## Data Mining:

## **Concepts and Techniques**

(3<sup>rd</sup> ed.)

#### — Chapter 5 —

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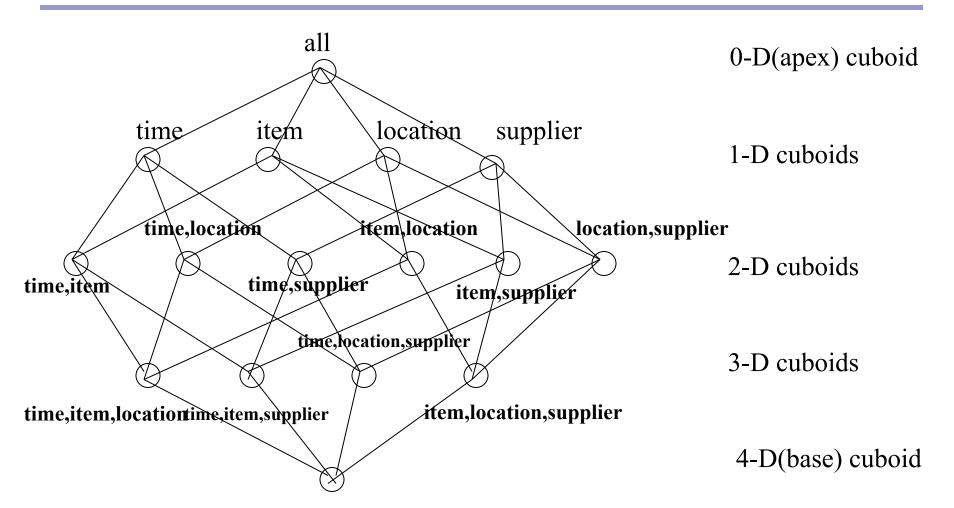
### **Chapter 5: Data Cube Technology**

Data Cube Computation: Preliminary Concepts



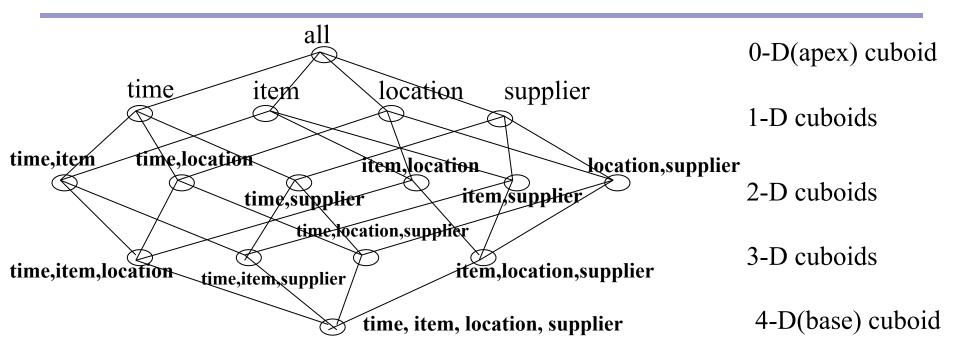
- Data Cube Computation Methods
- Processing Advanced Queries by Exploring DataCube Technology
- Multidimensional Data Analysis in Cube Space
- Summary

#### **Data Cube: A Lattice of Cuboids**



time, item, location, supplierc

#### **Data Cube: A Lattice of Cuboids**

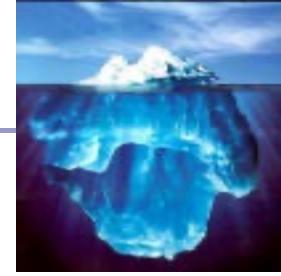


- Base vs. aggregate cells; ancestor vs. descendant cells; parent vs. child cells
  - 1. (9/15, milk, Urbana, Dairy\_land)
  - 2. (9/15, milk, Urbana, \*)
  - 3. (\*, milk, Urbana, \*)
  - 4. (\*, milk, Urbana, \*)
  - 5. (\*, milk, Chicago, \*)
  - 6. (\*, milk, \*, \*)

#### **Cube Materialization:** Full Cube vs. Iceberg Cube

 Full cube vs. iceberg cube compute cube sales iceberg as select month, city, customer group, count(\*) from salesInfo cube by month, city, customer group

having count(\*) >= min support



- Computing only the cuboid cells whose measure satisfies the iceberg condition
- Only a small portion of cells may be "above the water" in a sparse cube
- Avoid explosive growth: A cube with 100 dimensions
  - 2 base cells: (a1, a2, ...., a100), (b1, b2, ..., b100)
  - How many aggregate cells if "having count >= 1"?
  - What about "having count >= 2"?

#### **Iceberg Cube, Closed Cube & Cube Shell**

- Is iceberg cube good enough?
  - 2 base cells:  $\{(a_1, a_2, a_3 \ldots, a_{100}): 10, (a_1, a_2, b_3, \ldots, b_{100}): 10\}$
  - How many cells will the iceberg cube have if having count(\*) >= 10? Hint: A huge but tricky number!

#### Close cube:

- Closed cell c: if there exists no cell d, s.t. d is a descendant of c, and d has the same measure value as c.
- Closed cube: a cube consisting of only closed cells
- What is the closed cube of the above base cuboid? Hint: only 3 cells

#### Cube Shell

- Precompute only the cuboids involving a small # of dimensions, e.g., 3 For  $(A_1, A_2, ... A_{10})$ , how many combinations to compute?
- More dimension combinations will need to be computed on the fly

#### **Roadmap for Efficient Computation**

- General cube computation heuristics (Agarwal et al.'96)
- Computing full/iceberg cubes: 3 methodologies
  - Bottom-Up: Multi-Way array aggregation (Zhao, Deshpande & Naughton, SIGMOD'97)
  - Top-down:
    - BUC (Beyer & Ramarkrishnan, SIGMOD'99)
    - H-cubing technique (Han, Pei, Dong & Wang: SIGMOD'01)
  - Integrating Top-Down and Bottom-Up:
    - Star-cubing algorithm (Xin, Han, Li & Wah: VLDB'03)
- High-dimensional OLAP: A Minimal Cubing Approach (Li, et al. VLDB'04)
- Computing alternative kinds of cubes:
  - Partial cube, closed cube, approximate cube, etc.

#### General Heuristics (Agarwal et al. VLDB'96)

- Sorting, hashing, and grouping operations are applied to the dimension attributes in order to reorder and cluster related tuples
- Aggregates may be computed from previously computed aggregates,
   rather than from the base fact table
  - Smallest-child: computing a cuboid from the smallest, previously computed cuboid
  - Cache-results: caching results of a cuboid from which other cuboids are computed to reduce disk I/Os
  - Amortize-scans: computing as many as possible cuboids at the same time to amortize disk reads
  - Share-sorts: sharing sorting costs cross multiple cuboids when sort-based method is used
  - Share-partitions: sharing the partitioning cost across multiple cuboids when hash-based algorithms are used

#### **Chapter 5: Data Cube Technology**

- Data Cube Computation: Preliminary Concepts
- Data Cube Computation Methods



- Processing Advanced Queries by Exploring DataCube Technology
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#### **Data Cube Computation Methods**

Multi-Way Array Aggregation



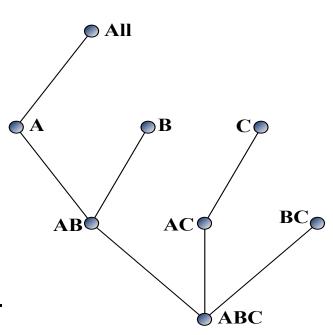
BUC

Star-Cubing

High-Dimensional OLAP

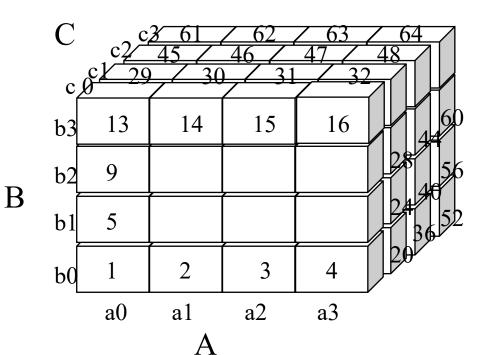
### **Multi-Way Array Aggregation**

- Array-based "bottom-up" algorithm
- Using multi-dimensional chunks
- No direct tuple comparisons
- Simultaneous aggregation on multiple dimensions
- Intermediate aggregate values are reused for computing ancestor cuboids
- Cannot do *Apriori* pruning: No iceberg optimization



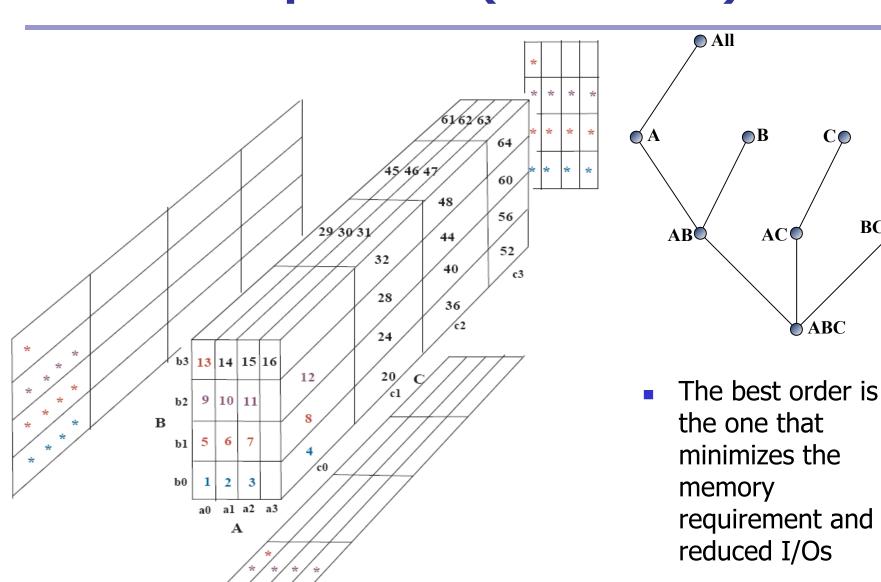
# Multi-way Array Aggregation for Cube Computation (MOLAP)

- Partition arrays into chunks (a small subcube which fits in memory).
- Compressed sparse array addressing: (chunk\_id, offset)
- Compute aggregates in "multiway" by visiting cube cells in the order which minimizes the # of times to visit each cell, and reduces memory access and storage cost.



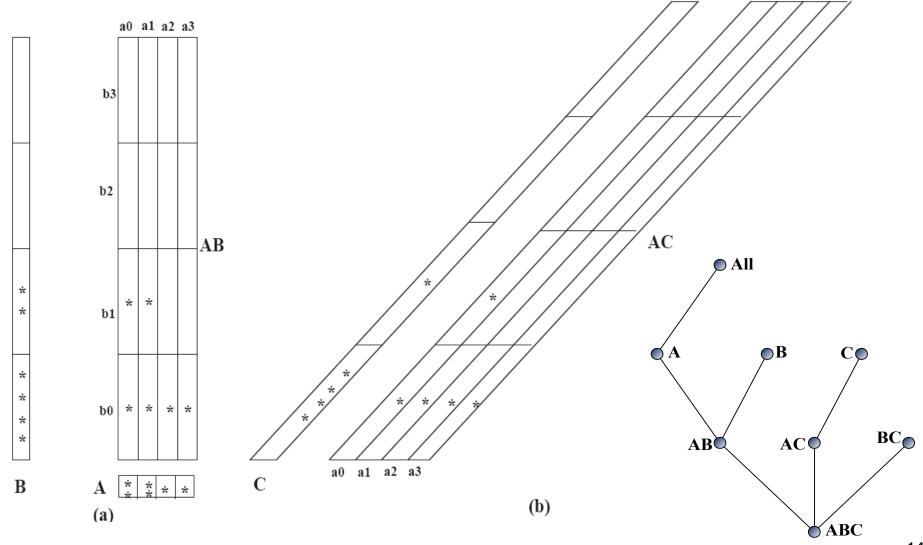
What is the best traversing order to do multi-way aggregation?

### **Multi-way Array Aggregation for Cube** Computation (3-D to 2-D)



BC

# Multi-way Array Aggregation for Cube Computation (2-D to 1-D)



# Multi-Way Array Aggregation for Cube Computation (Method Summary)

- Method: the planes should be sorted and computed according to their size in ascending order
  - Idea: keep the smallest plane in the main memory, fetch and compute only one chunk at a time for the largest plane
- Limitation of the method: computing well only for a small number of dimensions
  - If there are a large number of dimensions, "top-down" computation and iceberg cube computation methods can be explored

#### **Data Cube Computation Methods**

Multi-Way Array Aggregation

■ BUC ►

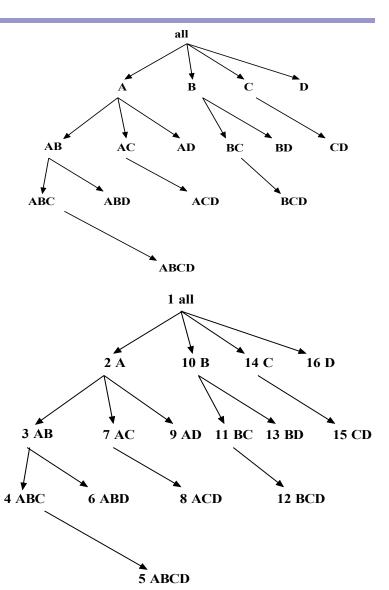


Star-Cubing

High-Dimensional OLAP

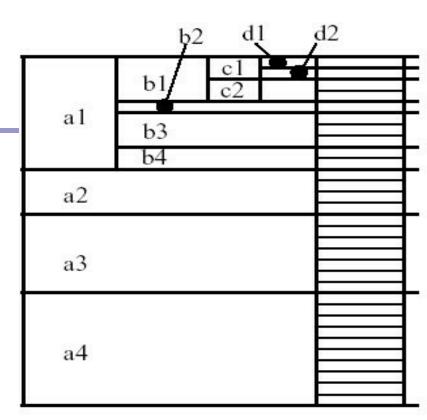
#### **Bottom-Up Computation (BUC)**

- BUC (Beyer & Ramakrishnan, SIGMOD'99)
- Bottom-up cube computation (Note: top-down in our view!)
- Divides dimensions into partitions and facilitates iceberg pruning
  - If a partition does not satisfy min\_sup, its descendants can be pruned
  - If  $minsup = 1 \Rightarrow$  compute full CUBE!
- No simultaneous aggregation



#### **BUC: Partitioning**

- Usually, entire data set can't fit in main memory
- Sort *distinct* values
  - partition into blocks that fit
- Continue processing
- Optimizations
  - Partitioning
    - External Sorting, Hashing, Counting Sort
  - Ordering dimensions to encourage pruning
    - Cardinality, Skew, Correlation
  - Collapsing duplicates
    - Can't do holistic aggregates anymore!



#### **Data Cube Computation Methods**

Multi-Way Array Aggregation

BUC

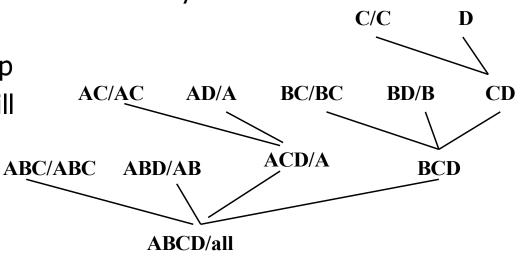
Star-Cubing



High-Dimensional OLAP

### **Star-Cubing: An Integrating Method**

- D. Xin, J. Han, X. Li, B. W. Wah, Star-Cubing: Computing Iceberg Cubes by Top-Down and Bottom-Up Integration, VLDB'03
- Explore shared dimensions
  - E.g., dimension A is the shared dimension of ACD and AD
  - ABD/AB means cuboid ABD has shared dimensions AB
- Allows for shared computations
  - e.g., cuboid AB is computed simultaneously as ABD
- Aggregate in a top-down manner but with the bottom-up sub-layer underneath which will allow Apriori pruning
- Shared dimensions grow in bottom-up fashion



#### **Iceberg Pruning in Shared Dimensions**

- Anti-monotonic property of shared dimensions
  - If the measure is anti-monotonic, and if the aggregate value on a shared dimension does not satisfy the iceberg condition, then all the cells extended from this shared dimension cannot satisfy the condition either
- Intuition: if we can compute the shared dimensions before the actual cuboid, we can use them to do Apriori pruning
- Problem: how to prune while still aggregate simultaneously on multiple dimensions?

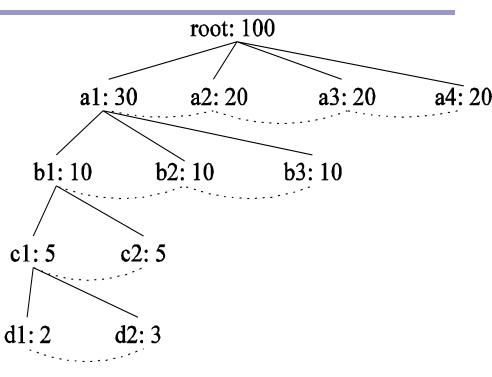
#### **Cell Trees**

 Use a tree structure similar to H-tree to represent cuboids

Collapses common prefixes c1: 5
 to save memory

Keep count at node

Traverse the tree to retrieve a particular tuple



#### **Star Attributes and Star Nodes**

- Intuition: If a single-dimensional aggregate on an attribute value p does not satisfy the iceberg condition, it is useless to distinguish them during the iceberg computation
  - E.g., b<sub>2</sub>, b<sub>3</sub>, b<sub>4</sub>, c<sub>1</sub>, c<sub>2</sub>, c<sub>4</sub>, d<sub>1</sub>, d<sub>2</sub>,
     d<sub>3</sub>
- Solution: Replace such attributes by a \*. Such attributes are <u>star</u>
   <u>attributes</u>, and the corresponding nodes in the cell tree are <u>star nodes</u>

Α	В	С	D	Count
a1	b1	c1	d1	1
a1	b1	c4	d3	1
a1	b2	c2	d2	1
a2	b3	c3	d4	1
a2	b4	c3	d4	1

#### **Example: Star Reduction**

- Suppose minsup = 2
- Perform one-dimensional aggregation. Replace attribute values whose count < 2 with \*. And collapse all \*'s together
- Resulting table has all such attributes replaced with the starattribute
- With regards to the iceberg computation, this new table is a lossless compression of the original table

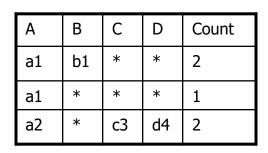
Α	В	С	D	Count
a1	b1	*	*	1
a1	b1	*	*	1
a1	*	*	*	1
a2	*	c3	d4	1
a2	*	c3	d4	1



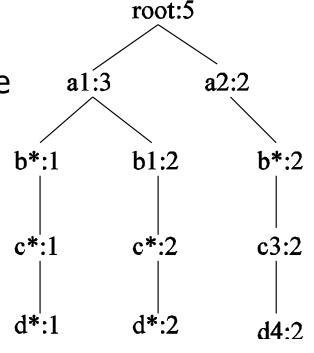
Α	В	С	D	Count
a1	b1	*	*	2
a1	*	*	*	1
a2	*	c3	d4	2

#### **Star Tree**

 Given the new compressed table, it is possible to construct the corresponding cell tree—called star tree

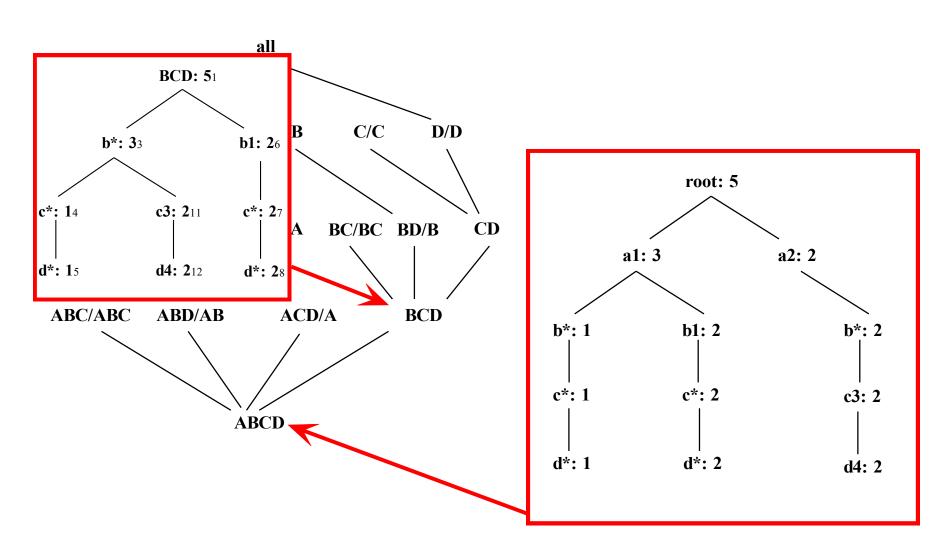


- Keep a <u>star table</u> at the side for easy lookup of star attributes
- The star tree is a lossless compression of the original cell tree

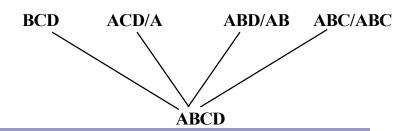


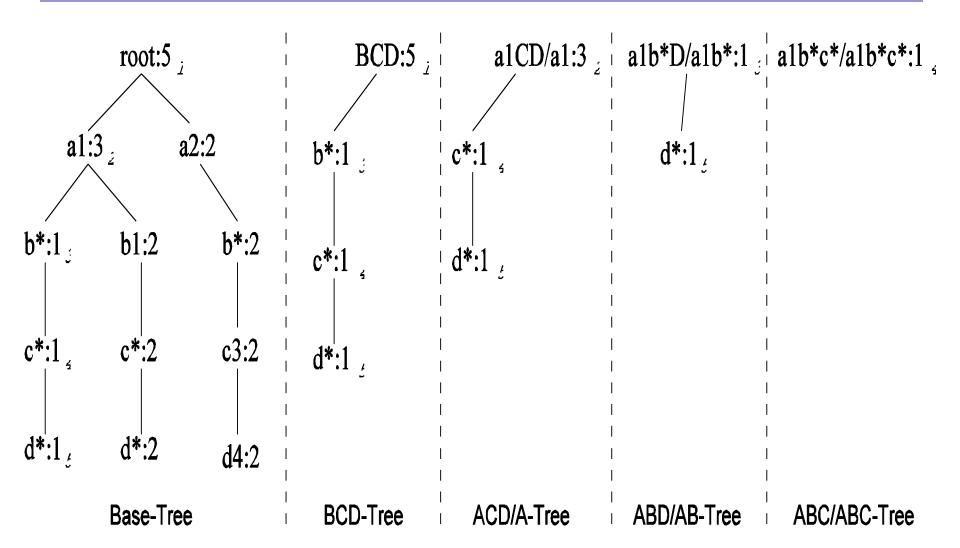
Star Table
b2 → *
b3 → *
b4 → *
c1 *
c2 *
d1 → *

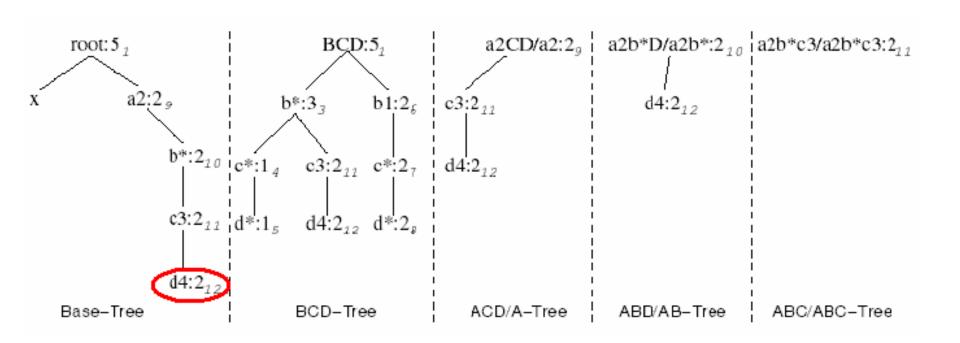
#### **Star-Cubing Algorithm—DFS on Lattice Tree**



#### **Multi-Way Aggregation**







- Start depth-first search at the root of the base star tree
- At each new node in the DFS, create corresponding star tree that are descendants of the current tree according to the integrated traversal ordering
  - E.g., in the base tree, when DFS reaches a1, the ACD/A tree is created
  - When DFS reaches b\*, the ABD/AD tree is created
- The counts in the base tree are carried over to the new trees
- When DFS reaches a leaf node (e.g., d\*), start backtracking
- On every backtracking branch, the count in the corresponding trees are output, the tree is destroyed, and the node in the base tree is destroyed
- Example
  - When traversing from d\* back to c\*, the alb\*c\*/alb\*c\* tree is output and destroyed
  - When traversing from c\* back to b\*, the a1b\*D/a1b\* tree is output and destroyed
  - When at b\*, jump to b1 and repeat similar process

#### **Data Cube Computation Methods**

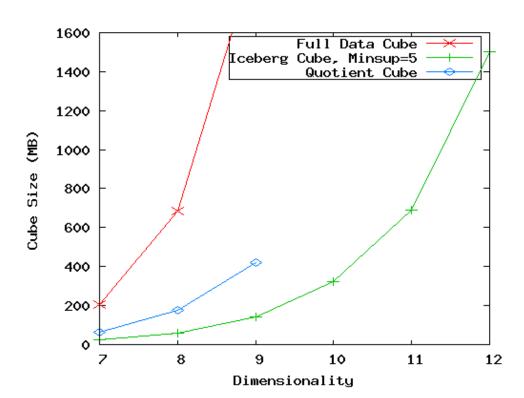
- Multi-Way Array Aggregation
- BUC

- Star-Cubing
- High-Dimensional OLAP



#### **The Curse of Dimensionality**

- None of the previous cubing method can handle high dimensionality!
- A database of 600k tuples. Each dimension has cardinality of 100 and zipf of 2.



#### **Motivation of High-D OLAP**

- X. Li, J. Han, and H. Gonzalez, High-Dimensional OLAP:
   A Minimal Cubing Approach, VLDB'04
- Challenge to current cubing methods:
  - The "curse of dimensionality" problem
  - Iceberg cube and compressed cubes: only delay the inevitable explosion
  - Full materialization: still significant overhead in accessing results on disk
- High-D OLAP is needed in applications
  - Science and engineering analysis
  - Bio-data analysis: thousands of genes
  - Statistical surveys: hundreds of variables

#### **Fast High-D OLAP with Minimal Cubing**

- Observation: OLAP occurs only on a small subset of dimensions at a time
- Semi-Online Computational Model
  - Partition the set of dimensions into shell fragments
  - Compute data cubes for each shell fragment while retaining inverted indices or value-list indices
  - 3. Given the pre-computed fragment cubes, dynamically compute cube cells of the highdimensional data cube online

#### **Properties of Proposed Method**

- Partitions the data vertically
- Reduces high-dimensional cube into a set of lower dimensional cubes
- Online re-construction of original high-dimensional space
- Lossless reduction
- Offers tradeoffs between the amount of pre-processing and the speed of online computation

#### **Example Computation**

Let the cube aggregation function be count

tid	A	В	С	D	E
1	a1	b1	с1	d1	e1
2	a1	b2	с1	d2	e1
3	a1	b2	с1	d1	e2
4	a2	b1	с1	d1	e2
5	a2	b1	с1	d1	е3

- Divide the 5 dimensions into 2 shell fragments:
  - (A, B, C) and (D, E)

#### **1-D Inverted Indices**

#### Build traditional invert index or RID list

Attribute Value	TID List	List Size
a1	1 2 3	3
a2	4 5	2
b1	1 4 5	3
b2	2 3	2
c1	1 2 3 4 5	5
d1	1 3 4 5	4
d2	2	1
e1	1 2	2
e2	3 4	2
e3	5	1

#### **Shell Fragment Cubes: Ideas**

- Generalize the 1-D inverted indices to multi-dimensional ones in the data cube sense
- Compute all cuboids for data cubes ABC and DE while retaining the inverted indices

Cell

- For example, shell fragment cube ABC contains 7 cuboids:
  - A, B, C
  - AB, AC, BC
  - ABC
- a1 b1
   123 \cappa 145
   1
   1

   7 cuboids:
   a1 b2
   123 \cappa 23
   23
   2

   a2 b1
   45 \cappa 145
   45
   2

   a2 b2
   45 \cappa 23
   \times 0
   0

Intersection

This completes the offline computation stage

TID List

List Size

#### **Shell Fragment Cubes: Size and Design**

- Given a database of T tuples, D dimensions, and F shell fragment size, the fragment cubes' space requirement is:
  - For F < 5, the growth is sub-linear  $O\left(T\left|\frac{D}{F}\right|(2^F-1)\right)$
- Shell fragments do not have to be disjoint
- Fragment groupings can be arbitrary to allow for maximum online performance
  - Known common combinations (e.g.,<city, state>) should be grouped together.
- Shell fragment sizes can be adjusted for optimal balance between offline and online computation

#### **ID\_Measure Table**

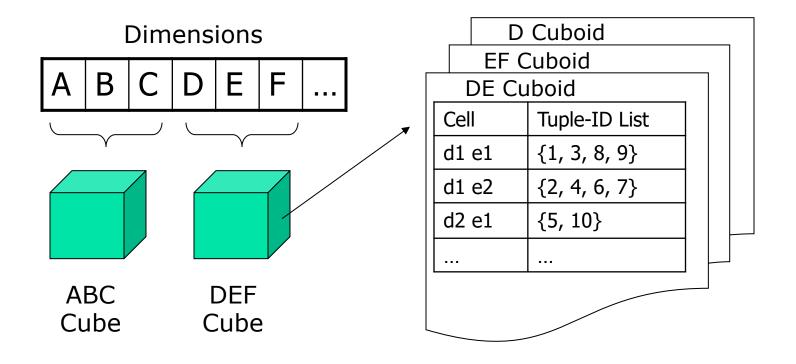
If measures other than count are present, store in ID\_measure table separate from the shell fragments

tid	count	sum
1	5	70
2	3	10
3	8	20
4	5	40
5	2	30

#### The Frag-Shells Algorithm

- Partition set of dimension  $(A_1,...,A_n)$  into a set of k fragments  $(P_1,...,P_k)$ .
- 2. Scan base table once and do the following
- insert <tid, measure> into ID\_measure table.
- for each attribute value a<sub>i</sub> of each dimension A<sub>i</sub>
- 5. build inverted index entry <a, tidlist>
- 6. For each fragment partition P<sub>i</sub>
- build local fragment cube S<sub>i</sub> by intersecting tid-lists in bottomup fashion.

### Frag-Shells (2)



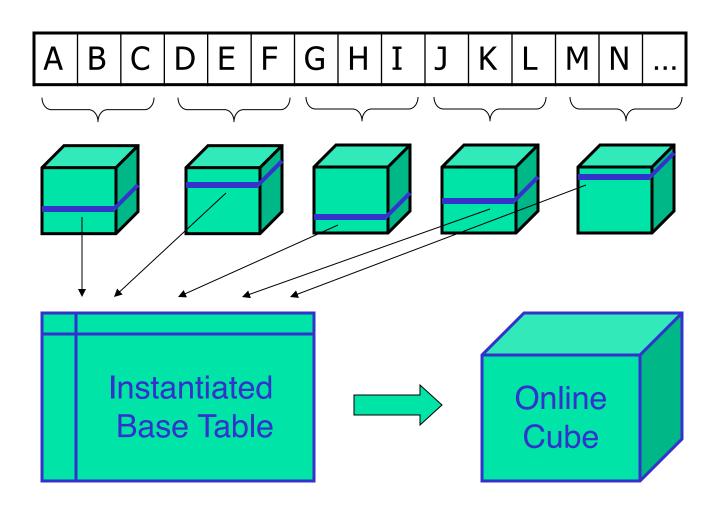
#### **Online Query Computation: Query**

- A query has the general form  $\langle a_1, a_2, ..., a_n : M \rangle$
- Each a<sub>i</sub> has 3 possible values
  - Instantiated value
  - 2. Aggregate \* function
  - 3. Inquire ? function
- For example,  $\langle 3 ? ? * 1:count \rangle$  returns a 2-D data cube.

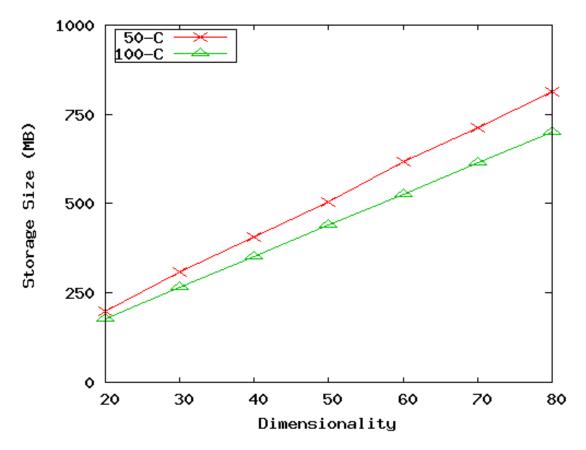
#### **Online Query Computation: Method**

- Given the fragment cubes, process a query as follows
  - Divide the query into fragment, same as the shell
  - Fetch the corresponding TID list for each fragment from the fragment cube
  - Intersect the TID lists from each fragment to construct **instantiated base table**
  - Compute the data cube using the base table with any cubing algorithm

## **Online Query Computation: Sketch**



# **Experiment: Size vs. Dimensionality (50 and 100 cardinality)**



- (50-C): 10<sup>6</sup> tuples, 0 skew, 50 cardinality, fragment size 3.
- (100-C): 10<sup>6</sup> tuples, 2 skew, 100 cardinality, fragment size 2.

#### **Experiments on Real World Data**

- UCI Forest CoverType data set
  - 54 dimensions, 581K tuples
  - Shell fragments of size 2 took 33 seconds and 325MB to compute
  - 3-D subquery with 1 instantiate D: 85ms~1.4 sec.
- Longitudinal Study of Vocational Rehab. Data
  - 24 dimensions, 8818 tuples
  - Shell fragments of size 3 took 0.9 seconds and 60MB to compute
  - 5-D query with 0 instantiated D: 227ms~2.6 sec.

## **Chapter 5: Data Cube Technology**

- Data Cube Computation: Preliminary Concepts
- Data Cube Computation Methods

- Processing Advanced Queries by Exploring Data Cube
   Technology
  - Sampling Cube
  - Ranking Cube
- Multidimensional Data Analysis in Cube Space
- Summary

## **Processing Advanced Queries by Exploring Data Cube Technology**

#### Sampling Cube

 X. Li, J. Han, Z. Yin, J.-G. Lee, Y. Sun, "Sampling Cube: A Framework for Statistical OLAP over Sampling Data", SIGMOD'08

#### Ranking Cube

- D. Xin, J. Han, H. Cheng, and X. Li. Answering top-k queries with multi-dimensional selections: The ranking cube approach. VLDB'06
- Other advanced cubes for processing data and queries
  - Stream cube, spatial cube, multimedia cube, text cube, RFID cube, etc. — to be studied in volume 2

## **Statistical Surveys and OLAP**

- Statistical survey: A popular tool to collect information about a population based on a sample
  - Ex.: TV ratings, US Census, election polls
- A common tool in politics, health, market research, science, and many more
- An efficient way of collecting information (Data collection is expensive)
- Many statistical tools available, to determine validity
  - Confidence intervals
  - Hypothesis tests
- OLAP (multidimensional analysis) on survey data
  - highly desirable but can it be done well?

## **Surveys: Sample vs. Whole Population**

#### Data is only a sample of **population**

<b>Age\Education</b>	High-school	College	Graduate	
18				
19				
20				
•••				

#### **Problems for Drilling in Multidim. Space**

Data is only a **sample** of population but samples could be small when drilling to certain multidimensional space

<b>Age\Education</b>	High-school	College	Graduate
18			
19			
20			
•••			

## **OLAP on Survey (i.e., Sampling) Data**

- Semantics of query is unchanged
- Input data has changed

Age/Education	High-school	College	Graduate
18			
19			
20			
•••			

## **Challenges for OLAP on Sampling Data**

- Computing confidence intervals in OLAP context
- No data?
  - Not exactly. No data in subspaces in cube
  - Sparse data
  - Causes include sampling bias and query selection bias
- Curse of dimensionality
  - Survey data can be high dimensional
  - Over 600 dimensions in real world example
  - Impossible to fully materialize

## **Example 1: Confidence Interval**

What is the average income of 19-year-old high-school students? Return not only query result but also confidence interval

Age/Education	High-school	College	Graduate
18			
19			
20			

### **Confidence Interval**

- Confidence interval at ar x:  $ar x \pm t_c \hat \sigma_{ar x}$ 
  - x is a sample of data set;  $\bar{x}$  is the mean of sample

  - $t_c$  is the critical t-value, calculated standard error of the mean
- Example: \$50,000 ± \$3,000 with 95% confidence
  - Treat points in cube cell as samples
  - Compute confidence interval as traditional sample set
- Return answer in the form of confidence interval
  - Indicates quality of query answer
  - User selects desired confidence interval

#### **Efficient Computing Confidence Interval Measures**

- Efficient computation in all cells in data cube
  - Both mean and confidence interval are algebraic
  - Why confidence interval mea The picture can't be displayed. Igebraic?

$$\bar{x} \pm t_c \hat{\sigma}_{\bar{x}}$$

 $\bar{x}$  is algebraic

 $\hat{\sigma}_{ar{x}} = rac{s}{\sqrt{l}}$  where both s and l (count) are algebraic

 Thus one can calculate cells efficiently at more general cuboids without having to start at the base cuboid each time

## **Example 2: Query Expansion**

What is the average income of 19-year-old college students?

Age/Education	High-school	College	Graduate
18			
19			
20			
•••			

#### **Boosting Confidence by Query Expansion**

- From the example: The queried cell "19-year-old college students" contains only 2 samples
- Confidence interval is large (i.e., low confidence). why?
  - Small sample size
  - High standard deviation with samples
- Small sample sizes can occur at relatively low dimensional selections
  - Collect more data?— expensive!
  - Use data in other cells? Maybe, but have to be careful

# **Intra-Cuboid Expansion: Choice 1**

Expand query to include 18 and 20 year olds?

Age/Education	High-school	College	Graduate
18			
19			
20			
•••			

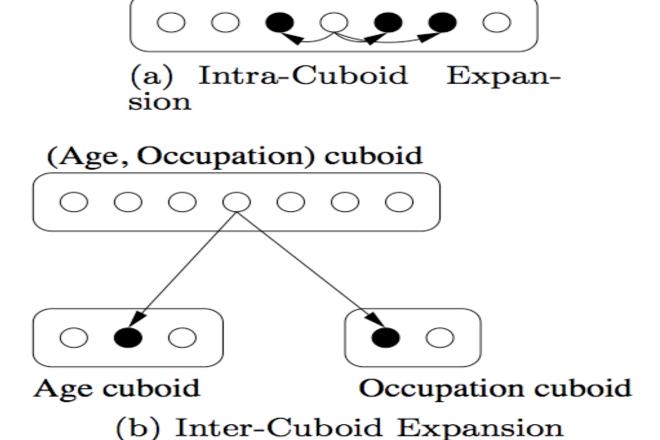
# **Intra-Cuboid Expansion: Choice 2**

Expand query to include **high-school** and **graduate** students?

Age/Education	High-school	College	Graduate
18			
19			
20			

## **Query Expansion**

(Age, Occupation) cuboid



## **Intra-Cuboid Expansion**

- Combine other cells' data into own to "boost" confidence
  - If share semantic and cube similarity
  - Use only if necessary
  - Bigger sample size will decrease confidence interval
- Cell segment similarity
  - Some dimensions are clear: Age
  - Some are fuzzy: Occupation
  - May need domain knowledge
- Cell value similarity
  - How to determine if two cells' samples come from the same population?
  - Two-sample t-test (confidence-based)

# **Inter-Cuboid Expansion**

- If a query dimension is
  - Not correlated with cube value
  - But is causing small sample size by drilling down too much
- Remove dimension (i.e., generalize to \*) and move to a more general cuboid
- Can use two-sample t-test to determine similarity between two cells across cuboids
- Can also use a different method to be shown later

## **Query Expansion Experiments**

- Real world sample data: 600 dimensions and 750,000 tuples
- 0.05% to simulate "sample" (allows error checking)

(a) Intra-Cuboid Expansion with Age dimension and Average Number of Children cube measure

Q	uery	Average (	Query Ans	wer Error	Sa	mpling Siz	es
Gender	Marital	No Expand	Expand	% Improve	Population	Sample	Expanded
FEMALE	MARRIED	0.48	0.32	33%	2473.0	2.2	28.3
FEMALE	SINGLE	0.31	0.21	30%	612.6	0.6	6.4
FEMALE	DIVORCED	0.49	0.43	11%	321.1	0.3	3.4
MALE	MARRIED	0.42	0.21	49%	4296.8	4.4	37.6
MALE	SINGLE	0.26	0.21	16%	571.8	0.5	3.6
MALE	DIVORCED	0.33	0.27	19%	224.7	0.2	1.2
	Average	0.38	0.27	26%	1416.7	1.4	13.4

## **Chapter 5: Data Cube Technology**

- Data Cube Computation: Preliminary Concepts
- Data Cube Computation Methods



- Processing Advanced Queries by Exploring Data Cube
   Technology
  - Sampling Cube
  - Ranking Cube



- Multidimensional Data Analysis in Cube Space
- Summary

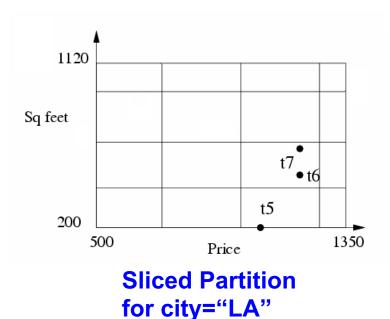
# Ranking Cubes – Efficient Computation of Ranking queries

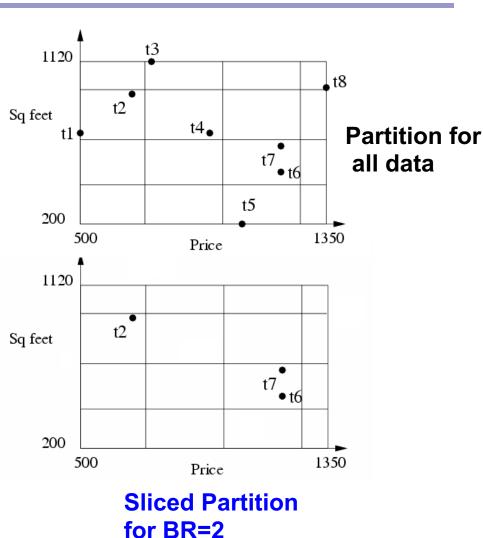
- Data cube helps not only OLAP but also ranked search
- (top-k) ranking query: only returns the best k results according to a user-specified preference, consisting of (1) a selection condition and (2) a ranking function
- Ex.: Search for apartments with expected price 1000 and expected square feet 800
  - Select top 1 from Apartment
  - where City = "LA" and Num\_Bedroom = 2
  - order by [price 1000]^2 + [sq feet 800]^2 asc
- Efficiency question: Can we only search what we need?
  - Build a ranking cube on both selection dimensions and ranking dimensions

# Ranking Cube: Partition Data on Both Selection and Ranking Dimensions

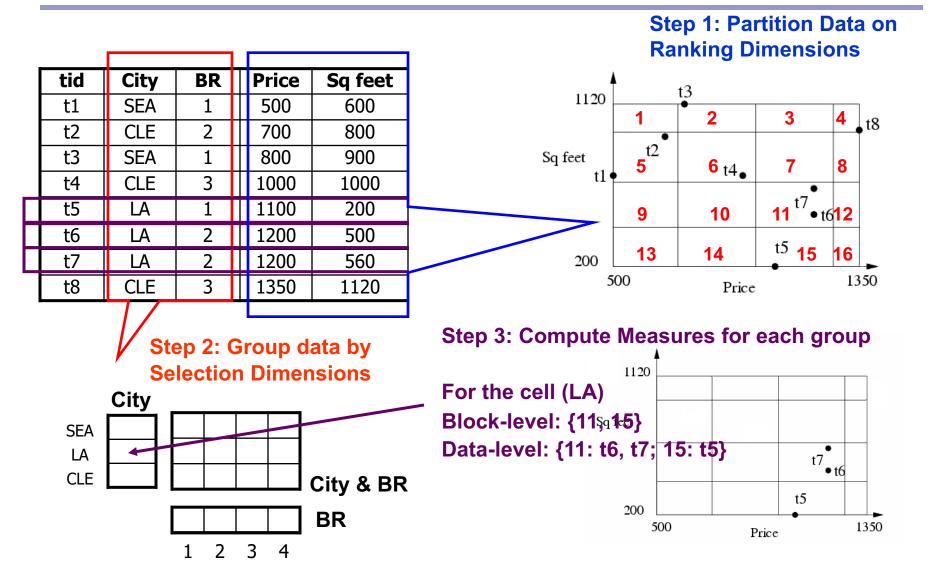
One single data partition as the template

Slice the data partition by selection conditions





## **Materialize Ranking-Cube**

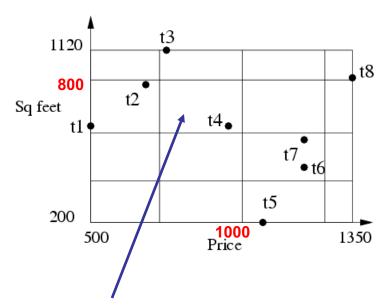


# Search with Ranking-Cube: Simultaneously Push Selection and Ranking

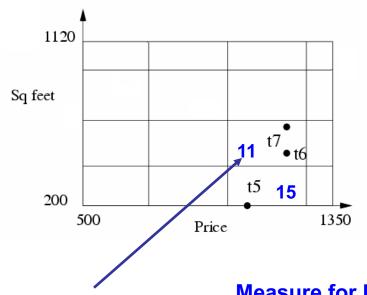
Select top 1 from Apartment where city = "LA" order by [price – 1000]^2 + [sq feet - 800]^2 asc

Bin boundary for price	[500, 600, 800, 1100,1350]
Bin boundary for sq feet	[200, 400, 600, 800, 1120]

Given the bin boundaries, locate the block with top score



Without ranking-cube: start search from here



With ranking-cube: start search from here

**Measure for LA: {11, 15}** 

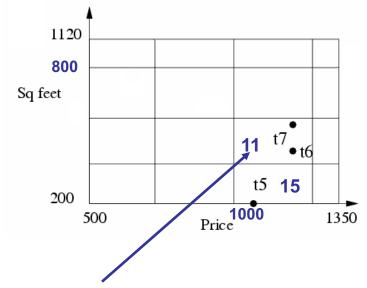
**{11: t6,t7; 15:t5}** 

#### **Processing Ranking Query: Execution Trace**

#### Select top 1 from Apartment where city = "LA" order by [price – 1000]^2 + [sq feet - 800]^2 asc

Bin boundary for price	[500, 600, 800, 1100,1350]
Bin boundary for sq feet	[200, 400, 600, 800, 1120]

f=[price-1000]^2 + [sq feet - 800]^2



#### With rankingcube: start search from here

Measure for LA: {11, 15} {11: t6,t7; 15:t5}

#### **Execution Trace:**

- 1. Retrieve High-level measure for LA {11, 15}
- 2. Estimate *lower bound score* for block 11, 15 f(block 11) = 40,000, f(block 15) = 160,000
- 3. Retrieve block 11
- 4. Retrieve low-level measure for block 11
- 5. f(t6) = 130,000, f(t7) = 97,600

Output t7, done!

#### Ranking Cube: Methodology and Extension

- Ranking cube methodology
  - Push selection and ranking simultaneously
  - It works for many sophisticated ranking functions
- How to support high-dimensional data?
  - Materialize only those atomic cuboids that contain single selection dimensions
    - Uses the idea similar to high-dimensional OLAP
    - Achieves low space overhead and high performance in answering ranking queries with a high number of selection dimensions

## **Chapter 5: Data Cube Technology**

- Data Cube Computation: Preliminary Concepts
- Data Cube Computation Methods
- Processing Advanced Queries by Exploring DataCube Technology
- Multidimensional Data Analysis in Cube Space



Summary

# Multidimensional Data Analysis in Cube Space

 Prediction Cubes: Data Mining in Multi-Dimensional Cube Space



- Multi-Feature Cubes: Complex Aggregation at Multiple Granularities
- Discovery-Driven Exploration of Data Cubes

## **Data Mining in Cube Space**

- Data cube greatly increases the analysis bandwidth
- Four ways to interact OLAP-styled analysis and data mining
  - Using cube space to define data space for mining
  - Using OLAP queries to generate features and targets for mining, e.g., multi-feature cube
  - Using data-mining models as building blocks in a multistep mining process, e.g., prediction cube
  - Using data-cube computation techniques to speed up repeated model construction
    - Cube-space data mining may require building a model for each candidate data space
    - Sharing computation across model-construction for different candidates may lead to efficient mining

#### **Prediction Cubes**

- Prediction cube: A cube structure that stores prediction models in multidimensional data space and supports prediction in OLAP manner
- Prediction models are used as building blocks to define the interestingness of subsets of data, i.e., to answer which subsets of data indicate better prediction

## How to Determine the Prediction Power of an Attribute?

- Ex. A customer table D:
  - Two dimensions Z: Time (Month, Year) and Location (State, Country)
  - Two features X: Gender and Salary
  - One class-label attribute Y: Valued Customer
- Q: "Are there times and locations in which the value of a customer depended greatly on the customers gender (i.e., Gender: predictiveness attribute V)?"
- Idea:
  - Compute the difference between the model built on that using X to predict Y and that built on using X – V to predict Y
  - If the difference is large, V must play an important role at predicting Y

#### **Efficient Computation of Prediction Cubes**

- Naïve method: Fully materialize the prediction cube, i.e., exhaustively build models and evaluate them for each cell and for each granularity
- Better approach: Explore score function decomposition that reduces prediction cube computation to data cube computation

# Multidimensional Data Analysis in Cube Space

- Prediction Cubes: Data Mining in Multi-Dimensional Cube Space
- Multi-Feature Cubes: Complex Aggregation at Multiple Granularities



## **Complex Aggregation at Multiple Granularities: Multi-Feature Cubes**

- Multi-feature cubes (Ross, et al. 1998): Compute complex queries involving multiple dependent aggregates at multiple granularities
- Ex. Grouping by all subsets of {item, region, month}, find the maximum price in 2010 for each group, and the total sales among all maximum price tuples

```
select item, region, month, max(price), sum(R.sales)
from purchases
where year = 2010
cube by item, region, month: R
such that R.price = max(price)
```

 Continuing the last example, among the max price tuples, find the min and max shelf live, and find the fraction of the total sales due to tuple that have min shelf life within the set of all max price tuples

# Multidimensional Data Analysis in Cube Space

- Prediction Cubes: Data Mining in Multi-Dimensional Cube Space
- Multi-Feature Cubes: Complex Aggregation at Multiple Granularities
- Discovery-Driven Exploration of Data Cubes



#### **Discovery-Driven Exploration of Data Cubes**

- Hypothesis-driven
  - exploration by user, huge search space
- Discovery-driven (Sarawagi, et al.'98)
  - Effective navigation of large OLAP data cubes
  - pre-compute measures indicating exceptions, guide user in the data analysis, at all levels of aggregation
  - Exception: significantly different from the value anticipated, based on a statistical model
  - Visual cues such as background color are used to reflect the degree of exception of each cell

#### Kinds of Exceptions and their Computation

#### Parameters

- SelfExp: surprise of cell relative to other cells at same level of aggregation
- InExp: surprise beneath the cell
- PathExp: surprise beneath cell for each drill-down path
- Computation of exception indicator (modeling fitting and computing SelfExp, InExp, and PathExp values) can be overlapped with cube construction
- Exception themselves can be stored, indexed and retrieved like precomputed aggregates

### **Examples: Discovery-Driven Data Cubes**

item	all
region	all

Sum of sales	mont	month											
	Jan	Feb	Mar	Apr	May	Jun	<b>J</b> ul	Aug	Sep	Oct	Nov	Dec	
Total		1%	-1%	0%	1%	3%	-1	-9%	-1%	2%	-4%	3%	

Avg sales	mon	ith										
item	Jan	Feb	Mar	Арг	May	Jun	Jul	Aug	Sep	Oct	Nov	Dec
Sony b/w printer		9%	-8%	2%	-5%	14%	4%	0%	41%	-13%	-15%	-11%
Sony color printer		0%	0%	3%	2%	4%	-10%	-13%	0%	4%	-6%	4%
HP b/w printer		-2%	1%	2%	3%	8%	0%	-12%	-9%	3%	-3%	6%
HP color printer		0%	0%	-2%	1%	0%	-1%	-7%	-2%	1%	-5%	1%
IBM home computer		1%	-2%	-1%	-1%	3%	3%	-10%	4%	1%	4%	-1%
IBM laptop computer		0%	0%	-1%	3%	4%	2%	-10%	-2%	0%	-9%	3%
Toshiba home computer		-2%	-5%	1%	1%	-1%	1%	5%	-3%	-5%	-1%	-1%
Toshiba laptop computer		1%	0%	3%	0%	-2%	-2%	-5%	3%	2%	-1%	0%
Logitech mouse		3%	-2%	-1%	0%	4%	6%	-11%	2%	1%	4%	0%
Ergo-way mouse		0%	0%	2%	3%	1%	-2%	-2%	-5%	0%	-5%	8%

item	IBM home computer											
Avg sales	month											
region	Jan	Feb	Mac	Apr	May	Jun	Jul	Aug	Sep	Oct	Nov	Dec
North South East West		-1% -1% -1% 4%	-3% 1% -2% <b>0</b> %	-1% -9% 2% -1%	0% 6% -3% -3%	3% -1% 1% 5%	4% -39% 18% 1%	-7% 9% -2% -18%	1% -34% 11% 8%	0% 4% -3% 5%	-3% 1% -2% -8%	-3% 7% -1% 1%

## **Chapter 5: Data Cube Technology**

- Data Cube Computation: Preliminary Concepts
- Data Cube Computation Methods
- Processing Advanced Queries by Exploring DataCube Technology
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## **Data Cube Technology: Summary**

- Data Cube Computation: Preliminary Concepts
- Data Cube Computation Methods
  - MultiWay Array Aggregation
  - BUC
  - Star-Cubing
  - High-Dimensional OLAP with Shell-Fragments
- Processing Advanced Queries by Exploring Data Cube Technology
  - Sampling Cubes
  - Ranking Cubes
- Multidimensional Data Analysis in Cube Space
  - Discovery-Driven Exploration of Data Cubes
  - Multi-feature Cubes
  - Prediction Cubes

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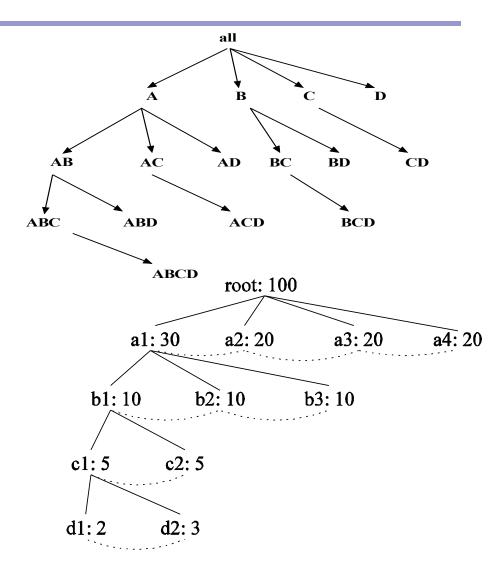
## **Surplus Slides**

## **Chapter 5: Data Cube Technology**

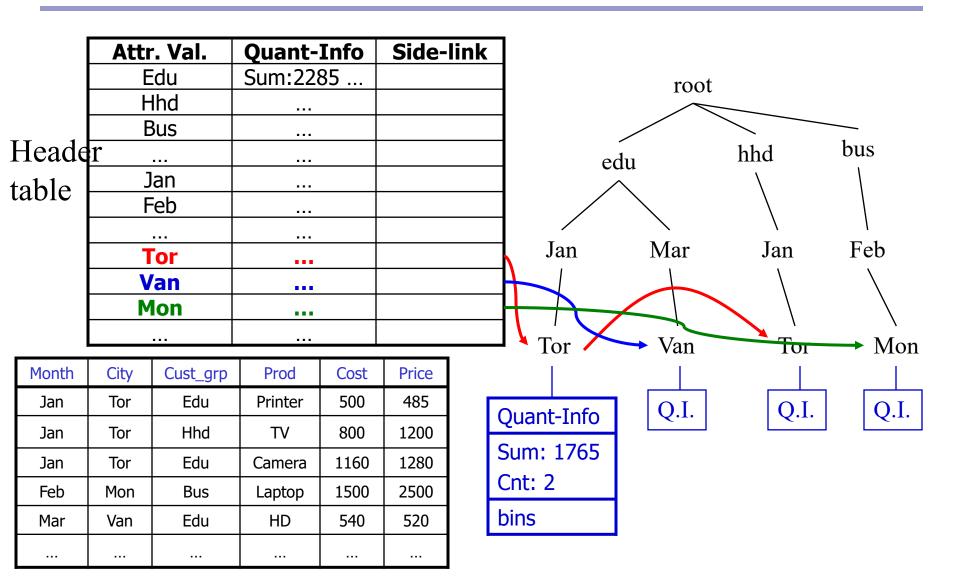
- Efficient Methods for Data Cube Computation
  - Preliminary Concepts and General Strategies for Cube Computation
  - Multiway Array Aggregation for Full Cube Computation
  - BUC: Computing Iceberg Cubes from the Apex Cuboid Downward
  - H-Cubing: Exploring an H-Tree Structure
  - Star-cubing: Computing Iceberg Cubes Using a Dynamic Star-tree
     Structure
  - Precomputing Shell Fragments for Fast High-Dimensional OLAP
- Data Cubes for Advanced Applications
  - Sampling Cubes: OLAP on Sampling Data
  - Ranking Cubes: Efficient Computation of Ranking Queries
- Knowledge Discovery with Data Cubes
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## **H-Cubing: Using H-Tree Structure**

- Bottom-up computation
- Exploring an H-tree structure
- If the current computation of an H-tree cannot pass min\_sup, do not proceed further (pruning)
- No simultaneous aggregation



### **H-tree: A Prefix Hyper-tree**



### **Computing Cells Involving "City"**

Header Table H<sub>Tor</sub>

Attr. Val.

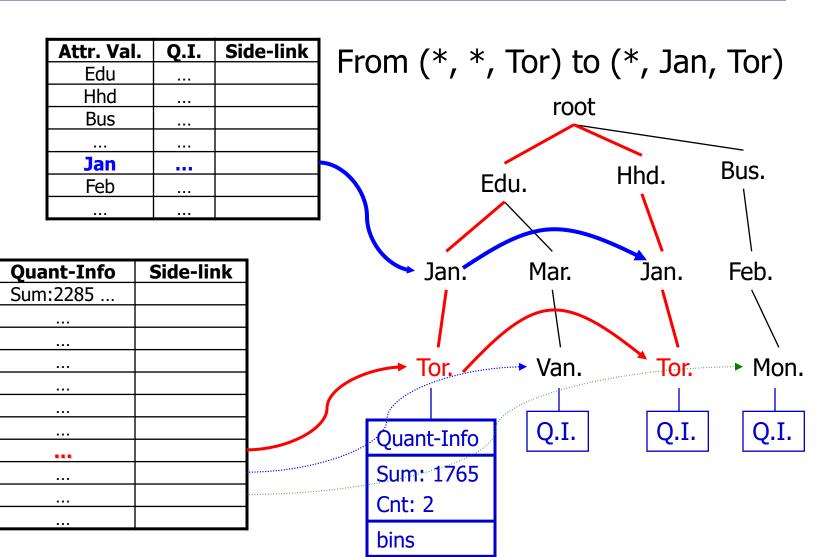
Edu

Hhd Bus

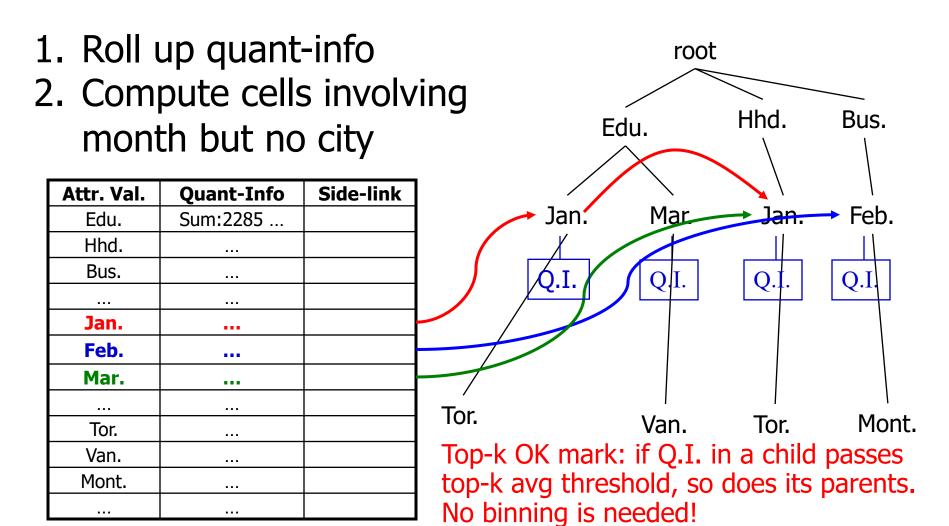
<u>Jan</u> Feb

Tor

Van Mon



#### **Computing Cells Involving Month But No City**



#### **Computing Cells Involving Only Cust\_grp**

