

# Sorting

# Merge Sort

- Merge sort is based divide and conquer strategy.
- Can be implemented as external sorting, when the dataset is so big that it is impossible to load the whole dataset into memory, here sorting is done in chunks.
- Merging is the process of combining two sorted files to make one bigger sorted file.
- Selection is the process of dividing a file into two parts:  $k$  smallest elements and  $n - k$  largest elements.
- Selection and merging are opposite operations
  - selection splits a list into two lists
  - merging joins two files to make one file

# Algorithm – Merge Sort

**1.Divide:** Divide the list or array recursively into two halves until it can no more be divided.

**2.Conquer:** Each subarray is sorted individually using the merge sort algorithm.

**3.Merge:** The sorted subarrays are merged back together in sorted order. The process continues until all elements from both subarrays have been merged.

Index	0	1	2	3	4	5	6
Values	9	4	7	6	3	1	5

1

0	1	2	3
9	4	7	6

4	5	6
3	1	5

2

0	1
9	4

2	3
7	6

12

4	5
3	1

6
5

3

7

13

17

0
9

1
4

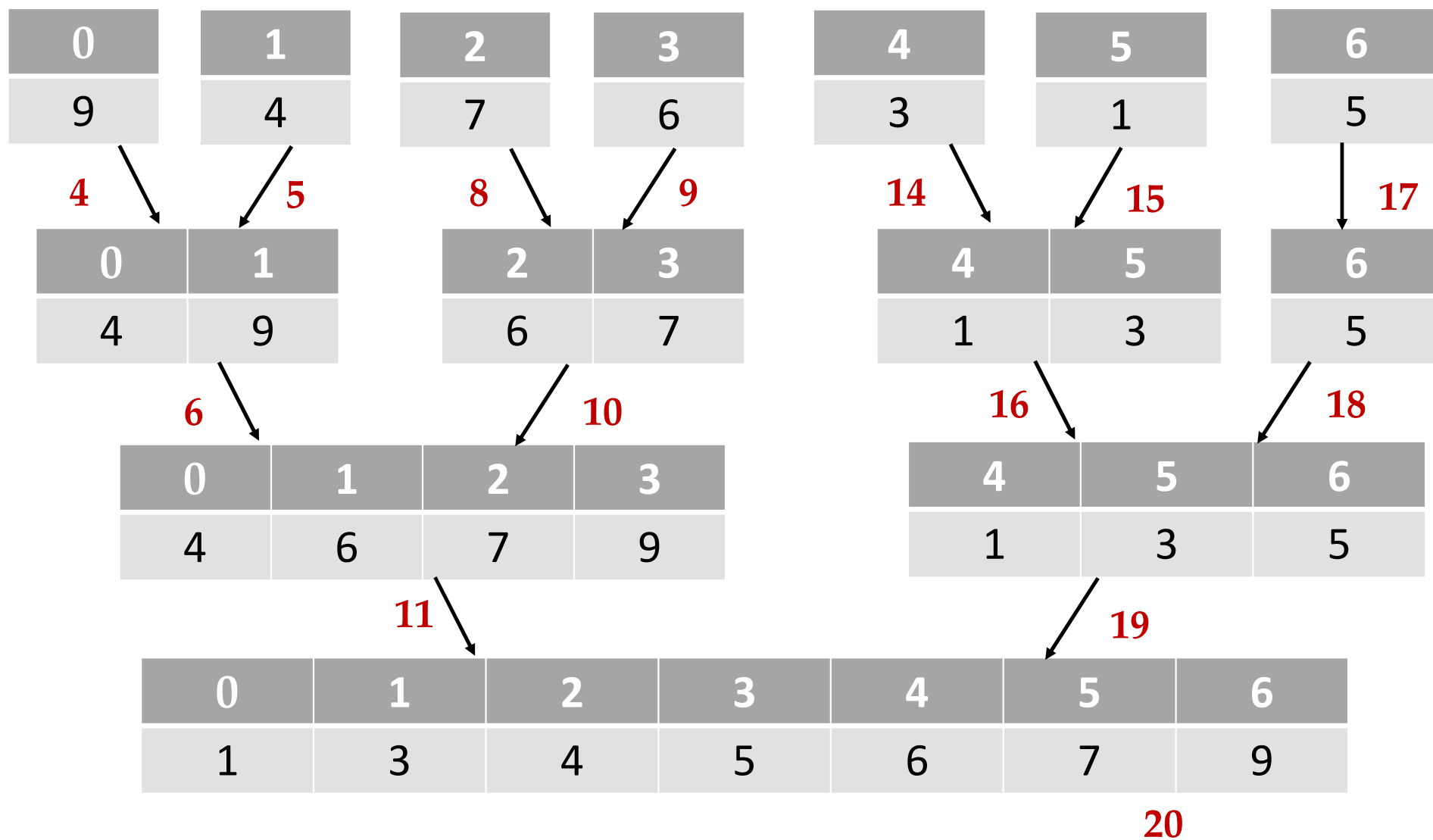
2
7

3
6

4
3

5
1

6
5



# Performance – Merge Sort

- Worst case complexity :  $O(n \log n)$
- Best case complexity :  $O(n \log n)$
- Average case complexity :  $O(n \log n)$
- Worst case space complexity:  $O(n)$  auxiliary

# Quick Sort

- It is an example of a divide-and-conquer algorithmic technique.
- It is also called partition exchange sort.
- It uses recursive calls for sorting the elements, and it is one of the famous algorithms among comparison-based sorting algorithms.
- Divide: The array  $A[\text{low} \dots \text{high}]$  is partitioned into two non-empty sub arrays  $A[\text{low} \dots q]$  and  $A[q + 1 \dots \text{high}]$ , such that each element of  $A[\text{low} \dots \text{high}]$  is less than or equal to each element of  $A[q + 1 \dots \text{high}]$ . The index  $q$  is computed as part of this partitioning procedure.
- Conquer: The two sub arrays  $A[\text{low} \dots q]$  and  $A[q + 1 \dots \text{high}]$  are sorted by recursive calls to Quick sort.

# Algorithm – Quick Sort

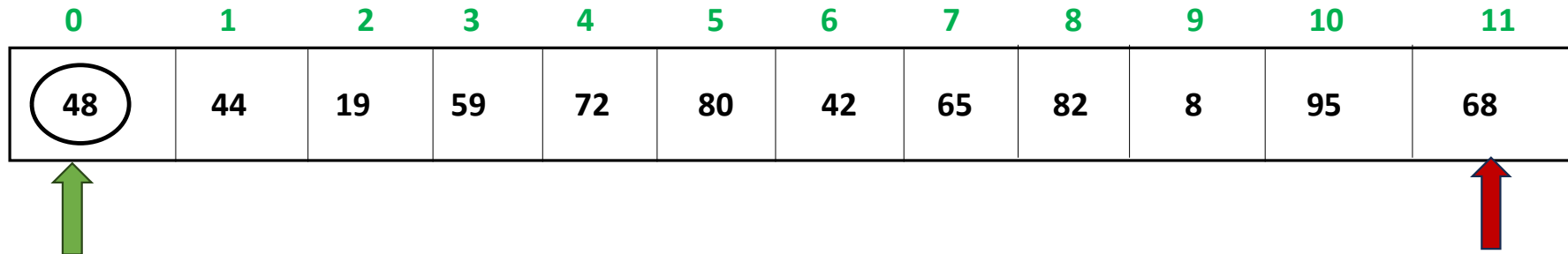
The recursive algorithm consists of four steps:

- If there are one or no elements in the array to be sorted, return.
- Pick an element in the array to serve as the “pivot” point.  
(Usually the left-most element in the array is used.)
- Split the array into two parts – one with elements larger than the pivot and the other with elements smaller than the pivot.
- Recursively repeat the algorithm for both halves of the original array.

Tip: In this algorithm, we place the pivot element at right place.



0	1	2	3	4	5	6	7	8	9	10	11
48	44	19	59	72	80	42	65	82	8	95	68



```

public static int partition(int arr[], int low, int high)
{
    int left, right, pivot, t;

    pivot=arr[low];    // pivot = 48
    left=low;          // left = 0
    right =high;       // right = 11

    while(left <= right)
    {
        while((arr[left]<=pivot) && (left<high))
            left++;

        while(arr[right] > pivot)
            right--;
    }
}

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public static int partition(int arr[], int low, int high)
```

```
{
    // 0    11
    int left, right, pivot, t;
```

```
    pivot=arr[low];    // pivot = 48
```

```
    left=low;          // left = 0
```

```
    right =high;       // right = 11
```

```
    while(left <= right)
```

```
    {
```

```
        while((arr[left]<=pivot) && (left<high))
```

```
            left++;
```

```
        while(arr[right] > pivot)
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            right--;
```

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    pivot=arr[low];    // pivot = 48
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```
    while(left <= right)
```

```
    {
```

```
        while((arr[left]<=pivot) && (left<high))
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```
            left++;
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```
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```
            right--;
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```
        if(left < right)
```

```
        {
```

```
            t=arr[left];
```

```
            arr[left] = arr[right];
```

```
            arr[right] = t;
```

```
            left++; right--;
```

```
        }
```

```
        else left++;
```

```
    } // end of while loop
```

```
    arr[low] = arr[right];
```

```
    arr[right] =pivot;
```

```
    return right;    // right =
```

```
    4
```

```
    } // end of function
```

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4
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        while((arr[left]<=pivot) && (left<high))
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```

```
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```

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            t=arr[left];
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            arr[right] = t;
```

```
            left++; right--;
```

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        }
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    arr[low] = arr[right];
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    arr[right]=pivot;
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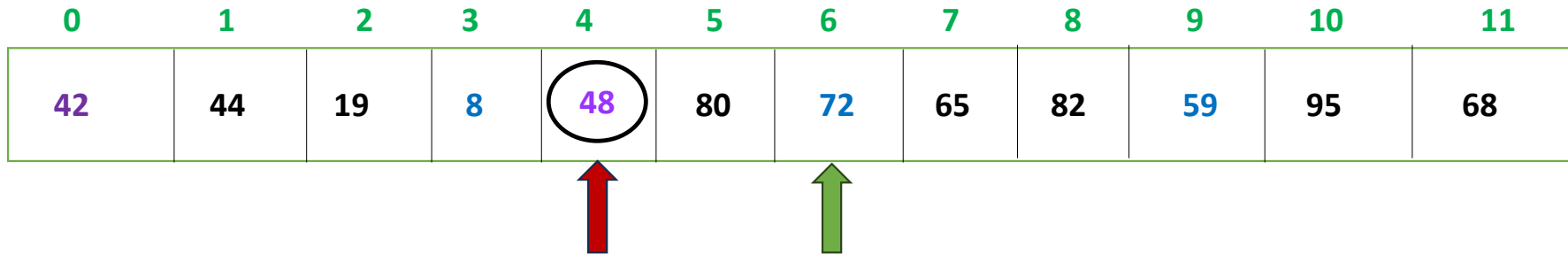
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```

```
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```

```
        while((arr[left]<=pivot) && (left<high))
```

```
            left++;
```

```
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```

```
            right--;
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```

```
            left++; right--;
```

```
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```
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```

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```

```
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```

```
    return right; // right = 4
} // end of function
```

```
public static void QuickSort(int arr[],
    int low,int high)
```

```
{
    //0    11
    int pivloc;
```

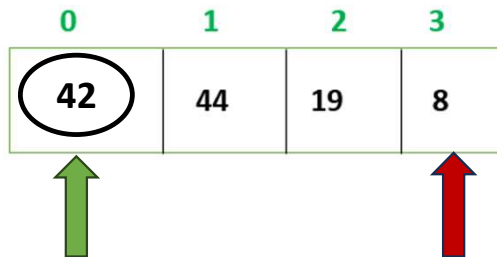
```
    if(low>=high) return;
```

```
    pivloc = partition(arr,low,high); //4
```

```
    QuickSort(arr,low,pivloc-1);
    // 0    3
```

```
    QuickSort(arr,pivloc+1, high);
    // 5    11
```

```
}
```



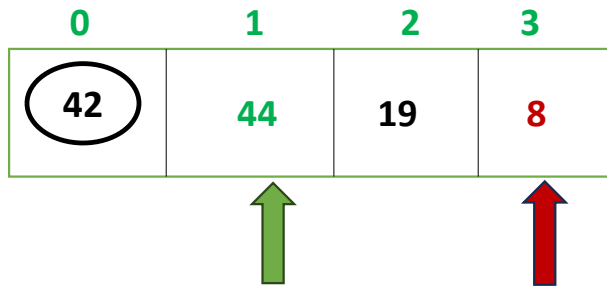
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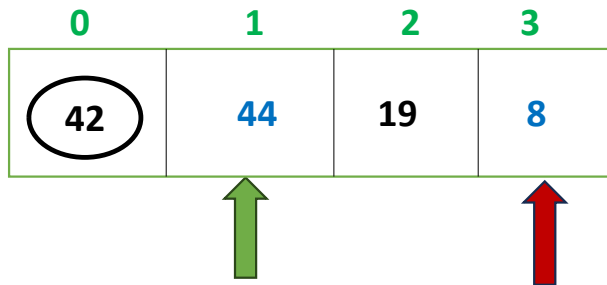
```
    left=low;          // left = 0
```

```
    right =high;       // right = 3
```

```
    while(left <= right)
```

```
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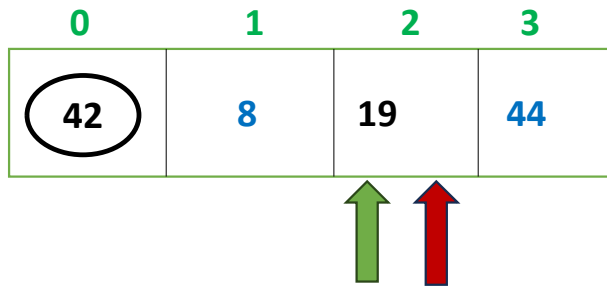
```

    if(left < right)
    {
        t=arr[left];
        arr[left] = arr[right] ;
        arr[right] = t;
        left++; right--;
    }
    else left++;
} // end of while loop

arr[low] = arr[right];
arr[right] =pivot;

return right;    // right = 3
} // end of function

```

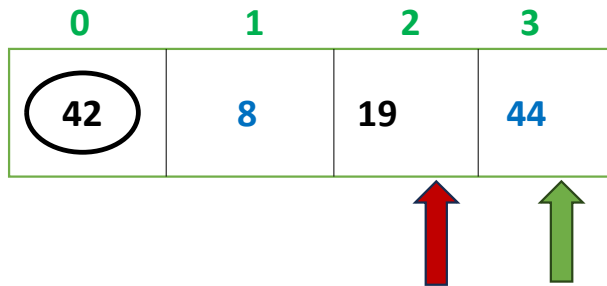


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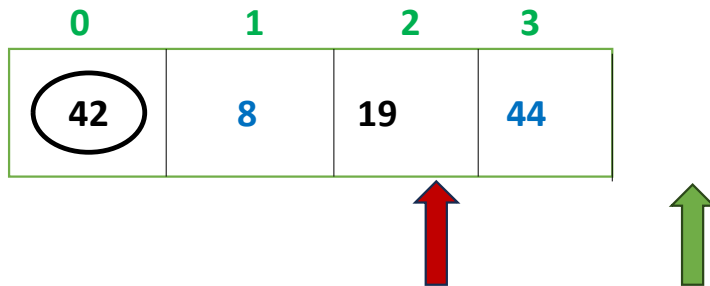


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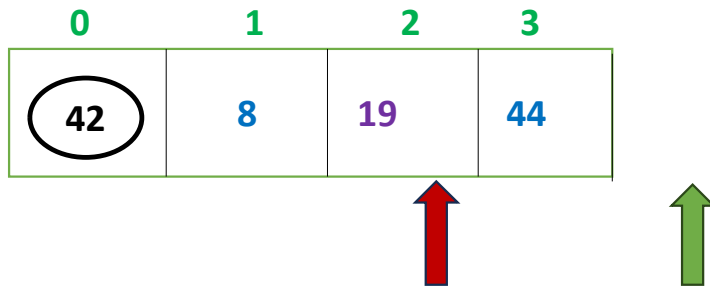
        while(arr[right] > pivot)
            right--;
    }
}

```

```

if(left < right) //false
{
    t=arr[left];
    arr[left] = arr[right] ;
    arr[right] = t;
    left++; right--;
}
else left++;
} // end of while loop

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        {
            t=arr[left];
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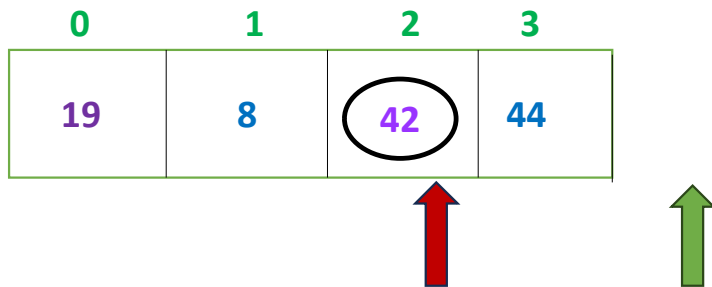
```

```
        else left++;
```

```
    } // end of while loop
```

```
    arr[low] = arr[right];
    arr[right] =pivot;
```

```
    return right;    // right = 2
} // end of function
```



```

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        }
        else left++;
    } // end of while loop

    arr[low] = arr[right];
    arr[right] =pivot;

    return right;    // right =
2
} // end of function
  
```

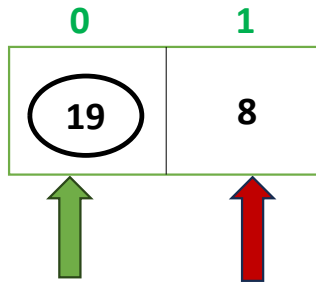
```

public static void QuickSort(int arr[],
    int low,int high)
{
    // 0 3
    int pivloc;

    if(low>=high) return;

    pivloc = partition(arr,low,high); //2

    QuickSort(arr,low,pivloc-1);
    // 0 1
    QuickSort(arr,pivloc+1, high);
    // 3 3
}
  
```



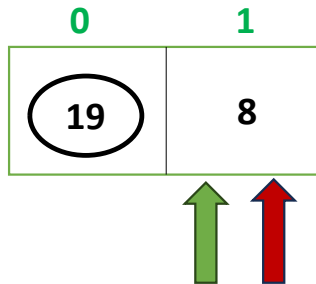
```
public static int partition(int arr[], int low, int high)
{
    int left, right, pivot, t;

    pivot=arr[low];    // pivot = 19
    left=low;          // left = 0
    right =high;       // right = 1

    while(left <= right)
    {
        while((arr[left]<=pivot) && (left<high))
            left++;

        while(arr[right] > pivot)
            right--;
    }
}
```



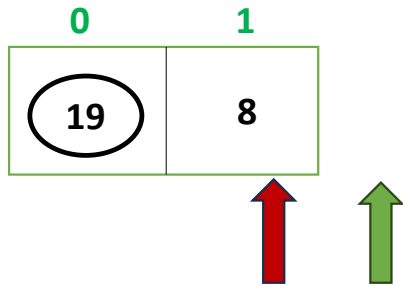


```
public static int partition(int arr[], int low, int high)
{
    int left, right, pivot, t;

    pivot=arr[low];    // pivot = 19
    left=low;          // left = 0
    right =high;        // right = 1

    while(left <= right)
    {
        while((arr[left]<=pivot) && (left<high))
            left++;

        while(arr[right] > pivot)
            right--;
    }
}
```



```

public static int partition(int arr[], int low, int high)
{
    int left, right, pivot, t;

    pivot=arr[low];    // pivot = 19
    left=low;          // left = 0
    right =high;       // right = 1

    while(left <= right)
    {
        while((arr[left]<=pivot) && (left<high))
            left++;

        while(arr[right] > pivot)
            right--;
    }

```

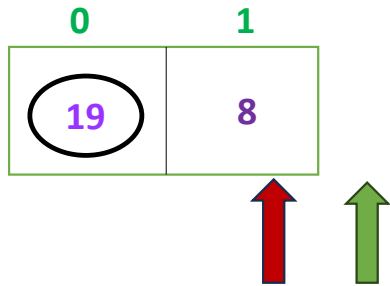
```

    if(left < right) //false
    {
        t=arr[left];
        arr[left] = arr[right] ;
        arr[right] = t;
        left++; right--;
    }
    else left++;
} // end of while loop

arr[low] = arr[right];
arr[right] =pivot;

return right;    // right =
1
} // end of function

```



```

public static int partition(int arr[], int low, int high)
{
    int left, right, pivot, t;

    pivot=arr[low];    // pivot = 19
    left=low;          // left = 0
    right =high;        // right = 1

    while(left <= right)
    {
        while((arr[left]<=pivot) && (left<high))
            left++;

        while(arr[right] > pivot)
            right--;
    }
}

```

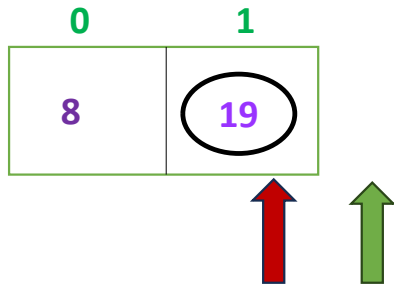
```

if(left < right) //false
{
    t=arr[left];
    arr[left] = arr[right] ;
    arr[right] = t;
    left++; right--;
}
else left++;
} // end of while loop

arr[low] = arr[right];
arr[right] =pivot;

return right;    // right = 1
} // end of function

```



```
public static int partition(int arr[], int low, int high)
```

```
{
    // 0 1
    int left, right, pivot, t;

    pivot=arr[low];    // pivot = 19
    left=low;          // left = 0
    right =high;       // right = 1

    while(left <= right)
    {
        while((arr[left]<=pivot) && (left<high))
            left++;

        while(arr[right] > pivot)
            right--;

        if(left < right) //false
        {
            t=arr[left];
            arr[left] = arr[right];
            arr[right] = t;
            left++; right--;
        }
        else left++;
    } // end of while loop

    arr[low] = arr[right];
    arr[right] =pivot;

    return right; // right = 1
} // end of function
```

```
public static void QuickSort(int arr[],
    int low,int high)
{
    int pivloc;

    if(low>=high) return;

    pivloc = partition(arr,low,high); //1

    QuickSort(arr,low,pivloc-1);
        // 0 0 //*****
    QuickSort(arr,pivloc+1, high);
        // 2 1 //*****
}
```

0	1	2	3	4	5	6	7	8	9	10	11
8	19	42	44	48	80	72	65	82	59	95	68

```
public static int partition(int arr[], int low, int high)
```

```
{
    int left, right, pivot, t;
```

```
    pivot=arr[low];    // pivot = 80
    left=low;          // left = 5
    right =high;       // right = 11
```

```
    while(left <= right)
    {
```

```
        while((arr[left]<=pivot) && (left<high))
            left++;
```

```
        while(arr[right] > pivot)
            right--;
```

```
        if(left < right)
```

```
        {
            t=arr[left];
            arr[left] = arr[right] ;
            arr[right] = t;
            left++; right--;
```

```
        }
        else left++;
    } // end of while loop
```

```
    arr[low] = arr[right];
    arr[right] =pivot;
```

```
    return right; // right = 4
} // end of function
```

```
public static void QuickSort(int arr[],
    int low,int high)
```

```
{
    int pivloc;

    if(low>=high) return;

    pivloc = partition(arr,low,high);
```

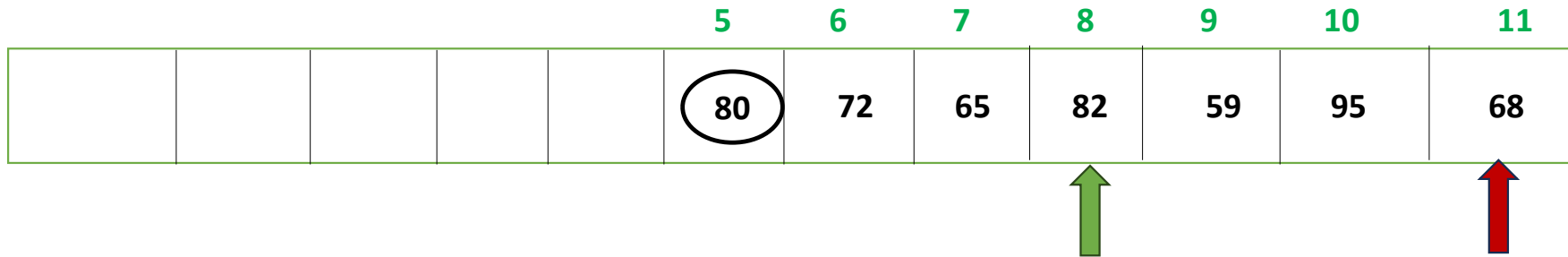
```
    QuickSort(arr,low,pivloc-1);
```

```
        // 0 3
```

```
    QuickSort(arr,pivloc+1, high);
```

```
        // 5 11
```

```
}
```



```
public static int partition(int arr[], int low, int high)
{
```

```
    int left, right, pivot, t;
```

```
    pivot=arr[low];    // pivot = 80
```

```
    left=low;          // left = 5
```

```
    right =high;       // right = 11
```

```
    while(left <= right)
```

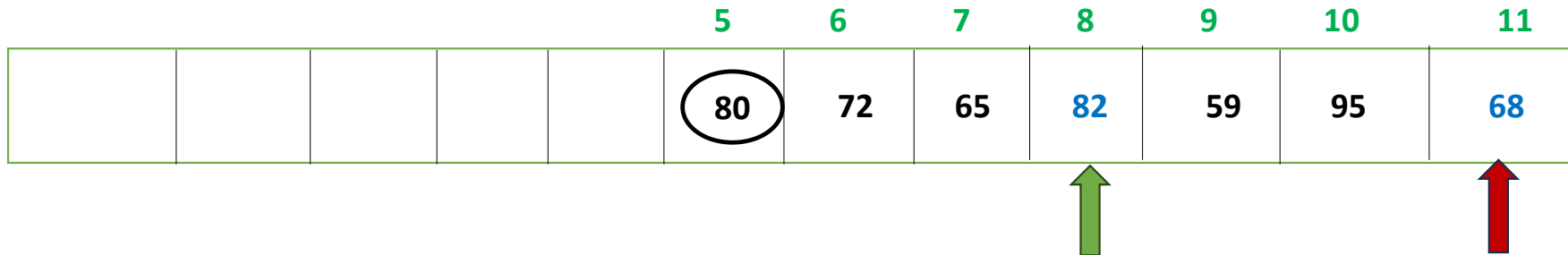
```
    {
```

```
        while((arr[left]<=pivot) && (left<high))
```

```
            left++;
```

```
        while(arr[right] > pivot)
```

```
            right--;
```



```

public static int partition(int arr[], int low, int high)
{
    int left, right, pivot, t;

    pivot=arr[low];    // pivot = 80
    left=low;          // left = 5
    right =high;       // right = 11

    while(left <= right)
    {
        while((arr[left]<=pivot) && (left<high))
            left++;

        while(arr[right] > pivot)
            right--;

        if(left < right) //true
        {
            t=arr[left];
            arr[left] = arr[right] ;
            arr[right] = t;
            left++; right--;
        }
        else left++;
    } // end of while loop

    arr[low] = arr[right];
    arr[right] =pivot;

    return right;    // right =
2
} // end of function

```

					5	6	7	8	9	10	11
					80	72	65	68	59	95	82

```
public static int partition(int arr[], int low, int high)
{
```

```
    int left, right, pivot, t;
```

```
    pivot=arr[low];    // pivot = 80
```

```
    left=low;          // left = 5
```

```
    right =high;       // right = 11
```

```
    while(left <= right)
```

```
    {
        while((arr[left]<=pivot) && (left<high))
            left++;
```

```
        while(arr[right] > pivot)
            right--;
```

```
        if(left < right) //false
```

```
        {
            t=arr[left];
            arr[left] = arr[right] ;
            arr[right] = t;
            left++; right--;
        }
```

```
        else left++;
```

```
    } // end of while loop
```



					5	6	7	8	9	10	11
					80	72	65	68	59	95	82



```
public static int partition(int arr[], int low, int high)
{
```

```
    int left, right, pivot, t;
```

```
    pivot=arr[low];    // pivot = 80
```

```
    left=low;          // left = 5
```

```
    right =high;       // right = 11
```

```
    while(left <= right)
```

```
    {
```



```
        while((arr[left]<=pivot) && (left<high))
```

```
            left++;
```

```
        while(arr[right] > pivot)
```

```
            right--;
```

					5	6	7	8	9	10	11
					80	72	65	68	59	95	82

```

public static int partition(int arr[], int low, int high)
{
    int left, right, pivot, t;

    pivot=arr[low];    // pivot = 80
    left=low;          // left = 5
    right =high;       // right = 11

    while(left <= right)
    {
        while((arr[left]<=pivot) && (left<high))
            left++;

        while(arr[right] > pivot)
            right--;

        if(left < right) //false
        {
            t=arr[left];
            arr[left] = arr[right] ;
            arr[right] = t;
            left++; right--;
        }
        else left++;
    } // end of while loop

    arr[low] = arr[right];
    arr[right] =pivot;

    return right;    // right =
9
} // end of function

```

					5	6	7	8	9	10	11
					59	72	65	68	80	95	82

```
public static int partition(int arr[], int low, int high)
```

```
{
    // 5    11
    int left, right, pivot, t;
```

```
    pivot=arr[low];    // pivot = 80
    left=low;          // left = 5
    right =high;       // right = 11
```

```
    while(left <= right)
    {
```

```
        while((arr[left]<=pivot) && (left<high))
            left++;
```

```
        while(arr[right] > pivot)
            right--;
```

```
        if(left < right) //false
```

```
        {
            t=arr[left];
            arr[left] = arr[right] ;
            arr[right] = t;
            left++; right--;
        }
```

```
        else left++;
```

```
    } // end of while loop
```

```
    arr[low] = arr[right];
    arr[right] =pivot;
```

```
    return right; // right = 9
```

```
// end of function
```

```
public static void QuickSort(int arr[],
    int low, int high)
```

```
{
    // 5    11
    int pivloc;
```

```
    if(low>=high) return;
```

```
    pivloc = partition(arr,low,high); //9
```

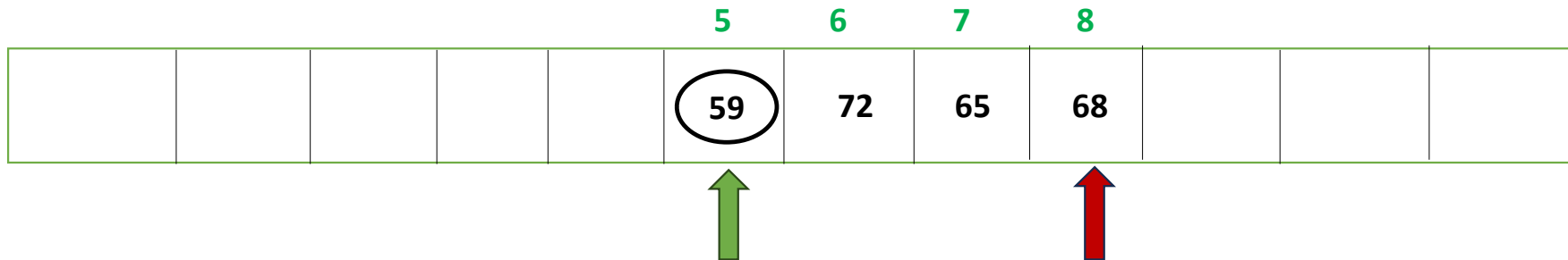
```
    QuickSort(arr,low,pivloc-1);
```

```
    // 5    8
```

```
    QuickSort(arr,pivloc+1, high);
```

```
    // 10    11
```

```
}
```



```
public static int partition(int arr[], int low, int high)
{
```

```
    int left, right, pivot, t;
```

```
    pivot=arr[low];    // pivot = 59
```

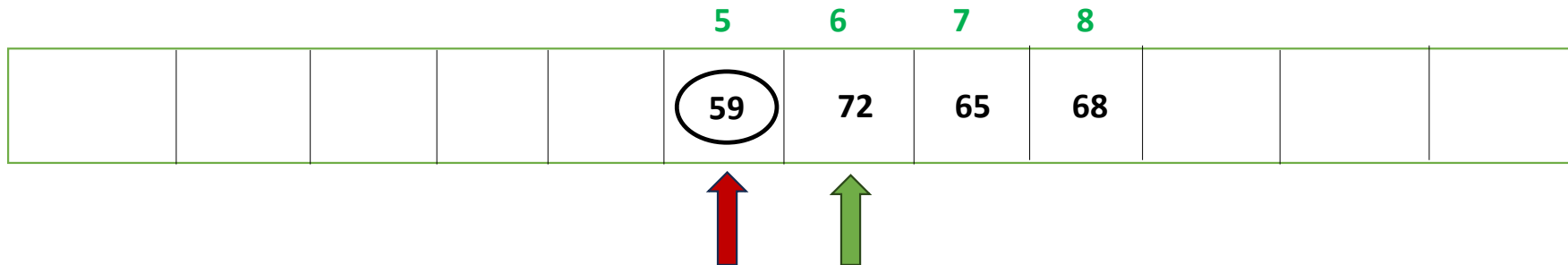
```
    left=low;          // left = 5
```

```
    right =high;        // right = 8
```

```
    while(left <= right)
```

```
    {
        while((arr[left]<=pivot) && (left<high))
            left++;
```

```
        while(arr[right] > pivot)
            right--;
```



```
public static int partition(int arr[], int low, int high)
```

```
{
```

```
    int left, right, pivot, t;
```

```
    pivot=arr[low];    // pivot = 59
```

```
    left=low;          // left = 5
```

```
    right =high;       // right = 8
```

```
    while(left <= right)
```

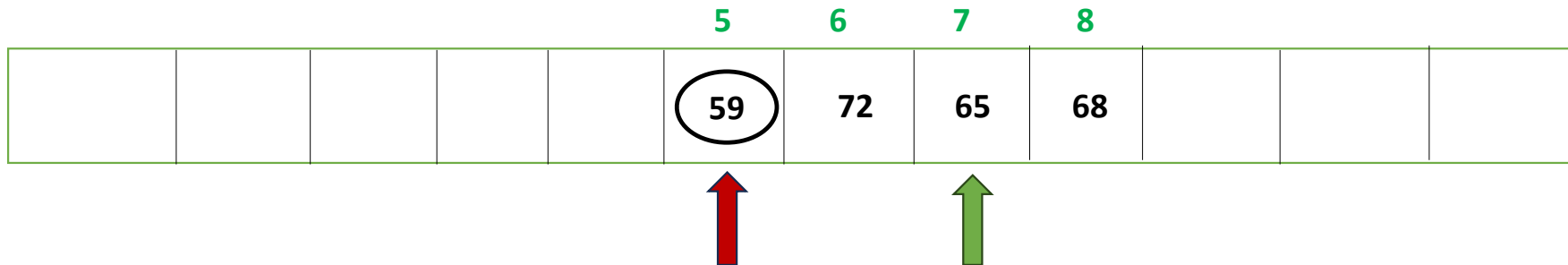
```
    {
```

```
        while((arr[left]<=pivot) && (left<high))
```

```
            left++;
```

```
        while(arr[right] > pivot)
```

```
            right--;
```



```

public static int partition(int arr[], int low, int high)
{
    int left, right, pivot, t;

    pivot=arr[low];    // pivot = 59
    left=low;          // left = 5
    right =high;       // right = 8

    while(left <= right)
    {
        while((arr[left]<=pivot) && (left<high))
            left++;

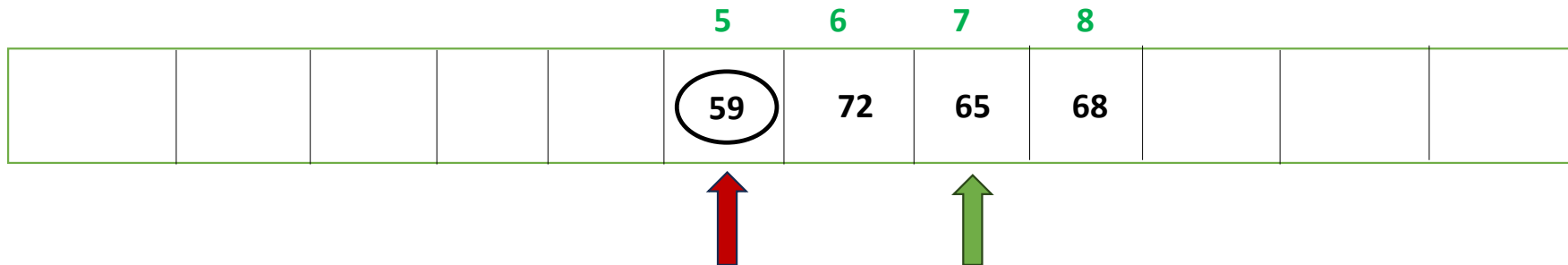
        while(arr[right] > pivot)
            right--;

        if(left < right) //false
        {
            t=arr[left];
            arr[left] = arr[right] ;
            arr[right] = t;
            left++; right--;
        }
        else left++;
    } // end of while loop

    arr[low] = arr[right];
    arr[right] =pivot;

    return right;    // right = 5
} // end of function

```



```

public static int partition(int arr[], int low, int high)
{
    // 5    8
    int left, right, pivot, t;

    pivot=arr[low];    // pivot = 59
    left=low;          // left = 5
    right =high;       // right = 8

    while(left <= right)
    {
        while((arr[left]<=pivot) && (left<high))
            left++;

        while(arr[right] > pivot)
            right--;

        if(left < right) //false
        {
            t=arr[left];
            arr[left] = arr[right] ;
            arr[right] = t;
            left++; right--;
        }
        else left++;
    } // end of while loop

    arr[low] = arr[right];
    arr[right] =pivot;

    return right; // right = 5
} // end of function

```

```

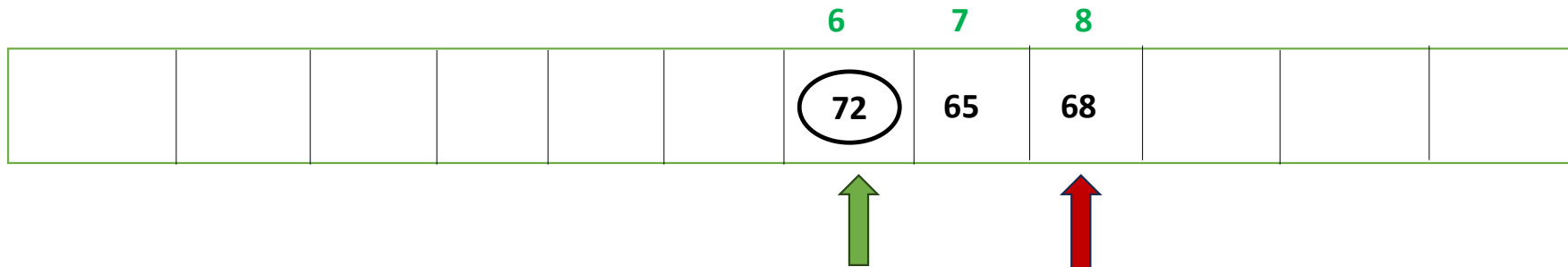
public static void QuickSort(int arr[],
                             int low,int high)
{
    // 5    8
    int pivloc;

    if(low>=high) return;

    pivloc = partition(arr,low,high); //5

    QuickSort(arr,low,pivloc-1);
    // 5    4
    QuickSort(arr,pivloc+1, high);
    // 6    8
}

```



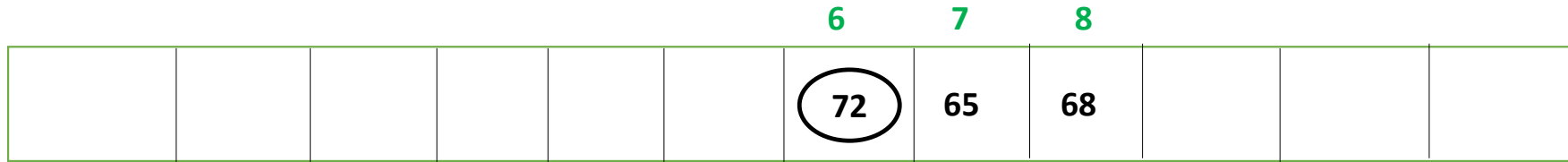
```
public static int partition(int arr[], int low, int high)
{
    int left, right, pivot, t;
```

```
    pivot=arr[low];    // pivot = 72
    left=low;          // left = 6
    right =high;        // right = 8
```

```
    while(left <= right)
    {
        while((arr[left]<=pivot) && (left<high))
            left++;
```

```
        while(arr[right] > pivot)
            right--;
```



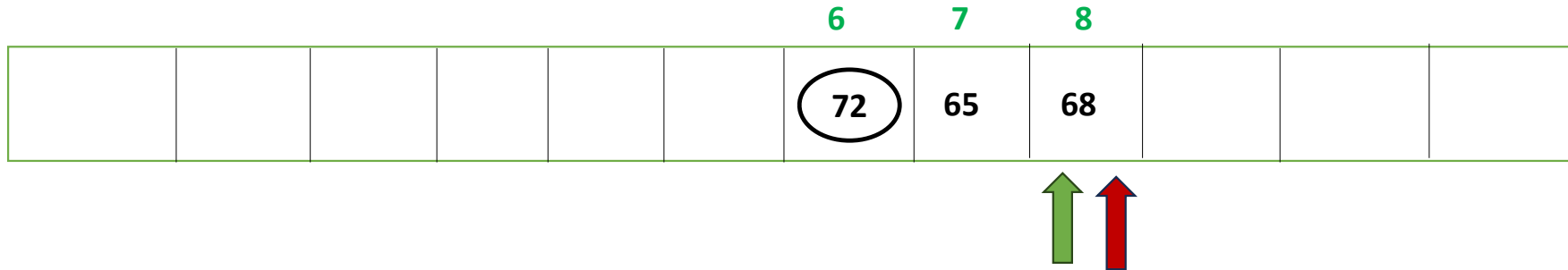


```
public static int partition(int arr[], int low, int high)
{
    int left, right, pivot, t;
```

```
    pivot=arr[low];    // pivot = 72
    left=low;          // left = 6
    right =high;       // right = 8
```

```
    while(left <= right)
    {
        while((arr[left]<=pivot) && (left<high))
            left++;
```

```
        while(arr[right] > pivot)
            right--;
```



```

public static int partition(int arr[], int low, int high)
{
    int left, right, pivot, t;

    pivot=arr[low];    // pivot = 72
    left=low;          // left = 6
    right =high;       // right = 8

    while(left <= right)
    {
        while((arr[left]<=pivot) && (left<high))
            left++;

        while(arr[right] > pivot)
            right--;
    }

```

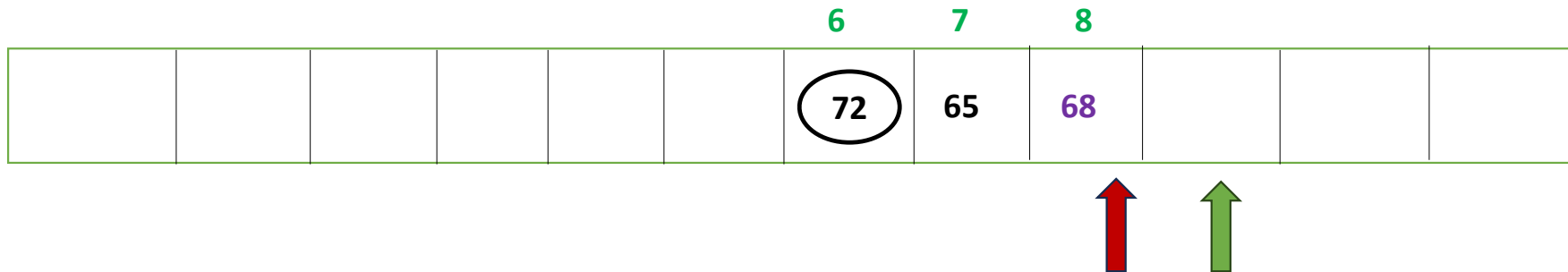
```

    if(left < right) //false
    {
        t=arr[left];
        arr[left] = arr[right] ;
        arr[right] = t;
        left++; right--;
    }
    else left++;
} // end of while loop

arr[low] = arr[right];
arr[right] =pivot;

return right;    // right =
} // end of function

```



```

public static int partition(int arr[], int low, int high)
{
    int left, right, pivot, t;

    pivot=arr[low];    // pivot = 72
    left=low;          // left = 6
    right =high;        // right = 8

    while(left <= right)
    {
        while((arr[left]<=pivot) && (left<high))
            left++;

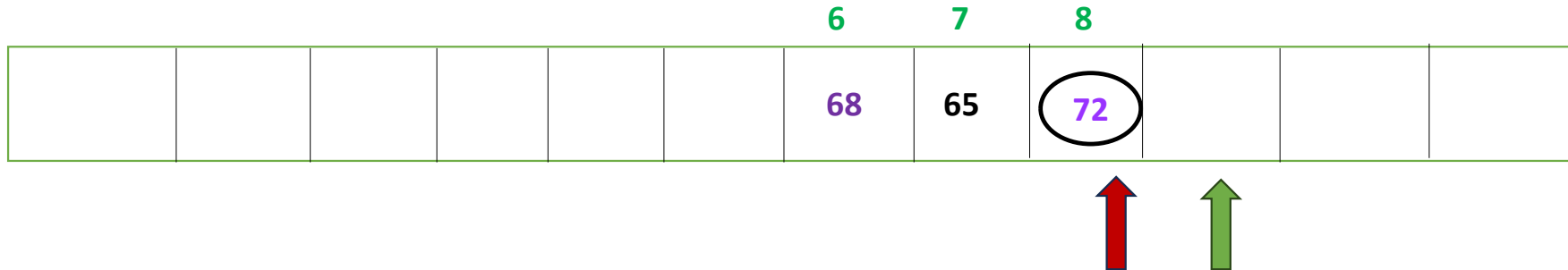
        while(arr[right] > pivot)
            right--;

        if(left < right) //false
        {
            t=arr[left];
            arr[left] = arr[right] ;
            arr[right] = t;
            left++; right--;
        }
        else left++;
    } // end of while loop

    arr[low] = arr[right];
    arr[right] =pivot;

    return right;    // right =
} // end of function

```



```
public static int partition(int arr[], int low, int high)
```

```
{
    // 6      8
    int left, right, pivot, t;
```

```
    pivot=arr[low];    // pivot = 72
    left=low;          // left = 6
    right =high;       // right = 8
```

```
    while(left <= right)
    {
```

```
        while((arr[left]<=pivot) && (left<high))
            left++;
```

```
        while(arr[right] > pivot)
            right--;
```

```
        if(left < right) //false
```

```
        {
            t=arr[left];
            arr[left] = arr[right] ;
            arr[right] = t;
            left++; right--;
        }
```

```
        else left++;
```

```
    } // end of while loop
```

```
    arr[low] = arr[right];
    arr[right] =pivot;
```

```
    return right; // right = 8
} // end of function
```

```
public static void QuickSort(int arr[],
    int low,int high)
```

```
{
    // 6      8
    int pivloc;
```

```
    if(low>=high) return;
```

```
    pivloc = partition(arr,low,high); //8
```

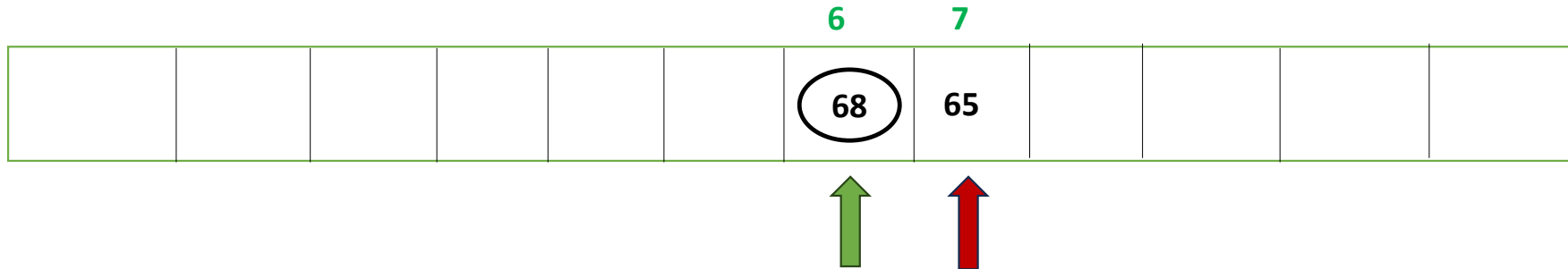
```
    QuickSort(arr,low,pivloc-1);
```

```
    // 6      7
```

```
    QuickSort(arr,pivloc+1, high);
```

```
    // 9      8
```

```
}
```

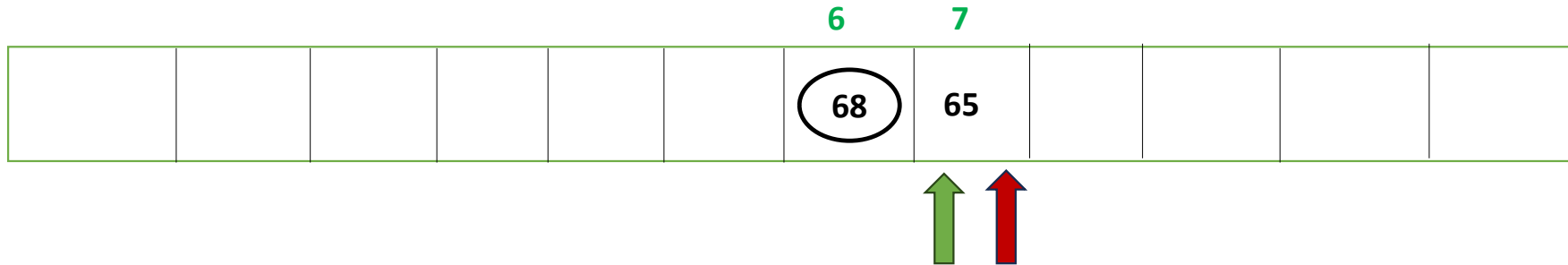


```
public static int partition(int arr[], int low, int high)
{
    int left, right, pivot, t;
```

```
    pivot=arr[low];    // pivot = 68
    left=low;          // left = 6
    right =high;       // right = 7
```

```
    while(left <= right)
    {
        while((arr[left]<=pivot) && (left<high))
            left++;
```

```
        while(arr[right] > pivot)
            right--;
```

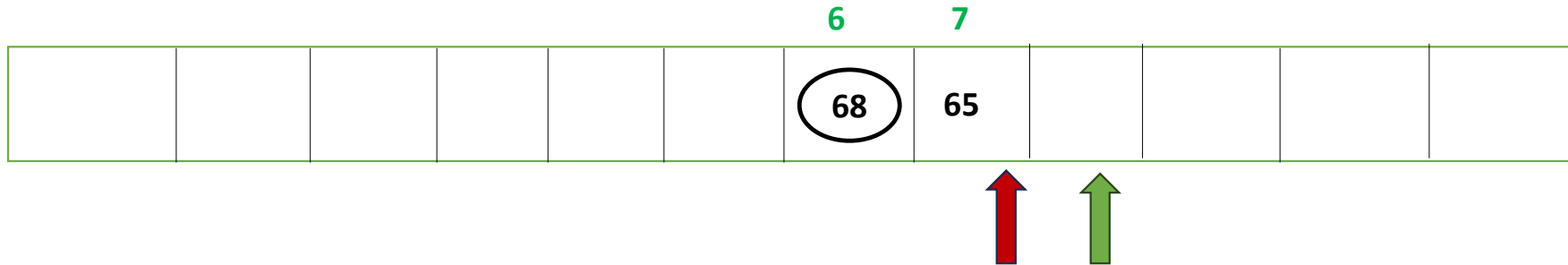


```
public static int partition(int arr[], int low, int high)
{
    int left, right, pivot, t;
```

```
    pivot=arr[low];    // pivot = 68
    left=low;          // left = 6
    right =high;       // right = 7
```

```
    while(left <= right)
    {
        while((arr[left]<=pivot) && (left<high))
            left++;
```

```
        while(arr[right] > pivot)
            right--;
```



```
public static int partition(int arr[], int low, int high)
{
    int left, right, pivot, t;
```

```
    pivot=arr[low];    // pivot = 68
    left=low;          // left = 6
    right =high;       // right = 7
```

```
    while(left <= right)
    {
```

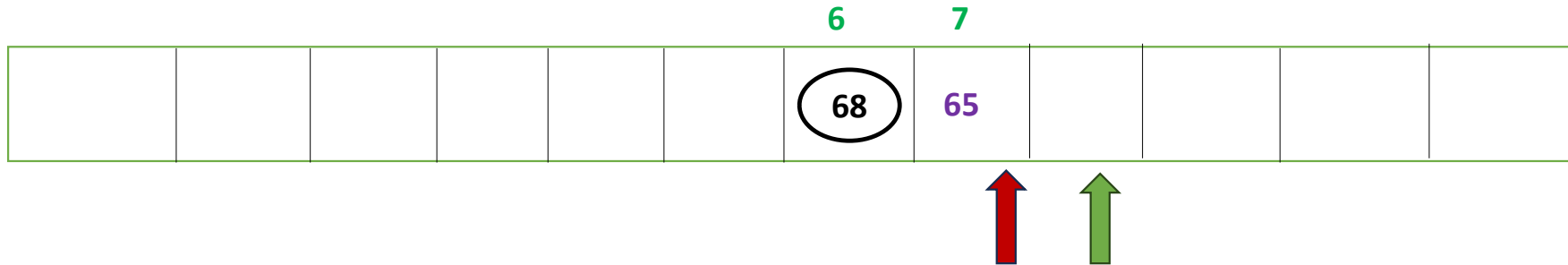
```
        while((arr[left]<=pivot) && (left<high))
            left++;
```

```
        while(arr[right] > pivot)
            right--;
```

```
        if(left < right) //false
        {
            t=arr[left];
            arr[left] = arr[right] ;
            arr[right] = t;
            left++; right--;
        }
        else left++;
    } // end of while loop
```

```
    arr[low] = arr[right];
    arr[right] =pivot;
```

```
    return right;    // right = 8
} // end of function
```



```

public static int partition(int arr[], int low, int high)
{
    int left, right, pivot, t;

    pivot=arr[low];    // pivot = 68
    left=low;          // left = 6
    right =high;       // right = 7

    while(left <= right)
    {
        while((arr[left]<=pivot) && (left<high))
            left++;

        while(arr[right] > pivot)
            right--;

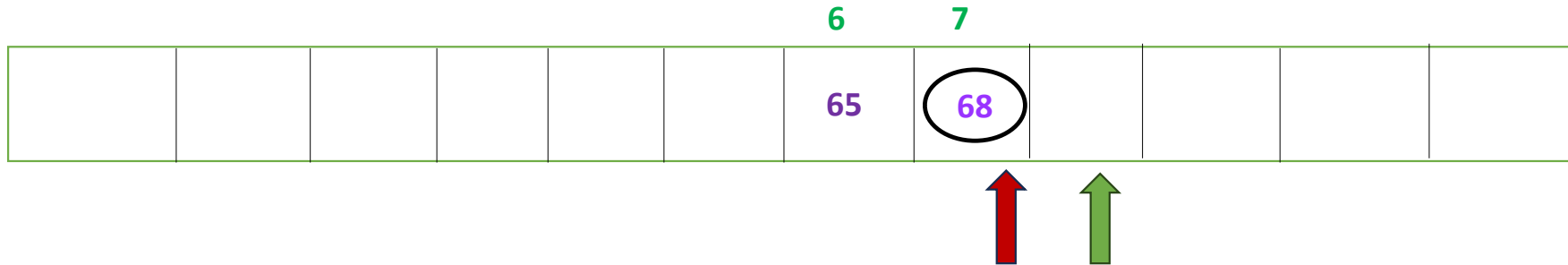
        if(left < right) //false
        {
            t=arr[left];
            arr[left] = arr[right] ;
            arr[right] = t;
            left++; right--;
        }
        else left++;
    } // end of while loop

    arr[low] = arr[right];
    arr[right] =pivot;

    return right;    // right =
8
} // end of function

```





```

public static int partition(int arr[], int low, int high)
{
    int left, right, pivot, t;

    pivot=arr[low];    // pivot = 68
    left=low;          // left = 6
    right =high;        // right = 7

    while(left <= right)
    {
        while((arr[left]<=pivot) && (left<high))
            left++;

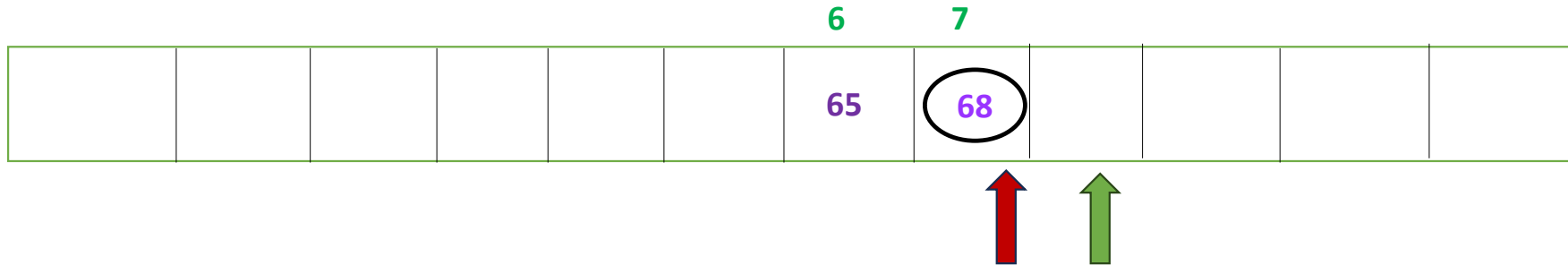
        while(arr[right] > pivot)
            right--;

        if(left < right) //false
        {
            t=arr[left];
            arr[left] = arr[right] ;
            arr[right] = t;
            left++; right--;
        }
        else left++;
    } // end of while loop

    arr[low] = arr[right];
    arr[right] =pivot;

    return right;    // right =
                    7
} // end of function

```



```

public static int partition(int arr[], int low, int high)
{
    int left, right, pivot, t;

    pivot=arr[low];    // pivot = 68
    left=low;          // left = 6
    right =high;       // right = 7

    while(left <= right)
    {
        while((arr[left]<=pivot) && (left<high))
            left++;

        while(arr[right] > pivot)
            right--;

        if(left < right) //false
        {
            t=arr[left];
            arr[left] = arr[right] ;
            arr[right] = t;
            left++; right--;
        }
        else left++;
    } // end of while loop

    arr[low] = arr[right];
    arr[right] =pivot;

    return right; // right = 7
} // end of function

```

```

public static void QuickSort(int arr[],
    int low,int high)
{
    // 6    7
    int pivloc;

    if(low>=high) return;

    pivloc = partition(arr,low,high); //7

    QuickSort(arr,low,pivloc-1);
        // 6    6
    QuickSort(arr,pivloc+1, high);
        // 8    7
}

```

											10	11
											95	82

```
public static int partition(int arr[], int low, int high)
```

```
{
    // 5    11
    int left, right, pivot, t;
```

```
    pivot=arr[low];    // pivot = 95
    left=low;          // left = 5
    right =high;       // right = 11
```

```
    while(left <= right)
    {
```

```
        while((arr[left]<=pivot) && (left<high))
            left++;
```

```
        while(arr[right] > pivot)
            right--;
```

```
        if(left < right) //false
        {
            t=arr[left];
            arr[left] = arr[right] ;
            arr[right] = t;
            left++; right--;
        }
        else left++;
    } // end of while loop
```

```
    arr[low] = arr[right];
    arr[right] =pivot;
```

```
    return right; // right = 9
} // end of function
```

```
public static void QuickSort(int arr[],
    int low, int high)
```

```
{
    // 5    11
    int pivloc;
```

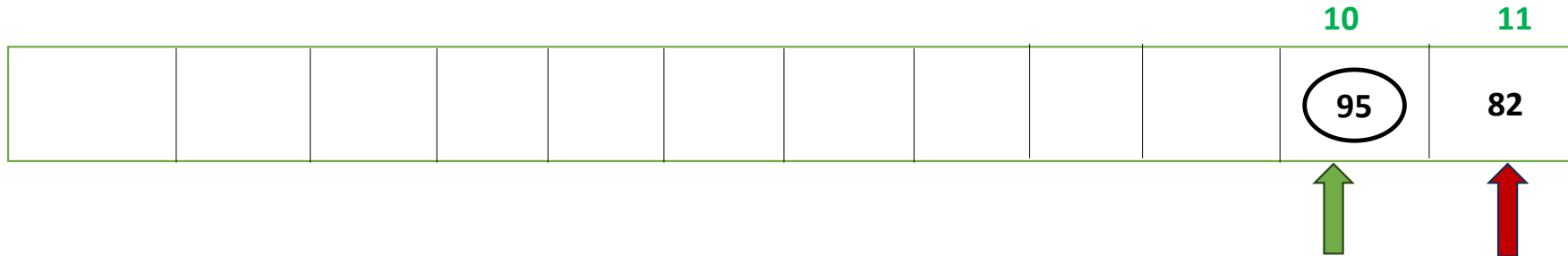
```
    if(low>=high) return;
```

```
    pivloc = partition(arr,low,high); //9
```

```
    QuickSort(arr,low,pivloc-1);
```

```
        // 5    8
    QuickSort(arr,pivloc+1, high);
```

```
        // 10   11
}
```



```
public static int partition(int arr[], int low, int high)
{
    int left, right, pivot, t;

    pivot=arr[low];    // pivot = 95
    left=low;          // left = 10
    right =high;       // right = 11

    while(left <= right)
    {
        while((arr[left]<=pivot) && (left<high))
            left++;

        while(arr[right] > pivot)
            right--;
    }
}
```

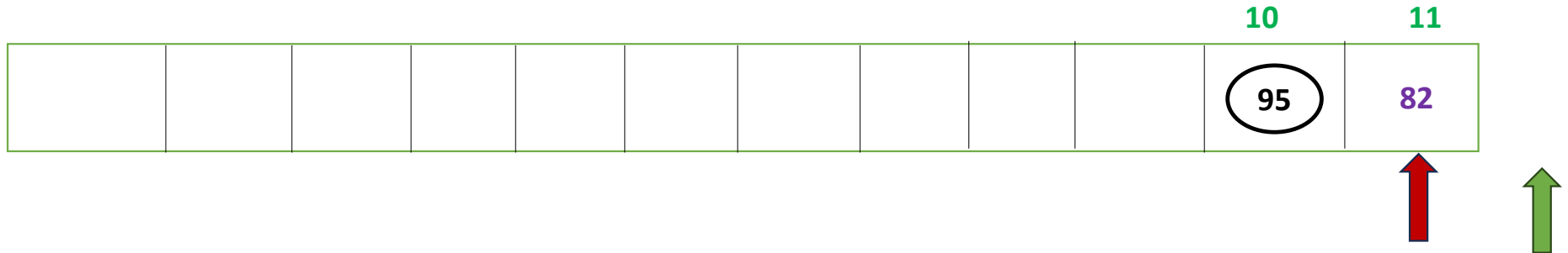


```
public static int partition(int arr[], int low, int high)
{
    int left, right, pivot, t;
```

```
    pivot=arr[low];    // pivot = 95
    left=low;          // left = 10
    right =high;       // right = 11
```

```
    while(left <= right)
    {
        while((arr[left]<=pivot) && (left<high))
            left++;
```

```
        while(arr[right] > pivot)
            right--;
```



```
public static int partition(int arr[], int low, int high)
{
    int left, right, pivot, t;
```

```
    pivot=arr[low];    // pivot = 95
    left=low;          // left = 10
    right =high;       // right = 11
```

```
    while(left <= right)
    {
```

```
        while((arr[left]<=pivot) && (left<high))
            left++;
```

```
        while(arr[right] > pivot)
            right--;
```

```
        if(left < right) //false
```

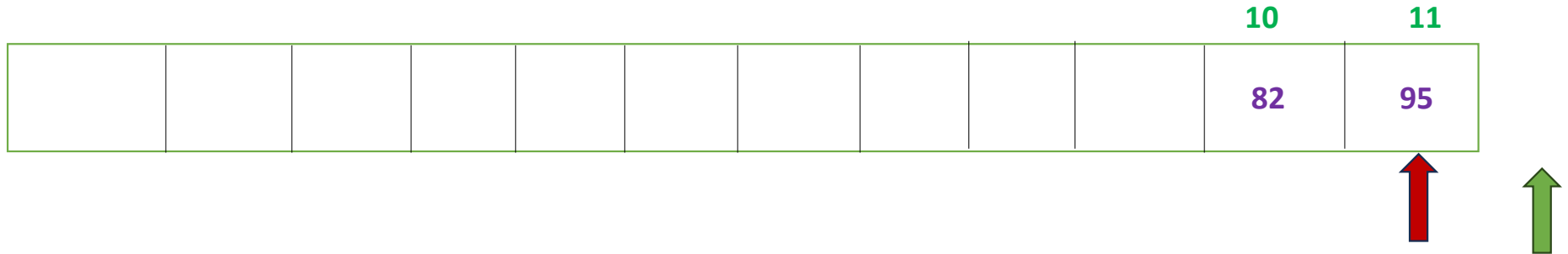
```
        {
            t=arr[left];
            arr[left] = arr[right];
            arr[right] = t;
            left++; right--;
        }
```

```
        else left++;
```

```
    } // end of while loop
```

```
    arr[low] = arr[right];
    arr[right] =pivot;
```

```
    return right;    // right =
9
} // end of function
```



```

public static int partition(int arr[], int low, int high)
{
    int left, right, pivot, t;

    pivot=arr[low];    // pivot = 95
    left=low;          // left = 10
    right =high;       // right = 11

    while(left <= right)
    {
        while((arr[left]<=pivot) && (left<high))
            left++;

        while(arr[right] > pivot)
            right--;
    }
}

```

```

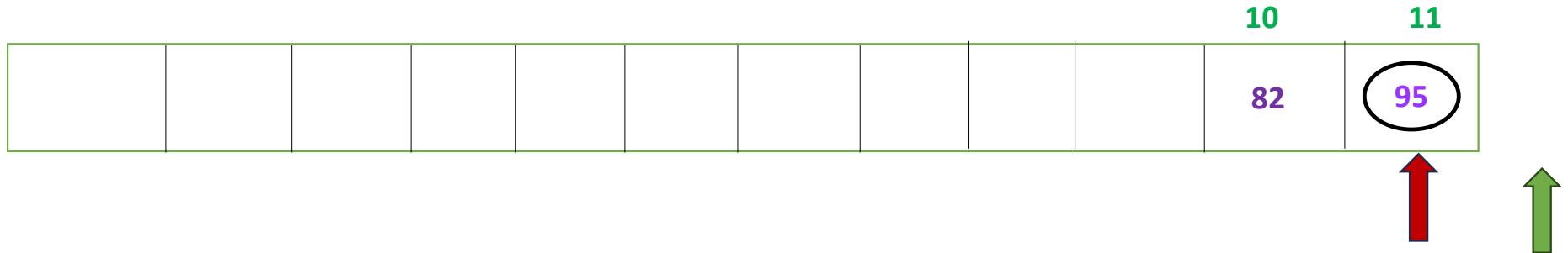
    if(left < right) //false
    {
        t=arr[left];
        arr[left] = arr[right] ;
        arr[right] = t;
        left++; right--;
    }
    else left++;

} // end of while loop

arr[low] = arr[right];
arr[right] =pivot;

return right;    // right =
11
} // end of function

```



```

public static int partition(int arr[], int low, int high)
{
    int left, right, pivot, t;

    pivot=arr[low];    // pivot = 95
    left=low;          // left = 10
    right =high;       // right = 11

    while(left <= right)
    {
        while((arr[left]<=pivot) && (left<high))
            left++;

        while(arr[right] > pivot)
            right--;

        if(left < right) //false
        {
            t=arr[left];
            arr[left] = arr[right];
            arr[right] = t;
            left++; right--;
        }
        else left++;
    } // end of while loop

    arr[low] = arr[right];
    arr[right] =pivot;

    return right;    // right = 11
} // end of function

```

```

public static void QuickSort(int arr[],
                             int low, int high)
{
    // 10      11
    int pivloc;

    if(low>=high) return;

    pivloc = partition(arr,low,high); //11

    QuickSort(arr,low,pivloc-1);
        // 10      10
    QuickSort(arr,pivloc+1, high);
        // 12      11
}

```



# Performance – Quick Sort

- Worst case Complexity:  $O(n^2)$
- Best case Complexity:  $O(n \log n)$
- Average case Complexity:  $O(n \log n)$
- Worst case space Complexity:  $O(1)$