```
In [ ]: # This mounts your Google Drive to the Colab VM.
        from google.colab import drive
        drive.mount('/content/drive')
        # TODO: Enter the foldername in your Drive where you have saved the unzipped
        # assignment folder, e.g. 'cs6353/assignments/assignment2/'
        FOLDERNAME = 'CS6353/Assignments/assignment2/'
        assert FOLDERNAME is not None, "[!] Enter the foldername."
        # Now that we've mounted your Drive, this ensures that
        # the Python interpreter of the Colab VM can load
        # python files from within it.
        import sys
        sys.path.append('/content/drive/My Drive/{}'.format(FOLDERNAME))
        # This downloads the CIFAR-10 dataset to your Drive
        # if it doesn't already exist.
        %cd /content/drive/My\ Drive/$FOLDERNAME/cs6353/datasets/
        !bash get_datasets.sh
        %cd /content/drive/My\ Drive/$FOLDERNAME
        # Install requirements from colab_requirements.txt
        # TODO: Please change your path below to the colab_requirements.txt file
        ! python -m pip install -r /content/drive/My\ Drive/$FOLDERNAME/colab_requirements.txt
```

```
Mounted at /content/drive
/content/drive/My Drive/CS6353/Assignments/assignment2/assignment2/cs6353/datasets
--2024-09-30 00:42:53-- http://www.cs.toronto.edu/~kriz/cifar-10-python.tar.gz
Resolving www.cs.toronto.edu (www.cs.toronto.edu)... 128.100.3.30
Connecting to www.cs.toronto.edu (www.cs.toronto.edu) | 128.100.3.30 | :80... connected.
HTTP request sent, awaiting response... 200 OK
Length: 170498071 (163M) [application/x-gzip]
Saving to: 'cifar-10-python.tar.gz'
cifar-10-python.tar 100%[==========] 162.60M 51.8MB/s
                                                                    in 3.3s
2024-09-30 00:42:57 (49.8 MB/s) - 'cifar-10-python.tar.gz' saved [170498071/17049807
1]
cifar-10-batches-py/
cifar-10-batches-py/data_batch_4
cifar-10-batches-py/readme.html
cifar-10-batches-py/test_batch
cifar-10-batches-py/data batch 3
cifar-10-batches-py/batches.meta
cifar-10-batches-py/data_batch_2
cifar-10-batches-py/data_batch_5
cifar-10-batches-py/data_batch_1
/content/drive/My Drive/CS6353/Assignments/assignment2/assignment2
Requirement already satisfied: anyio==3.7.1 in /usr/local/lib/python3.10/dist-package
s (from -r /content/drive/My Drive/CS6353/Assignments/assignment2/assignment2//colab_
requirements.txt (line 1)) (3.7.1)
Collecting appnope==0.1.3 (from -r /content/drive/My Drive/CS6353/Assignments/assignm
ent2/assignment2//colab_requirements.txt (line 2))
  Downloading appnope-0.1.3-py2.py3-none-any.whl.metadata (1.2 kB)
Requirement already satisfied: argon2-cffi==23.1.0 in /usr/local/lib/python3.10/dist-
packages (from -r /content/drive/My Drive/CS6353/Assignments/assignment2/assignment
2//colab_requirements.txt (line 3)) (23.1.0)
Requirement already satisfied: argon2-cffi-bindings==21.2.0 in /usr/local/lib/python
3.10/dist-packages (from -r /content/drive/My Drive/CS6353/Assignments/assignment2/as
signment2//colab_requirements.txt (line 4)) (21.2.0)
Collecting arrow==1.2.3 (from -r /content/drive/My Drive/CS6353/Assignments/assignmen
t2/assignment2//colab requirements.txt (line 5))
  Downloading arrow-1.2.3-py3-none-any.whl.metadata (6.9 kB)
Collecting asttokens==2.2.1 (from -r /content/drive/My Drive/CS6353/Assignments/assig
nment2/assignment2//colab_requirements.txt (line 6))
  Downloading asttokens-2.2.1-py2.py3-none-any.whl.metadata (4.8 kB)
Collecting async-lru==2.0.4 (from -r /content/drive/My Drive/CS6353/Assignments/assig
nment2/assignment2//colab_requirements.txt (line 7))
  Downloading async_lru-2.0.4-py3-none-any.whl.metadata (4.5 kB)
Collecting attrs==23.1.0 (from -r /content/drive/My Drive/CS6353/Assignments/assignme
nt2/assignment2//colab requirements.txt (line 8))
  Downloading attrs-23.1.0-py3-none-any.whl.metadata (11 kB)
Collecting Babel==2.12.1 (from -r /content/drive/My Drive/CS6353/Assignments/assignme
nt2/assignment2//colab_requirements.txt (line 9))
  Downloading Babel-2.12.1-py3-none-any.whl.metadata (1.3 kB)
Requirement already satisfied: backcall==0.2.0 in /usr/local/lib/python3.10/dist-pack
ages (from -r /content/drive/My Drive/CS6353/Assignments/assignment2/assignment2//col
ab_requirements.txt (line 10)) (0.2.0)
Collecting beautifulsoup4==4.12.2 (from -r /content/drive/My Drive/CS6353/Assignment
s/assignment2/assignment2//colab_requirements.txt (line 11))
  Downloading beautifulsoup4-4.12.2-py3-none-any.whl.metadata (3.6 kB)
Collecting bleach==6.0.0 (from -r /content/drive/My Drive/CS6353/Assignments/assignme
nt2/assignment2//colab requirements.txt (line 12))
  Downloading bleach-6.0.0-py3-none-any.whl.metadata (29 kB)
```

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Collecting certifi==2023.7.22 (from -r /content/drive/My Drive/CS6353/Assignments/ass
ignment2/assignment2//colab_requirements.txt (line 13))
  Downloading certifi-2023.7.22-py3-none-any.whl.metadata (2.2 kB)
Collecting cffi==1.15.1 (from -r /content/drive/My Drive/CS6353/Assignments/assignmen
t2/assignment2//colab_requirements.txt (line 14))
  Downloading cffi-1.15.1-cp310-cp310-manylinux_2_17_x86_64.manylinux2014_x86 64.whl.
metadata (1.1 kB)
Collecting charset-normalizer==3.2.0 (from -r /content/drive/My Drive/CS6353/Assignme
nts/assignment2/assignment2//colab_requirements.txt (line 15))
  Downloading charset_normalizer-3.2.0-cp310-cp310-manylinux_2_17_x86_64.manylinux201
4 x86 64.whl.metadata (31 kB)
Collecting comm==0.1.4 (from -r /content/drive/My Drive/CS6353/Assignments/assignment
2/assignment2//colab_requirements.txt (line 16))
  Downloading comm-0.1.4-py3-none-any.whl.metadata (4.2 kB)
Collecting contourpy==1.1.0 (from -r /content/drive/My Drive/CS6353/Assignments/assig
nment2/assignment2//colab_requirements.txt (line 17))
  Downloading contourpy-1.1.0-cp310-cp310-manylinux_2_17_x86_64.manylinux2014_x86_64.
whl.metadata (5.7 kB)
Collecting cycler==0.11.0 (from -r /content/drive/My Drive/CS6353/Assignments/assignm
ent2/assignment2//colab requirements.txt (line 18))
  Downloading cycler-0.11.0-py3-none-any.whl.metadata (785 bytes)
Collecting debugpy==1.6.7.post1 (from -r /content/drive/My Drive/CS6353/Assignments/a
ssignment2/assignment2//colab_requirements.txt (line 19))
  Downloading debugpy-1.6.7.post1-cp310-cp310-manylinux_2_17_x86_64.manylinux2014_x86
64.whl.metadata (1.1 kB)
Requirement already satisfied: decorator<=5.0 in /usr/local/lib/python3.10/dist-packa
ges (from -r /content/drive/My Drive/CS6353/Assignments/assignment2/assignment2//cola
b_requirements.txt (line 20)) (4.4.2)
Requirement already satisfied: defusedxml==0.7.1 in /usr/local/lib/python3.10/dist-pa
ckages (from -r /content/drive/My Drive/CS6353/Assignments/assignment2//cs
olab_requirements.txt (line 21)) (0.7.1)
Collecting executing==1.2.0 (from -r /content/drive/My Drive/CS6353/Assignments/assig
nment2/assignment2//colab requirements.txt (line 22))
  Downloading executing-1.2.0-py2.py3-none-any.whl.metadata (8.9 kB)
Collecting fastjsonschema==2.18.0 (from -r /content/drive/My Drive/CS6353/Assignment
s/assignment2/assignment2//colab_requirements.txt (line 23))
  Downloading fastjsonschema-2.18.0-py3-none-any.whl.metadata (2.0 kB)
Collecting fonttools==4.42.1 (from -r /content/drive/My Drive/CS6353/Assignments/assi
gnment2/assignment2//colab requirements.txt (line 24))
  Downloading fonttools-4.42.1-cp310-cp310-manylinux_2_17_x86_64.manylinux2014_x86_6
4.whl.metadata (150 kB)
                                         ---- 151.0/151.0 kB 4.9 MB/s eta 0:00:00
Collecting fqdn==1.5.1 (from -r /content/drive/My Drive/CS6353/Assignments/assignment
2/assignment2//colab_requirements.txt (line 25))
  Downloading fqdn-1.5.1-py3-none-any.whl.metadata (1.4 kB)
Collecting idna==3.4 (from -r /content/drive/My Drive/CS6353/Assignments/assignment2/
assignment2//colab requirements.txt (line 26))
  Downloading idna-3.4-py3-none-any.whl.metadata (9.8 kB)
Collecting imageio==2.31.1 (from -r /content/drive/My Drive/CS6353/Assignments/assign
ment2/assignment2//colab_requirements.txt (line 27))
  Downloading imageio-2.31.1-py3-none-any.whl.metadata (4.7 kB)
Requirement already satisfied: ipykernel<=5.5.6 in /usr/local/lib/python3.10/dist-pac
kages (from -r /content/drive/My Drive/CS6353/Assignments/assignment2/assignment2//co
lab_requirements.txt (line 28)) (5.5.6)
Requirement already satisfied: ipython<=7.34.0 in /usr/local/lib/python3.10/dist-pack
ages (from -r /content/drive/My Drive/CS6353/Assignments/assignment2/assignment2//col
ab_requirements.txt (line 29)) (7.34.0)
Collecting isoduration==20.11.0 (from -r /content/drive/My Drive/CS6353/Assignments/a
ssignment2/assignment2//colab requirements.txt (line 30))
  Downloading isoduration-20.11.0-py3-none-any.whl.metadata (5.7 kB)
```

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Collecting jedi==0.19.0 (from -r /content/drive/My Drive/CS6353/Assignments/assignmen
t2/assignment2//colab_requirements.txt (line 31))
  Downloading jedi-0.19.0-py2.py3-none-any.whl.metadata (22 kB)
Collecting Jinja2==3.1.2 (from -r /content/drive/My Drive/CS6353/Assignments/assignme
nt2/assignment2//colab_requirements.txt (line 32))
  Downloading Jinja2-3.1.2-py3-none-any.whl.metadata (3.5 kB)
Collecting json5==0.9.14 (from -r /content/drive/My Drive/CS6353/Assignments/assignme
nt2/assignment2//colab_requirements.txt (line 33))
  Downloading json5-0.9.14-py2.py3-none-any.whl.metadata (10 kB)
Collecting jsonpointer==2.4 (from -r /content/drive/My Drive/CS6353/Assignments/assig
nment2/assignment2//colab requirements.txt (line 34))
  Downloading jsonpointer-2.4-py2.py3-none-any.whl.metadata (2.5 kB)
Collecting jsonschema==4.19.0 (from -r /content/drive/My Drive/CS6353/Assignments/ass
ignment2/assignment2//colab_requirements.txt (line 35))
  Downloading jsonschema-4.19.0-py3-none-any.whl.metadata (8.2 kB)
Collecting jsonschema-specifications==2023.7.1 (from -r /content/drive/My Drive/CS635
3/Assignments/assignment2/assignment2//colab requirements.txt (line 36))
  Downloading jsonschema_specifications-2023.7.1-py3-none-any.whl.metadata (2.8 kB)
Collecting jupyter-events==0.7.0 (from -r /content/drive/My Drive/CS6353/Assignments/
assignment2/assignment2//colab requirements.txt (line 37))
  Downloading jupyter_events-0.7.0-py3-none-any.whl.metadata (5.5 kB)
Collecting jupyter-lsp==2.2.0 (from -r /content/drive/My Drive/CS6353/Assignments/ass
ignment2/assignment2//colab_requirements.txt (line 38))
  Downloading jupyter_lsp-2.2.0-py3-none-any.whl.metadata (1.8 kB)
Requirement already satisfied: jupyter_client<8.0 in /usr/local/lib/python3.10/dist-p
ackages (from -r /content/drive/My Drive/CS6353/Assignments/assignment2/assignment2/
colab_requirements.txt (line 39)) (6.1.12)
Collecting jupyter_core==5.3.1 (from -r /content/drive/My Drive/CS6353/Assignments/as
signment2/assignment2//colab_requirements.txt (line 40))
  Downloading jupyter_core-5.3.1-py3-none-any.whl.metadata (3.4 kB)
Collecting jupyter_server==2.7.2 (from -r /content/drive/My Drive/CS6353/Assignments/
assignment2/assignment2//colab_requirements.txt (line 41))
  Downloading jupyter_server-2.7.2-py3-none-any.whl.metadata (8.6 kB)
Collecting jupyter_server_terminals==0.4.4 (from -r /content/drive/My Drive/CS6353/As
signments/assignment2//colab requirements.txt (line 42))
  Downloading jupyter_server_terminals-0.4.4-py3-none-any.whl.metadata (6.3 kB)
Collecting jupyterlab==4.0.5 (from -r /content/drive/My Drive/CS6353/Assignments/assi
gnment2/assignment2//colab requirements.txt (line 43))
  Downloading jupyterlab-4.0.5-py3-none-any.whl.metadata (15 kB)
Collecting jupyterlab-pygments==0.2.2 (from -r /content/drive/My Drive/CS6353/Assignm
ents/assignment2/assignment2//colab_requirements.txt (line 44))
  Downloading jupyterlab_pygments-0.2.2-py2.py3-none-any.whl.metadata (1.9 kB)
Collecting jupyterlab server==2.24.0 (from -r /content/drive/My Drive/CS6353/Assignme
nts/assignment2/assignment2//colab_requirements.txt (line 45))
  Downloading jupyterlab_server-2.24.0-py3-none-any.whl.metadata (5.8 kB)
Collecting kiwisolver==1.4.5 (from -r /content/drive/My Drive/CS6353/Assignments/assi
gnment2/assignment2//colab requirements.txt (line 46))
  Downloading kiwisolver-1.4.5-cp310-cp310-manylinux_2_12_x86_64.manylinux2010_x86_6
4.whl.metadata (6.4 kB)
Collecting MarkupSafe==2.1.3 (from -r /content/drive/My Drive/CS6353/Assignments/assi
gnment2/assignment2//colab_requirements.txt (line 47))
 Downloading MarkupSafe-2.1.3-cp310-cp310-manylinux_2_17_x86_64.manylinux2014_x86_6
4.whl.metadata (3.0 kB)
Collecting matplotlib==3.7.2 (from -r /content/drive/My Drive/CS6353/Assignments/assi
gnment2/assignment2//colab_requirements.txt (line 48))
 Downloading matplotlib-3.7.2-cp310-cp310-manylinux_2_17_x86_64.manylinux2014_x86_6
4.whl.metadata (5.6 kB)
Collecting matplotlib-inline==0.1.6 (from -r /content/drive/My Drive/CS6353/Assignmen
ts/assignment2/assignment2//colab_requirements.txt (line 49))
  Downloading matplotlib_inline-0.1.6-py3-none-any.whl.metadata (2.8 kB)
```

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Collecting mistune==3.0.1 (from -r /content/drive/My Drive/CS6353/Assignments/assignm
ent2/assignment2//colab_requirements.txt (line 50))
  Downloading mistune-3.0.1-py3-none-any.whl.metadata (1.7 kB)
Collecting nbclient==0.8.0 (from -r /content/drive/My Drive/CS6353/Assignments/assign
ment2/assignment2//colab_requirements.txt (line 51))
  Downloading nbclient-0.8.0-py3-none-any.whl.metadata (7.8 kB)
Collecting nbconvert==7.7.4 (from -r /content/drive/My Drive/CS6353/Assignments/assig
nment2/assignment2//colab_requirements.txt (line 52))
  Downloading nbconvert-7.7.4-py3-none-any.whl.metadata (8.0 kB)
Collecting nbformat==5.9.2 (from -r /content/drive/My Drive/CS6353/Assignments/assign
ment2/assignment2//colab_requirements.txt (line 53))
  Downloading nbformat-5.9.2-py3-none-any.whl.metadata (3.4 kB)
Collecting nest-asyncio==1.5.7 (from -r /content/drive/My Drive/CS6353/Assignments/as
signment2/assignment2//colab_requirements.txt (line 54))
  Downloading nest asyncio-1.5.7-py3-none-any.whl.metadata (2.7 kB)
Collecting notebook_shim==0.2.3 (from -r /content/drive/My Drive/CS6353/Assignments/a
ssignment2/assignment2//colab requirements.txt (line 55))
  Downloading notebook_shim-0.2.3-py3-none-any.whl.metadata (4.0 kB)
Collecting numpy<1.24,>=1.22 (from -r /content/drive/My Drive/CS6353/Assignments/assi
gnment2/assignment2//colab requirements.txt (line 56))
  Downloading numpy-1.23.5-cp310-cp310-manylinux_2_17_x86_64.manylinux2014_x86_64.wh
1.metadata (2.3 kB)
Collecting overrides==7.4.0 (from -r /content/drive/My Drive/CS6353/Assignments/assig
nment2/assignment2//colab_requirements.txt (line 57))
  Downloading overrides-7.4.0-py3-none-any.whl.metadata (5.7 kB)
Collecting packaging==23.1 (from -r /content/drive/My Drive/CS6353/Assignments/assign
ment2/assignment2//colab_requirements.txt (line 58))
  Downloading packaging-23.1-py3-none-any.whl.metadata (3.1 kB)
Collecting pandas<=1.5.3 (from -r /content/drive/My Drive/CS6353/Assignments/assignme
nt2/assignment2//colab_requirements.txt (line 59))
  Downloading pandas-1.5.3-cp310-cp310-manylinux_2_17_x86_64.manylinux2014_x86_64.wh
1.metadata (11 kB)
Collecting pandocfilters==1.5.0 (from -r /content/drive/My Drive/CS6353/Assignments/a
ssignment2/assignment2//colab_requirements.txt (line 60))
  Downloading pandocfilters-1.5.0-py2.py3-none-any.whl.metadata (9.0 kB)
Collecting parso==0.8.3 (from -r /content/drive/My Drive/CS6353/Assignments/assignmen
t2/assignment2//colab_requirements.txt (line 61))
  Downloading parso-0.8.3-py2.py3-none-any.whl.metadata (7.5 kB)
Collecting pexpect==4.8.0 (from -r /content/drive/My Drive/CS6353/Assignments/assignm
ent2/assignment2//colab_requirements.txt (line 62))
  Downloading pexpect-4.8.0-py2.py3-none-any.whl.metadata (2.2 kB)
Requirement already satisfied: pickleshare==0.7.5 in /usr/local/lib/python3.10/dist-p
ackages (from -r /content/drive/My Drive/CS6353/Assignments/assignment2/assignment2/
colab_requirements.txt (line 63)) (0.7.5)
Collecting Pillow==10.0.0 (from -r /content/drive/My Drive/CS6353/Assignments/assignm
ent2/assignment2//colab_requirements.txt (line 64))
  Downloading Pillow-10.0.0-cp310-cp310-manylinux_2_28_x86_64.whl.metadata (9.5 kB)
Collecting platformdirs==3.10.0 (from -r /content/drive/My Drive/CS6353/Assignments/a
ssignment2/assignment2//colab_requirements.txt (line 65))
  Downloading platformdirs-3.10.0-py3-none-any.whl.metadata (11 kB)
Collecting prometheus-client==0.17.1 (from -r /content/drive/My Drive/CS6353/Assignme
nts/assignment2/assignment2//colab requirements.txt (line 66))
  Downloading prometheus_client-0.17.1-py3-none-any.whl.metadata (24 kB)
Collecting prompt-toolkit==3.0.39 (from -r /content/drive/My Drive/CS6353/Assignment
s/assignment2/assignment2//colab_requirements.txt (line 67))
  Downloading prompt toolkit-3.0.39-py3-none-any.whl.metadata (6.4 kB)
Requirement already satisfied: psutil==5.9.5 in /usr/local/lib/python3.10/dist-packag
es (from -r /content/drive/My Drive/CS6353/Assignments/assignment2/assignment2//colab
requirements.txt (line 68)) (5.9.5)
Requirement already satisfied: ptyprocess==0.7.0 in /usr/local/lib/python3.10/dist-pa
```

olab_requirements.txt (line 69)) (0.7.0)

```
Collecting pure-eval==0.2.2 (from -r /content/drive/My Drive/CS6353/Assignments/assig
nment2/assignment2//colab requirements.txt (line 70))
  Downloading pure_eval-0.2.2-py3-none-any.whl.metadata (6.2 kB)
Collecting pycparser==2.21 (from -r /content/drive/My Drive/CS6353/Assignments/assign
ment2/assignment2//colab requirements.txt (line 71))
  Downloading pycparser-2.21-py2.py3-none-any.whl.metadata (1.1 kB)
Collecting Pygments==2.16.1 (from -r /content/drive/My Drive/CS6353/Assignments/assig
nment2/assignment2//colab_requirements.txt (line 72))
  Downloading Pygments-2.16.1-py3-none-any.whl.metadata (2.5 kB)
Collecting pyparsing==3.0.9 (from -r /content/drive/My Drive/CS6353/Assignments/assig
nment2/assignment2//colab_requirements.txt (line 73))
  Downloading pyparsing-3.0.9-py3-none-any.whl.metadata (4.2 kB)
Requirement already satisfied: python-dateutil==2.8.2 in /usr/local/lib/python3.10/di
st-packages (from -r /content/drive/My Drive/CS6353/Assignments/assignment2/assignmen
t2//colab requirements.txt (line 74)) (2.8.2)
Collecting python-json-logger==2.0.7 (from -r /content/drive/My Drive/CS6353/Assignme
nts/assignment2/assignment2//colab requirements.txt (line 75))
  Downloading python json logger-2.0.7-py3-none-any.whl.metadata (6.5 kB)
Collecting pytz==2023.3 (from -r /content/drive/My Drive/CS6353/Assignments/assignmen
t2/assignment2//colab_requirements.txt (line 76))
  Downloading pytz-2023.3-py2.py3-none-any.whl.metadata (22 kB)
Collecting PyYAML==6.0.1 (from -r /content/drive/My Drive/CS6353/Assignments/assignme
nt2/assignment2//colab requirements.txt (line 77))
 Downloading PyYAML-6.0.1-cp310-cp310-manylinux_2_17_x86_64.manylinux2014_x86_64.wh
1.metadata (2.1 kB)
Requirement already satisfied: pyzmq<25 in /usr/local/lib/python3.10/dist-packages (f
rom -r /content/drive/My Drive/CS6353/Assignments/assignment2/assignment2//colab_requ
irements.txt (line 78)) (24.0.1)
Collecting referencing==0.30.2 (from -r /content/drive/My Drive/CS6353/Assignments/as
signment2/assignment2//colab_requirements.txt (line 79))
  Downloading referencing-0.30.2-py3-none-any.whl.metadata (2.6 kB)
Collecting requests==2.31.0 (from -r /content/drive/My Drive/CS6353/Assignments/assig
nment2/assignment2//colab requirements.txt (line 80))
  Downloading requests-2.31.0-py3-none-any.whl.metadata (4.6 kB)
Collecting rfc3339-validator==0.1.4 (from -r /content/drive/My Drive/CS6353/Assignmen
ts/assignment2/assignment2//colab requirements.txt (line 81))
  Downloading rfc3339_validator-0.1.4-py2.py3-none-any.whl.metadata (1.5 kB)
Collecting rfc3986-validator==0.1.1 (from -r /content/drive/My Drive/CS6353/Assignmen
ts/assignment2/assignment2//colab_requirements.txt (line 82))
  Downloading rfc3986_validator-0.1.1-py2.py3-none-any.whl.metadata (1.7 kB)
Collecting rpds-py==0.9.2 (from -r /content/drive/My Drive/CS6353/Assignments/assignm
ent2/assignment2//colab_requirements.txt (line 83))
  Downloading rpds_py-0.9.2-cp310-cp310-manylinux_2_17_x86_64.manylinux2014_x86_64.wh
1.metadata (3.7 kB)
Collecting scipy==1.11.2 (from -r /content/drive/My Drive/CS6353/Assignments/assignme
nt2/assignment2//colab requirements.txt (line 84))
  Downloading scipy-1.11.2-cp310-cp310-manylinux_2_17_x86_64.manylinux2014_x86_64.wh
1.metadata (59 kB)
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Collecting seaborn==0.12.2 (from -r /content/drive/My Drive/CS6353/Assignments/assign
ment2/assignment2//colab_requirements.txt (line 85))
  Downloading seaborn-0.12.2-py3-none-any.whl.metadata (5.4 kB)
Collecting Send2Trash==1.8.2 (from -r /content/drive/My Drive/CS6353/Assignments/assi
gnment2/assignment2//colab_requirements.txt (line 86))
  Downloading Send2Trash-1.8.2-py3-none-any.whl.metadata (4.0 kB)
Requirement already satisfied: six==1.16.0 in /usr/local/lib/python3.10/dist-packages
(from -r /content/drive/My Drive/CS6353/Assignments/assignment2/assignment2//colab_re
quirements.txt (line 87)) (1.16.0)
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ckages (from -r /content/drive/My Drive/CS6353/Assignments/assignment2//csignment2//c

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Collecting sniffio==1.3.0 (from -r /content/drive/My Drive/CS6353/Assignments/assignm
ent2/assignment2//colab_requirements.txt (line 88))
  Downloading sniffio-1.3.0-py3-none-any.whl.metadata (3.6 kB)
Collecting soupsieve==2.4.1 (from -r /content/drive/My Drive/CS6353/Assignments/assig
nment2/assignment2//colab_requirements.txt (line 89))
  Downloading soupsieve-2.4.1-py3-none-any.whl.metadata (4.7 kB)
Collecting stack-data==0.6.2 (from -r /content/drive/My Drive/CS6353/Assignments/assi
gnment2/assignment2//colab_requirements.txt (line 90))
  Downloading stack_data-0.6.2-py3-none-any.whl.metadata (18 kB)
Collecting terminado==0.17.1 (from -r /content/drive/My Drive/CS6353/Assignments/assi
gnment2/assignment2//colab_requirements.txt (line 91))
  Downloading terminado-0.17.1-py3-none-any.whl.metadata (5.9 kB)
Collecting tinycss2==1.2.1 (from -r /content/drive/My Drive/CS6353/Assignments/assign
ment2/assignment2//colab_requirements.txt (line 92))
  Downloading tinycss2-1.2.1-py3-none-any.whl.metadata (3.0 kB)
Collecting tornado<=6.3.2 (from -r /content/drive/My Drive/CS6353/Assignments/assignm
ent2/assignment2//colab requirements.txt (line 93))
  Downloading tornado-6.3.2-cp38-abi3-manylinux_2_5_x86_64.manylinux1_x86_64.manylinu
x_2_17_x86_64.manylinux2014_x86_64.whl.metadata (2.5 kB)
Collecting traitlets==5.9.0 (from -r /content/drive/My Drive/CS6353/Assignments/assig
nment2/assignment2//colab_requirements.txt (line 94))
  Downloading traitlets-5.9.0-py3-none-any.whl.metadata (10 kB)
Collecting tzdata==2023.3 (from -r /content/drive/My Drive/CS6353/Assignments/assignm
ent2/assignment2//colab_requirements.txt (line 95))
  Downloading tzdata-2023.3-py2.py3-none-any.whl.metadata (1.4 kB)
Collecting uri-template==1.3.0 (from -r /content/drive/My Drive/CS6353/Assignments/as
signment2/assignment2//colab_requirements.txt (line 96))
  Downloading uri_template-1.3.0-py3-none-any.whl.metadata (8.8 kB)
Collecting urllib3==2.0.4 (from -r /content/drive/My Drive/CS6353/Assignments/assignm
ent2/assignment2//colab_requirements.txt (line 97))
  Downloading urllib3-2.0.4-py3-none-any.whl.metadata (6.6 kB)
Collecting wcwidth==0.2.6 (from -r /content/drive/My Drive/CS6353/Assignments/assignm
ent2/assignment2//colab requirements.txt (line 98))
  Downloading wcwidth-0.2.6-py2.py3-none-any.whl.metadata (11 kB)
Collecting webcolors==1.13 (from -r /content/drive/My Drive/CS6353/Assignments/assign
ment2/assignment2//colab_requirements.txt (line 99))
  Downloading webcolors-1.13-py3-none-any.whl.metadata (2.6 kB)
Requirement already satisfied: webencodings==0.5.1 in /usr/local/lib/python3.10/dist-
packages (from -r /content/drive/My Drive/CS6353/Assignments/assignment2/assignment
2//colab_requirements.txt (line 100)) (0.5.1)
Collecting websocket-client==1.6.2 (from -r /content/drive/My Drive/CS6353/Assignment
s/assignment2/assignment2//colab_requirements.txt (line 101))
  Downloading websocket client-1.6.2-py3-none-any.whl.metadata (7.5 kB)
Requirement already satisfied: exceptiongroup in /usr/local/lib/python3.10/dist-packa
ges (from anyio==3.7.1->-r /content/drive/My Drive/CS6353/Assignments/assignment2/ass
ignment2//colab_requirements.txt (line 1)) (1.2.2)
Requirement already satisfied: typing-extensions>=4.0.0 in /usr/local/lib/python3.10/
dist-packages (from async-lru==2.0.4->-r /content/drive/My Drive/CS6353/Assignments/a
ssignment2/assignment2//colab_requirements.txt (line 7)) (4.12.2)
Collecting jupyter_client<8.0 (from -r /content/drive/My Drive/CS6353/Assignments/ass
ignment2/assignment2//colab_requirements.txt (line 39))
 Downloading jupyter client-7.4.9-py3-none-any.whl.metadata (8.5 kB)
Requirement already satisfied: tomli in /usr/local/lib/python3.10/dist-packages (from
jupyterlab==4.0.5->-r /content/drive/My Drive/CS6353/Assignments/assignment2/assignme
nt2//colab_requirements.txt (line 43)) (2.0.1)
Requirement already satisfied: ipython-genutils in /usr/local/lib/python3.10/dist-pac
kages (from ipykernel<=5.5.6->-r /content/drive/My Drive/CS6353/Assignments/assignmen
t2/assignment2//colab_requirements.txt (line 28)) (0.2.0)
Requirement already satisfied: setuptools>=18.5 in /usr/local/lib/python3.10/dist-pac
kages (from ipython<=7.34.0->-r /content/drive/My Drive/CS6353/Assignments/assignment
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2/assignment2//colab requirements.txt (line 29)) (71.0.4)
Requirement already satisfied: entrypoints in /usr/local/lib/python3.10/dist-packages
(from jupyter_client<8.0->-r /content/drive/My Drive/CS6353/Assignments/assignment2/a
ssignment2//colab requirements.txt (line 39)) (0.4)
Downloading appnope-0.1.3-py2.py3-none-any.whl (4.4 kB)
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Downloading asttokens-2.2.1-py2.py3-none-any.whl (26 kB)
Downloading async_lru-2.0.4-py3-none-any.whl (6.1 kB)
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Downloading Babel-2.12.1-py3-none-any.whl (10.1 MB)
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Downloading beautifulsoup4-4.12.2-py3-none-any.whl (142 kB)
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Downloading bleach-6.0.0-py3-none-any.whl (162 kB)
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Downloading certifi-2023.7.22-py3-none-any.whl (158 kB)
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Downloading cffi-1.15.1-cp310-cp310-manylinux_2_17_x86_64.manylinux2014_x86_64.whl (4
41 kB)
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4.whl (3.0 MB)
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hl (4.5 MB)
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Downloading json5-0.9.14-py2.py3-none-any.whl (19 kB)
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Downloading notebook shim-0.2.3-py3-none-any.whl (13 kB)
Downloading overrides-7.4.0-py3-none-any.whl (17 kB)
Downloading packaging-23.1-py3-none-any.whl (48 kB)
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Downloading pandocfilters-1.5.0-py2.py3-none-any.whl (8.7 kB)
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Downloading tornado-6.3.2-cp38-abi3-manylinux_2_5_x86_64.manylinux1_x86_64.manylinux_
2_17_x86_64.manylinux2014_x86_64.whl (426 kB)
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Installing collected packages: wcwidth, pytz, pure-eval, json5, fastjsonschema, execu
ting, appnope, websocket-client, webcolors, urllib3, uri-template, tzdata, traitlets,
tornado, tinycss2, soupsieve, sniffio, Send2Trash, rpds-py, rfc3986-validator, rfc333
9-validator, PyYAML, python-json-logger, pyparsing, Pygments, pycparser, prompt-toolk
it, prometheus-client, platformdirs, Pillow, pexpect, parso, pandocfilters, packagin
g, overrides, numpy, nest-asyncio, mistune, MarkupSafe, kiwisolver, jupyterlab-pygmen
ts, jsonpointer, idna, fqdn, fonttools, debugpy, cycler, charset-normalizer, certifi,
bleach, Babel, attrs, async-lru, asttokens, terminado, stack-data, scipy, requests, r
eferencing, pandas, matplotlib-inline, jupyter core, Jinja2, jedi, imageio, contourp
y, comm, cffi, beautifulsoup4, arrow, matplotlib, jupyter_server_terminals, jupyter_c
lient, jsonschema-specifications, isoduration, seaborn, jsonschema, nbformat, nbclien
t, jupyter-events, nbconvert, jupyter_server, notebook_shim, jupyterlab_server, jupyt
er-lsp, jupyterlab
 Attempting uninstall: wcwidth
    Found existing installation: wcwidth 0.2.13
    Uninstalling wcwidth-0.2.13:
      Successfully uninstalled wcwidth-0.2.13
 Attempting uninstall: pytz
    Found existing installation: pytz 2024.2
   Uninstalling pytz-2024.2:
      Successfully uninstalled pytz-2024.2
 Attempting uninstall: fastjsonschema
    Found existing installation: fastjsonschema 2.20.0
    Uninstalling fastjsonschema-2.20.0:
      Successfully uninstalled fastjsonschema-2.20.0
 Attempting uninstall: websocket-client
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s that are installed. This behaviour is the source of the following dependency confli
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wcwidth-0.2.6 webcolors-1.13 websocket-client-1.6.2
```

Image features exercise

Complete and hand in this completed worksheet (including its outputs and any supporting code outside of the worksheet) with your assignment submission. For more details see the assignments page on the course website.

We have seen that we can achieve reasonable performance on an image classification task by training a linear classifier on the pixels of the input image. In this exercise we will show that we can improve our classification performance by training linear classifiers not on raw pixels but on features that are computed from the raw pixels.

All of your work for this exercise will be done in this notebook.

```
In []: from __future__ import print_function
    import random
    import numpy as np
    from cs6353.data_utils import load_CIFAR10
    import matplotlib.pyplot as plt

// wmatplotlib inline
    plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
    plt.rcParams['image.interpolation'] = 'nearest'
    plt.rcParams['image.cmap'] = 'gray'

# for auto-reloading extenrnal modules
    # see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ipython
    %load_ext autoreload
    %autoreload 2
```

Load data

Similar to previous exercises, we will load CIFAR-10 data from disk.

```
In [ ]: from cs6353.features import color_histogram_hsv, hog_feature
         def get_CIFAR10_data(cifar10_dir='cs6353/datasets/cifar-10-batches-py', num_training=4
             # Load the raw CIFAR-10 data
             X_train, y_train, X_test, y_test = load_CIFAR10(cifar10_dir)
             # Subsample the data
             mask = list(range(num_training, num_training + num_validation))
             X val = X train[mask]
             y_val = y_train[mask]
             mask = list(range(num_training))
             X_train = X_train[mask]
             y_train = y_train[mask]
             mask = list(range(num test))
             X_{\text{test}} = X_{\text{test}}[mask]
             y_{\text{test}} = y_{\text{test}}[mask]
             return X_train, y_train, X_val, y_val, X_test, y_test
         # Cleaning up variables to prevent loading data multiple times (which may cause memory
         try:
            del X_train, y_train
            del X_test, y_test
            print('Clear previously loaded data.')
         except:
            pass
```

Extract Features

For each image we will compute a Histogram of Oriented Gradients (HOG) as well as a color histogram using the hue channel in HSV color space. We form our final feature vector for each image by concatenating the HOG and color histogram feature vectors.

Roughly speaking, HOG should capture the texture of the image while ignoring color information, and the color histogram represents the color of the input image while ignoring texture. As a result, we expect that using both together ought to work better than using either alone. Verifying this assumption would be a good thing to try for your interests.

The hog_feature and color_histogram_hsv functions both operate on a single image and return a feature vector for that image. The extract_features function takes a set of images and a list of feature functions and evaluates each feature function on each image, storing the results in a matrix where each column is the concatenation of all feature vectors for a single image.

```
In [ ]: from cs6353.features import *
        num_color_bins = 10 # Number of bins in the color histogram
        feature_fns = [hog_feature, lambda img: color_histogram_hsv(img, nbin=num_color_bins)]
        X_train_feats = extract_features(X_train, feature_fns, verbose=True)
        X_val_feats = extract_features(X_val, feature_fns)
        X_test_feats = extract_features(X_test, feature_fns)
        # Preprocessing: Subtract the mean feature
        mean_feat = np.mean(X_train_feats, axis=0, keepdims=True)
        X_train_feats -= mean_feat
        X_val_feats -= mean_feat
        X_test_feats -= mean_feat
        # Preprocessing: Divide by standard deviation. This ensures that each feature
        # has roughly the same scale.
        std_feat = np.std(X_train_feats, axis=0, keepdims=True)
        X_train_feats /= std_feat
        X val feats /= std feat
        X_test_feats /= std_feat
        # Preprocessing: Add a bias dimension
        X_train_feats = np.hstack([X_train_feats, np.ones((X_train_feats.shape[0], 1))])
        X_val_feats = np.hstack([X_val_feats, np.ones((X_val_feats.shape[0], 1))])
        X_test_feats = np.hstack([X_test_feats, np.ones((X_test_feats.shape[0], 1))])
```

Done extracting features for 1000 / 49000 images Done extracting features for 2000 / 49000 images Done extracting features for 3000 / 49000 images Done extracting features for 4000 / 49000 images Done extracting features for 5000 / 49000 images Done extracting features for 6000 / 49000 images Done extracting features for 7000 / 49000 images Done extracting features for 8000 / 49000 images Done extracting features for 9000 / 49000 images Done extracting features for 10000 / 49000 images Done extracting features for 11000 / 49000 images Done extracting features for 12000 / 49000 images Done extracting features for 13000 / 49000 images Done extracting features for 14000 / 49000 images Done extracting features for 15000 / 49000 images Done extracting features for 16000 / 49000 images Done extracting features for 17000 / 49000 images Done extracting features for 18000 / 49000 images Done extracting features for 19000 / 49000 images Done extracting features for 20000 / 49000 images Done extracting features for 21000 / 49000 images Done extracting features for 22000 / 49000 images Done extracting features for 23000 / 49000 images Done extracting features for 24000 / 49000 images Done extracting features for 25000 / 49000 images Done extracting features for 26000 / 49000 images Done extracting features for 27000 / 49000 images Done extracting features for 28000 / 49000 images Done extracting features for 29000 / 49000 images Done extracting features for 30000 / 49000 images Done extracting features for 31000 / 49000 images Done extracting features for 32000 / 49000 images Done extracting features for 33000 / 49000 images Done extracting features for 34000 / 49000 images Done extracting features for 35000 / 49000 images Done extracting features for 36000 / 49000 images Done extracting features for 37000 / 49000 images Done extracting features for 38000 / 49000 images Done extracting features for 39000 / 49000 images Done extracting features for 40000 / 49000 images Done extracting features for 41000 / 49000 images Done extracting features for 42000 / 49000 images Done extracting features for 43000 / 49000 images Done extracting features for 44000 / 49000 images Done extracting features for 45000 / 49000 images Done extracting features for 46000 / 49000 images Done extracting features for 47000 / 49000 images Done extracting features for 48000 / 49000 images

Train SVM on features

Using the multiclass SVM code developed earlier in the assignment, train SVMs on top of the features extracted above; this should achieve better results than training SVMs directly on top of raw pixels.

In []: # Use the validation set to tune the learning rate and regularization strength

```
from cs6353.classifiers.linear classifier import LinearSVM
learning_rates = [1e-7, 1e-5, 1e-4, 1e-3, 2e-7]
regularization_strengths = [1, 1e-1, 2e-1, 5e-1, 1e-2, 5e3]
results = {}
best val = -1
best_svm = None
# TODO:
# Use the validation set to set the learning rate and regularization strength. #
# This should be identical to the validation that you did for the SVM; save
# the best trained classifier in best_svm. You might also want to play
# with different numbers of bins in the color histogram. If you are careful
                                                                 #
# you should be able to get accuracy of near 0.44 on the validation set.
                                                                 #
for lr in learning_rates:
   for reg in regularization strengths:
      svm = LinearSVM()
      svm.train(X_train_feats, y_train, learning_rate=lr, reg=reg, num_iters=1500, \)
      y train pred = svm.predict(X train feats)
      y_val_pred = svm.predict(X_val_feats)
      train_results = y_train_pred == y_train
      y_train_accuracy = np.mean(train_results)
      val_results = y_val_pred == y_val
      y_val_accuracy = np.mean(val_results)
      results[(lr, reg)] = (y_train_accuracy, y_val_accuracy)
      if y_val_accuracy > best_val:
         best_val = y_val_accuracy
         best svm = svm
END OF YOUR CODE
# Print out results.
for lr, reg in sorted(results):
   train_accuracy, val_accuracy = results[(lr, reg)]
   print('lr %e reg %e train accuracy: %f val accuracy: %f' % (
             lr, reg, train_accuracy, val_accuracy))
print('best validation accuracy achieved during cross-validation: %f' % best_val)
```

iteration 0 / 1500: loss 9.013532 iteration 100 / 1500: loss 9.005905 iteration 200 / 1500: loss 8.999067 iteration 300 / 1500: loss 9.010873 iteration 400 / 1500: loss 9.012125 iteration 500 / 1500: loss 9.006480 iteration 600 / 1500: loss 8.998394 iteration 700 / 1500: loss 8.996802 iteration 800 / 1500: loss 9.006092 iteration 900 / 1500: loss 9.003871 iteration 1000 / 1500: loss 9.006651 iteration 1100 / 1500: loss 8.996429 iteration 1200 / 1500: loss 8.993661 iteration 1300 / 1500: loss 8.987182 iteration 1400 / 1500: loss 8.996445 iteration 0 / 1500: loss 9.000013 iteration 100 / 1500: loss 8.995990 iteration 200 / 1500: loss 8.995294 iteration 300 / 1500: loss 9.006803 iteration 400 / 1500: loss 8.995009 iteration 500 / 1500: loss 8.987107 iteration 600 / 1500: loss 8.997460 iteration 700 / 1500: loss 8.988426 iteration 800 / 1500: loss 8.985681 iteration 900 / 1500: loss 8.985636 iteration 1000 / 1500: loss 8.997433 iteration 1100 / 1500: loss 8.983115 iteration 1200 / 1500: loss 8.985105 iteration 1300 / 1500: loss 8.993259 iteration 1400 / 1500: loss 8.993054 iteration 0 / 1500: loss 8.998570 iteration 100 / 1500: loss 8.971324 iteration 200 / 1500: loss 8.997724 iteration 300 / 1500: loss 8.982777 iteration 400 / 1500: loss 9.003107 iteration 500 / 1500: loss 9.001476 iteration 600 / 1500: loss 8.985405 iteration 700 / 1500: loss 8.991129 iteration 800 / 1500: loss 8.990169 iteration 900 / 1500: loss 8.989853 iteration 1000 / 1500: loss 8.997513 iteration 1100 / 1500: loss 8.988364 iteration 1200 / 1500: loss 8.981983 iteration 1300 / 1500: loss 8.979658 iteration 1400 / 1500: loss 8.979322 iteration 0 / 1500: loss 9.020787 iteration 100 / 1500: loss 9.017756 iteration 200 / 1500: loss 9.009067 iteration 300 / 1500: loss 9.011930 iteration 400 / 1500: loss 9.004455 iteration 500 / 1500: loss 9.006968 iteration 600 / 1500: loss 9.006946 iteration 700 / 1500: loss 9.016035 iteration 800 / 1500: loss 9.002542 iteration 900 / 1500: loss 9.010131 iteration 1000 / 1500: loss 9.013870 iteration 1100 / 1500: loss 8.998080 iteration 1200 / 1500: loss 9.014795 iteration 1300 / 1500: loss 8.999988 iteration 1400 / 1500: loss 9.006232

iteration 0 / 1500: loss 8.992293 iteration 100 / 1500: loss 9.003871 iteration 200 / 1500: loss 9.006667 iteration 300 / 1500: loss 9.015637 iteration 400 / 1500: loss 9.006338 iteration 500 / 1500: loss 9.003154 iteration 600 / 1500: loss 8.997350 iteration 700 / 1500: loss 8.987879 iteration 800 / 1500: loss 8.982116 iteration 900 / 1500: loss 9.008131 iteration 1000 / 1500: loss 8.997903 iteration 1100 / 1500: loss 9.001313 iteration 1200 / 1500: loss 8.991351 iteration 1300 / 1500: loss 8.986975 iteration 1400 / 1500: loss 8.998100 iteration 0 / 1500: loss 16.445010 iteration 100 / 1500: loss 15.079379 iteration 200 / 1500: loss 13.983241 iteration 300 / 1500: loss 13.073827 iteration 400 / 1500: loss 12.329636 iteration 500 / 1500: loss 11.722678 iteration 600 / 1500: loss 11.230366 iteration 700 / 1500: loss 10.831539 iteration 800 / 1500: loss 10.500262 iteration 900 / 1500: loss 10.227037 iteration 1000 / 1500: loss 10.003496 iteration 1100 / 1500: loss 9.818231 iteration 1200 / 1500: loss 9.669582 iteration 1300 / 1500: loss 9.547674 iteration 1400 / 1500: loss 9.450321 iteration 0 / 1500: loss 8.975145 iteration 100 / 1500: loss 8.896527 iteration 200 / 1500: loss 8.834638 iteration 300 / 1500: loss 8.775904 iteration 400 / 1500: loss 8.694544 iteration 500 / 1500: loss 8.638067 iteration 600 / 1500: loss 8.543439 iteration 700 / 1500: loss 8.438022 iteration 800 / 1500: loss 8.474371 iteration 900 / 1500: loss 8.313164 iteration 1000 / 1500: loss 8.326647 iteration 1100 / 1500: loss 8.207184 iteration 1200 / 1500: loss 8.155812 iteration 1300 / 1500: loss 8.114780 iteration 1400 / 1500: loss 8.070573 iteration 0 / 1500: loss 9.000184 iteration 100 / 1500: loss 8.944632 iteration 200 / 1500: loss 8.865356 iteration 300 / 1500: loss 8.796489 iteration 400 / 1500: loss 8.741757 iteration 500 / 1500: loss 8.624932 iteration 600 / 1500: loss 8.556358 iteration 700 / 1500: loss 8.498920 iteration 800 / 1500: loss 8.419911 iteration 900 / 1500: loss 8.314671 iteration 1000 / 1500: loss 8.255334 iteration 1100 / 1500: loss 8.307116 iteration 1200 / 1500: loss 8.238507 iteration 1300 / 1500: loss 8.061611 iteration 1400 / 1500: loss 8.078579

iteration 0 / 1500: loss 8.979697 iteration 100 / 1500: loss 8.907890 iteration 200 / 1500: loss 8.843051 iteration 300 / 1500: loss 8.779633 iteration 400 / 1500: loss 8.724639 iteration 500 / 1500: loss 8.623214 iteration 600 / 1500: loss 8.565148 iteration 700 / 1500: loss 8.506168 iteration 800 / 1500: loss 8.374103 iteration 900 / 1500: loss 8.340418 iteration 1000 / 1500: loss 8.256675 iteration 1100 / 1500: loss 8.258177 iteration 1200 / 1500: loss 8.175996 iteration 1300 / 1500: loss 7.962400 iteration 1400 / 1500: loss 8.021050 iteration 0 / 1500: loss 8.990459 iteration 100 / 1500: loss 8.937378 iteration 200 / 1500: loss 8.837634 iteration 300 / 1500: loss 8.780671 iteration 400 / 1500: loss 8.691435 iteration 500 / 1500: loss 8.618017 iteration 600 / 1500: loss 8.532597 iteration 700 / 1500: loss 8.531897 iteration 800 / 1500: loss 8.381886 iteration 900 / 1500: loss 8.282453 iteration 1000 / 1500: loss 8.281086 iteration 1100 / 1500: loss 8.268697 iteration 1200 / 1500: loss 8.118914 iteration 1300 / 1500: loss 8.096367 iteration 1400 / 1500: loss 7.982691 iteration 0 / 1500: loss 8.993519 iteration 100 / 1500: loss 8.950262 iteration 200 / 1500: loss 8.859969 iteration 300 / 1500: loss 8.815860 iteration 400 / 1500: loss 8.701106 iteration 500 / 1500: loss 8.628908 iteration 600 / 1500: loss 8.587463 iteration 700 / 1500: loss 8.503385 iteration 800 / 1500: loss 8.444351 iteration 900 / 1500: loss 8.376981 iteration 1000 / 1500: loss 8.224956 iteration 1100 / 1500: loss 8.142255 iteration 1200 / 1500: loss 8.129663 iteration 1300 / 1500: loss 8.132952 iteration 1400 / 1500: loss 7.974167 iteration 0 / 1500: loss 16.745371 iteration 100 / 1500: loss 8.997250 iteration 200 / 1500: loss 8.996818 iteration 300 / 1500: loss 8.997674 iteration 400 / 1500: loss 8.996294 iteration 500 / 1500: loss 8.996386 iteration 600 / 1500: loss 8.996522 iteration 700 / 1500: loss 8.997703 iteration 800 / 1500: loss 8.996459 iteration 900 / 1500: loss 8.996154 iteration 1000 / 1500: loss 8.996721 iteration 1100 / 1500: loss 8.997367 iteration 1200 / 1500: loss 8.996567 iteration 1300 / 1500: loss 8.996511 iteration 1400 / 1500: loss 8.997005

iteration 0 / 1500: loss 8.998873 iteration 100 / 1500: loss 8.211621 iteration 200 / 1500: loss 7.751104 iteration 300 / 1500: loss 7.285559 iteration 400 / 1500: loss 6.727619 iteration 500 / 1500: loss 6.215527 iteration 600 / 1500: loss 6.037269 iteration 700 / 1500: loss 5.224562 iteration 800 / 1500: loss 5.672082 iteration 900 / 1500: loss 5.022154 iteration 1000 / 1500: loss 5.708719 iteration 1100 / 1500: loss 5.580490 iteration 1200 / 1500: loss 5.462514 iteration 1300 / 1500: loss 5.353922 iteration 1400 / 1500: loss 4.728410 iteration 0 / 1500: loss 9.013173 iteration 100 / 1500: loss 8.322357 iteration 200 / 1500: loss 7.673927 iteration 300 / 1500: loss 6.920234 iteration 400 / 1500: loss 6.174442 iteration 500 / 1500: loss 6.117465 iteration 600 / 1500: loss 5.860024 iteration 700 / 1500: loss 5.276261 iteration 800 / 1500: loss 4.905651 iteration 900 / 1500: loss 4.950825 iteration 1000 / 1500: loss 5.097077 iteration 1100 / 1500: loss 5.222958 iteration 1200 / 1500: loss 4.436571 iteration 1300 / 1500: loss 5.081638 iteration 1400 / 1500: loss 4.419436 iteration 0 / 1500: loss 8.992998 iteration 100 / 1500: loss 8.298625 iteration 200 / 1500: loss 7.548628 iteration 300 / 1500: loss 6.753199 iteration 400 / 1500: loss 6.312741 iteration 500 / 1500: loss 6.110861 iteration 600 / 1500: loss 5.904919 iteration 700 / 1500: loss 5.725787 iteration 800 / 1500: loss 5.394149 iteration 900 / 1500: loss 4.801168 iteration 1000 / 1500: loss 5.104601 iteration 1100 / 1500: loss 4.775095 iteration 1200 / 1500: loss 4.671688 iteration 1300 / 1500: loss 4.504473 iteration 1400 / 1500: loss 4.531796 iteration 0 / 1500: loss 8.983970 iteration 100 / 1500: loss 8.133287 iteration 200 / 1500: loss 7.559833 iteration 300 / 1500: loss 6.921541 iteration 400 / 1500: loss 6.128608 iteration 500 / 1500: loss 6.026581 iteration 600 / 1500: loss 5.617900 iteration 700 / 1500: loss 6.094780 iteration 800 / 1500: loss 5.027963 iteration 900 / 1500: loss 5.152269 iteration 1000 / 1500: loss 5.017656 iteration 1100 / 1500: loss 4.984861 iteration 1200 / 1500: loss 4.733104 iteration 1300 / 1500: loss 4.907429 iteration 1400 / 1500: loss 4.971434

iteration 0 / 1500: loss 8.998810 iteration 100 / 1500: loss 8.317201 iteration 200 / 1500: loss 7.486032 iteration 300 / 1500: loss 6.671095 iteration 400 / 1500: loss 6.339828 iteration 500 / 1500: loss 6.070355 iteration 600 / 1500: loss 5.434010 iteration 700 / 1500: loss 5.379509 iteration 800 / 1500: loss 5.075093 iteration 900 / 1500: loss 5.058158 iteration 1000 / 1500: loss 4.610936 iteration 1100 / 1500: loss 4.607124 iteration 1200 / 1500: loss 4.881768 iteration 1300 / 1500: loss 4.450071 iteration 1400 / 1500: loss 4.446012 iteration 0 / 1500: loss 16.844162 iteration 100 / 1500: loss 9.000173 iteration 200 / 1500: loss 8.999393 iteration 300 / 1500: loss 9.000491 iteration 400 / 1500: loss 9.000237 iteration 500 / 1500: loss 8.999904 iteration 600 / 1500: loss 8.999456 iteration 700 / 1500: loss 9.001182 iteration 800 / 1500: loss 8.999983 iteration 900 / 1500: loss 9.001006 iteration 1000 / 1500: loss 9.000078 iteration 1100 / 1500: loss 9.000734 iteration 1200 / 1500: loss 8.998640 iteration 1300 / 1500: loss 8.998972 iteration 1400 / 1500: loss 8.999032 iteration 0 / 1500: loss 9.008268 iteration 100 / 1500: loss 5.530308 iteration 200 / 1500: loss 5.125856 iteration 300 / 1500: loss 4.659448 iteration 400 / 1500: loss 4.841204 iteration 500 / 1500: loss 4.636888 iteration 600 / 1500: loss 4.829179 iteration 700 / 1500: loss 4.889966 iteration 800 / 1500: loss 4.827435 iteration 900 / 1500: loss 4.832629 iteration 1000 / 1500: loss 4.838947 iteration 1100 / 1500: loss 5.397892 iteration 1200 / 1500: loss 4.713454 iteration 1300 / 1500: loss 4.880191 iteration 1400 / 1500: loss 5.267529 iteration 0 / 1500: loss 8.986719 iteration 100 / 1500: loss 5.197790 iteration 200 / 1500: loss 4.804896 iteration 300 / 1500: loss 3.842488 iteration 400 / 1500: loss 3.791836 iteration 500 / 1500: loss 3.936980 iteration 600 / 1500: loss 3.780975 iteration 700 / 1500: loss 3.537026 iteration 800 / 1500: loss 3.145250 iteration 900 / 1500: loss 3.205181 iteration 1000 / 1500: loss 3.314481 iteration 1100 / 1500: loss 3.523786 iteration 1200 / 1500: loss 2.974993 iteration 1300 / 1500: loss 3.377697 iteration 1400 / 1500: loss 3.346372

```
iteration 0 / 1500: loss 9.012271
iteration 100 / 1500: loss 4.683300
iteration 200 / 1500: loss 4.280253
iteration 300 / 1500: loss 3.925573
iteration 400 / 1500: loss 3.610590
iteration 500 / 1500: loss 3.916129
iteration 600 / 1500: loss 3.948670
iteration 700 / 1500: loss 3.941106
iteration 800 / 1500: loss 3.777270
iteration 900 / 1500: loss 3.651549
iteration 1000 / 1500: loss 3.778945
iteration 1100 / 1500: loss 4.017471
iteration 1200 / 1500: loss 3.920450
iteration 1300 / 1500: loss 3.418260
iteration 1400 / 1500: loss 3.672257
iteration 0 / 1500: loss 8.996609
iteration 100 / 1500: loss 4.958472
iteration 200 / 1500: loss 4.414333
iteration 300 / 1500: loss 4.408473
iteration 400 / 1500: loss 3.975846
iteration 500 / 1500: loss 4.201985
iteration 600 / 1500: loss 4.546119
iteration 700 / 1500: loss 4.396723
iteration 800 / 1500: loss 4.417406
iteration 900 / 1500: loss 4.000232
iteration 1000 / 1500: loss 4.158696
iteration 1100 / 1500: loss 4.500879
iteration 1200 / 1500: loss 3.922109
iteration 1300 / 1500: loss 4.458384
iteration 1400 / 1500: loss 4.117051
iteration 0 / 1500: loss 8.995200
iteration 100 / 1500: loss 5.119368
iteration 200 / 1500: loss 3.472156
iteration 300 / 1500: loss 3.869788
iteration 400 / 1500: loss 3.524658
iteration 500 / 1500: loss 3.423991
iteration 600 / 1500: loss 3.785522
iteration 700 / 1500: loss 3.408188
iteration 800 / 1500: loss 3.604609
iteration 900 / 1500: loss 3.154217
iteration 1000 / 1500: loss 3.066422
iteration 1100 / 1500: loss 3.364834
iteration 1200 / 1500: loss 3.153840
iteration 1300 / 1500: loss 3.339472
iteration 1400 / 1500: loss 2.779781
iteration 0 / 1500: loss 16.692660
iteration 100 / 1500: loss 5432540045339055261188022265079119509313939275896963849584
4560278167174515637554374574713126125350384537236711829092834056260251402653378456210
4262418698034048090222360572857565483370427711488.000000
iteration 200 / 1500: loss inf
iteration 300 / 1500: loss inf
iteration 400 / 1500: loss nan
```

file:///C:/Utah/CS6353/Submission2/features.html

```
/content/drive/MyDrive/CS6353/Assignments/assignment2/assignment2/cs6353/classifiers/
linear_svm.py:100: RuntimeWarning: overflow encountered in scalar multiply
  loss += reg * np.sum(W * W)
/usr/local/lib/python3.10/dist-packages/numpy/core/fromnumeric.py:88: RuntimeWarning:
overflow encountered in reduce

/content/drive/MyDrive/CS6353/Assignments/assignment2/assignment2/cs6353/classifiers/
linear_svm.py:100: RuntimeWarning: overflow encountered in multiply
  loss += reg * np.sum(W * W)
/content/drive/MyDrive/CS6353/Assignments/assignment2/assignment2/cs6353/classifiers/
linear_svm.py:125: RuntimeWarning: overflow encountered in multiply
  dW += 2 * reg * W
/content/drive/MyDrive/CS6353/Assignments/assignment2/assignment2/cs6353/classifiers/
linear_classifier.py:70: RuntimeWarning: invalid value encountered in subtract
  self.W -= learning_rate * grad
```

iteration 500 / 1500: loss nan iteration 600 / 1500: loss nan iteration 700 / 1500: loss nan iteration 800 / 1500: loss nan iteration 900 / 1500: loss nan iteration 1000 / 1500: loss nan iteration 1100 / 1500: loss nan iteration 1200 / 1500: loss nan iteration 1300 / 1500: loss nan iteration 1400 / 1500: loss nan iteration 0 / 1500: loss 8.979867 iteration 100 / 1500: loss 8.996251 iteration 200 / 1500: loss 9.001369 iteration 300 / 1500: loss 8.980656 iteration 400 / 1500: loss 8.981561 iteration 500 / 1500: loss 8.991502 iteration 600 / 1500: loss 8.959770 iteration 700 / 1500: loss 8.987205 iteration 800 / 1500: loss 8.983566 iteration 900 / 1500: loss 8.986715 iteration 1000 / 1500: loss 8.981800 iteration 1100 / 1500: loss 8.968632 iteration 1200 / 1500: loss 8.956905 iteration 1300 / 1500: loss 8.979529 iteration 1400 / 1500: loss 8.977704 iteration 0 / 1500: loss 8.998422 iteration 100 / 1500: loss 8.985798 iteration 200 / 1500: loss 8.977414 iteration 300 / 1500: loss 8.982007 iteration 400 / 1500: loss 8.981535 iteration 500 / 1500: loss 8.980430 iteration 600 / 1500: loss 8.981968 iteration 700 / 1500: loss 8.979893 iteration 800 / 1500: loss 8.966357 iteration 900 / 1500: loss 8.966229 iteration 1000 / 1500: loss 8.976326 iteration 1100 / 1500: loss 8.984724 iteration 1200 / 1500: loss 8.966523 iteration 1300 / 1500: loss 8.988293 iteration 1400 / 1500: loss 8.977714 iteration 0 / 1500: loss 9.011928 iteration 100 / 1500: loss 9.015683 iteration 200 / 1500: loss 9.009162 iteration 300 / 1500: loss 8.990739 iteration 400 / 1500: loss 9.006050 iteration 500 / 1500: loss 9.002419 iteration 600 / 1500: loss 8.984172 iteration 700 / 1500: loss 9.013493 iteration 800 / 1500: loss 8.995792 iteration 900 / 1500: loss 9.005634 iteration 1000 / 1500: loss 8.984671 iteration 1100 / 1500: loss 8.989461 iteration 1200 / 1500: loss 8.991261 iteration 1300 / 1500: loss 8.983193 iteration 1400 / 1500: loss 8.981880 iteration 0 / 1500: loss 8.985978 iteration 100 / 1500: loss 9.013909 iteration 200 / 1500: loss 9.004129 iteration 300 / 1500: loss 8.995814 iteration 400 / 1500: loss 8.986354

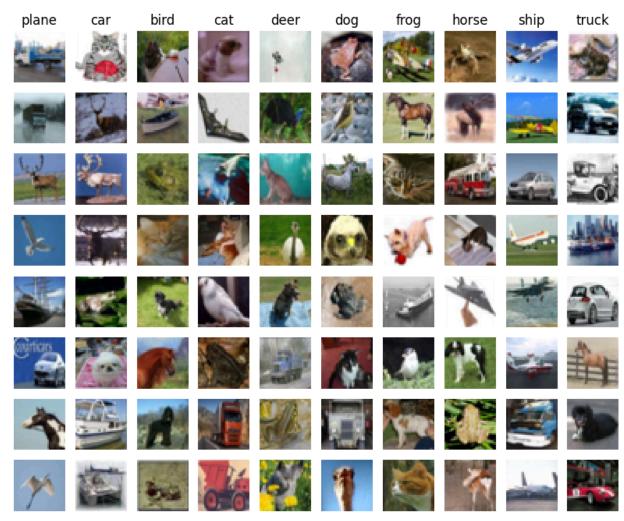
```
iteration 500 / 1500: loss 8.992970
iteration 600 / 1500: loss 8.992309
iteration 700 / 1500: loss 8.989405
iteration 800 / 1500: loss 8.986906
iteration 900 / 1500: loss 8.982426
iteration 1000 / 1500: loss 8.975887
iteration 1100 / 1500: loss 8.983723
iteration 1200 / 1500: loss 8.980348
iteration 1300 / 1500: loss 8.975027
iteration 1400 / 1500: loss 8.960443
iteration 0 / 1500: loss 9.001468
iteration 100 / 1500: loss 9.014731
iteration 200 / 1500: loss 8.998339
iteration 300 / 1500: loss 8.998015
iteration 400 / 1500: loss 8.990683
iteration 500 / 1500: loss 8.991826
iteration 600 / 1500: loss 8.984588
iteration 700 / 1500: loss 8.984822
iteration 800 / 1500: loss 8.990561
iteration 900 / 1500: loss 8.981084
iteration 1000 / 1500: loss 8.977509
iteration 1100 / 1500: loss 8.970272
iteration 1200 / 1500: loss 8.982036
iteration 1300 / 1500: loss 8.977331
iteration 1400 / 1500: loss 8.988174
iteration 0 / 1500: loss 17.012696
iteration 100 / 1500: loss 14.360557
iteration 200 / 1500: loss 12.591737
iteration 300 / 1500: loss 11.406741
iteration 400 / 1500: loss 10.606751
iteration 500 / 1500: loss 10.077585
iteration 600 / 1500: loss 9.722681
iteration 700 / 1500: loss 9.484263
iteration 800 / 1500: loss 9.323231
iteration 900 / 1500: loss 9.214641
iteration 1000 / 1500: loss 9.141867
iteration 1100 / 1500: loss 9.093606
iteration 1200 / 1500: loss 9.060933
iteration 1300 / 1500: loss 9.040592
iteration 1400 / 1500: loss 9.026970
lr 1.000000e-07 reg 1.000000e-02 train accuracy: 0.111816 val accuracy: 0.100000
lr 1.000000e-07 reg 1.000000e-01 train accuracy: 0.122163 val accuracy: 0.113000
lr 1.000000e-07 reg 2.000000e-01 train accuracy: 0.126980 val accuracy: 0.123000
lr 1.000000e-07 reg 5.000000e-01 train accuracy: 0.088551 val accuracy: 0.082000
lr 1.000000e-07 reg 1.000000e+00 train accuracy: 0.105776 val accuracy: 0.114000
lr 1.000000e-07 reg 5.000000e+03 train accuracy: 0.147490 val accuracy: 0.138000
lr 2.000000e-07 reg 1.000000e-02 train accuracy: 0.141531 val accuracy: 0.139000
lr 2.000000e-07 reg 1.000000e-01 train accuracy: 0.141959 val accuracy: 0.156000
lr 2.000000e-07 reg 2.000000e-01 train accuracy: 0.126653 val accuracy: 0.116000
lr 2.000000e-07 reg 5.000000e-01 train accuracy: 0.130714 val accuracy: 0.161000
lr 2.000000e-07 reg 1.000000e+00 train accuracy: 0.155041 val accuracy: 0.144000
lr 2.000000e-07 reg 5.000000e+03 train accuracy: 0.272918 val accuracy: 0.261000
lr 1.000000e-05 reg 1.000000e-02 train accuracy: 0.406796 val accuracy: 0.396000
lr 1.000000e-05 reg 1.000000e-01 train accuracy: 0.408510 val accuracy: 0.410000
lr 1.000000e-05 reg 2.000000e-01 train accuracy: 0.409163 val accuracy: 0.414000
lr 1.000000e-05 reg 5.000000e-01 train accuracy: 0.407816 val accuracy: 0.410000
lr 1.000000e-05 reg 1.000000e+00 train accuracy: 0.408490 val accuracy: 0.400000
lr 1.000000e-05 reg 5.000000e+03 train accuracy: 0.407367 val accuracy: 0.410000
lr 1.000000e-04 reg 1.000000e-02 train accuracy: 0.451776 val accuracy: 0.443000
lr 1.000000e-04 reg 1.000000e-01 train accuracy: 0.451367 val accuracy: 0.448000
```

```
lr 1.000000e-04 reg 2.000000e-01 train accuracy: 0.449531 val accuracy: 0.449000 lr 1.000000e-04 reg 5.000000e-01 train accuracy: 0.450388 val accuracy: 0.446000 lr 1.000000e-04 reg 1.000000e+00 train accuracy: 0.448592 val accuracy: 0.441000 lr 1.000000e-04 reg 5.000000e+03 train accuracy: 0.332102 val accuracy: 0.348000 lr 1.000000e-03 reg 1.000000e-02 train accuracy: 0.500061 val accuracy: 0.492000 lr 1.000000e-03 reg 1.000000e-01 train accuracy: 0.499041 val accuracy: 0.493000 lr 1.000000e-03 reg 2.000000e-01 train accuracy: 0.498041 val accuracy: 0.487000 lr 1.000000e-03 reg 5.000000e-01 train accuracy: 0.490449 val accuracy: 0.476000 lr 1.000000e-03 reg 5.000000e+00 train accuracy: 0.484878 val accuracy: 0.474000 lr 1.000000e-03 reg 5.000000e+03 train accuracy: 0.100265 val accuracy: 0.087000 best validation accuracy achieved during cross-validation: 0.493000
```

```
In [ ]: # Evaluate your trained SVM on the test set
    y_test_pred = best_svm.predict(X_test_feats)
    test_accuracy = np.mean(y_test == y_test_pred)
    print(test_accuracy)
```

0.48

```
In [ ]: # An important way to gain intuition about how an algorithm works is to
        # visualize the mistakes that it makes. In this visualization, we show examples
        # of images that are misclassified by our current system. The first column
        # shows images that our system labeled as "plane" but whose true label is
        # something other than "plane".
        examples per class = 8
        classes = ['plane', 'car', 'bird', 'cat', 'deer', 'dog', 'frog', 'horse', 'ship', 'tru
        for cls, cls name in enumerate(classes):
            idxs = np.where((y_test != cls) & (y_test_pred == cls))[0]
            idxs = np.random.choice(idxs, examples_per_class, replace=False)
            for i, idx in enumerate(idxs):
                plt.subplot(examples per class, len(classes), i * len(classes) + cls + 1)
                plt.imshow(X_test[idx].astype('uint8'))
                plt.axis('off')
                if i == 0:
                    plt.title(cls_name)
        plt.show()
```



Inline question 1:

Describe the misclassification results that you see. Do they make sense?

Yes, some of the misclassifications make sense:

- 1. Birds in flight are misclassified as planes, due the background colour of the image and the similarity in the images. Also images having significant blue background are misclassified as planes due to the similarity in the background colour.
- 2. Cat, deer, dog, frog and horse images are also misclassified due to common features like legs, eyes, shape of their body, similarities in fur textures, etc.
- 3. Vehicles like trucks and cars are also often misclassified due to similarity in their shapes and common features like wheels, etc.
- 4. Similar background images like ships and planes are also misclassified.

In conclusion, the combination of HOG and color histogram feature vectors is insufficient for achieving highly accurate classification between these classes. Improving feature extraction or dataset augmentation can further improve the systems accuracy.

Neural Network on image features

Earlier in this assignment we saw that training a two-layer neural network on raw pixels achieved better classification performance than linear classifiers on raw pixels. In this notebook we have seen that linear classifiers on image features outperform linear classifiers on raw pixels.

For completeness, we should also try training a neural network on image features. This approach should outperform all previous approaches: you should easily be able to achieve over 55% classification accuracy on the test set; our best model achieves about 60% classification accuracy.

```
In [ ]: # Preprocessing: Remove the bias dimension
       # Make sure to run this cell only ONCE
       print(X_train_feats.shape)
       X_train_feats = X_train_feats[:, :-1]
       X_val_feats = X_val_feats[:, :-1]
       X_test_feats = X_test_feats[:, :-1]
       print(X_train_feats.shape)
       (49000, 155)
       (49000, 154)
In [ ]: from cs6353.classifiers.neural net import TwoLayerNet
       input_dim = X_train_feats.shape[1]
       hidden dim = 500
       num_classes = 10
       net = TwoLayerNet(input_dim, hidden_dim, num_classes)
       best_net = None
       # TODO: Train a two-layer neural network on image features. You may want to
       # cross-validate various parameters as in previous sections. Store your best
       # model in the best_net variable.
       learning_rates = [3e-1, 1e-2, 2e-3]
       regularization_strengths = [2e-7, 1e-7, 2e-5]
       hidden_layer_sizes = [100, 150, 175]
       num_of_epochs = [1500, 3000]
       results = {}
       best val = -1
       for lr in learning rates:
           for reg in regularization_strengths:
            for hls in hidden layer sizes:
              for epochs in num_of_epochs:
                net = TwoLayerNet(input_dim, hls, num_classes)
                stats = net.train(X_train_feats, y_train, X_val_feats, y_val,
                    num_iters=epochs, batch_size=200,
                    learning_rate=lr, learning_rate_decay=0.95,
                    reg=reg, verbose=True)
```

```
iteration 0 / 1500: loss 2.302585
iteration 100 / 1500: loss 1.837699
iteration 200 / 1500: loss 1.430180
iteration 300 / 1500: loss 1.461022
iteration 400 / 1500: loss 1.337830
iteration 500 / 1500: loss 1.316799
iteration 600 / 1500: loss 1.329158
iteration 700 / 1500: loss 1.259146
iteration 800 / 1500: loss 1.408602
iteration 900 / 1500: loss 1.379886
iteration 1000 / 1500: loss 1.123509
iteration 1100 / 1500: loss 1.109656
iteration 1200 / 1500: loss 1.054326
iteration 1300 / 1500: loss 1.163406
iteration 1400 / 1500: loss 1.215077
0.3 2e-07 100 1500 0.6139591836734694 0.572
iteration 0 / 3000: loss 2.302585
iteration 100 / 3000: loss 1.921849
iteration 200 / 3000: loss 1.503588
iteration 300 / 3000: loss 1.250968
iteration 400 / 3000: loss 1.316346
iteration 500 / 3000: loss 1.273989
iteration 600 / 3000: loss 1.394202
iteration 700 / 3000: loss 1.367919
iteration 800 / 3000: loss 1.254400
iteration 900 / 3000: loss 1.148793
iteration 1000 / 3000: loss 1.215016
iteration 1100 / 3000: loss 1.107165
iteration 1200 / 3000: loss 1.201162
iteration 1300 / 3000: loss 1.124361
iteration 1400 / 3000: loss 1.127846
iteration 1500 / 3000: loss 1.118782
iteration 1600 / 3000: loss 1.054724
iteration 1700 / 3000: loss 1.089153
iteration 1800 / 3000: loss 1.006425
iteration 1900 / 3000: loss 0.993421
iteration 2000 / 3000: loss 1.038893
iteration 2100 / 3000: loss 1.058492
iteration 2200 / 3000: loss 1.082460
iteration 2300 / 3000: loss 1.161133
iteration 2400 / 3000: loss 1.076711
iteration 2500 / 3000: loss 1.013445
iteration 2600 / 3000: loss 0.984464
iteration 2700 / 3000: loss 1.010282
iteration 2800 / 3000: loss 1.090771
iteration 2900 / 3000: loss 1.057545
0.3 2e-07 100 3000 0.6583061224489796 0.585
iteration 0 / 1500: loss 2.302585
iteration 100 / 1500: loss 1.825610
iteration 200 / 1500: loss 1.480830
iteration 300 / 1500: loss 1.360206
iteration 400 / 1500: loss 1.478022
iteration 500 / 1500: loss 1.315065
iteration 600 / 1500: loss 1.247591
iteration 700 / 1500: loss 1.234418
iteration 800 / 1500: loss 1.380980
iteration 900 / 1500: loss 1.182532
iteration 1000 / 1500: loss 1.106733
iteration 1100 / 1500: loss 1.216349
iteration 1200 / 1500: loss 1.142483
```

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iteration 1300 / 1500: loss 1.217735
iteration 1400 / 1500: loss 1.201116
0.3 2e-07 150 1500 0.6227142857142857 0.571
iteration 0 / 3000: loss 2.302585
iteration 100 / 3000: loss 1.923236
iteration 200 / 3000: loss 1.405291
iteration 300 / 3000: loss 1.520795
iteration 400 / 3000: loss 1.328728
iteration 500 / 3000: loss 1.313827
iteration 600 / 3000: loss 1.339707
iteration 700 / 3000: loss 1.355101
iteration 800 / 3000: loss 1.221677
iteration 900 / 3000: loss 1.210339
iteration 1000 / 3000: loss 1.281490
iteration 1100 / 3000: loss 1.150248
iteration 1200 / 3000: loss 1.182286
iteration 1300 / 3000: loss 1.270046
iteration 1400 / 3000: loss 1.064207
iteration 1500 / 3000: loss 1.195812
iteration 1600 / 3000: loss 1.081500
iteration 1700 / 3000: loss 1.002393
iteration 1800 / 3000: loss 1.079138
iteration 1900 / 3000: loss 1.019485
iteration 2000 / 3000: loss 1.005818
iteration 2100 / 3000: loss 1.060225
iteration 2200 / 3000: loss 1.071140
iteration 2300 / 3000: loss 1.012516
iteration 2400 / 3000: loss 1.021231
iteration 2500 / 3000: loss 0.827208
iteration 2600 / 3000: loss 0.889679
iteration 2700 / 3000: loss 0.937680
iteration 2800 / 3000: loss 0.904265
iteration 2900 / 3000: loss 0.817346
0.3 2e-07 150 3000 0.6850612244897959 0.579
iteration 0 / 1500: loss 2.302585
iteration 100 / 1500: loss 1.857560
iteration 200 / 1500: loss 1.572749
iteration 300 / 1500: loss 1.267005
iteration 400 / 1500: loss 1.354619
iteration 500 / 1500: loss 1.258958
iteration 600 / 1500: loss 1.166776
iteration 700 / 1500: loss 1.230874
iteration 800 / 1500: loss 1.238824
iteration 900 / 1500: loss 1.201996
iteration 1000 / 1500: loss 1.145441
iteration 1100 / 1500: loss 1.084606
iteration 1200 / 1500: loss 1.008969
iteration 1300 / 1500: loss 0.981302
iteration 1400 / 1500: loss 0.996228
0.3 2e-07 175 1500 0.6257959183673469 0.574
iteration 0 / 3000: loss 2.302585
iteration 100 / 3000: loss 1.903254
iteration 200 / 3000: loss 1.487875
iteration 300 / 3000: loss 1.355269
iteration 400 / 3000: loss 1.339793
iteration 500 / 3000: loss 1.281435
iteration 600 / 3000: loss 1.255357
iteration 700 / 3000: loss 1.129785
iteration 800 / 3000: loss 1.081565
iteration 900 / 3000: loss 1.254100
```

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iteration 1000 / 3000: loss 1.138822
iteration 1100 / 3000: loss 1.263180
iteration 1200 / 3000: loss 1.079415
iteration 1300 / 3000: loss 0.975581
iteration 1400 / 3000: loss 0.958881
iteration 1500 / 3000: loss 1.028240
iteration 1600 / 3000: loss 1.039519
iteration 1700 / 3000: loss 1.084825
iteration 1800 / 3000: loss 1.106511
iteration 1900 / 3000: loss 0.983309
iteration 2000 / 3000: loss 1.020936
iteration 2100 / 3000: loss 0.952577
iteration 2200 / 3000: loss 0.955561
iteration 2300 / 3000: loss 1.010738
iteration 2400 / 3000: loss 0.891842
iteration 2500 / 3000: loss 0.871702
iteration 2600 / 3000: loss 0.999913
iteration 2700 / 3000: loss 0.888187
iteration 2800 / 3000: loss 1.022731
iteration 2900 / 3000: loss 0.960904
0.3 2e-07 175 3000 0.6928775510204082 0.59
iteration 0 / 1500: loss 2.302585
iteration 100 / 1500: loss 1.914205
iteration 200 / 1500: loss 1.488031
iteration 300 / 1500: loss 1.446658
iteration 400 / 1500: loss 1.182026
iteration 500 / 1500: loss 1.261541
iteration 600 / 1500: loss 1.325419
iteration 700 / 1500: loss 1.345249
iteration 800 / 1500: loss 1.226613
iteration 900 / 1500: loss 1.193734
iteration 1000 / 1500: loss 1.296815
iteration 1100 / 1500: loss 1.259790
iteration 1200 / 1500: loss 1.192646
iteration 1300 / 1500: loss 1.051605
iteration 1400 / 1500: loss 1.090569
0.3 1e-07 100 1500 0.6111836734693877 0.551
iteration 0 / 3000: loss 2.302585
iteration 100 / 3000: loss 1.861578
iteration 200 / 3000: loss 1.420475
iteration 300 / 3000: loss 1.437324
iteration 400 / 3000: loss 1.407257
iteration 500 / 3000: loss 1.301119
iteration 600 / 3000: loss 1.259529
iteration 700 / 3000: loss 1.143872
iteration 800 / 3000: loss 1.079263
iteration 900 / 3000: loss 1.073315
iteration 1000 / 3000: loss 1.274614
iteration 1100 / 3000: loss 1.184006
iteration 1200 / 3000: loss 1.109554
iteration 1300 / 3000: loss 1.022257
iteration 1400 / 3000: loss 1.019454
iteration 1500 / 3000: loss 1.184491
iteration 1600 / 3000: loss 1.130063
iteration 1700 / 3000: loss 1.090259
iteration 1800 / 3000: loss 1.064923
iteration 1900 / 3000: loss 0.993765
iteration 2000 / 3000: loss 1.027432
iteration 2100 / 3000: loss 1.057841
iteration 2200 / 3000: loss 0.985762
```

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iteration 2300 / 3000: loss 1.074963
iteration 2400 / 3000: loss 1.102784
iteration 2500 / 3000: loss 0.983353
iteration 2600 / 3000: loss 1.088187
iteration 2700 / 3000: loss 1.023639
iteration 2800 / 3000: loss 1.041927
iteration 2900 / 3000: loss 0.879632
0.3 1e-07 100 3000 0.6611836734693878 0.555
iteration 0 / 1500: loss 2.302585
iteration 100 / 1500: loss 1.824135
iteration 200 / 1500: loss 1.436204
iteration 300 / 1500: loss 1.453721
iteration 400 / 1500: loss 1.473710
iteration 500 / 1500: loss 1.478476
iteration 600 / 1500: loss 1.361429
iteration 700 / 1500: loss 1.214201
iteration 800 / 1500: loss 1.207533
iteration 900 / 1500: loss 1.217915
iteration 1000 / 1500: loss 1.131833
iteration 1100 / 1500: loss 1.011908
iteration 1200 / 1500: loss 1.211687
iteration 1300 / 1500: loss 1.083478
iteration 1400 / 1500: loss 0.963578
0.3 1e-07 150 1500 0.6167142857142857 0.576
iteration 0 / 3000: loss 2.302585
iteration 100 / 3000: loss 1.818691
iteration 200 / 3000: loss 1.654387
iteration 300 / 3000: loss 1.352701
iteration 400 / 3000: loss 1.372019
iteration 500 / 3000: loss 1.215856
iteration 600 / 3000: loss 1.320398
iteration 700 / 3000: loss 1.231753
iteration 800 / 3000: loss 1.305710
iteration 900 / 3000: loss 1.152225
iteration 1000 / 3000: loss 1.164774
iteration 1100 / 3000: loss 1.239725
iteration 1200 / 3000: loss 1.180680
iteration 1300 / 3000: loss 1.172873
iteration 1400 / 3000: loss 1.103864
iteration 1500 / 3000: loss 1.139673
iteration 1600 / 3000: loss 0.949171
iteration 1700 / 3000: loss 0.955011
iteration 1800 / 3000: loss 0.911333
iteration 1900 / 3000: loss 1.116908
iteration 2000 / 3000: loss 1.103250
iteration 2100 / 3000: loss 1.018802
iteration 2200 / 3000: loss 1.064770
iteration 2300 / 3000: loss 0.968589
iteration 2400 / 3000: loss 0.928128
iteration 2500 / 3000: loss 0.990355
iteration 2600 / 3000: loss 0.987239
iteration 2700 / 3000: loss 1.062059
iteration 2800 / 3000: loss 0.981290
iteration 2900 / 3000: loss 0.892102
0.3 1e-07 150 3000 0.6801428571428572 0.575
iteration 0 / 1500: loss 2.302585
iteration 100 / 1500: loss 1.915168
iteration 200 / 1500: loss 1.406389
iteration 300 / 1500: loss 1.233515
iteration 400 / 1500: loss 1.301279
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iteration 500 / 1500: loss 1.224305
iteration 600 / 1500: loss 1.292745
iteration 700 / 1500: loss 1.171320
iteration 800 / 1500: loss 1.213119
iteration 900 / 1500: loss 1.230728
iteration 1000 / 1500: loss 1.097455
iteration 1100 / 1500: loss 1.161020
iteration 1200 / 1500: loss 1.148332
iteration 1300 / 1500: loss 1.108262
iteration 1400 / 1500: loss 1.103696
0.3 1e-07 175 1500 0.6268367346938776 0.563
iteration 0 / 3000: loss 2.302585
iteration 100 / 3000: loss 1.897716
iteration 200 / 3000: loss 1.552027
iteration 300 / 3000: loss 1.390646
iteration 400 / 3000: loss 1.308007
iteration 500 / 3000: loss 1.230168
iteration 600 / 3000: loss 1.279816
iteration 700 / 3000: loss 1.308391
iteration 800 / 3000: loss 1.173698
iteration 900 / 3000: loss 1.273260
iteration 1000 / 3000: loss 1.165451
iteration 1100 / 3000: loss 1.155267
iteration 1200 / 3000: loss 1.070129
iteration 1300 / 3000: loss 1.145944
iteration 1400 / 3000: loss 1.140940
iteration 1500 / 3000: loss 1.183665
iteration 1600 / 3000: loss 1.100796
iteration 1700 / 3000: loss 1.092760
iteration 1800 / 3000: loss 1.149449
iteration 1900 / 3000: loss 0.951859
iteration 2000 / 3000: loss 1.006551
iteration 2100 / 3000: loss 0.835124
iteration 2200 / 3000: loss 0.898580
iteration 2300 / 3000: loss 0.891952
iteration 2400 / 3000: loss 0.998279
iteration 2500 / 3000: loss 1.117451
iteration 2600 / 3000: loss 1.095574
iteration 2700 / 3000: loss 1.011762
iteration 2800 / 3000: loss 0.947734
iteration 2900 / 3000: loss 0.993534
0.3 1e-07 175 3000 0.6863061224489796 0.592
iteration 0 / 1500: loss 2.302585
iteration 100 / 1500: loss 1.889219
iteration 200 / 1500: loss 1.449334
iteration 300 / 1500: loss 1.459348
iteration 400 / 1500: loss 1.374681
iteration 500 / 1500: loss 1.313737
iteration 600 / 1500: loss 1.326432
iteration 700 / 1500: loss 1.382270
iteration 800 / 1500: loss 1.173156
iteration 900 / 1500: loss 1.208045
iteration 1000 / 1500: loss 1.107190
iteration 1100 / 1500: loss 1.263532
iteration 1200 / 1500: loss 1.164127
iteration 1300 / 1500: loss 1.183337
iteration 1400 / 1500: loss 1.077219
0.3 2e-05 100 1500 0.6079591836734693 0.564
iteration 0 / 3000: loss 2.302585
iteration 100 / 3000: loss 1.897828
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iteration 200 / 3000: loss 1.467057
iteration 300 / 3000: loss 1.395959
iteration 400 / 3000: loss 1.392540
iteration 500 / 3000: loss 1.331435
iteration 600 / 3000: loss 1.271580
iteration 700 / 3000: loss 1.266743
iteration 800 / 3000: loss 1.250985
iteration 900 / 3000: loss 1.280351
iteration 1000 / 3000: loss 1.102922
iteration 1100 / 3000: loss 1.242154
iteration 1200 / 3000: loss 1.358491
iteration 1300 / 3000: loss 1.182420
iteration 1400 / 3000: loss 1.256858
iteration 1500 / 3000: loss 1.223502
iteration 1600 / 3000: loss 1.174015
iteration 1700 / 3000: loss 1.073848
iteration 1800 / 3000: loss 0.985025
iteration 1900 / 3000: loss 1.109320
iteration 2000 / 3000: loss 1.040313
iteration 2100 / 3000: loss 1.035139
iteration 2200 / 3000: loss 1.063179
iteration 2300 / 3000: loss 1.059575
iteration 2400 / 3000: loss 0.957594
iteration 2500 / 3000: loss 0.968469
iteration 2600 / 3000: loss 1.080336
iteration 2700 / 3000: loss 0.986587
iteration 2800 / 3000: loss 0.865402
iteration 2900 / 3000: loss 1.099529
0.3 2e-05 100 3000 0.6579183673469388 0.579
iteration 0 / 1500: loss 2.302585
iteration 100 / 1500: loss 1.876340
iteration 200 / 1500: loss 1.464171
iteration 300 / 1500: loss 1.304314
iteration 400 / 1500: loss 1.284944
iteration 500 / 1500: loss 1.276695
iteration 600 / 1500: loss 1.275961
iteration 700 / 1500: loss 1.214174
iteration 800 / 1500: loss 1.171265
iteration 900 / 1500: loss 1.305379
iteration 1000 / 1500: loss 1.229707
iteration 1100 / 1500: loss 1.146509
iteration 1200 / 1500: loss 1.152636
iteration 1300 / 1500: loss 1.087768
iteration 1400 / 1500: loss 1.136095
0.3 2e-05 150 1500 0.6160612244897959 0.563
iteration 0 / 3000: loss 2.302585
iteration 100 / 3000: loss 1.938511
iteration 200 / 3000: loss 1.428322
iteration 300 / 3000: loss 1.374366
iteration 400 / 3000: loss 1.402192
iteration 500 / 3000: loss 1.363606
iteration 600 / 3000: loss 1.398350
iteration 700 / 3000: loss 1.223098
iteration 800 / 3000: loss 1.147972
iteration 900 / 3000: loss 1.238309
iteration 1000 / 3000: loss 1.203515
iteration 1100 / 3000: loss 1.074834
iteration 1200 / 3000: loss 1.097596
iteration 1300 / 3000: loss 0.994037
iteration 1400 / 3000: loss 1.036411
```

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iteration 1500 / 3000: loss 1.029644
iteration 1600 / 3000: loss 1.094589
iteration 1700 / 3000: loss 0.905588
iteration 1800 / 3000: loss 1.019745
iteration 1900 / 3000: loss 1.042735
iteration 2000 / 3000: loss 0.979338
iteration 2100 / 3000: loss 1.006893
iteration 2200 / 3000: loss 0.931205
iteration 2300 / 3000: loss 0.968058
iteration 2400 / 3000: loss 0.828188
iteration 2500 / 3000: loss 1.026215
iteration 2600 / 3000: loss 1.086503
iteration 2700 / 3000: loss 0.896616
iteration 2800 / 3000: loss 0.878320
iteration 2900 / 3000: loss 0.985768
0.3 2e-05 150 3000 0.6832857142857143 0.586
iteration 0 / 1500: loss 2.302585
iteration 100 / 1500: loss 1.900189
iteration 200 / 1500: loss 1.449862
iteration 300 / 1500: loss 1.386672
iteration 400 / 1500: loss 1.458359
iteration 500 / 1500: loss 1.313744
iteration 600 / 1500: loss 1.167334
iteration 700 / 1500: loss 1.186287
iteration 800 / 1500: loss 1.261683
iteration 900 / 1500: loss 1.260529
iteration 1000 / 1500: loss 1.179343
iteration 1100 / 1500: loss 1.073347
iteration 1200 / 1500: loss 1.040158
iteration 1300 / 1500: loss 1.123835
iteration 1400 / 1500: loss 1.153764
0.3 2e-05 175 1500 0.6233673469387755 0.577
iteration 0 / 3000: loss 2.302585
iteration 100 / 3000: loss 1.882834
iteration 200 / 3000: loss 1.345935
iteration 300 / 3000: loss 1.401120
iteration 400 / 3000: loss 1.217637
iteration 500 / 3000: loss 1.287546
iteration 600 / 3000: loss 1.267964
iteration 700 / 3000: loss 1.278788
iteration 800 / 3000: loss 1.187089
iteration 900 / 3000: loss 1.150295
iteration 1000 / 3000: loss 1.190415
iteration 1100 / 3000: loss 1.195944
iteration 1200 / 3000: loss 1.141844
iteration 1300 / 3000: loss 1.230643
iteration 1400 / 3000: loss 1.221038
iteration 1500 / 3000: loss 1.012293
iteration 1600 / 3000: loss 1.025338
iteration 1700 / 3000: loss 1.021385
iteration 1800 / 3000: loss 1.018242
iteration 1900 / 3000: loss 1.017006
iteration 2000 / 3000: loss 0.932952
iteration 2100 / 3000: loss 0.870121
iteration 2200 / 3000: loss 0.975799
iteration 2300 / 3000: loss 0.957460
iteration 2400 / 3000: loss 0.922303
iteration 2500 / 3000: loss 0.926949
iteration 2600 / 3000: loss 0.798439
iteration 2700 / 3000: loss 1.029576
```

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iteration 2800 / 3000: loss 0.922554
iteration 2900 / 3000: loss 0.905369
0.3 2e-05 175 3000 0.6830204081632653 0.58
iteration 0 / 1500: loss 2.302585
iteration 100 / 1500: loss 2.302368
iteration 200 / 1500: loss 2.302862
iteration 300 / 1500: loss 2.302603
iteration 400 / 1500: loss 2.302851
iteration 500 / 1500: loss 2.303004
iteration 600 / 1500: loss 2.303145
iteration 700 / 1500: loss 2.302993
iteration 800 / 1500: loss 2.302778
iteration 900 / 1500: loss 2.302412
iteration 1000 / 1500: loss 2.302888
iteration 1100 / 1500: loss 2.302488
iteration 1200 / 1500: loss 2.302207
iteration 1300 / 1500: loss 2.302131
iteration 1400 / 1500: loss 2.302267
0.01 2e-07 100 1500 0.10404081632653062 0.08
iteration 0 / 3000: loss 2.302585
iteration 100 / 3000: loss 2.302385
iteration 200 / 3000: loss 2.302665
iteration 300 / 3000: loss 2.302539
iteration 400 / 3000: loss 2.302594
iteration 500 / 3000: loss 2.302518
iteration 600 / 3000: loss 2.302699
iteration 700 / 3000: loss 2.302904
iteration 800 / 3000: loss 2.302663
iteration 900 / 3000: loss 2.302749
iteration 1000 / 3000: loss 2.303077
iteration 1100 / 3000: loss 2.303139
iteration 1200 / 3000: loss 2.302096
iteration 1300 / 3000: loss 2.303164
iteration 1400 / 3000: loss 2.302028
iteration 1500 / 3000: loss 2.302835
iteration 1600 / 3000: loss 2.301581
iteration 1700 / 3000: loss 2.301586
iteration 1800 / 3000: loss 2.299801
iteration 1900 / 3000: loss 2.297119
iteration 2000 / 3000: loss 2.295164
iteration 2100 / 3000: loss 2.291991
iteration 2200 / 3000: loss 2.285401
iteration 2300 / 3000: loss 2.274336
iteration 2400 / 3000: loss 2.263266
iteration 2500 / 3000: loss 2.258734
iteration 2600 / 3000: loss 2.220088
iteration 2700 / 3000: loss 2.160037
iteration 2800 / 3000: loss 2.162099
iteration 2900 / 3000: loss 2.169093
0.01 2e-07 100 3000 0.22542857142857142 0.229
iteration 0 / 1500: loss 2.302585
iteration 100 / 1500: loss 2.302540
iteration 200 / 1500: loss 2.302596
iteration 300 / 1500: loss 2.302595
iteration 400 / 1500: loss 2.302602
iteration 500 / 1500: loss 2.302839
iteration 600 / 1500: loss 2.302399
iteration 700 / 1500: loss 2.302638
iteration 800 / 1500: loss 2.302492
iteration 900 / 1500: loss 2.302391
```

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iteration 1000 / 1500: loss 2.302188
iteration 1100 / 1500: loss 2.302269
iteration 1200 / 1500: loss 2.302604
iteration 1300 / 1500: loss 2.301440
iteration 1400 / 1500: loss 2.301645
0.01 2e-07 150 1500 0.09973469387755102 0.113
iteration 0 / 3000: loss 2.302585
iteration 100 / 3000: loss 2.302563
iteration 200 / 3000: loss 2.302631
iteration 300 / 3000: loss 2.302477
iteration 400 / 3000: loss 2.302772
iteration 500 / 3000: loss 2.302506
iteration 600 / 3000: loss 2.302655
iteration 700 / 3000: loss 2.302647
iteration 800 / 3000: loss 2.302432
iteration 900 / 3000: loss 2.302394
iteration 1000 / 3000: loss 2.302795
iteration 1100 / 3000: loss 2.302198
iteration 1200 / 3000: loss 2.302038
iteration 1300 / 3000: loss 2.302742
iteration 1400 / 3000: loss 2.301864
iteration 1500 / 3000: loss 2.301677
iteration 1600 / 3000: loss 2.299826
iteration 1700 / 3000: loss 2.298890
iteration 1800 / 3000: loss 2.296451
iteration 1900 / 3000: loss 2.293659
iteration 2000 / 3000: loss 2.286151
iteration 2100 / 3000: loss 2.274136
iteration 2200 / 3000: loss 2.267897
iteration 2300 / 3000: loss 2.258705
iteration 2400 / 3000: loss 2.234010
iteration 2500 / 3000: loss 2.219267
iteration 2600 / 3000: loss 2.222774
iteration 2700 / 3000: loss 2.162052
iteration 2800 / 3000: loss 2.145215
iteration 2900 / 3000: loss 2.097989
0.01 2e-07 150 3000 0.22053061224489795 0.227
iteration 0 / 1500: loss 2.302585
iteration 100 / 1500: loss 2.302712
iteration 200 / 1500: loss 2.302499
iteration 300 / 1500: loss 2.302624
iteration 400 / 1500: loss 2.302353
iteration 500 / 1500: loss 2.302877
iteration 600 / 1500: loss 2.302841
iteration 700 / 1500: loss 2.302409
iteration 800 / 1500: loss 2.302593
iteration 900 / 1500: loss 2.302764
iteration 1000 / 1500: loss 2.302312
iteration 1100 / 1500: loss 2.302225
iteration 1200 / 1500: loss 2.302077
iteration 1300 / 1500: loss 2.302521
iteration 1400 / 1500: loss 2.301736
0.01 2e-07 175 1500 0.16438775510204082 0.137
iteration 0 / 3000: loss 2.302585
iteration 100 / 3000: loss 2.302372
iteration 200 / 3000: loss 2.302878
iteration 300 / 3000: loss 2.302751
iteration 400 / 3000: loss 2.302939
iteration 500 / 3000: loss 2.302657
iteration 600 / 3000: loss 2.302907
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```
iteration 700 / 3000: loss 2.302776
iteration 800 / 3000: loss 2.302607
iteration 900 / 3000: loss 2.301990
iteration 1000 / 3000: loss 2.302340
iteration 1100 / 3000: loss 2.302366
iteration 1200 / 3000: loss 2.302131
iteration 1300 / 3000: loss 2.302303
iteration 1400 / 3000: loss 2.301259
iteration 1500 / 3000: loss 2.301075
iteration 1600 / 3000: loss 2.300169
iteration 1700 / 3000: loss 2.297560
iteration 1800 / 3000: loss 2.292704
iteration 1900 / 3000: loss 2.289782
iteration 2000 / 3000: loss 2.282547
iteration 2100 / 3000: loss 2.278380
iteration 2200 / 3000: loss 2.263431
iteration 2300 / 3000: loss 2.228548
iteration 2400 / 3000: loss 2.226201
iteration 2500 / 3000: loss 2.171598
iteration 2600 / 3000: loss 2.194760
iteration 2700 / 3000: loss 2.184700
iteration 2800 / 3000: loss 2.101624
iteration 2900 / 3000: loss 2.104112
0.01 2e-07 175 3000 0.22610204081632654 0.238
iteration 0 / 1500: loss 2.302585
iteration 100 / 1500: loss 2.302644
iteration 200 / 1500: loss 2.302478
iteration 300 / 1500: loss 2.302388
iteration 400 / 1500: loss 2.302529
iteration 500 / 1500: loss 2.302468
iteration 600 / 1500: loss 2.302544
iteration 700 / 1500: loss 2.302569
iteration 800 / 1500: loss 2.302753
iteration 900 / 1500: loss 2.302768
iteration 1000 / 1500: loss 2.302321
iteration 1100 / 1500: loss 2.302215
iteration 1200 / 1500: loss 2.302138
iteration 1300 / 1500: loss 2.301607
iteration 1400 / 1500: loss 2.301439
0.01 1e-07 100 1500 0.1070204081632653 0.102
iteration 0 / 3000: loss 2.302585
iteration 100 / 3000: loss 2.302703
iteration 200 / 3000: loss 2.302399
iteration 300 / 3000: loss 2.302826
iteration 400 / 3000: loss 2.302619
iteration 500 / 3000: loss 2.302652
iteration 600 / 3000: loss 2.302965
iteration 700 / 3000: loss 2.302807
iteration 800 / 3000: loss 2.302518
iteration 900 / 3000: loss 2.302443
iteration 1000 / 3000: loss 2.302669
iteration 1100 / 3000: loss 2.302155
iteration 1200 / 3000: loss 2.302319
iteration 1300 / 3000: loss 2.302065
iteration 1400 / 3000: loss 2.302032
iteration 1500 / 3000: loss 2.301116
iteration 1600 / 3000: loss 2.300535
iteration 1700 / 3000: loss 2.300073
iteration 1800 / 3000: loss 2.297418
iteration 1900 / 3000: loss 2.293003
```

```
iteration 2000 / 3000: loss 2.294170
iteration 2100 / 3000: loss 2.281406
iteration 2200 / 3000: loss 2.270719
iteration 2300 / 3000: loss 2.257893
iteration 2400 / 3000: loss 2.237729
iteration 2500 / 3000: loss 2.194151
iteration 2600 / 3000: loss 2.200797
iteration 2700 / 3000: loss 2.188218
iteration 2800 / 3000: loss 2.194815
iteration 2900 / 3000: loss 2.120827
0.01 1e-07 100 3000 0.23751020408163265 0.24
iteration 0 / 1500: loss 2.302585
iteration 100 / 1500: loss 2.302671
iteration 200 / 1500: loss 2.302384
iteration 300 / 1500: loss 2.302482
iteration 400 / 1500: loss 2.301626
iteration 500 / 1500: loss 2.302649
iteration 600 / 1500: loss 2.302525
iteration 700 / 1500: loss 2.302765
iteration 800 / 1500: loss 2.302801
iteration 900 / 1500: loss 2.302926
iteration 1000 / 1500: loss 2.302169
iteration 1100 / 1500: loss 2.302026
iteration 1200 / 1500: loss 2.302011
iteration 1300 / 1500: loss 2.302523
iteration 1400 / 1500: loss 2.301994
0.01 1e-07 150 1500 0.1466938775510204 0.136
iteration 0 / 3000: loss 2.302585
iteration 100 / 3000: loss 2.302607
iteration 200 / 3000: loss 2.302527
iteration 300 / 3000: loss 2.302969
iteration 400 / 3000: loss 2.302510
iteration 500 / 3000: loss 2.302596
iteration 600 / 3000: loss 2.302503
iteration 700 / 3000: loss 2.302206
iteration 800 / 3000: loss 2.302721
iteration 900 / 3000: loss 2.302597
iteration 1000 / 3000: loss 2.302324
iteration 1100 / 3000: loss 2.302197
iteration 1200 / 3000: loss 2.302448
iteration 1300 / 3000: loss 2.302359
iteration 1400 / 3000: loss 2.301896
iteration 1500 / 3000: loss 2.300958
iteration 1600 / 3000: loss 2.300187
iteration 1700 / 3000: loss 2.300165
iteration 1800 / 3000: loss 2.298185
iteration 1900 / 3000: loss 2.291383
iteration 2000 / 3000: loss 2.284457
iteration 2100 / 3000: loss 2.273926
iteration 2200 / 3000: loss 2.266884
iteration 2300 / 3000: loss 2.250609
iteration 2400 / 3000: loss 2.228279
iteration 2500 / 3000: loss 2.204118
iteration 2600 / 3000: loss 2.212226
iteration 2700 / 3000: loss 2.154979
iteration 2800 / 3000: loss 2.122800
iteration 2900 / 3000: loss 2.097730
0.01 1e-07 150 3000 0.22844897959183674 0.237
iteration 0 / 1500: loss 2.302585
iteration 100 / 1500: loss 2.302739
```

```
iteration 200 / 1500: loss 2.302319
iteration 300 / 1500: loss 2.302449
iteration 400 / 1500: loss 2.302542
iteration 500 / 1500: loss 2.302447
iteration 600 / 1500: loss 2.302920
iteration 700 / 1500: loss 2.302200
iteration 800 / 1500: loss 2.302850
iteration 900 / 1500: loss 2.302698
iteration 1000 / 1500: loss 2.302572
iteration 1100 / 1500: loss 2.302235
iteration 1200 / 1500: loss 2.301657
iteration 1300 / 1500: loss 2.301871
iteration 1400 / 1500: loss 2.301647
0.01 1e-07 175 1500 0.15210204081632653 0.123
iteration 0 / 3000: loss 2.302585
iteration 100 / 3000: loss 2.302565
iteration 200 / 3000: loss 2.302949
iteration 300 / 3000: loss 2.302270
iteration 400 / 3000: loss 2.302519
iteration 500 / 3000: loss 2.301678
iteration 600 / 3000: loss 2.302605
iteration 700 / 3000: loss 2.302892
iteration 800 / 3000: loss 2.303030
iteration 900 / 3000: loss 2.302206
iteration 1000 / 3000: loss 2.302667
iteration 1100 / 3000: loss 2.302402
iteration 1200 / 3000: loss 2.301703
iteration 1300 / 3000: loss 2.301596
iteration 1400 / 3000: loss 2.301610
iteration 1500 / 3000: loss 2.301427
iteration 1600 / 3000: loss 2.299857
iteration 1700 / 3000: loss 2.297366
iteration 1800 / 3000: loss 2.294597
iteration 1900 / 3000: loss 2.286632
iteration 2000 / 3000: loss 2.283065
iteration 2100 / 3000: loss 2.261999
iteration 2200 / 3000: loss 2.252287
iteration 2300 / 3000: loss 2.219027
iteration 2400 / 3000: loss 2.229507
iteration 2500 / 3000: loss 2.223188
iteration 2600 / 3000: loss 2.199199
iteration 2700 / 3000: loss 2.159499
iteration 2800 / 3000: loss 2.123331
iteration 2900 / 3000: loss 2.099282
0.01 1e-07 175 3000 0.22853061224489796 0.238
iteration 0 / 1500: loss 2.302585
iteration 100 / 1500: loss 2.302442
iteration 200 / 1500: loss 2.302642
iteration 300 / 1500: loss 2.302479
iteration 400 / 1500: loss 2.302237
iteration 500 / 1500: loss 2.302822
iteration 600 / 1500: loss 2.302235
iteration 700 / 1500: loss 2.302426
iteration 800 / 1500: loss 2.302163
iteration 900 / 1500: loss 2.302943
iteration 1000 / 1500: loss 2.302986
iteration 1100 / 1500: loss 2.302309
iteration 1200 / 1500: loss 2.302039
iteration 1300 / 1500: loss 2.302187
iteration 1400 / 1500: loss 2.301045
```

```
0.01 2e-05 100 1500 0.14420408163265305 0.114
iteration 0 / 3000: loss 2.302585
iteration 100 / 3000: loss 2.302538
iteration 200 / 3000: loss 2.302608
iteration 300 / 3000: loss 2.302563
iteration 400 / 3000: loss 2.302659
iteration 500 / 3000: loss 2.302384
iteration 600 / 3000: loss 2.302592
iteration 700 / 3000: loss 2.302677
iteration 800 / 3000: loss 2.302580
iteration 900 / 3000: loss 2.302607
iteration 1000 / 3000: loss 2.302196
iteration 1100 / 3000: loss 2.302608
iteration 1200 / 3000: loss 2.302411
iteration 1300 / 3000: loss 2.302046
iteration 1400 / 3000: loss 2.301888
iteration 1500 / 3000: loss 2.301288
iteration 1600 / 3000: loss 2.300899
iteration 1700 / 3000: loss 2.299483
iteration 1800 / 3000: loss 2.298019
iteration 1900 / 3000: loss 2.294437
iteration 2000 / 3000: loss 2.288907
iteration 2100 / 3000: loss 2.282757
iteration 2200 / 3000: loss 2.274444
iteration 2300 / 3000: loss 2.255691
iteration 2400 / 3000: loss 2.226529
iteration 2500 / 3000: loss 2.216729
iteration 2600 / 3000: loss 2.219719
iteration 2700 / 3000: loss 2.173546
iteration 2800 / 3000: loss 2.129247
iteration 2900 / 3000: loss 2.164320
0.01 2e-05 100 3000 0.2257142857142857 0.231
iteration 0 / 1500: loss 2.302585
iteration 100 / 1500: loss 2.302590
iteration 200 / 1500: loss 2.302669
iteration 300 / 1500: loss 2.302881
iteration 400 / 1500: loss 2.302754
iteration 500 / 1500: loss 2.302584
iteration 600 / 1500: loss 2.302606
iteration 700 / 1500: loss 2.302535
iteration 800 / 1500: loss 2.302563
iteration 900 / 1500: loss 2.302261
iteration 1000 / 1500: loss 2.302769
iteration 1100 / 1500: loss 2.302256
iteration 1200 / 1500: loss 2.302271
iteration 1300 / 1500: loss 2.302136
iteration 1400 / 1500: loss 2.301716
0.01 2e-05 150 1500 0.18193877551020407 0.201
iteration 0 / 3000: loss 2.302585
iteration 100 / 3000: loss 2.302464
iteration 200 / 3000: loss 2.302680
iteration 300 / 3000: loss 2.302705
iteration 400 / 3000: loss 2.302140
iteration 500 / 3000: loss 2.302290
iteration 600 / 3000: loss 2.302594
iteration 700 / 3000: loss 2.302060
iteration 800 / 3000: loss 2.302608
iteration 900 / 3000: loss 2.301997
iteration 1000 / 3000: loss 2.301984
iteration 1100 / 3000: loss 2.302805
```

```
iteration 1200 / 3000: loss 2.302528
iteration 1300 / 3000: loss 2.301978
iteration 1400 / 3000: loss 2.301621
iteration 1500 / 3000: loss 2.301262
iteration 1600 / 3000: loss 2.299780
iteration 1700 / 3000: loss 2.298482
iteration 1800 / 3000: loss 2.297186
iteration 1900 / 3000: loss 2.291540
iteration 2000 / 3000: loss 2.286660
iteration 2100 / 3000: loss 2.276794
iteration 2200 / 3000: loss 2.274018
iteration 2300 / 3000: loss 2.236958
iteration 2400 / 3000: loss 2.219090
iteration 2500 / 3000: loss 2.187036
iteration 2600 / 3000: loss 2.197137
iteration 2700 / 3000: loss 2.159185
iteration 2800 / 3000: loss 2.123648
iteration 2900 / 3000: loss 2.154456
0.01 2e-05 150 3000 0.22646938775510203 0.236
iteration 0 / 1500: loss 2.302585
iteration 100 / 1500: loss 2.302417
iteration 200 / 1500: loss 2.302522
iteration 300 / 1500: loss 2.302280
iteration 400 / 1500: loss 2.302275
iteration 500 / 1500: loss 2.303152
iteration 600 / 1500: loss 2.302241
iteration 700 / 1500: loss 2.302172
iteration 800 / 1500: loss 2.302780
iteration 900 / 1500: loss 2.302562
iteration 1000 / 1500: loss 2.302184
iteration 1100 / 1500: loss 2.302570
iteration 1200 / 1500: loss 2.302123
iteration 1300 / 1500: loss 2.301957
iteration 1400 / 1500: loss 2.301381
0.01 2e-05 175 1500 0.10026530612244898 0.087
iteration 0 / 3000: loss 2.302585
iteration 100 / 3000: loss 2.302693
iteration 200 / 3000: loss 2.302444
iteration 300 / 3000: loss 2.302715
iteration 400 / 3000: loss 2.302563
iteration 500 / 3000: loss 2.302223
iteration 600 / 3000: loss 2.302527
iteration 700 / 3000: loss 2.302216
iteration 800 / 3000: loss 2.302796
iteration 900 / 3000: loss 2.301881
iteration 1000 / 3000: loss 2.302430
iteration 1100 / 3000: loss 2.302662
iteration 1200 / 3000: loss 2.302348
iteration 1300 / 3000: loss 2.302231
iteration 1400 / 3000: loss 2.301804
iteration 1500 / 3000: loss 2.301310
iteration 1600 / 3000: loss 2.300744
iteration 1700 / 3000: loss 2.298646
iteration 1800 / 3000: loss 2.295363
iteration 1900 / 3000: loss 2.292592
iteration 2000 / 3000: loss 2.285332
iteration 2100 / 3000: loss 2.278908
iteration 2200 / 3000: loss 2.266085
iteration 2300 / 3000: loss 2.260659
iteration 2400 / 3000: loss 2.252183
```

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iteration 2500 / 3000: loss 2.214742
iteration 2600 / 3000: loss 2.145333
iteration 2700 / 3000: loss 2.179101
iteration 2800 / 3000: loss 2.140991
iteration 2900 / 3000: loss 2.153157
0.01 2e-05 175 3000 0.23173469387755102 0.255
iteration 0 / 1500: loss 2.302585
iteration 100 / 1500: loss 2.302598
iteration 200 / 1500: loss 2.302633
iteration 300 / 1500: loss 2.302686
iteration 400 / 1500: loss 2.302631
iteration 500 / 1500: loss 2.302598
iteration 600 / 1500: loss 2.302514
iteration 700 / 1500: loss 2.302789
iteration 800 / 1500: loss 2.302664
iteration 900 / 1500: loss 2.302579
iteration 1000 / 1500: loss 2.302507
iteration 1100 / 1500: loss 2.302752
iteration 1200 / 1500: loss 2.302552
iteration 1300 / 1500: loss 2.302490
iteration 1400 / 1500: loss 2.302505
0.002 2e-07 100 1500 0.09985714285714285 0.107
iteration 0 / 3000: loss 2.302585
iteration 100 / 3000: loss 2.302579
iteration 200 / 3000: loss 2.302575
iteration 300 / 3000: loss 2.302496
iteration 400 / 3000: loss 2.302408
iteration 500 / 3000: loss 2.302436
iteration 600 / 3000: loss 2.302518
iteration 700 / 3000: loss 2.302472
iteration 800 / 3000: loss 2.302752
iteration 900 / 3000: loss 2.302604
iteration 1000 / 3000: loss 2.302600
iteration 1100 / 3000: loss 2.302580
iteration 1200 / 3000: loss 2.302732
iteration 1300 / 3000: loss 2.302572
iteration 1400 / 3000: loss 2.302624
iteration 1500 / 3000: loss 2.302704
iteration 1600 / 3000: loss 2.302743
iteration 1700 / 3000: loss 2.302557
iteration 1800 / 3000: loss 2.302759
iteration 1900 / 3000: loss 2.302641
iteration 2000 / 3000: loss 2.302648
iteration 2100 / 3000: loss 2.302766
iteration 2200 / 3000: loss 2.302628
iteration 2300 / 3000: loss 2.302586
iteration 2400 / 3000: loss 2.302570
iteration 2500 / 3000: loss 2.302693
iteration 2600 / 3000: loss 2.302557
iteration 2700 / 3000: loss 2.302556
iteration 2800 / 3000: loss 2.302496
iteration 2900 / 3000: loss 2.302458
0.002 2e-07 100 3000 0.10004081632653061 0.098
iteration 0 / 1500: loss 2.302585
iteration 100 / 1500: loss 2.302588
iteration 200 / 1500: loss 2.302496
iteration 300 / 1500: loss 2.302537
iteration 400 / 1500: loss 2.302579
iteration 500 / 1500: loss 2.302557
iteration 600 / 1500: loss 2.302507
```

```
iteration 700 / 1500: loss 2.302604
iteration 800 / 1500: loss 2.302646
iteration 900 / 1500: loss 2.302490
iteration 1000 / 1500: loss 2.302423
iteration 1100 / 1500: loss 2.302663
iteration 1200 / 1500: loss 2.302497
iteration 1300 / 1500: loss 2.302672
iteration 1400 / 1500: loss 2.302370
0.002 2e-07 150 1500 0.10044897959183674 0.078
iteration 0 / 3000: loss 2.302585
iteration 100 / 3000: loss 2.302579
iteration 200 / 3000: loss 2.302596
iteration 300 / 3000: loss 2.302467
iteration 400 / 3000: loss 2.302614
iteration 500 / 3000: loss 2.302534
iteration 600 / 3000: loss 2.302573
iteration 700 / 3000: loss 2.302641
iteration 800 / 3000: loss 2.302703
iteration 900 / 3000: loss 2.302621
iteration 1000 / 3000: loss 2.302544
iteration 1100 / 3000: loss 2.302563
iteration 1200 / 3000: loss 2.302517
iteration 1300 / 3000: loss 2.302529
iteration 1400 / 3000: loss 2.302607
iteration 1500 / 3000: loss 2.302554
iteration 1600 / 3000: loss 2.302661
iteration 1700 / 3000: loss 2.302581
iteration 1800 / 3000: loss 2.302563
iteration 1900 / 3000: loss 2.302562
iteration 2000 / 3000: loss 2.302551
iteration 2100 / 3000: loss 2.302514
iteration 2200 / 3000: loss 2.302467
iteration 2300 / 3000: loss 2.302622
iteration 2400 / 3000: loss 2.302478
iteration 2500 / 3000: loss 2.302706
iteration 2600 / 3000: loss 2.302542
iteration 2700 / 3000: loss 2.302449
iteration 2800 / 3000: loss 2.302618
iteration 2900 / 3000: loss 2.302611
0.002 2e-07 150 3000 0.10044897959183674 0.078
iteration 0 / 1500: loss 2.302585
iteration 100 / 1500: loss 2.302589
iteration 200 / 1500: loss 2.302597
iteration 300 / 1500: loss 2.302553
iteration 400 / 1500: loss 2.302659
iteration 500 / 1500: loss 2.302710
iteration 600 / 1500: loss 2.302721
iteration 700 / 1500: loss 2.302615
iteration 800 / 1500: loss 2.302544
iteration 900 / 1500: loss 2.302553
iteration 1000 / 1500: loss 2.302593
iteration 1100 / 1500: loss 2.302596
iteration 1200 / 1500: loss 2.302605
iteration 1300 / 1500: loss 2.302567
iteration 1400 / 1500: loss 2.302612
0.002 2e-07 175 1500 0.10004081632653061 0.098
iteration 0 / 3000: loss 2.302585
iteration 100 / 3000: loss 2.302597
iteration 200 / 3000: loss 2.302583
iteration 300 / 3000: loss 2.302671
```

```
iteration 400 / 3000: loss 2.302533
iteration 500 / 3000: loss 2.302603
iteration 600 / 3000: loss 2.302617
iteration 700 / 3000: loss 2.302582
iteration 800 / 3000: loss 2.302616
iteration 900 / 3000: loss 2.302623
iteration 1000 / 3000: loss 2.302487
iteration 1100 / 3000: loss 2.302506
iteration 1200 / 3000: loss 2.302589
iteration 1300 / 3000: loss 2.302561
iteration 1400 / 3000: loss 2.302524
iteration 1500 / 3000: loss 2.302663
iteration 1600 / 3000: loss 2.302599
iteration 1700 / 3000: loss 2.302477
iteration 1800 / 3000: loss 2.302498
iteration 1900 / 3000: loss 2.302489
iteration 2000 / 3000: loss 2.302415
iteration 2100 / 3000: loss 2.302623
iteration 2200 / 3000: loss 2.302620
iteration 2300 / 3000: loss 2.302544
iteration 2400 / 3000: loss 2.302818
iteration 2500 / 3000: loss 2.302699
iteration 2600 / 3000: loss 2.302597
iteration 2700 / 3000: loss 2.302661
iteration 2800 / 3000: loss 2.302787
iteration 2900 / 3000: loss 2.302555
0.002 2e-07 175 3000 0.10042857142857142 0.079
iteration 0 / 1500: loss 2.302585
iteration 100 / 1500: loss 2.302615
iteration 200 / 1500: loss 2.302602
iteration 300 / 1500: loss 2.302554
iteration 400 / 1500: loss 2.302594
iteration 500 / 1500: loss 2.302588
iteration 600 / 1500: loss 2.302597
iteration 700 / 1500: loss 2.302612
iteration 800 / 1500: loss 2.302725
iteration 900 / 1500: loss 2.302512
iteration 1000 / 1500: loss 2.302500
iteration 1100 / 1500: loss 2.302682
iteration 1200 / 1500: loss 2.302623
iteration 1300 / 1500: loss 2.302530
iteration 1400 / 1500: loss 2.302615
0.002 1e-07 100 1500 0.10026530612244898 0.087
iteration 0 / 3000: loss 2.302585
iteration 100 / 3000: loss 2.302594
iteration 200 / 3000: loss 2.302584
iteration 300 / 3000: loss 2.302602
iteration 400 / 3000: loss 2.302587
iteration 500 / 3000: loss 2.302636
iteration 600 / 3000: loss 2.302575
iteration 700 / 3000: loss 2.302645
iteration 800 / 3000: loss 2.302553
iteration 900 / 3000: loss 2.302697
iteration 1000 / 3000: loss 2.302674
iteration 1100 / 3000: loss 2.302590
iteration 1200 / 3000: loss 2.302633
iteration 1300 / 3000: loss 2.302619
iteration 1400 / 3000: loss 2.302499
iteration 1500 / 3000: loss 2.302598
iteration 1600 / 3000: loss 2.302629
```

```
iteration 1700 / 3000: loss 2.302622
iteration 1800 / 3000: loss 2.302624
iteration 1900 / 3000: loss 2.302539
iteration 2000 / 3000: loss 2.302532
iteration 2100 / 3000: loss 2.302595
iteration 2200 / 3000: loss 2.302503
iteration 2300 / 3000: loss 2.302622
iteration 2400 / 3000: loss 2.302468
iteration 2500 / 3000: loss 2.302413
iteration 2600 / 3000: loss 2.302551
iteration 2700 / 3000: loss 2.302616
iteration 2800 / 3000: loss 2.302598
iteration 2900 / 3000: loss 2.302543
0.002 1e-07 100 3000 0.10044897959183674 0.078
iteration 0 / 1500: loss 2.302585
iteration 100 / 1500: loss 2.302642
iteration 200 / 1500: loss 2.302588
iteration 300 / 1500: loss 2.302567
iteration 400 / 1500: loss 2.302566
iteration 500 / 1500: loss 2.302675
iteration 600 / 1500: loss 2.302394
iteration 700 / 1500: loss 2.302549
iteration 800 / 1500: loss 2.302631
iteration 900 / 1500: loss 2.302534
iteration 1000 / 1500: loss 2.302519
iteration 1100 / 1500: loss 2.302509
iteration 1200 / 1500: loss 2.302641
iteration 1300 / 1500: loss 2.302715
iteration 1400 / 1500: loss 2.302517
0.002 1e-07 150 1500 0.10042857142857142 0.079
iteration 0 / 3000: loss 2.302585
iteration 100 / 3000: loss 2.302533
iteration 200 / 3000: loss 2.302635
iteration 300 / 3000: loss 2.302541
iteration 400 / 3000: loss 2.302550
iteration 500 / 3000: loss 2.302608
iteration 600 / 3000: loss 2.302529
iteration 700 / 3000: loss 2.302490
iteration 800 / 3000: loss 2.302635
iteration 900 / 3000: loss 2.302563
iteration 1000 / 3000: loss 2.302611
iteration 1100 / 3000: loss 2.302656
iteration 1200 / 3000: loss 2.302471
iteration 1300 / 3000: loss 2.302592
iteration 1400 / 3000: loss 2.302592
iteration 1500 / 3000: loss 2.302543
iteration 1600 / 3000: loss 2.302757
iteration 1700 / 3000: loss 2.302626
iteration 1800 / 3000: loss 2.302368
iteration 1900 / 3000: loss 2.302462
iteration 2000 / 3000: loss 2.302676
iteration 2100 / 3000: loss 2.302615
iteration 2200 / 3000: loss 2.302693
iteration 2300 / 3000: loss 2.302603
iteration 2400 / 3000: loss 2.302740
iteration 2500 / 3000: loss 2.302679
iteration 2600 / 3000: loss 2.302763
iteration 2700 / 3000: loss 2.302647
iteration 2800 / 3000: loss 2.302581
iteration 2900 / 3000: loss 2.302335
```

```
0.002 1e-07 150 3000 0.10042857142857142 0.079
iteration 0 / 1500: loss 2.302585
iteration 100 / 1500: loss 2.302603
iteration 200 / 1500: loss 2.302597
iteration 300 / 1500: loss 2.302547
iteration 400 / 1500: loss 2.302540
iteration 500 / 1500: loss 2.302520
iteration 600 / 1500: loss 2.302701
iteration 700 / 1500: loss 2.302650
iteration 800 / 1500: loss 2.302689
iteration 900 / 1500: loss 2.302506
iteration 1000 / 1500: loss 2.302701
iteration 1100 / 1500: loss 2.302623
iteration 1200 / 1500: loss 2.302350
iteration 1300 / 1500: loss 2.302557
iteration 1400 / 1500: loss 2.302481
0.002 1e-07 175 1500 0.10042857142857142 0.079
iteration 0 / 3000: loss 2.302585
iteration 100 / 3000: loss 2.302570
iteration 200 / 3000: loss 2.302630
iteration 300 / 3000: loss 2.302594
iteration 400 / 3000: loss 2.302570
iteration 500 / 3000: loss 2.302643
iteration 600 / 3000: loss 2.302646
iteration 700 / 3000: loss 2.302613
iteration 800 / 3000: loss 2.302608
iteration 900 / 3000: loss 2.302604
iteration 1000 / 3000: loss 2.302671
iteration 1100 / 3000: loss 2.302721
iteration 1200 / 3000: loss 2.302441
iteration 1300 / 3000: loss 2.302680
iteration 1400 / 3000: loss 2.302514
iteration 1500 / 3000: loss 2.302565
iteration 1600 / 3000: loss 2.302696
iteration 1700 / 3000: loss 2.302617
iteration 1800 / 3000: loss 2.302794
iteration 1900 / 3000: loss 2.302595
iteration 2000 / 3000: loss 2.302544
iteration 2100 / 3000: loss 2.302607
iteration 2200 / 3000: loss 2.302527
iteration 2300 / 3000: loss 2.302755
iteration 2400 / 3000: loss 2.302579
iteration 2500 / 3000: loss 2.302476
iteration 2600 / 3000: loss 2.302660
iteration 2700 / 3000: loss 2.302676
iteration 2800 / 3000: loss 2.302607
iteration 2900 / 3000: loss 2.302570
0.002 1e-07 175 3000 0.10026530612244898 0.087
iteration 0 / 1500: loss 2.302585
iteration 100 / 1500: loss 2.302591
iteration 200 / 1500: loss 2.302597
iteration 300 / 1500: loss 2.302583
iteration 400 / 1500: loss 2.302533
iteration 500 / 1500: loss 2.302484
iteration 600 / 1500: loss 2.302482
iteration 700 / 1500: loss 2.302593
iteration 800 / 1500: loss 2.302693
iteration 900 / 1500: loss 2.302502
iteration 1000 / 1500: loss 2.302777
iteration 1100 / 1500: loss 2.302601
```

```
iteration 1200 / 1500: loss 2.302549
iteration 1300 / 1500: loss 2.302636
iteration 1400 / 1500: loss 2.302662
0.002 2e-05 100 1500 0.10042857142857142 0.079
iteration 0 / 3000: loss 2.302585
iteration 100 / 3000: loss 2.302579
iteration 200 / 3000: loss 2.302597
iteration 300 / 3000: loss 2.302641
iteration 400 / 3000: loss 2.302533
iteration 500 / 3000: loss 2.302470
iteration 600 / 3000: loss 2.302508
iteration 700 / 3000: loss 2.302558
iteration 800 / 3000: loss 2.302607
iteration 900 / 3000: loss 2.302523
iteration 1000 / 3000: loss 2.302558
iteration 1100 / 3000: loss 2.302545
iteration 1200 / 3000: loss 2.302477
iteration 1300 / 3000: loss 2.302635
iteration 1400 / 3000: loss 2.302544
iteration 1500 / 3000: loss 2.302573
iteration 1600 / 3000: loss 2.302606
iteration 1700 / 3000: loss 2.302544
iteration 1800 / 3000: loss 2.302621
iteration 1900 / 3000: loss 2.302547
iteration 2000 / 3000: loss 2.302579
iteration 2100 / 3000: loss 2.302634
iteration 2200 / 3000: loss 2.302504
iteration 2300 / 3000: loss 2.302654
iteration 2400 / 3000: loss 2.302525
iteration 2500 / 3000: loss 2.302428
iteration 2600 / 3000: loss 2.302682
iteration 2700 / 3000: loss 2.302359
iteration 2800 / 3000: loss 2.302484
iteration 2900 / 3000: loss 2.302696
0.002 2e-05 100 3000 0.10042857142857142 0.079
iteration 0 / 1500: loss 2.302585
iteration 100 / 1500: loss 2.302532
iteration 200 / 1500: loss 2.302548
iteration 300 / 1500: loss 2.302577
iteration 400 / 1500: loss 2.302604
iteration 500 / 1500: loss 2.302627
iteration 600 / 1500: loss 2.302595
iteration 700 / 1500: loss 2.302599
iteration 800 / 1500: loss 2.302627
iteration 900 / 1500: loss 2.302574
iteration 1000 / 1500: loss 2.302630
iteration 1100 / 1500: loss 2.302559
iteration 1200 / 1500: loss 2.302564
iteration 1300 / 1500: loss 2.302619
iteration 1400 / 1500: loss 2.302538
0.002 2e-05 150 1500 0.09985714285714285 0.107
iteration 0 / 3000: loss 2.302585
iteration 100 / 3000: loss 2.302601
iteration 200 / 3000: loss 2.302580
iteration 300 / 3000: loss 2.302550
iteration 400 / 3000: loss 2.302628
iteration 500 / 3000: loss 2.302581
iteration 600 / 3000: loss 2.302602
iteration 700 / 3000: loss 2.302615
iteration 800 / 3000: loss 2.302612
```

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iteration 900 / 3000: loss 2.302533
iteration 1000 / 3000: loss 2.302445
iteration 1100 / 3000: loss 2.302469
iteration 1200 / 3000: loss 2.302497
iteration 1300 / 3000: loss 2.302539
iteration 1400 / 3000: loss 2.302647
iteration 1500 / 3000: loss 2.302631
iteration 1600 / 3000: loss 2.302613
iteration 1700 / 3000: loss 2.302610
iteration 1800 / 3000: loss 2.302764
iteration 1900 / 3000: loss 2.302512
iteration 2000 / 3000: loss 2.302595
iteration 2100 / 3000: loss 2.302700
iteration 2200 / 3000: loss 2.302373
iteration 2300 / 3000: loss 2.302648
iteration 2400 / 3000: loss 2.302673
iteration 2500 / 3000: loss 2.302463
iteration 2600 / 3000: loss 2.302557
iteration 2700 / 3000: loss 2.302611
iteration 2800 / 3000: loss 2.302531
iteration 2900 / 3000: loss 2.302550
0.002 2e-05 150 3000 0.10044897959183674 0.078
iteration 0 / 1500: loss 2.302585
iteration 100 / 1500: loss 2.302608
iteration 200 / 1500: loss 2.302597
iteration 300 / 1500: loss 2.302553
iteration 400 / 1500: loss 2.302422
iteration 500 / 1500: loss 2.302544
iteration 600 / 1500: loss 2.302437
iteration 700 / 1500: loss 2.302565
iteration 800 / 1500: loss 2.302633
iteration 900 / 1500: loss 2.302391
iteration 1000 / 1500: loss 2.302695
iteration 1100 / 1500: loss 2.302614
iteration 1200 / 1500: loss 2.302506
iteration 1300 / 1500: loss 2.302456
iteration 1400 / 1500: loss 2.302767
0.002 2e-05 175 1500 0.09973469387755102 0.113
iteration 0 / 3000: loss 2.302585
iteration 100 / 3000: loss 2.302632
iteration 200 / 3000: loss 2.302558
iteration 300 / 3000: loss 2.302522
iteration 400 / 3000: loss 2.302640
iteration 500 / 3000: loss 2.302658
iteration 600 / 3000: loss 2.302640
iteration 700 / 3000: loss 2.302646
iteration 800 / 3000: loss 2.302487
iteration 900 / 3000: loss 2.302505
iteration 1000 / 3000: loss 2.302634
iteration 1100 / 3000: loss 2.302687
iteration 1200 / 3000: loss 2.302752
iteration 1300 / 3000: loss 2.302464
iteration 1400 / 3000: loss 2.302605
iteration 1500 / 3000: loss 2.302570
iteration 1600 / 3000: loss 2.302541
iteration 1700 / 3000: loss 2.302626
iteration 1800 / 3000: loss 2.302587
iteration 1900 / 3000: loss 2.302490
iteration 2000 / 3000: loss 2.302645
iteration 2100 / 3000: loss 2.302543
```

```
iteration 2200 / 3000: loss 2.302546
iteration 2300 / 3000: loss 2.302656
iteration 2400 / 3000: loss 2.302649
iteration 2500 / 3000: loss 2.302740
iteration 2600 / 3000: loss 2.302476
iteration 2700 / 3000: loss 2.302659
iteration 2800 / 3000: loss 2.302540
iteration 2900 / 3000: loss 2.302452
0.002 2e-05 175 3000 0.10044897959183674 0.078
In []: # Run your best neural net classifier on the test set. You should be able
# to get more than 55% accuracy.

test_acc = (best_net.predict(X_test_feats) == y_test).mean()
print(test_acc)

0.573
```