## lib/basic/eval.ath

```
1 ## This file defines two normal-form evaluators for
2 ## ground datatype terms. One of them, eval, is computational,
3 ## i.e., a procedure. The other, deval, is a method.
4 ## Both are rather slow, but the deductive version is
5 ## even slower.
7 (load-file "util.ath")
9 (define rule-table (make-symbol-hash-table))
10
11
   (define (equational-rule? p)
12
    (match p
       ((forall (some-list _) (= _ _)) true)
13
14
       (_ false)))
15
   (define (cond-rule? p)
16
17
     (match p
       ((forall (some-list vars) (if _ _)) true)
18
19
       (_ false)))
20
   (define (orient-bc p f)
21
    (match p
22
       ((forall (some-list vars)
23
24
         (iff ant (bind conclusion (= ((val-of f) (some-list args)) right))))
25
              ((= ((val-of f) (some-list args')) right')
                (let ((syms (get-term-syms* args))
27
                      (syms' (get-term-syms* args')))
                  (check ((&& (for-each syms constructor?)
29
                             (|| (negate (null? syms)) (negate (for-each syms' constructor?))))
30
                            (forall* vars (= ant conclusion)))
31
                          ((for-each syms' constructor?)
32
                            (forall* vars (if conclusion ant)))
                         (else ()))))
34
              (_ (forall* vars (if ant conclusion)))))
35
         (_ ())))
36
37
39 (define (get-rule f p)
    (match p
     ((forall (some-list vars) (= ((val-of f) (some-list args)) right))
41
       (let ((left-syms (get-term-syms* args)))
42
43
         (check ((&& (for-each left-syms constructor?)
                      (|| (negate (null? left-syms)) (negate (member? f (get-term-syms right))))) [p])
44
45
                  (else []))))
     ((forall (some-list vars) (if ant (bind conclusion (= ((val-of f) (some-list args)) right))))
46
47
       (let ((left-syms (get-term-syms* args)))
         (check ((for-each left-syms constructor?) [(forall* vars (if ant conclusion))])
48
                 (else []))))
49
     ((forall (some-list vars) (iff ant (= ((val-of f) (some-list args)) right)))
        [(orient-bc p f)])
51
     ((forall (some-list vars) (iff (bind conclusion (= ((val-of f) (some-list args)) right)) cond))
52
        [(orient-bc (forall* vars (iff cond conclusion)) f)])
53
     ((forall (some-list vars) ((val-of f) (some-list args)))
54
       [(forall* vars (= (make-term f args) true))])
55
     ((forall (some-list vars) (not ((val-of f) (some-list args))))
       [(forall* vars (= (make-term f args) false))])
     ((forall (some-list vars) (if ant ((val-of f) (some-list args))))
58
       (get-rule f (forall* vars (if ant (= (make-term f args) true)))))
59
     ((forall (some-list vars) (iff (bind left ((val-of f) (some-list _)))
60
                                      (bind right ((val-of f) (some-list _)))))
61
       (get-rule f (forall* vars (= left right))))
     ((\texttt{forall} \ (\textbf{some-list} \ \texttt{vars}) \ (\texttt{iff} \ \texttt{ant} \ ((\textbf{val-of} \ \texttt{f}) \ (\textbf{some-list} \ \texttt{args})))))\\
63
64
       (join (get-rule f (forall* vars (if ant (= (make-term f args) true))))
              (get-rule f (forall* vars (if (not ant) (= (make-term f args) false)))))))
65
     ((forall (some-list vars) (iff ((val-of f) (some-list args)) conclusion))
66
       (let ((p1 (forall* vars (iff (= (make-term f args) true) conclusion)))
              (p2 (forall* vars (if (not conclusion) (= (make-term f args) false)))))
68
```

```
(join (get-rule f p1) (get-rule f p2))))
      ((forall (some-list vars) (and (some-list props)))
70
           (flatten (map (lambda (p) (get-rule f (forall* vars p))) props)))
      ((and (some-list props)) (flatten (map (lambda (p) (get-rule f p)) props)))
72
     (_ [])))
73
74
75
   (define (get-rules f)
     (let ((wv (lambda (x y) ()))
77
            (all-rules (fold join (map (lambda (p) (check ((assertion? p) (let ((_ (wv "p: " p))
78
79
                                                                                       (res (get-rule f p))
                                                                                       (_ (wv "res: " res)))
80
                                                               (else []))) (ab)) []))
82
            ([equational-rules rest] (filter-and-complement all-rules equational-rule?))
83
            (cond-rules (filter rest cond-rule?)))
84
        [equational-rules cond-rules]))
85
87
   (define (ugen-vars s uvars)
88
     (filter (vars s) (lambda (v) (member? v uvars))))
89
90
   (define (var-condition uvars left right)
91
     92
93
            (cond1 (subset? right-uvars left-uvars))
94
            (uvar? (lambda (v) (member? v uvars)))
95
            (cond2 (negate (uvar? left))))
        (&& cond1 cond2)))
97
   (define (find-matching-rule rules t)
99
100
     (match rules
101
       ([] ())
        ((list-of (bind R (forall (some-list _vars) (= left right))) rest)
102
          (match [(match-terms t left) (var-condition _vars left right)]
103
            ([(some-sub sub) true] [R sub rest])
104
            (_ (find-matching-rule rest t))))
         ((\textbf{list-of} \ (\textbf{bind} \ \texttt{R} \ (\textbf{forall} \ (\textbf{some-list} \ \_\texttt{vars}) \ (\texttt{if} \ \_ \ (\texttt{=} \ \texttt{left} \ \texttt{right})))) \ \texttt{rest}) 
106
          (match [(match-terms t left) (var-condition _vars left right)]
107
            ([(some-sub sub) true] [R sub rest])
108
            (_ (find-matching-rule rest t))))))
109
111
   (define (lookup-rules f)
      (match (look-up-symbol rule-table f)
112
113
        ((some-list L) L)
        (_ (let ((L (get-rules f))
114
                (_ (enter-symbol rule-table f L)))
             L))))
116
117
118
   (define (update-rules f L)
119
      (match L
120
        ([eq-rules cond-rules]
121
122
          (match (look-up-symbol rule-table f)
            ([old-eq-rules old-cond-rules]
123
               (let ((eq-test (lambda (R) (negate (member? R old-eq-rules))))
124
                     (cond-test (lambda (R) (negate (member? R old-cond-rules))))
125
                     (new-eq-rules (join old-eq-rules (filter eq-rules eq-test)))
126
                     (new-cond-rules (join old-cond-rules (filter cond-rules cond-test))))
127
                (enter-symbol rule-table f [new-eq-rules new-cond-rules])))
128
            (_ (enter-symbol rule-table f L))))
130
        (_ ())))
131
132
   (define (built-in-constant? f args)
133
134
      (&& (null? args) (|| (equal? (sort-of f) "Int")
                          (equal? (sort-of f) "Real")
135
136
                           (equal? (sort-of f) "Ide"))))
137
```

138

```
(define (numeric? f)
      (member? f [+ - * /]))
140
141
142
   (define (apply-numeric f args)
     (match [f args]
143
        ([+ [t1 t2]] (plus t1 t2))
144
       ([+ [t]] t)
145
       ([- [t1 t2]] (minus t1 t2))
       ([* [t1 t2]] (times t1 t2))
147
       ([/ [t1 t2]] (div t1 t2))
148
149
       ([- [t]] (- t))))
150
   (define (eval1 t)
151
       (match t
152
153
         (((some-symbol f) (some-list args))
            (check ((constructor? f) (make-term f (map evall args)))
154
                   ((equal? f =) (equal? (eval1 (first args)) (eval1 (second args))))
155
                   ((numeric? f) (apply-numeric f (map evall args)))
                   (else (let ((args' (map evall args))
157
                                (t' (make-term f args'))
158
                                ([eq-rules cond-rules] (lookup-rules f))
159
160
                                (error-msg (join "Error: No matching rule found for the term\n" (val->string t))))
                            (try-rules t' (join eq-rules cond-rules)
                                     (lambda () (check ((built-in-constant? f args) t)
162
163
                                                         (else (halt)))))))))
         ((not arg) (negate (eval1 arg)))
164
         ((and (some-list args)) (fold (lambda (b1 b2) (&& b1 b2)) (map eval1 args) true))
165
         ((or (some-list args)) (fold (lambda (b1 b2) (|| b1 b2)) (map eval1 args) false))
166
         ((if arg1 arg2) (|| (negate (eval1 arg1)) (eval1 arg2)))
167
         ((some-var _) t))
168
     (try-rules s rules K)
169
170
                             (match (find-matching-rule rules s)
                               ([(forall (some-list _) (= _ right)) sub rest] (try (evall (sub right))
171
                                                                                       (try-rules s rest K)))
172
                               ([(forall (some-list _) (if p (= _ right))) sub rest]
173
                                 (try (let (([res sub'] (eval-cond p sub)))
174
                                         (check (res (evall (sub' (sub right))))
                                                (else (try-rules s rest K))))
176
                                       (try-rules s rest K)))
177
178
                               (_ (K)))
    (loop conditions sub type)
179
       (match conditions
180
181
         ([] (match type
                ('conjunction [true sub])
182
183
                (_ [false sub])))
         ((list-of cond more) (let (([res sub'] (eval-cond cond sub))
184
                                      (sub" (compose-subs sub' sub)))
                                  (match [type res]
186
187
                                     (['conjunction true] (loop more sub' type))
                                     (['disjunction false] (loop more sub' type))
188
                                    (['conjunction false] [false sub'])
189
                                     (['disjunction true] [true sub''])))))
    (eval-cond cond sub)
191
192
      (match cond
        ((= left right) (let ((left' (evall (sub left)))
193
                                (right' (evall (sub right))))
194
195
                            (match (match-terms left' right')
                              ((some-sub sub') [true (compose-subs sub' sub)])
196
                              (_ [false sub]))))
197
         (((some-symbol R) (some-list terms)) [(eval1 (sub cond)) sub])
198
199
         ((not p) (match (eval-cond p sub)
                    ([b sub'] [(negate b) sub'])))
200
         ((and (some-list args)) (loop args sub
                                                        'conjunction))
201
         ((or (some-list args)) (loop args sub
                                                       'disjunction))
202
         ((if arg1 arg2) (eval-cond (or (not arg1) arg2) sub))))
203
205
206
   (define (eval2 t)
     (let ((t' (eval1 t)))
207
       (match t
208
```

```
((some-term _) (rhs (= t t')))
         (_ t'))))
210
211
212 (define (decimal n)
    (match n
213
       (zero 0)
214
       ((succ k) (plus (decimal k) 1))))
215
217 (define (make-unary k)
    (check ((equal? k 0) zero)
218
             (else (succ (make-unary (minus k 1))))))
219
220
221 (define (eval t)
    (try (eval2 t)
222
223
           (println (join "Unable to reduce the term:\n" (val->string t) "\nto a normal form."))))
224
225
226 (define (eval t)
    (try (eval2 t)
227
          (println (join "Unable to reduce the term:\n" (val->string t) "\nto a normal form."))))
228
229
230
231 (set-precedence eval 100)
```