. The objects are a result of applying BEARscc functions as described in the README found at https://bitbucket.org/bsblabludwig/bearscc.git.

For greater detail, please see help file ?analysis_examples.

5.2.2   Usage

```
data("analysis_examples")
```

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