

## Knapsack

Shelflife [ ]

double fractional knapsack Bruteforce (weights[], values[], capacity)

- // Input :-
  - Array of weight of each item ,
  - Array of values of each item ,
  - Array of shelflife
  - Total ~~constraint~~ capacity

$n = \text{number of items}$ .

max-value = 0

- // Generate all subsets of items.

for each subset of item:

subset-weight = 0

subset-value = 0

- // calculate total weight and value for this subset
  - & for each item in subset

if subset-weight + weight[item] <= capacity

subset-weight += weight[item]

subset-value += value[item]

else

remaining-capacity = capacity - subset-weight

subset-value += values[item] \* (remaining-capacity / weights[item])

subset-weight = capacity  
break.

if subset\_value > max\_value

max\_value = subset\_value

### Time Complexity

- 1) As we first generate all possible subsets of given items.  
∴ Generation of subsets =  $O(2^n)$
- 2) Subset Evaluation:  
For each subset the algorithm runs for the subsets size times.
- 3) Total Time complexity :-  
 $O(n \cdot 2^n)$

## Knapsack - Greedy Approach

double functi fractionalKnapsack ( weight [ ], value [ ], shelflife [ ], capacity )

- // Input :-
  - 1) Array of weight of each item
  - 2) Array of value of each item.
  - 3) Array of shelflife of each item.
  - 4) Total capacity

// Output :- Maximum value,

// Sort according to shelflife / value ratio

```
vector < pair < double, pair < int, int >> v
for (i = 0; i < weights.size(); i++) {
    double ratio = value[i] / shelflife[i] * weight[i]
    v.push_back({ratio, {weights[i], values[i]}})
```

// Sort vector v

Sort ( v.begin, v.end)

current\_weight = 0

current\_value = 0

for (i = 0; i < v.size(); i++) :

w = v[i].second \* first

v = v[i].second, second.

if ( w + current\_weight <= capacity )

current\_value += v

else

$$\text{remaining\_capacity} = \text{capacity} - \text{current\_weight}$$

$$\text{current_value} += v * (\text{remaining\_capacity} / w)$$

$$\text{current\_weight} = \text{capacity}$$

break;

return current\_value.

\* Time Complexity :

- 1) As we first generate all possible subset of given items.  
 $\therefore$  Generation of

Time Complexity :  $\rightarrow n$

- 1) Creating a vector pair of ratio of shelflife / value and weight and value of each item  
=  $O(n)$

- 2) Sorting this created vector  
=  $O(n \log n)$

- 3) Calculating answer using: greedy approach  
=  $O(n)$

Total time complexity :-

$$= O(2n + n \log n)$$

$$= O(n \log n)$$

Test-cases.

Capacity	weight	values	shelflife	Max value
50	[10, 20, 30]	[60, 100, 120]	[2, 3, 5]	230
100	[10, 20, 30]	[10, 20, 115]	[2, 3, 5]	145
100	[10, 20, 30, 40, 50] 60, 70]	[10, 20, 5, 8, 55], [9, 12]	[2, 3, 5], [9, 12]	25.2852
50	[10, -20, 30]	[60, -100, 120]	[2, 3, 5]	error.
-12	[10, 20, 30]	[60, 100, 120]	[2, 3, 5)	error.

## Huffman Node Tree

HuffmanNode\* buildHuffmanTree (const string & text)  
unordered\_map <char

// Objective :- To find out the frequency of char  
and formation of tree

// Input :- A string name text.

A // Output :- return the top element of the  
tree

// calculate frequency of each element.

for (char ch : text) do

if (isalpha(ch)) do

frequencyMap[ch]++;

// Priority queue queue to build the tree based  
on frequency.

priority-queue

priority-queue <HuffmanNode\*, vector <HuffmanNode\*>,  
Compare > minHeap.

// Insert each char and its frequency as a node  
into the minHeap.

for (const auto& pair : frequencyMap) do  
minHeap.push (new HuffmanNode {pair.first,  
pair.second})

#1

```
// Build Huffman tree
while (minHeap.size() >= 1) do
    HuffmanNode* left = minHeap.top()
    minHeap.pop()
    HuffmanNode* right = minHeap.top()
    minHeap.pop()
    HuffmanNode* merged = new HuffmanNode('10', left->freq + right->freq)
```

```
def push(node, freq) {
    merged->left = left
    merged->right = right
    minHeap.push(merged)
}
return minHeap.top().info
```

```
// function to generate Huffman code.
```

```
void generateCode(HuffmanNode* root, const string& code,
                  map<char, string> & huffmanCode) {
    if (root->left == NULL && root->right == NULL) {
        huffmanCode[root->info] = code;
    } else {
        generateCode(root->left, code + "0", huffmanCode);
        generateCode(root->right, code + "1", huffmanCode);
    }
}
```

Objective:- To generate Huffman code.

Input :- 1) root node

2) a string var code

3) a map · hashmap.

Output :- ~~ex - traverse the void.~~

```
if (!root) return
```

```
If (root → character) = '0' do
    huffmanCodes [root → character] = code
    generateCodes (root → left, code + "0", huffmanCodes)
    generateCodes (root → right, code + "1", huffmanCodes)
```

// function to compress text using Huffman coding.

```
String compress (const string & text, map<char, string>&
    huffmanCode)
```

// Objective :- To compress Text

// Input :- a String, a hashMap

// Output :- a String.

```
for (char ch : text) do
    if (huffmanCode.find(ch) != huffmanCode.end())
        compressedText += huffmanCode[ch];
return compressedText.
```

```
else compress string at -writing
show tree() -> input
show root private o (E
downcast from o (E
show off member vars -> input
writer (tree !) {
```

## Time Complexity.

- 1) Count frequency of every letter using loop =  $O(n)$
- 2)  $\neq$
- 2) To build priority queue for each unique character K we will have =  $O(K \log K)$
- 3) for merging its the loop runs  $(K-1)$  times, =  $O(K^2)$

Overall Overall :-

$$\begin{aligned}\text{Time complexity} &= O(n) + O(K \log K) + O(K) \\ &= O(K \log K)\end{aligned}$$

Test Case :-

	File type	Original text size	Compressed size	Compressed ratio
1)	Text	1 016	441	0.43
2)	DOCX	50 216	21390	0.43
3)	HTML	50 450	21433	0.42
4)	PDF	2680	526	0.43
5)	PDF (empty)	no - content extracted.		