
MODULE *ProofStatus*

EXTENDS *Naturals, Sequences*

PROOF OBLIGATION STATUSES

We define a possible proof-obligation status to be a mapping from provers to outcomes.

CONSTANT *Prover*

The set of all back-end provers, containing the elements “zenon” and “isabelle”, among others.

ProofOutcome \triangleq { “notTried”, “failed”, “succeeded”, “stopped” }

ObligationStatus \triangleq

The set of all possible statuses for an obligation, where a status consists of a mapping from provers to the result of running that prover on the obligation, plus a triviality bit indicating whether or not *TLAPM* has determined the obligation to be trivial.

[*proverStatus* : [*Prover* \rightarrow *ProofOutcome*],
triviality : BOOLEAN
]

NullStatus \triangleq [*proverStatus* \mapsto [*p* \in *Prover* \mapsto “notTried”],
triviality \mapsto FALSE]

THEOREM *NullStatus* \in *ObligationStatus*

BY DEF *NullStatus, ObligationStatus, ProofOutcome*

PROOF -OUTCOME TREES

We define an abstract proof tree that represents a step or theorem and proof statuses of all its obligations.

CONSTANTS *Obligation, Step*

We assume uninterpreted sets of obligations (or obligation ids) and steps.

ProofOutcomeTree \triangleq

An abstract representation of a theorem or proof step and its proof. This uses a standard TLA+ recursive definition of this sort of tree, where *P*[0] is the set of steps with a (possibly missing or omitted) leaf proof, and *Pf*[*n*] is the set of all proof trees of depth at most *n*.

LET *Pf*[*n* \in *Nat*] \triangleq
 IF *n* = 0 THEN [*step* : *Step*,
leafProof : TRUE,
proofPresence : { “missing”, “OMITTED” }]
 \cup
 [*step* : *Step*,
leafProof : TRUE,
proofPresence : { “present” },
obligations : SUBSET (*Obligation* \times *ObligationStatus*)]
 ELSE [*step* : *Step*,
leafProof : FALSE,

$$\begin{aligned}
& \text{children} : \text{Seq}(\text{Pf}[n-1]) \\
& \cup \text{Pf}[n-1] \\
\text{IN} \quad & \text{UNION } \{ \text{Pf}[n] : n \in \text{Nat} \}
\end{aligned}$$

STATUS SPECIFICATIONS

CONSTANT *NumberOfStepStatuses*

For simplicity, a step status is a number from 1 to *NumberOfStepStatuses*.

StepStatus $\triangleq 1 \dots \text{NumberOfStepStatuses}$

StepStatusPredicate \triangleq

A set of elements, each representing a predicate on a proof tree, as defined by *ApplyStatusPredicate* below.

$$\begin{aligned}
& [\text{presence} : \{ \text{"missing"}, \text{"OMITTED"} \}, \\
& \quad \text{leaf} : \text{BOOLEAN} \\
&] \\
& \cup \\
& [\text{presence} : \{ \text{"present"} \}, \\
& \quad \text{oStatus} : \text{Prover} \times \text{ProofOutcome}, \\
& \quad \text{leaf} : \text{BOOLEAN} \\
&]
\end{aligned}$$

ApplyStatusPredicate(*pred*, *pfTree*) \triangleq

Defines the result of applying the *StepStatusPredicate* *pred* to the *ProofTree* *pfTree*.

$$\begin{aligned}
\text{LET } \text{ASP}[pf \in \text{ProofOutcomeTree}] & \triangleq \\
& \wedge \text{pred.leaf} \equiv pf.\text{leaf} \\
& \wedge \text{pred.presence} = pf.\text{presence} \\
& \wedge (\text{pred.presence} = \text{"present"}) \Rightarrow \\
& \quad \text{IF } pf.\text{leaf} \\
& \quad \text{THEN } \exists ob \in pf.\text{obligations} : \\
& \quad \quad ob[\text{pred.oStatus}[1]] = \text{pred.oStatus}[2] \\
& \quad \text{ELSE } \exists i \in pf.\text{children} : \text{ASP}[pf.\text{children}[i]] \\
\text{IN } & \text{ASP}[pfTree]
\end{aligned}$$

\ * Modification History
 \ * Last modified Wed Jun 30 03:06:52 PDT 2010 by lamport
 \ * Created Wed Jun 30 01:51:58 PDT 2010 by lamport