

# Math 306 - Numerical Methods

## Introduction to MATLAB

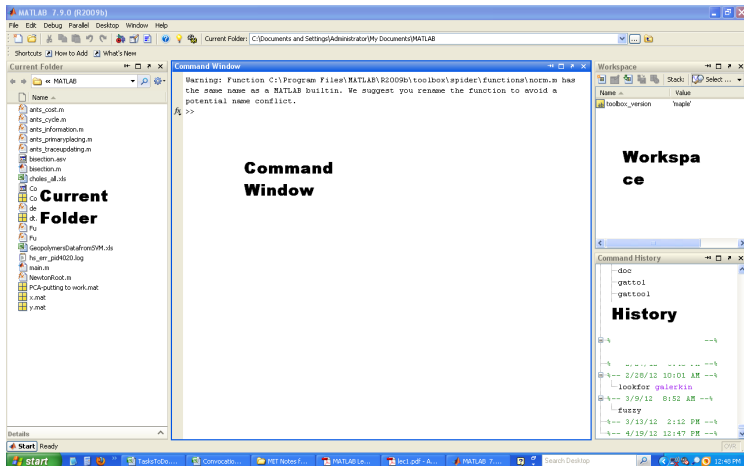
Sqn Ldr Dr Athar Kharal

Humanities and Science Department  
College of Aeronautical Engineering  
PAF Academy Risalpur

# Outline

- (1) Getting Started
- (2) Making Variables
- (3) Manipulating Variables
- (4) Basic Plotting

# The MATLAB Desktop



# Getting Started

Customization

[File -> Preferences](#)

Allows you personalize your MATLAB experience

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  - Commands are executed line by line
  - Like the computer languages Scheme and BASIC

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- `help`  
The most important function for learning MATLAB on your own



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- **More on help later**

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- Other types are also supported: complex, symbolic, 16-bit and 8 bit integers, etc.

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  - **NaN** represents 'Not a Number'

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  - `sprintf()` allows you to mix strings with variables
    - `>>class=6.094;`
    - `>>disp(sprintf('Hello%g', class))`

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    - `>>disp(sprintf('Hello%g', class))`
      - The format is C-syntax

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- To suppress output, end the line with a semicolon  
    `»m= 13/3;`

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- MATLAB makes vectors easy! That's its power!

# Row & Column Vectors

- Row vector: comma or space separated values between brackets

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- Column vector: semicolon separated values between brackets

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»column = [4;2;7;4];
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1	2	5	1	2	5
3	4	6	3	4	6
1	2	3	4	1	2

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- **Can do the same for entire environment**
  - » **save myenv; clear all; load myenv;**

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- And here are the answers:
  - »`r=[1 4 7 10 13];`
  - »`c=[13; 10; 7; 4; 1];`
  - »`save varExr c`
  - »`clear r c`
  - »`load varEx`

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- To clear cluttered command window
  - » `clc`

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- Call using parentheses – passing parameter to function
  - » `sqrt(2)`
  - » `log(2)`, `log10(0.23)`
  - » `cos(1.2)`, `atan(-.8)`
  - » `exp(2+4*i)`
  - » `round(1.4)`, `floor(3.3)`, `ceil(4.23)`
  - » `angle(i)`; `abs(1+i)`;



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- To search for a function by specifying keywords:  
    »doc + Search tab  
    »lookfor hyperbolic  
    One-word description of what you're looking for

# Exercise: Scalars

Verify that  $e^{ix} = \cos(x) + i \sin(x)$  for a few values of  $x$ .

```
»x = pi/3;
```

```
»a = exp(i*x)
```

```
»b = cos(x)+ i*sin(x)
```

```
»a-b
```

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  - To get a vector's length, use the length function

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- For vectors of real numbers '.' and ' give same result

# Addition and Subtraction

- Addition and subtraction are element-wise; sizes must match (unless one is a scalar):

$$\begin{array}{r} [12 \ 3 \ 32 \ -11] \\ + [2 \ 11 \ -30 \ 32] \\ \hline [14 \ 14 \ 2 \ 21] \end{array}$$

$$\begin{bmatrix} 12 \\ 1 \\ -10 \\ 0 \end{bmatrix} - \begin{bmatrix} 3 \\ -1 \\ 13 \\ 33 \end{bmatrix} = \begin{bmatrix} 9 \\ 2 \\ -23 \\ -33 \end{bmatrix}$$

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- Use the transpose to make sizes compatible  
`>>c = row' + column`  
`>>c = row + column'`

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 \begin{bmatrix} 12 \\ 1 \\ -10 \\ 0 \end{bmatrix}
 -
 \begin{bmatrix} 3 \\ -1 \\ 13 \\ 33 \end{bmatrix}
 =
 \begin{bmatrix} 9 \\ 2 \\ -23 \\ -33 \end{bmatrix}$$

- The following would give an error  
`>>c = row + column`
- Use the transpose to make sizes compatible  
`>>c = row' + column`  
`>>c = row + column'`
- Can sum up or multiply elements of vector  
`>>s=sum(row);`  
`>>p=prod(row);`

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  - **standard**



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- To do element-wise operations, use the dot. BOTH dimensions must match (unless one is scalar)!

```
»a=[1 2 3];b=[4;2;1];
```

```
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$3 \times 1 \quad . * \quad 3 \times 1 \quad = \quad 3 \times 1$

# Operators: element-wise (cont'd)

$$\begin{bmatrix} 1 & 1 & 1 \\ 2 & 2 & 2 \\ 3 & 3 & 3 \end{bmatrix} \begin{matrix} .* \\ \\ .* \end{matrix} \begin{bmatrix} 1 & 2 & 3 \\ 1 & 2 & 3 \\ 1 & 2 & 3 \end{bmatrix} \begin{matrix} = \\ \\ = \end{matrix} \begin{bmatrix} 1 & 2 & 3 \\ 2 & 4 & 6 \\ 3 & 6 & 9 \end{bmatrix}$$

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$$1 \times 3 + 2 \times 2 + 3 \times 1 = 11$$

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$$1 \times 3 * 3 \times 1 = 1 \times 1$$

$$\begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}^2 = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} * \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$$

# Operators: standard (cont'd)

$$\begin{array}{ccc} \begin{bmatrix} 1 & 1 & 1 \\ 2 & 2 & 2 \\ 3 & 3 & 3 \end{bmatrix} & * & \begin{bmatrix} 1 & 2 & 3 \\ 1 & 2 & 3 \\ 1 & 2 & 3 \end{bmatrix} & = & \begin{bmatrix} 3 & 6 & 9 \\ 6 & 12 & 18 \\ 9 & 18 & 27 \end{bmatrix} \\ 3 \times 3 & & 3 \times 3 & & 3 \times 3 \end{array}$$

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»a=[1 2 3]\*[3 5 4]'
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- Calculate the natural log of each element of the resulting vector  
»c=log(b)

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- The general function call is:

$$var = zeros(M, N)$$

where  $M$  = Number of rows and  $N$  = Number of columns.

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- To initialize logarithmically spaced values use `logspace`  
    similar to `linspace`

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- `>>e=c(:,2);   ⇒   e=[5;13];`

- `>>c(2,:)= [3 6];   %replaces second row of c`

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- ```
»x = linspace(0,2*pi,1000);  
»y=sin(x);  
»y(55)  
»y(100:110)  
»[minVal,minInd]=min(y)  
»[maxVal,maxInd]=max(y)  
»inds=find(y>-0.001 & y<0.001)
```

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- Replace the first row of the matrix with  $\cos(x)$ 
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  - `>>cs= sum(mat);` % default dimension is 1

# Plotting Vectors

- Example

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»x=linspace(0,4*pi,10);
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»y=sin(x);
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# Plotting Vectors

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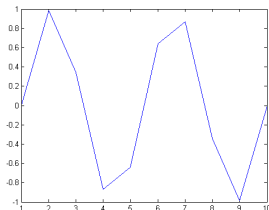
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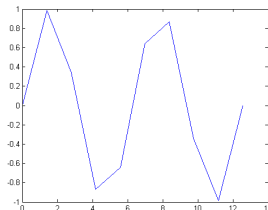
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Index based



x-values based

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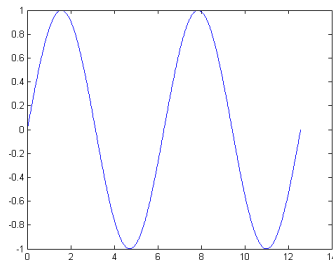
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```



- **x and y vectors must be same size or else there is an error**

1. (f1, g1) (f1, g1)



# Plot Options

- Can change the line color, marker style, and line style by adding a string argument  
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» `plot(x,y,'.')`
- Look at help document of `plot` for a full list of colors, markers, and linestyles

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- To plot two lines on the same graph  
    » `hold on;`
- To plot on a new figure  
    » `figure;`  
    » `plot(x,y);`
- Play with the figure GUI to learn more on how to  
    add axis labels  
    add a title  
    add a grid  
    zoom in/zoom out

# Exercise: Plotting

- Plot  $f(x) = e^x \cos(x)$  on the interval  $x = [0 \ 10]$ . Use a red solid line with a suitable number of points to get a good resolution.

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- **Work it out**
- ```
»x=0:.01:10;  
»plot(x,exp(x).*cos(x),'r');
```

# Thank you