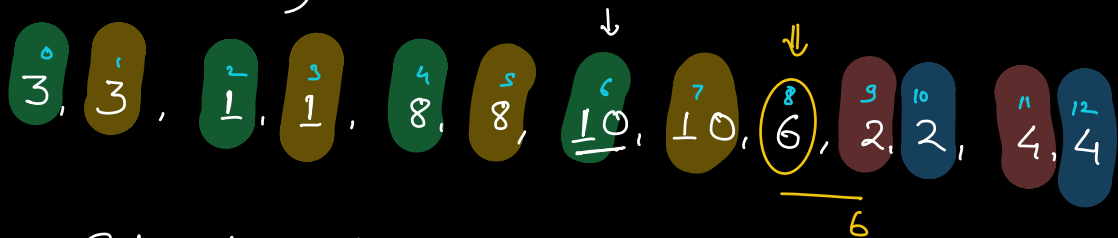




Q Every element appears twice except one element.  
Amazon Find the single no.

(All pairs of duplicates will always be adjacent to each other)



Before the single no  $\longrightarrow$  1st occurrence of all pairs  
 is on **even** index

After the single no  $\longrightarrow$  1st occurrence of all pairs  
 is on **odd** index

TC:  $O(\log N)$



mid is 1st occ of  $A[mid]$   
 mid is even

Google  
Facebook  
Amazon  
LinkedIn  
Goldman Sachs  
Flipkart  
Snapdeal  
MS  
Adobe  
Target  
...

Q Search in a sorted but rotated array.

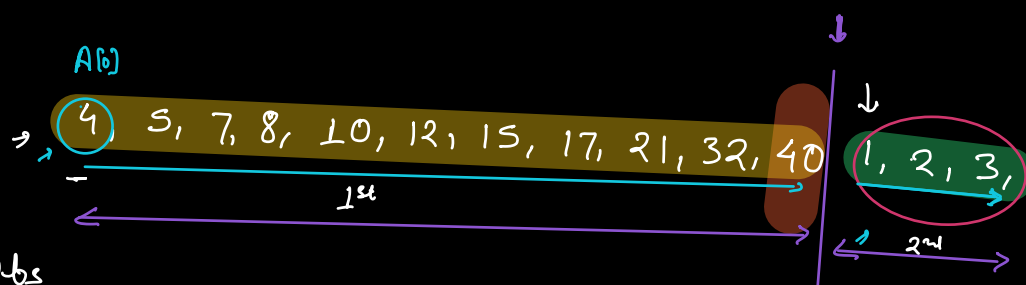
of distinct elements  
(No repetition)

A: <sup>0</sup>4, <sup>1</sup>5, <sup>2</sup>8, <sup>3</sup>10, <sup>4</sup>1, <sup>5</sup>2, <sup>6</sup>3

T = 2  $\longrightarrow$  5

T = 8  $\longrightarrow$  2

T = 20  $\longrightarrow$  -1

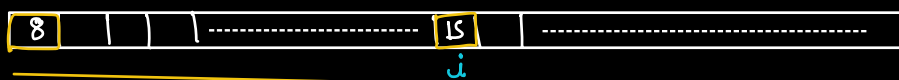


Obs

(1) Sorted and rotated array  $\Rightarrow$  Concatenation of 2 sorted arrays.

(2) All elements of 1<sup>st</sup> part will be greater than all elements of 2<sup>nd</sup> part.

$\Rightarrow$  A[0] will be greater than all elements of second half.



$$\left. \begin{array}{l} \text{if } A[i] < A[0] \longrightarrow \text{2nd part} \\ A[i] > A[0] \longrightarrow \text{1st part.} \end{array} \right\}$$

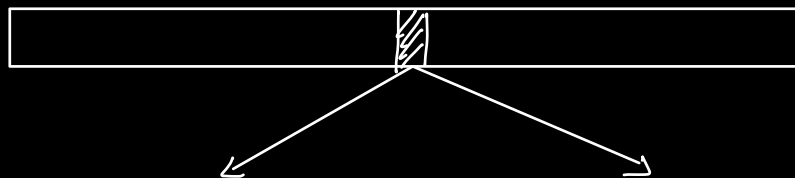
We want to find the pos at which the 1st part ends & 2nd begins. (boundaries of the 2 parts)



Find the pivot point

Find : Starting index of second half.

$\Rightarrow$  index of smallest value of 2nd half.



if  $A[mid] \geq A[0]$   
 mid is on 1st part  
 // Move to right  
 $l = mid + 1;$

if  $A[mid] < A[0]$   
 mid is on 2nd part  
 // Can mid be the ans?  
 Yes  $\rightarrow$  Store the ans  
 Move to left  
 $pivot = mid;$   
 $r = mid - 1$

<sup>0</sup>10, <sup>1</sup>20, <sup>2</sup>30, <sup>3</sup>1, <sup>4</sup>2, <sup>5</sup>3, <sup>6</sup>4, <sup>7</sup>5, <sup>8</sup>6, <sup>9</sup>7, <sup>10</sup>8, <sup>11</sup>9

$l$	$r$	mid	$A[mid]$	pivot	move to
0	11	5	3	<del>3</del> 5	left
0	4	2	30	<del>3</del> 5	right
3	4	3	1	<del>1</del> <u>3</u>	left

→ Break

<sup>0</sup>5, <sup>1</sup>8, <sup>2</sup>10, <sup>3</sup>14, <sup>4</sup>18, <sup>5</sup>22, <sup>6</sup>-15, <sup>7</sup>-9, <sup>8</sup>-6, <sup>9</sup>0, <sup>10</sup>2

$l$	$r$	mid	$A[mid]$	pivot (idx)	move to
0	10	5	22	-	right
6	10	8	-6	8	left
6	7	6	-15	6	left
6	5				

→ Break.

0 1 2 3  
1, 2, 3, 4

-1/-0/0

l	r	mid	A[mid]	pivot (idx)	move to
0	3	1	2	-	right
2	3	2	3	-	right
3	3	3	4	-	right
4	3				

→ Break ..

if no updates in pivot value → No rotations.

Step I

Find pivot index (using BS)  
↳ p

⇒  $O(\log N)$

Step II

if (target < A[p])

↳ Search on right part  
↳ BS(target, p, N-1)

if (target >= A[p])

↳ Search on left part  
↳ BS(target, 0, p-1)

goldfish



TC :  $O(\log N)$

SC :  $O(1)$

HW

Implement the solution using a single iteration of BS. [TC:  $O(\log N)$ ]

Q Given a no  $N$ . Find the  $\text{sqr}(N)$

↳  $\text{floor}(\text{sqr}(N))$   
(int part)

$$\text{sqr}(25) = 5$$

$$\text{sqr}(20) = 4$$

$$\text{sqr}(10) = 3$$

$$N > 0$$

$$N = 36$$

int  $\text{sqr}(N)$  {

⇒  $i = 1$ ;

while ( $i \times i \leq N$ ) {

{  $\text{ans} = i$ ;

$i++$ ;

}

return  $\text{ans}$ ;

}

Linear  
search

TC:  $O(\sqrt{N})$

i	$i \times i$	ans
1	1	1
2	4	2
3	9	3
4	16	4
5	25	5
⇒ 6	36	6
7	49	Break

Find max val of  $i$   
for which  $i \times i \leq N$

Min ans → 1

Max ans →  $N$

$[1, N]$

Searching for ans. ←

in  $[1, N]$  ←



$mid \times mid > N \rightarrow$  Move to left

$mid \times mid < N \rightarrow$  Store the ans  
Move to right.

Q Google Given an array of pos no. Find the max length K such that  $\rightarrow$  there exists no subarray of length K with  $\text{sum} \geq B$ .

$\rightarrow$  All subarrays of length K have  $\text{sum} < B$

A :  $\overset{0}{3}, \overset{1}{2}, \overset{2}{5}, \overset{3}{4}, \overset{4}{6}, \overset{5}{3}, \overset{6}{7}, \overset{7}{2}$

B = 20

$\Rightarrow 3$

K = 5 ✗

K = 4 ✗

K = 3 ✓

Brute force

$K_{\min} \rightarrow 0$   
 $K_{\max} \rightarrow N$

Iterate from  $K_i = \underline{N} \rightarrow 0$

$\rightarrow$  Check if  $K_i$  satisfies the condition  
 { All subarrays of length K have  $\text{sum} < B$  }

Find sum of all subarray of length K

PS Approach

TC :  $O(N) + O(N) \Rightarrow O(N)$

$\uparrow$   
Builds

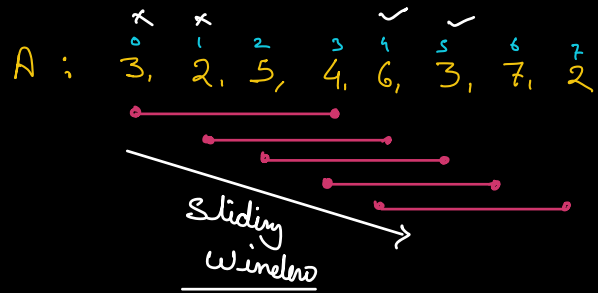
$\downarrow$   
SC :  $O(N)$

Sliding window

TC :  $O(N)$

SC :  $O(1)$





Write a fn which returns true if a given length  $K$  satisfies the condition (all subarrays of size  $K$  have sum  $< B$ )

boolean check(A[], K, B) {

// Get sum of first window of size  $K \rightarrow [0, K-1] \Rightarrow$  sum

if (sum  $\geq B$ )  
    ret false;

for ( $i = K$ ;  $i < N$ ;  $i++$ ) {

    sum += A[i];

    sum -= A[i-K];

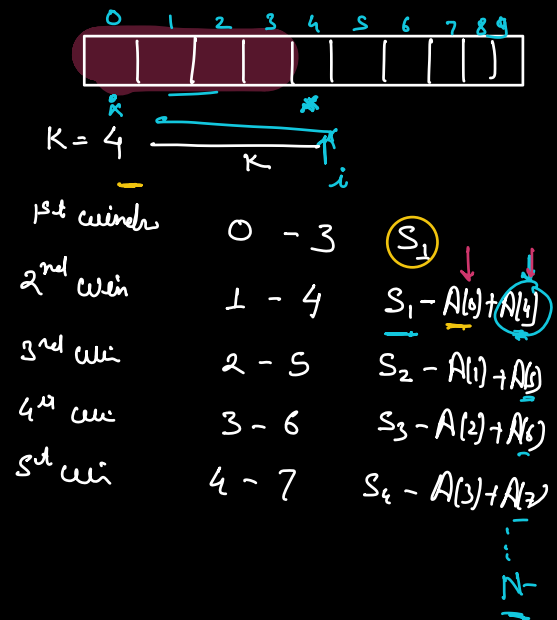
    if (sum  $\geq B$ )

        ret false;

}

ret true;

}



Linear iteration

for ( $K = N$ ;  $K \geq 0$ ;  $K--$ ) {

    if (check(A, K, B))

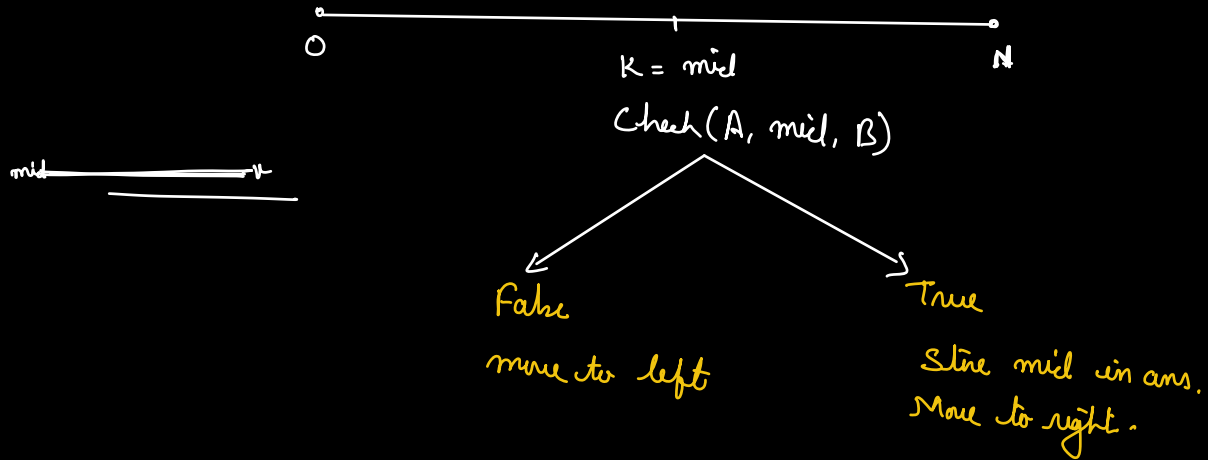
        ret K;

}

TC :  $O(N^2)$

target :  $K_{max}$

Search Space :  $[0, N]$



0 1 2 3 4 5  
3, 2, 1, 5, 4, 7

K = 3

B = 6

```

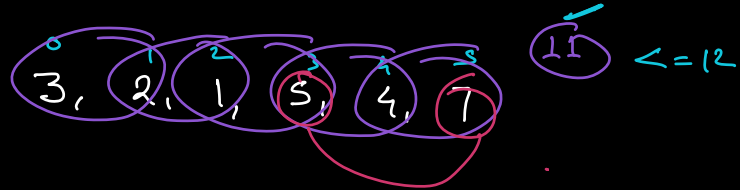
int BS on Ans (A[], B) {
    // define range of search space
    l = 0; r = N; // All possible values of k
                    // (length of subarray)
    while (l <= r) {
        mid = (l + r) / 2;
        if (check(A, mid, B)) {
            ans = mid;
            l = mid + 1;
        } else {
            r = mid - 1;
        }
    }
    return ans;
}

```

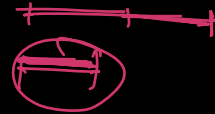
Tc :  $O(N \log N)$

Sc :  $O(1)$

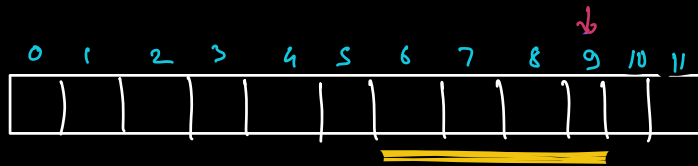
B=12



7, 5, 4, 3, 2, 1



7, 12, 16, 19, 21, 22



5x