## ECG Filtering to Remove Noise By Ata Jodeiri Seyedian

## 1 Time interval selection:

• Important quantities:

 $F_s: \frac{Sample}{Second} \rightarrow Sampling \ rate \ (How \ many \ samples \ per \ second) = \frac{1}{T_s}$ 

 $T_s: \frac{Second}{Sample} \rightarrow Sampling interval (Period between samples) = \frac{1}{F_s}$ 

• Getting samples within a period of time:

 $\alpha * F_s \rightarrow How many samples in \alpha second$ 

For example, if  $F_s = 100$ , then  $1 * F_s = how many samples in 1 second = 1 \times 100 = 100 samples.$ 

Similarly,  $3 * F_s = how many samples in 3 second = 3 \times 100 = 300 samples.$ 

• Convert time to samples and vice versa:

Time (Second) 
$$\times$$
  $F_s$  ( $\frac{Sample}{Second}$ ) =  $Samples$ 

Sequence (Sample) 
$$\times T_s$$
 ( $\frac{Second}{Sample}$ ) =  $Seconds$ 

• Creating time vector for Fs = 10 and length(Data) = 5:

$$t = [0:1:length(Data) - 1] .* Ts; \rightarrow [0,0.1,0.2,0.3,0.4]$$

• Creating time vector for Fs = 10 and from time = 1 to time = 2:

$$t = [1:Ts:2]; \rightarrow [1, 1.1, 1.2, 1.3, 1.4, 1.5, 1.6, 1.7, 1.8, 1.9, 2]$$

• If we need to select specific time duration:

X := data of size Nx1, where N is the number of samples. To select the interval [2, 5] seconds:

$$Y = X(2 * Fs : 5 * Fs);$$

• Creating frequency vector for one-sided FFT plot with Fs = 20 and  $N_{fft} = \text{length}(\text{Data}) = 10$ :

$$f = linspace(0, Fs/2, (N_{fft}/2) + 1); \rightarrow [0, 2, 4, 6, 8, 10]$$

## 2 Low-Pass filter:

$$Y(z) = H(z) \times X(z) \tag{1}$$

$$H(z) = \frac{Y(z)}{X(z)} = \frac{1}{32} \times \frac{(1 - z^{-6})^2}{(1 - z^{-1})^2}$$
 (2)

$$H(z) = \left(\frac{1}{32}\right) \times \left(\frac{1 - 2z^{-6} + z^{-12}}{1 - 2z^{-1} + z^{-2}}\right) \tag{3}$$

$$H(z) = \left(\frac{1}{32}\right) \times \left(\frac{(1)z^{0} + (0)z^{-1} + (0)z^{-2} + (0)z^{-3} + (0)z^{-4} + (0)z^{-5} - 2z^{-6} + (0)z^{-7} + (0)z^{-8} + (0)z^{-9} + (0)z^{-10} + (0)z^{-11} + (1)z^{-12}}{1 - 2z^{-1} + z^{-2}}\right) \tag{4}$$

You need to keep it in the form:

$$H(z) = \frac{\left(\frac{1}{32}\right) \times \left[(1)z^{0} + (0)z^{-1} + (0)z^{-2} + (0)z^{-3} + (0)z^{-4} + (0)z^{-5} + (-2)z^{-6} + (0)z^{-7} + (0)z^{-8} + (0)z^{-9} + (0)z^{-10} + (0)z^{-11} + (1)z^{-12}\right]}{(1) + (-2)z^{-1} + (1)z^{-2}} \tag{5}$$

$$a = [1, -2, 1] \tag{7}$$