

Please work the problems in a neat, clear manner. Show enough detail to allow me to follow your solutions; Make it easy for me to grade.

1. Let $\vec{a} = \langle 1, 1, -2 \rangle$ and $\vec{b} = \langle 9, 2, -6 \rangle$. Find:

(a) $\vec{a} \cdot \vec{b}$

(b) $\vec{a} \times \vec{b}$

(c) $\|\vec{b}\|$

(d) $\hat{\mathbf{b}}$ (a unit vector in the direction of \vec{b}).

(e) The angle (to the nearest degree) between \vec{a} and \vec{b} .

(f) The area of the parallelogram that can be formed by vectors \vec{a} and \vec{b} .

(g) $\text{proj}_{\vec{a}} \vec{b}$

2. Given vectors \vec{a} and \vec{b} such that $\|\vec{a}\| = 3$, $\|\vec{b}\| = 4$ and $\vec{a} \cdot \vec{b} = 6\sqrt{3}$, find $\|(\vec{a} + 2\vec{b}) \times (3\vec{a} - \vec{b})\|$.

3. Find all values of b such that the vectors $\langle -6, b, 2 \rangle$ and $\langle b, b^2, b \rangle$ are orthogonal.

4. Find the parametric and symmetric equations of the line that goes through the point $P(-2, 3, 5)$ and is parallel to the line with vector equation $\vec{r}(t) = \langle 1 - t, 2 + t, -4 - 4t \rangle$.

5. Find an equation ($ax + by + cz = d$) of the plane that contains the point $(-2, 1, 3)$ and is perpendicular to the line through the points $(-2, 1, 3)$ and $(1, 0, -1)$.