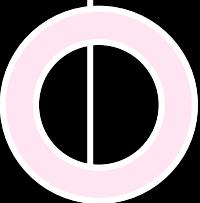




ME 222 : NATURE AND PROPERTIES OF MATERIALS

GROUP PROJECT REPORT

GROUP 2



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**C A L C U L A T I N G
C O E F F I C I E N T O F
R E S T I T U T I O N O F
D I F F E R E N T
S P H E R I C A L
B O D I E S H I T T I N G
A F L A T S U R F A C E**

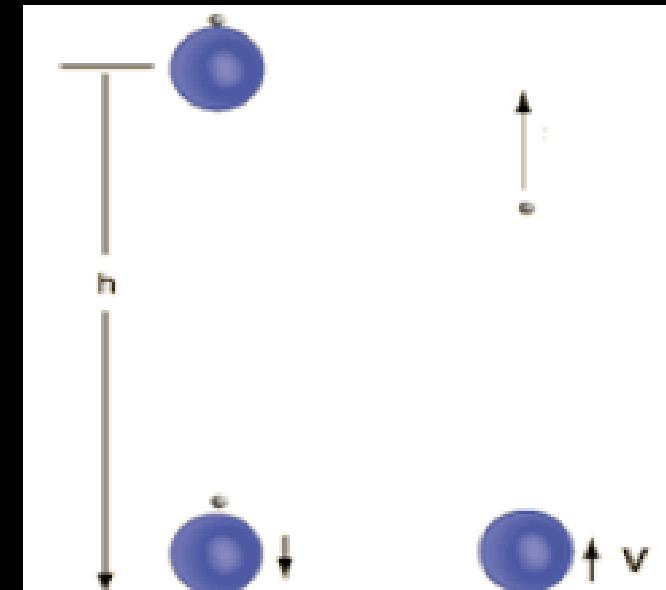
Contents

- Introduction
- Materials required
- Experimental Setup
- Procedure
- Observations
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- Experiment Analysis
- Sources of Error
- Conclusion

Introduction

- Coefficient of restitution(e) is the ratio of velocities of two entities after and before collision.
- It depends on number of factors including material of the colliding bodies.
- Typically, e lies between 0 to 1

$$\text{Coefficient of restitution } (e) = \frac{|\text{Relative velocity after collision}|}{|\text{Relative velocity before collision}|}$$



Formula

- The general formula for coefficient of restitution is - $e = \frac{v_{fb} - v_{fa}}{v_{ia} - v_{ib}}$
Where,
 - v_{fa} - final velocity of A
 - v_{fb} - final velocity of B
 - v_{ib} - initial velocity of A
 - v_{ia} - initial velocity of B
- In our experiment, the velocity of body B (ground) is zero and hence the formula is reduced to -

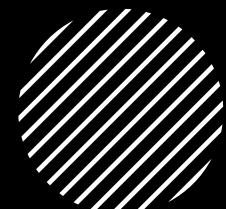
$$e = |v_f| / |v_i|$$





Materials Required

- Spherical Balls – Rubber ball and Table Tennis ball
- Smooth hard surface floor
- Ruler
- Smartphone
- Clamp and pins
- Ruler



● Software - OpenCV

- Used in video processing.
- Is integrated with various libraries for the analysis of the performed experiment.
- Identifies the ball and calculates its velocity.
- Our code is displayed in the next slide.





File Edit Selection View Go Run Terminal Help Velocity_find.py - Visual Studio Code

C: > Users > Atharv > Velocity_find.py > ...

```
1 from imutils.video import VideoStream
2 import argparse
3 import imutils
4 import time
5 import cv2
6 import numpy as np
7
8 ap = argparse.ArgumentParser()
9 ap.add_argument("-v", "--video", help="path to the video file")
10 ap.add_argument("-a", "--min-area", type=int, default=400, help="minimum area size")
11 args = vars(ap.parse_args())
12
13 if args.get("video", None) is None:
14     vs = VideoStream(src=0).start()
15     time.sleep(2.0)
16
17 else:
18     vs = cv2.VideoCapture(args["video"])
19
20 firstFrame = None
21
22 fps = 240
23 i = 0
24 vel_per_pix = 0
25 vel_per_m = 0
```

PROBLEMS OUTPUT DEBUG CONSOLE TERMINAL

```
5.290266895736453
3.600439426306183
0.42560847985560624
3.1786227486326526
5.45516258493961
3.2067433830913257
3.2073600052262603
3.2063733528903025
2.797412657818828
3.7249436342211943
3.009900655025843
PS C:\Users\Atharv>
```

+ ^ x

powershell
Python

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Experimental Setup

- A clamp is set at the required heights to drop the ball.
- A scale is set at the back to use it for giving pixel to height ratio in OpenCV.
- A smartphone is set using pins and clamps to record the videos.





////

Procedure

- Drop the ball from certain specific heights from the clamp to ensure that the ball falls vertically.
- Record the video using the smartphone.
- Instantaneous velocity of the ball before and after collision is measured using OpenCV.
- Appropriate calculations are performed to find the coefficient of restitution.





File Edit Selection View Go Run Terminal Help Velocity_find.py - Visual Studio Code

Get Started Doc_Scan.py Velocity_find.py C:\...\ME Velocity_find.py C:\...\Atharv X Vel_fnd_2.py

C: > Users > Atharv > Velocity_find.py > ...

```
73     i = 0
74     print(vel_per_m)
75 else :
76     vel_per_pix = 0
77     vel_per_m = 0
78 cv2.putText(frame, "Velocity: {}".format(str(vel_per_m)), (10, 20),
79 cv2.FONT_HERSHEY_SIMPLEX, 0.5, (0, 0, 255), 2)
80
81 cv2.imshow("Security Feed", frame)
82 key = cv2.waitKey(1) & 0xFF
83 if key == ord("q"):
84     print(frame.shape)
85     break
86 # cleanup the camera and close any open windows
87 vs.stop() if args.get("video", None) is None else vs.release()
88 cv2.destroyAllWindows()
89
```

PROBLEMS OUTPUT DEBUG CONSOLE TERMINAL

2.503283006313707
2.589944497474801
2.649130163846239
2.5412303245672163
2.792743107143942
2.3345444215628026
2.3350526124961295
2.1953719965247345
2.082959601894621
1.8862630466745618
1.655318134075743

PS C:\Users\Atharv> python velocity_find.py --video Drop_5.mp4

+ ^ x

powershell

Python

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108°F 15:35
Sunny 08/04/2022



Observations for Rubber ball

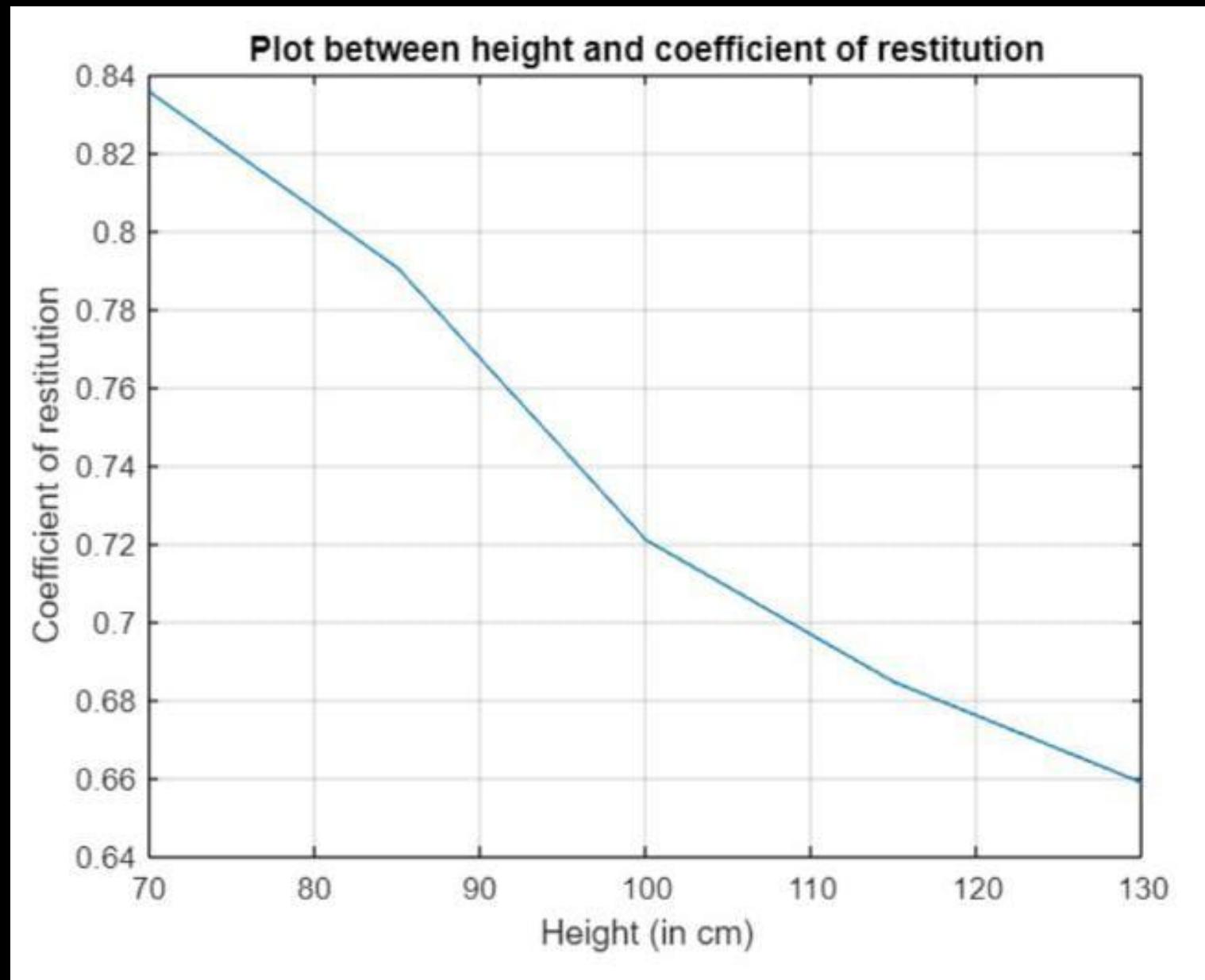


Observation Table

Sr. No	Height of ball drop - h (m)	Initial velocity - V _i (m/s)	Final velocity - V _f (m/s)	Coefficient of restitution - e = V _f /V _i
1	0.70	3.10793	2.56539	0.82543
2	0.85	3.45045	2.72716	0.79037
3	1.00	3.88551	2.80101	0.72088
4	1.15	4.54763	3.11294	0.68452
5	1.30	5.29351	3.48709	0.65875



Graph





Observations for Table Tennis ball

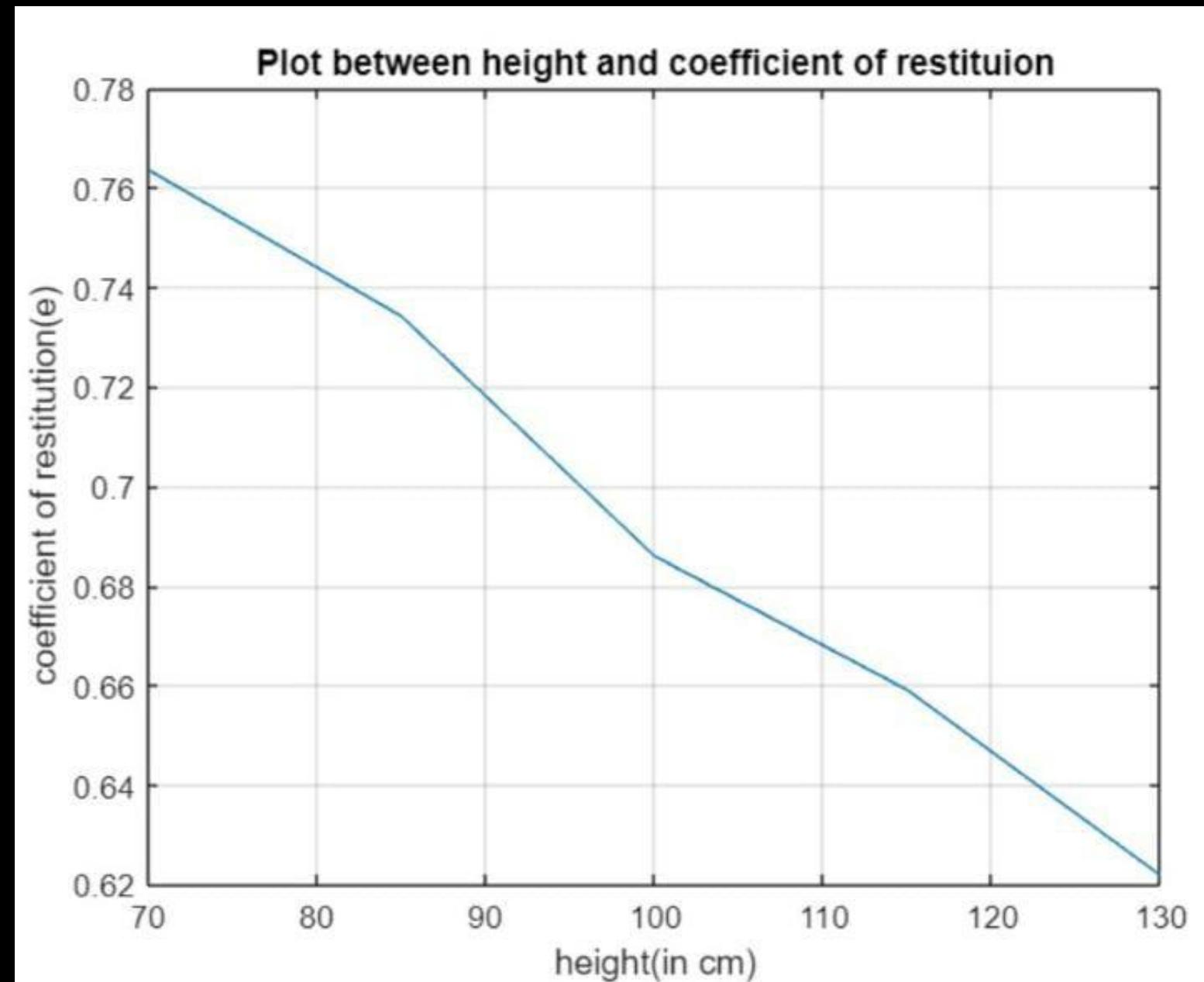


Observation Table

Sr. No	Height of ball drop - h (m)	Initial velocity - V _i (m/s)	Final velocity - V _f (m/s)	Coefficient of restitution - e = V _f /V _i
1	0.70	2.94515	2.23871	0.76353
2	0.85	3.31237	2.43174	0.73414
3	1.00	3.65479	2.50711	0.68598
4	1.15	4.46898	2.94537	0.65907
5	1.30	5.17342	3.21703	0.62184



Graph



Experiment Analysis

- From the above observations, it can be seen that the coefficient of restitution is different for different materials – rubber and plastic and thus it is a material property.
- The coefficient of restitution is observed to be inversely proportional to the height from which the ball is dropped





Sources of Error

- The surface is not perfectly flat.
- The camera angle also causes some errors in the readings.
- Errors while detecting the ball in OpenCV affects the velocity obtained.
- Error while measuring the height from which the ball is dropped.





Conclusion

- We have successfully analysed the variation of coefficient of restitution with change in the material of the colliding bodies.
- We have also observed the trend of change in the coefficient of restitution with a change in height from which the ball is dropped.

