Please work the problems below on the paper provided to you in a neat, clear and complete manner. Make it easy for me to grade.

- 1. An objects velocity  $\mathbf{v}$  at time t seconds is given by  $\mathbf{v}(t) = \langle 1, 1 \cos t, -\sin t \rangle$ , for t > 0 seconds.
  - (a) Find the position function  $\mathbf{r}(t)$ , given that  $\mathbf{r}(0) = \langle 0, 0, 0 \rangle$ .
  - (b) Find the unit tangent vector  $\hat{\mathbf{T}}$  to  $\mathbf{r}(t)$  at time  $t = \pi/2$ .
  - (c) Find the accelleration function a(t).
- 2.  $\mathbf{r}(t) = \langle 2t, \frac{4}{3}t^{3/2}, \frac{1}{2}t^2 \rangle$ , for  $t \ge 0$ , is the vector position function of a curve.
  - (a) Find the arc length function s(t), for  $t \ge 0$ .
  - (b) Find the length of the curve over the interval  $0 \le t \le 6$ . Hint: The answer is between 25 and 32.
  - (c) What are the coordinates of the point, six units along the curve from r(0)? Hint: Find t, when s = 6.
  - (d) Find the curvature,  $\kappa$ , at t = 1