lib/basic/fmaps_unittest.ath

```
1 load "fmaps"
3 open FMap
5 (define M1 [[1 --> 'a] [2 --> 'b] [1 --> 'c]])
6 (define M2 [['a --> true] ['b --> false] ['foo --> true]])
7 (eval M2 o M1)
  (define [t1 t2] [(alist->fmap M2) (alist->fmap M1)])
n define capitals :=
    [['paris --> 'france] ['tokyo --> 'japan] ['cairo --> 'egypt]]
12
13
14 define countries :=
15
    [['france --> 'europe] ['algeria --> 'africa] ['japan --> 'asia]]
16
17 (eval countries o capitals)
19 #(falsify composition-is-comm 20)
21 #(falsify composition-is-assoc 20)
22
23 #(falsify (close (((m3 \circ m2) o m1) = m3 \circ (m2 \circ m1))) 20)
25 #(falsify comp2-is-comm 10)
27 #(falsify comp2-is-assoc 80)
29 # (falsify comp2-app-lemma 10)
31 (eval [[1 --> 'a] [2 --> 'b]] <-> [[1 --> 'a] [3 --> 'c]])
33 (eval [[1 --> 'a] [2 --> 'b]] <-> [[1 --> 'a] [2 --> 'foo] [3 --> 'c]])
35 define compatible-theorem-1 := (forall m . m \leftarrow > m)
37 (falsify compatible-theorem-1 20)
38
39 define compatible-theorem-2 := (forall m1 m2 . m1 <-> m2 <==> m2 <-> m1)
40
  (running-time (lambda () (falsify compatible-theorem-2 10)) 0)
41
42
   # with new eval1: 4.22
44 define compatible-theorem-3 := (forall m1 m2 m3 \cdot m1 <-> m2 & m2 <-> m3 ==> m1 <-> m3)
45
46 # (falsify compatible-theorem-3 10)
47
48 (define [s t hyp] [(apply ?tail:(Map 'T1 'T2)
                              ?k:'T1)
50
                       (apply ([?key:'T1 val] ++ ?tail:(Map 'T1 'T2))
51
52
                              ?k:'T1)
53
                       (?key:'T1 =/= ?k:'T1)])/
55
56 (assume hyp
57
    (!chain [s = t [apply-axioms]]))
58
60 define M' := [[1 --> 'a] [2 --> 'bar] [1 --> 'c]]
_{\rm 62} (eval agree-on M M' [1])
63 (eval agree-on M M' [2])
65 define ag-conjecture-1 :=
    (forall S m . agree-on m m S)
67
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68 # Older map identity:
69 #assert* map-identity :=
70 # (m1 = m2 <==> dom m1 = dom m2 & (agree-on m1 m2 dom m1));;
71
72 define agree-characterization :=
     (forall S m1 m2 . (agree-on m1 m2 S) <==> forall x . x in S ==> m1 applied-to x = m2 applied-to x)
73
74
75 # by-induction agree-characterization {
      (S as Set.null) =>
76 #
         pick-any m1 m2
77 #
78 #
           let {dir1 := assume hyp := (agree-on m1 m2 null)
                           pick-any x
79 #
                             (!chain [(x in S) ==> false [Set.null-characterization]
80 #
                                                ==> (m1 applied-to x = m2 applied-to x) [prop-taut]]);
81 #
                dir2 := assume \ hyp := (forall \ x \ . \ x \ in \ null ==> m1 \ applied-to \ x = m2 \ applied-to \ x)
82
                           (!chain-> [true ==> (agree-on m1 m2 S) [agree-on-axioms]])}
83
84 #
              (!equiv dir1 dir2)
85 # | (S as (Set.insert h t)) =>
86 #
         let {dir1 := assume hyp := (agree-on m1 m2 S)
87 # }
88
89 #(falsify agree-characterization 10)
90 #(!induction* agree-characterization)
91
92 (eval (empty-map: (Map Int Int) at 1))
93
94 (eval M applied-to 1)
95 (eval M applied-to 2)
96 (eval M applied-to 97)
   (eval M - 1 applied-to 2)
   (eval M - 1 applied-to 1)
98
   (define M1 [[1 --> 'a] [2 --> 'b] [1 --> 'c]])
100
101
   (define M2 [['a --> true] ['b --> false] ['foo --> true]])
102
103
   (eval M2 o M1)
104
105
   #(falsify composition-is-assoc 10)
106
107
108 define [n] := [?n:N]
109
110 let {m := (alist->fmap [[1 --> 2] [2 --> 3] [3 --> 1]]);
        _ := (print "\nm iterated once: " (eval m ^
111
        _ := (print "\nm iterated twice: " (eval m ^^ 2));
112
        _ := (print "\nm iterated thrice: " (eval m ^^ 3))}
113
     (print "\nAre m and m^3 identical?: " (eval m = m ^{^3} 3))
115
116
   (eval [[1 --> 'a] [2 --> 'b]] <-> [[1 --> 'a] [3 --> 'c]])
117
   (eval [[1 --> 'a] [2 --> 'b]] <-> [[1 --> 'a] [2 --> 'foo] [3 --> 'c]])
118
119
   define compatible-theorem-1 := (forall m . m <-> m)
120
121
   (falsify compatible-theorem-1 20)
122
123
124 define compatible-theorem-2 := (forall m1 m2 . m1 <-> m2 <==> m2 <-> m1)
125
   #(running-time (lambda () (falsify compatible-theorem-2 50)) 0)
126
   # with new eval1: 4.22
127
129 define compatible-theorem-3 := (forall m1 m2 m3 \cdot m1 <-> m2 & m2 <-> m3 ==> m1 <-> m3)
130
131
   #(falsify compatible-theorem-3 10)
132
133 #(define remove-correctness
134 # (forall m x . (m - x) applied-to x = NONE))
135
136 #(holds? remove-correctness)
# (!induction* remove-correctness)
```

```
138
139  #(falsify remove-correctness 100)
140
141  #(define conj
142  # (close (agree-on m1 m2 A) <==> m1 ^ A = m2 ^ A))
143  #? (close (agree-on m1 m2 A) <==> m1 | ^ A = m2 | ^ A))
144
145  #(!induction* conj)
```