

Q K smaller elements.

I/p $\rightarrow A = [8, 3, 10, 4, 11, 2, 7, 6, 5, 1]$, $K=4$

O/p $\rightarrow [1, 2, 3, 4]$

Sorting Approach

T.C = $O(n \log n)$

S.C = $O(N) / O(\log N)$

Min heap Approach

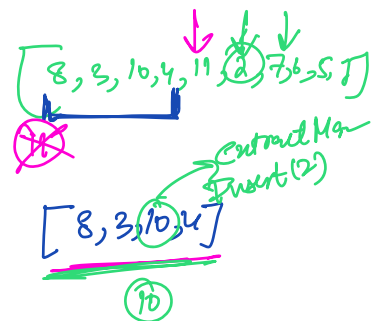
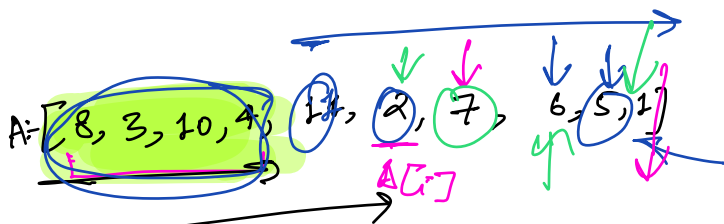
- Create a min heap $\rightarrow O(N)$
- Keep extracting min. $\rightarrow K$ times. $\rightarrow K \log N$

T.C = $O(N) + O(K \log N)$

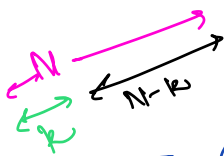
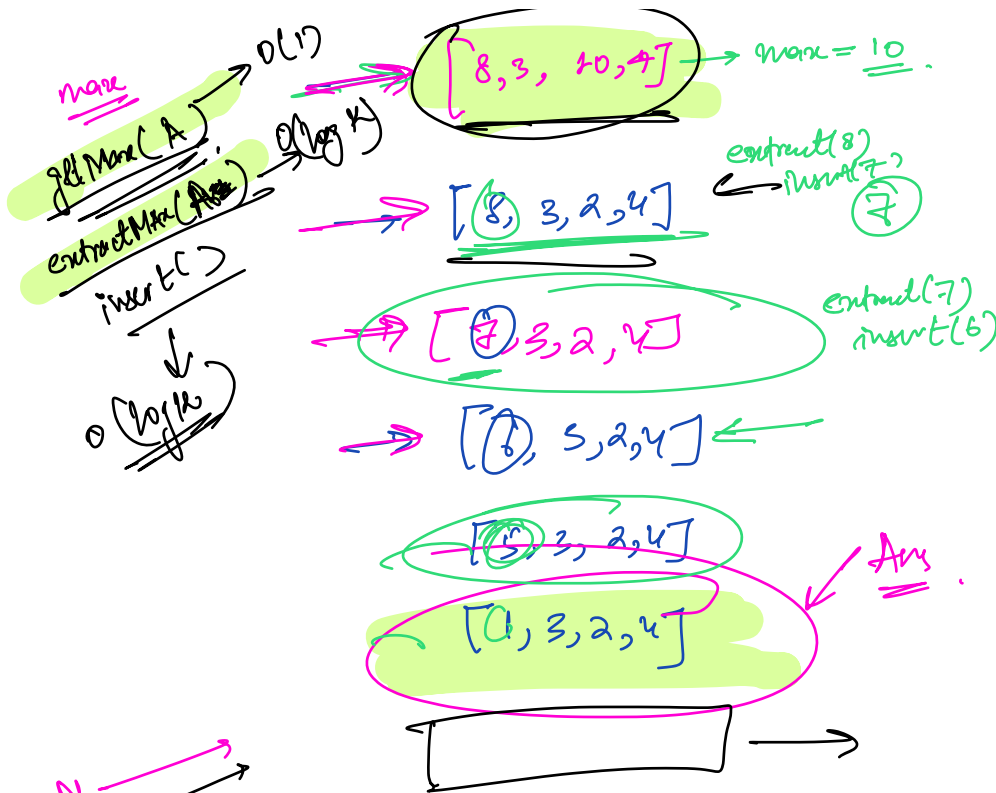
S.C = $O(1)$

Cannot modify the given array.

\downarrow
S.C = $O(N)$

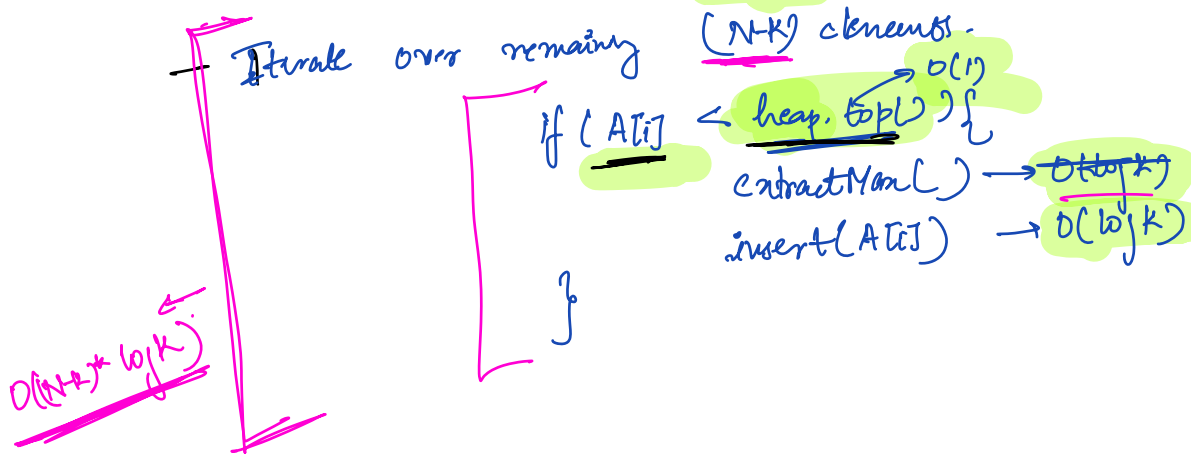


$A[i] < \text{getMax}()$



— Create a max heap of first K elements from the given array.

$\hookrightarrow O(K)$



$K \approx \frac{N}{2}$

T.C = $O(K) + \frac{O((N-K) * \log K)}{O(1)}$
 S.C = $O(K)$

Q.

Given an array.

Nearly sorted, K -sorted array

* every element is at most K positions away from its sorted position.

Goal:- Sort the array.

→ A: $[6, 5, 3, 2, 8, 10, 9]$, $K=3$

sorted A: $[2, 3, 5, 6, 8, 9, 10]$

(9)
[6, 5, 3, 2]
(2)

$|actualIndex - sortedIndex| \leq K$

$0 - K \leq K$

$K \leq K \therefore 0 = K$

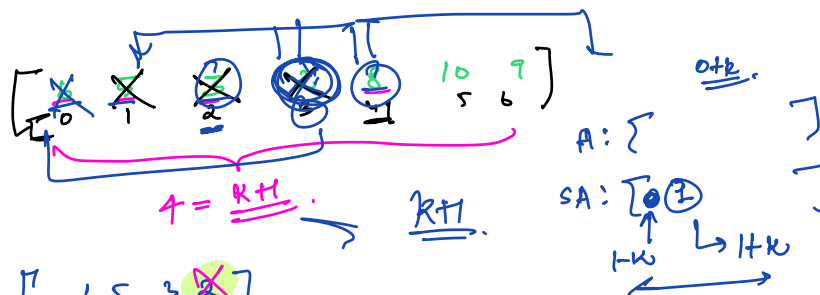


$0 \dots 2 = 3$

$0 \dots 3 = 4$

$(0 \dots K) = K+1$

→ min of first $(K+1)$ elements will be $A[0]$ sorted array.



$(K+1)$ elements
min → $A[0]$

[6 5 3 2]

[6 5 2]

extracting

extract(2)
insert(8)

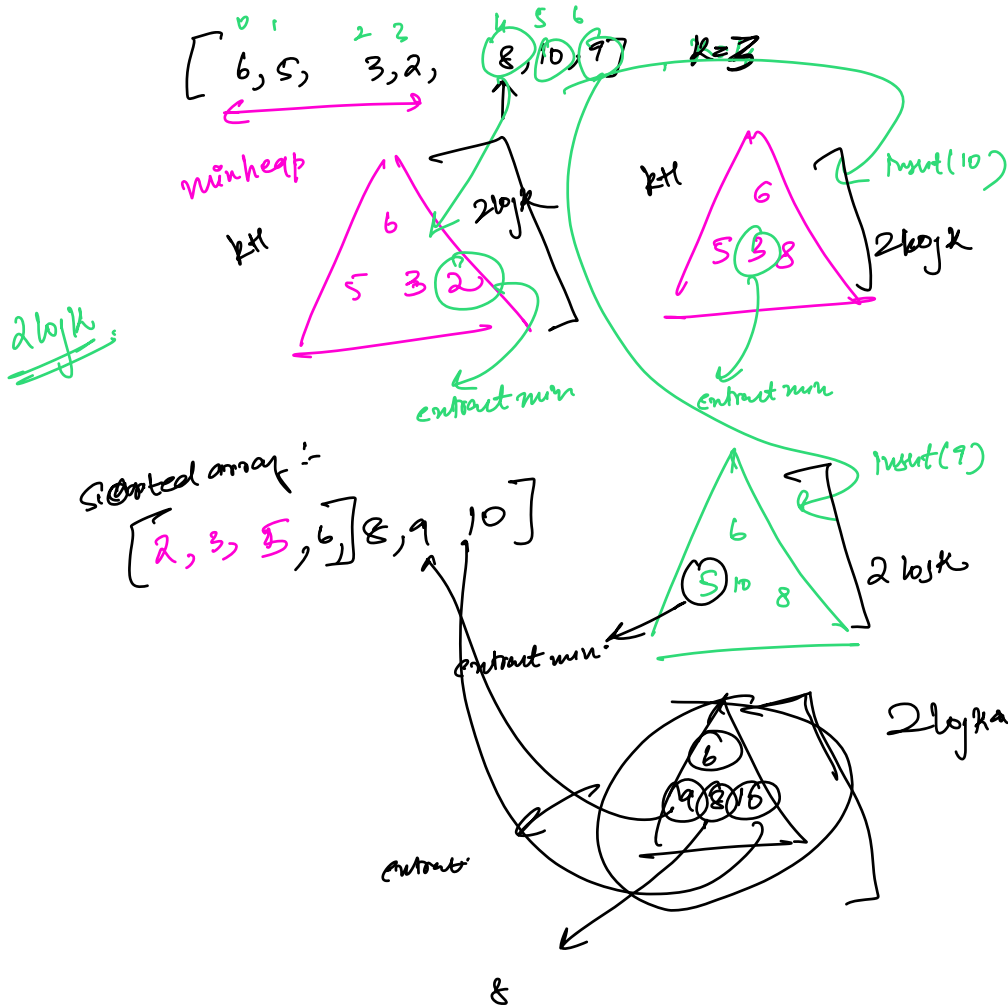
✓ all min.

T.C = $O(k)$
 ↓
 create heap
 of size $k+1$

+ $O(N-k) \log k$

$N \log k$

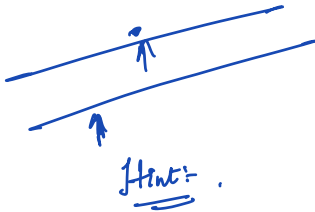
\leftarrow $(N-k+1)$
 $k+1$



Q. Given an array. Sort it in place.
 \rightarrow S.C. $O(1)$

Bubble Sort
 Insertion Sort
 Selection Sort

$\rightarrow O(N^2)$ T.C.
 $S.C = O(1)$



Selection Sort \rightarrow How a heap is created.

$\rightarrow [8, 3, 7, 6, 1, 5, 10, 4, 9]$

- Create heap
- extract max.

Selection Sort.

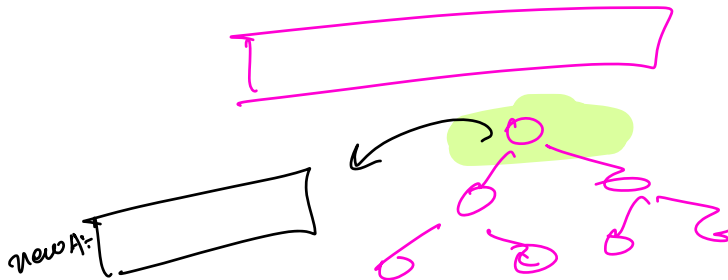
* get min : $O(N)$
 * put in correct position : $O(1)$

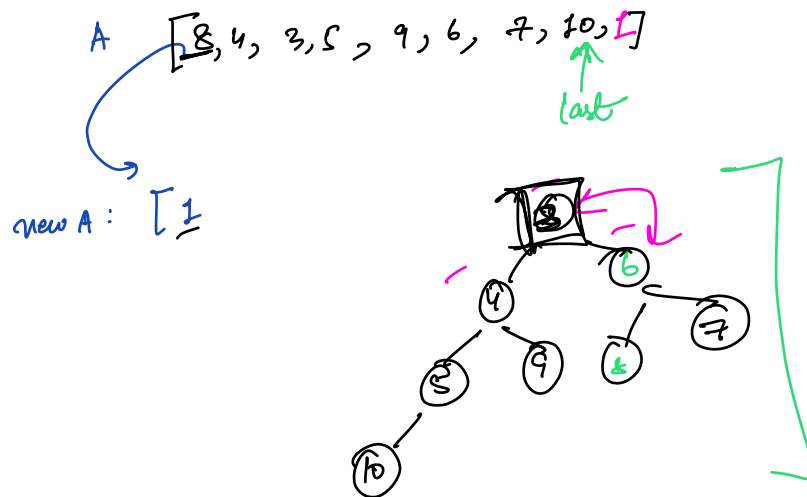
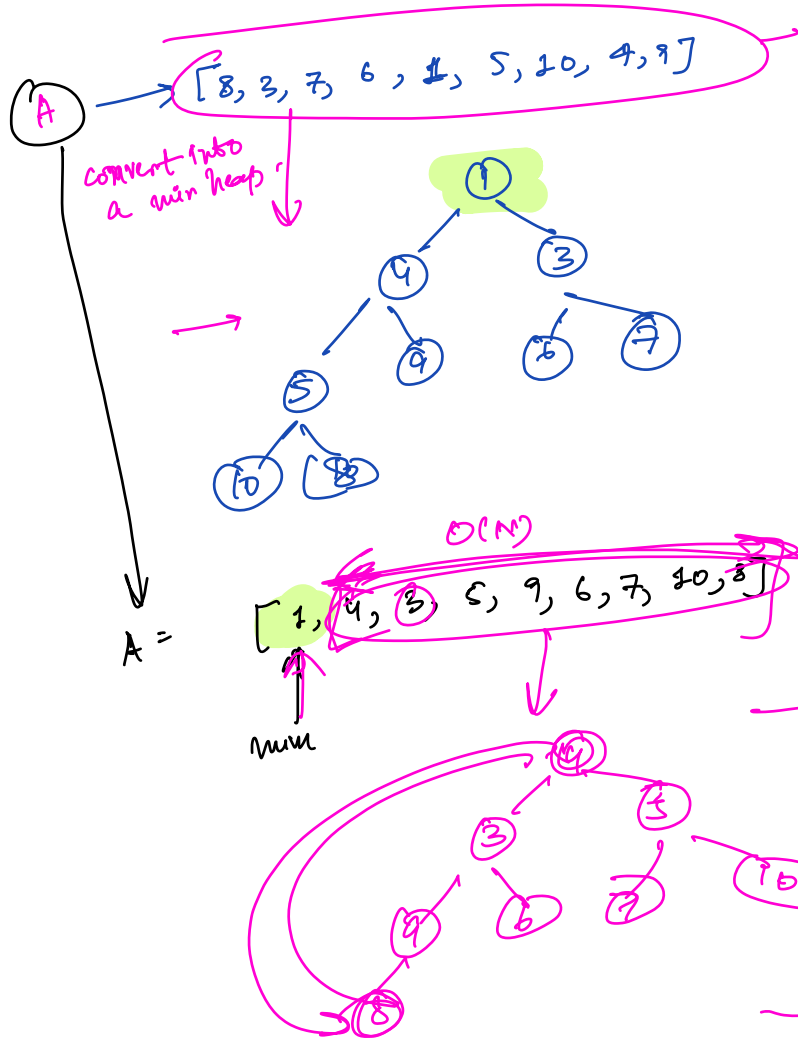
$\log N$

min heap

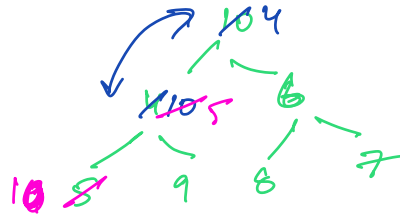
N

$\rightarrow O(N^2)$

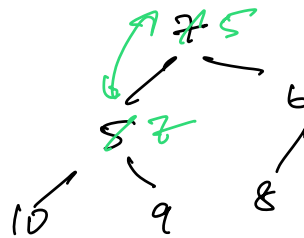




A: [10, 4, 6, 5, 9, 8, 7, 3, 1]
 new A: [1, 3]



A: [7, 5, 6, 10, 9, 8, 4, 3, 1]
 new A: [1, 3, 4]



A: [8, 7, 6, 10, 9, 5, 4, 3, 1]
 Sorted A: [1, 3, 4, 5]



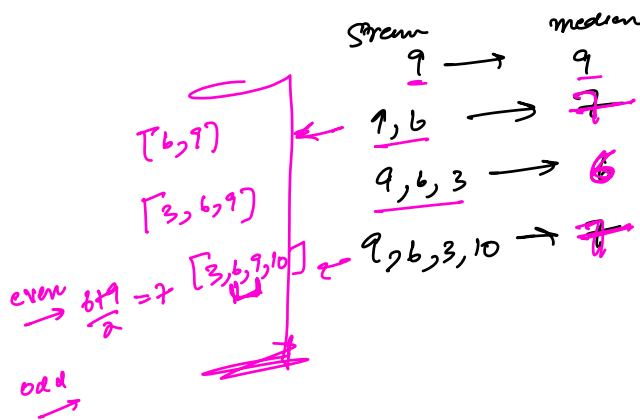
A: [10, 9, 8, 7, 6, 5, 4, 3, 1]

sorted A: [1, 3, 4, 5, 6, 7, 8, 9, 10]

Heap Sort

T.C = $O(N \log N)$
 S.C = $O(1)$

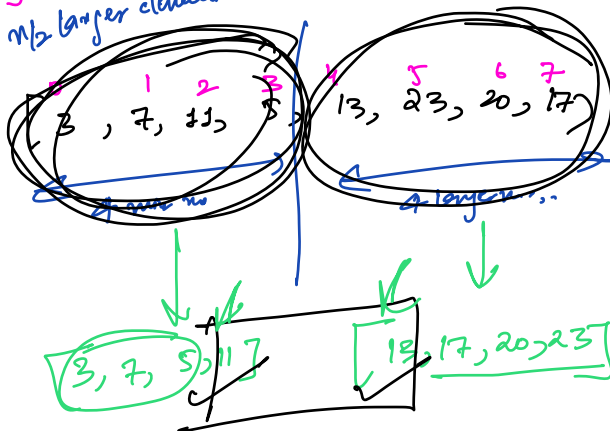
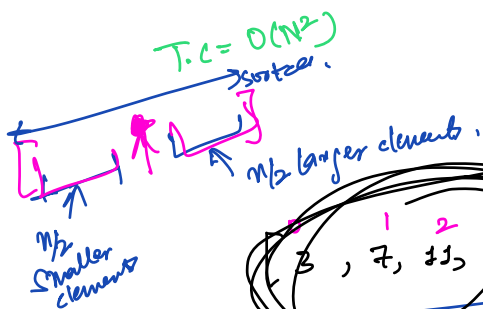
Q. Given a stream of integers. Find the median with every insertion.



Sort Elements every time.
 if odd \rightarrow return middle
 if even \rightarrow return avg(middle)

$$T.C = (n \log n * n) \\ = (n^2 \log n)$$

for every element $\hookrightarrow O(N)$



$\frac{n}{2}$ smaller \rightarrow need max \rightarrow maxheap
 $\frac{n}{2}$ larger \rightarrow need min \rightarrow minheap.

$[3, 7, 11, 5, 13, 23, 20, 7, 21]$

$[3, 7, 11, 5, 13, 23, 20, 7, 21]$

$[3, 7, 11, 5, 13, 23, 20, 7, 21]$

Steps:

1) Divide the elements into 2 groups.

2) If no. of elements = even

$\text{return avg}(\text{max}(\text{left}), \text{min}(\text{right}))$

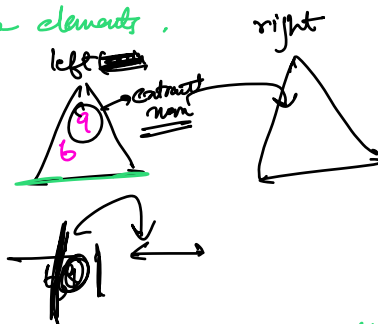
If no. of elements = odd
 if left group has extra element

$\text{return max}(\text{left})$

$\text{else return min}(\text{right})$

How to divide the elements.

a, b

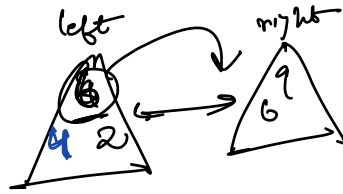


median
 9

if (new_num > median)
 go to right
 else
 go to left.

$[9, 6]$

[9, 6, 4, 2]



median



$$\max(\text{left}) = 6$$

$$\max(\text{right}) = 9$$

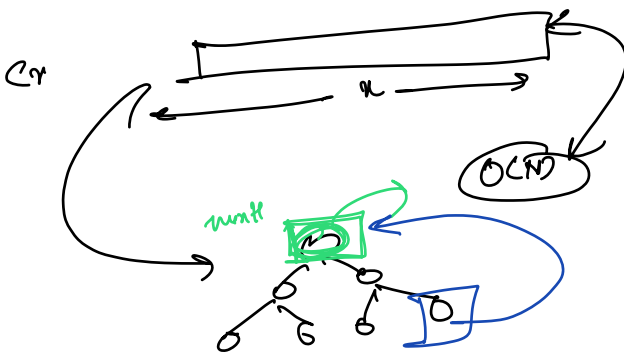
$$\frac{6+9}{2} = 7.5$$



$(2 \log N) * N$

$$\text{median} = \frac{4+9}{2} = 6.5$$

T.C = $n \log n$



list / array
priority-queue \rightarrow heap

