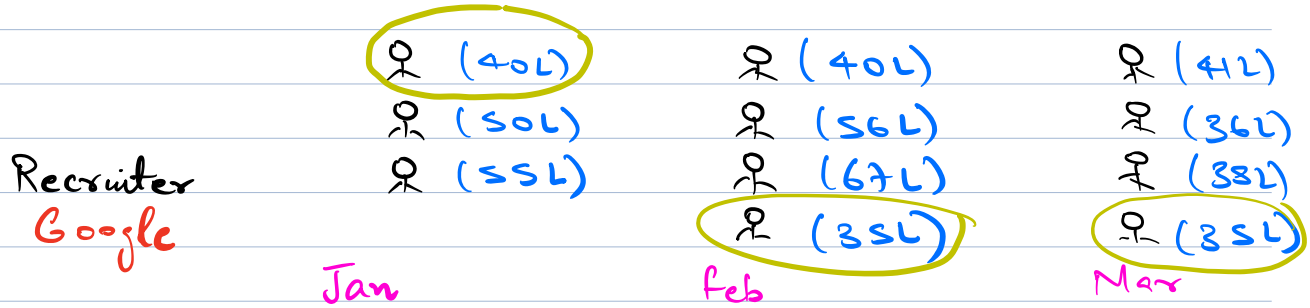
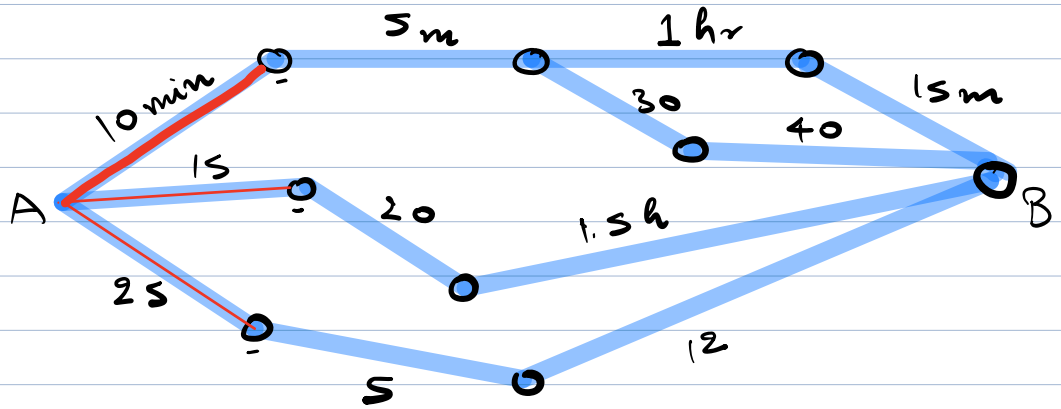


Reduce overall cost



Goal : Reach B in min time

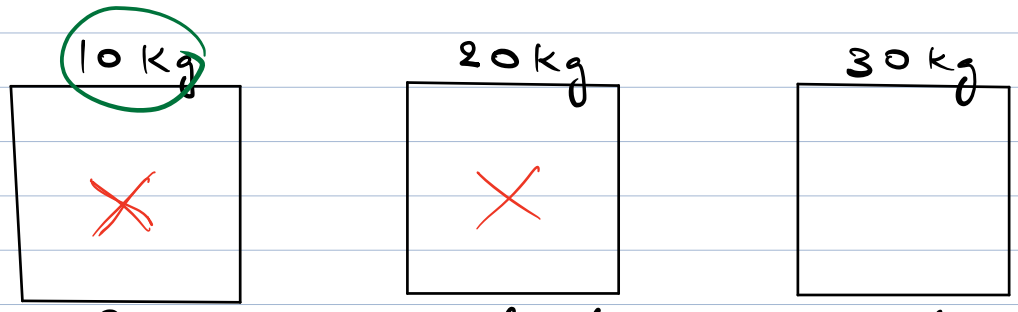
Fractional Knapsack

Given N items → total weight
→ cost (value)

Given a bag of capacity W

Pick some items st. value in the bag is maximized.

Supermarket

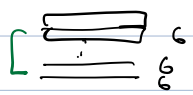


Rice $60 → 1 kg = $6

Wheat $100 → $5

Pulse $120 → $4

30 kg pulse = 120
20 kg wheat = 100
220 ✗



20 kg pulse	→ $80
20 kg wheat	→ $100
10 kg Rice	→ $60
w = 50 k	$240

?

Constraint : Either select all or select nothing

20	→
20 kg wheat	→ 100
10 kg Rice	→ 60
w = 50 k	160

0/1 Knapsack ⇒ DP

Steps

1) Sort all the items on the basis of per unit cost. (total val / total weight)

2) Iterate, pick the best & keep updating the bag's capacity.

$$T.C. = O(N \log N + N)$$
$$= O(N \log N)$$

Gautam (CEO) [famous]

BMW approaches Gautam Special sale

N Cars

A → A[i] time till which the i^{th} car is free of cost (sale is active

B → B[i] beauty of the i^{th} car

Maximise the overall beauty value of the purchased car.

→ It takes 1 unit of time to purchase one car

0 1 2 3 4

A → [3, 1, 3, 2, 3]

B → [6, 5, 3, 1, 9]

T = 0	9	5
T = 1	6	6
T = 2	3	9
T = 3	18	20

1) Sort the cars on the basis of sale end time.

A → 1, 5, 5, 5, 3, 3, 3

B → 5, 4, 3, 8, 20, 7, 10

	0	1	2	3	4	5	6
A →	1	3	3	3	5	5	5
B →	5	20	7	10	4	3	8

T = 0	~~0 (5)~~	3 (10)
T = 1	1 (20)	
T = 2	2 (7)	
T = 3	4 (4)	
T = 4	~~5 (8)~~	6 (8)
T = 5		

min ⇒ Min Heap

Code

```
int t = 0;
```

```
minHeap m ;
totalBeauty = 0;
for (i = 0; i < N; i++) {
    if ( t < A[i] ) {
        totalBeauty += B[i];
        m.insert ( B[i] );
        t++;
    }
    else {
        if ( B[i] > m.peek() ) {
            totalBeauty -= m.deleteMin();
            m.insert (B[i]);
            totalBeauty += B[i];
        }
    }
}
```

Iterate over the heap & find total beauty sum.

$$T.C. = O(N \log N + N \log N)$$
$$= O(N \log N)$$
$$S.C. = O(N)$$

Q.. Given N jobs that we need to perform.

Paypal

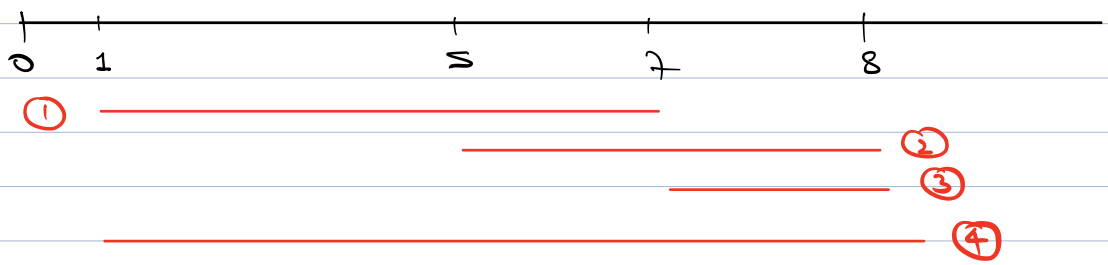
Each job → start time, End time

Const : Only able to perform 1 job at a time

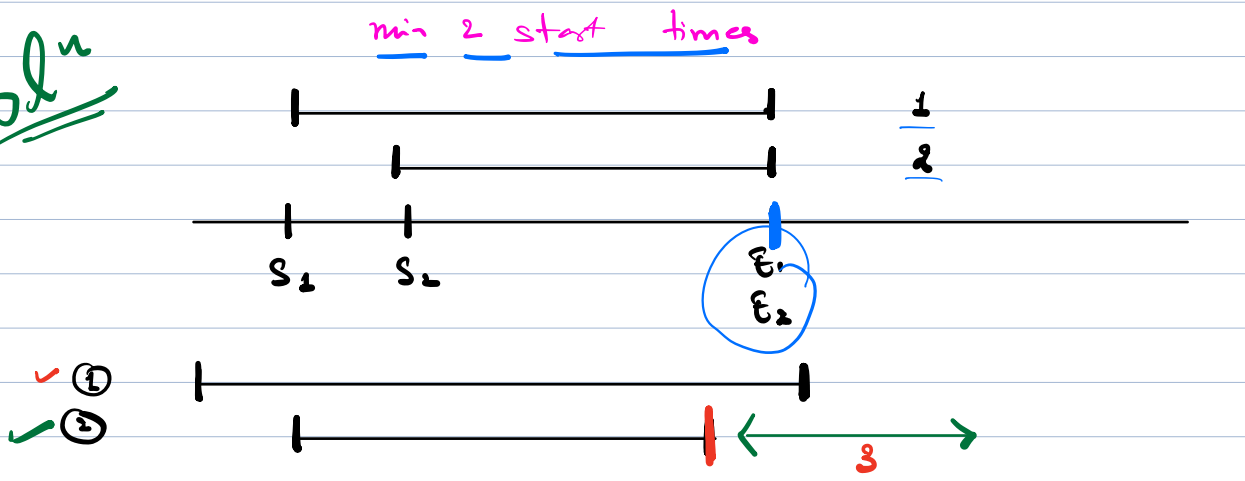
Find the max no. of jobs that we can perform.

	0	1	2	3
Start	1	5	7	1
End	7	8	8	8

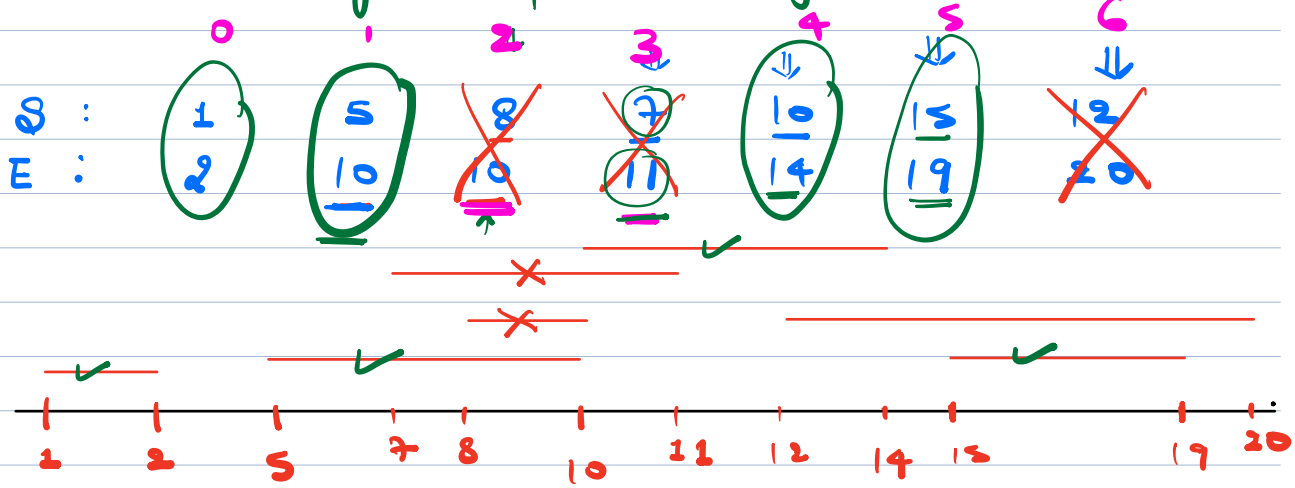
0 & 2 Ans = 2



Soln



Goal : Every time select the job with the least end time. out of the possible jobs



Assume jobs are sorted on basis of ET

Code

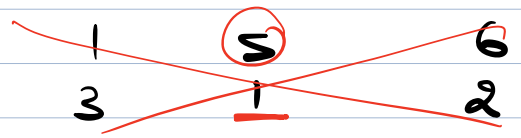
```
count = 1;
lastEndTime = E[0];

for (i=1; i<N; i++) {
    if (S[i] >= lastEndTime) {
        count++;
        lastEndTime = E[i];
    }
}
```

T.C. $= O(N \log N + N)$

$= O(N \log N)$

S.C. = O(N)

Doubt



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