

Bayes' Theorem: Basics

- Total probability Theorem:

$$p(B) = \sum_i p(B|A_i)p(A_i)$$

- Bayes' Theorem:

p (purple arrow) *test data* (purple arrow) *A?* (purple arrow) *B?* (purple arrow)

$$\boxed{p(H|X)} = \frac{p(X|H)P(H)}{\underbrace{p(X)}_{\text{เท่าต้นเสมอ, ละเว้นได้}}} \propto \boxed{p(X|H)} \boxed{P(H)}$$

posteriori probability likelihood prior probability

What we should choose What we just see What we knew previously

- **X**: a data sample (“evidence”)

Prediction can be done based on Bayes' Theorem:

- **H**: X belongs to class C

พิจารณาว่าขึ้น class อะไร ทำกับค่าไหน

Classification is to derive the maximum posteriori

Naïve Bayes Classifier: Making a Naïve Assumption

- Practical difficulty of Naïve Bayes inference: It requires initial knowledge of many probabilities, which may not be available or involving significant computational cost
- A Naïve Special Case
 - Make an additional assumption to simplify the model, but achieve comparable performance.

attributes are conditionally independent
(i.e., no dependence relation between attributes)

$$p(X|C_i) = \prod_k p(x_k|C_i) = p(x_1|C_i) \cdot p(x_2|C_i) \cdots p(x_n|C_i)$$

- Only need to count the class distribution w.r.t. features

Naïve Bayes Classifier: Categorical vs. Continuous Valued Features

- If feature x_k is categorical, $p(x_k = v_k | C_i)$ is the # of tuples in C_i with $x_k = v_k$, divided by $|C_{i,D}|$ (# of tuples of C_i in D)

$$p(X|C_i) = \prod_k p(x_k|C_i) = p(x_1|C_i) \cdot p(x_2|C_i) \cdots p(x_n|C_i)$$

- If feature x_k is continuous-valued, $p(x_k = v_k | C_i)$ is usually computed based on Gaussian distribution with a mean μ and standard deviation σ

$$p(x_k = v_k | C_i) = N(x_k | \mu_{C_i}, \sigma_{C_i}) = \frac{1}{\sqrt{2\pi}\sigma_{C_i}} e^{-\frac{(x - \mu_{C_i})^2}{2\sigma^2}}$$

Naïve Bayes Classifier: Training Dataset

Class:

C1:buys_computer = 'yes'

C2:buys_computer = 'no'

Data to be classified:

X = (age <=30, Income = medium,

Student = yes, Credit_rating = Fair)

classified ทำหน้าที่ฝึกฝนแบบจำลองเพื่อทำนายค่าของตัวแปรที่ไม่ใช่

$$P(H | X) = ?$$

$$P(H | \bar{X}) = ?$$

training data

$$P(X|H)P(H) \rightarrow \frac{9}{14}$$

สนใจแค่ yes ไม่สนใจ X

X				Y
age	income	student	credit_rating	buys_computer
<=30	high	no	fair	no ✓
<=30	high	no	excellent	no ✓
31...40	high	no	fair	yes ✓
>40	medium	no	fair	yes ✓
>40	low	yes	fair	yes ✓
>40	low	yes	excellent	no ✓
31...40	low	yes	excellent	yes ✓
<=30	medium	no	fair	no ✓
<=30	low	yes	fair	yes ✓
>40	medium	yes	fair	yes ✓
<=30	medium	yes	excellent	yes ✓
31...40	medium	no	excellent	yes ✓
31...40	high	yes	fair	yes ✓
>40	medium	no	excellent	no ✓

yes = 9
No = 5

Training data

Naïve Bayes Classifier: An Example

ทุกเงื่อนไขจะไม่ขัดแย้งกัน

□ $P(C_i): P(\text{buys_computer} = \text{"yes"}) = 9/14 = 0.643$

$P(\text{buys_computer} = \text{"no"}) = 5/14 = 0.357$

□ Compute $P(X | C_i)$ for each class

สนใจแค่คนที่ซื้อ

$P(\text{age} = \text{"<=30"} | \text{buys_computer} = \text{"yes"}) = 2/9 = 0.222$

$P(\text{age} = \text{"<= 30"} | \text{buys_computer} = \text{"no"}) = 3/5 = 0.6$

$P(\text{income} = \text{"medium"} | \text{buys_computer} = \text{"yes"}) = 4/9 = 0.444$

$P(\text{income} = \text{"medium"} | \text{buys_computer} = \text{"no"}) = 2/5 = 0.4$

$P(\text{student} = \text{"yes"} | \text{buys_computer} = \text{"yes"}) = 6/9 = 0.667$

$P(\text{student} = \text{"yes"} | \text{buys_computer} = \text{"no"}) = 1/5 = 0.2$

$P(\text{credit_rating} = \text{"fair"} | \text{buys_computer} = \text{"yes"}) = 6/9 = 0.667$

$P(\text{credit_rating} = \text{"fair"} | \text{buys_computer} = \text{"no"}) = 2/5 = 0.4$

□ $X = (\text{age} \leq 30, \text{income} = \text{medium}, \text{student} = \text{yes}, \text{credit_rating} = \text{fair})$

$P(X | C_i): P(X | \text{buys_computer} = \text{"yes"}) = 0.222 \times 0.444 \times 0.667 \times 0.667 = 0.044$

$P(X | \text{buys_computer} = \text{"no"}) = 0.6 \times 0.4 \times 0.2 \times 0.4 = 0.019$

$P(X | C_i) * P(C_i): P(X | \text{buys_computer} = \text{"yes"}) * P(\text{buys_computer} = \text{"yes"}) = 0.028$

$P(X | \text{buys_computer} = \text{"no"}) * P(\text{buys_computer} = \text{"no"}) = 0.007$

Therefore, X belongs to class ("buys_computer = yes")

age	income	student	credit_rating	buys_computer
<=30	high	no	fair	no
<=30	high	no	excellent	no
31...40	high	no	fair	yes
>40	medium	no	fair	yes
>40	low	yes	fair	yes
>40	low	yes	excellent	no
31...40	low	yes	excellent	yes
<=30	medium	no	fair	no
<=30	low	yes	fair	yes
>40	medium	yes	fair	yes
<=30	medium	yes	excellent	yes
31...40	medium	no	excellent	yes
31...40	high	yes	fair	yes
>40	medium	no	excellent	no

$\hat{X} = \text{age} = 42$, student = yes ?

$$P(\hat{H} | \hat{X}) = ? \quad 42 \text{ yes } 2$$

$$P(H=y | (\text{age} = 42, \text{student} = \text{yes})) = P(\text{age} = 42 | \text{pop}_y) P(\text{student} | \text{pop}_y) P(\text{pop}_y)$$

$\downarrow \quad \times \quad \downarrow \quad \times \quad \downarrow$
 $3/9 \quad \quad 6/9 \quad \quad 9/14$

$$P(H_{\text{bug}} = N | (\text{age} = 41, \text{stu} = \text{yes})) =$$

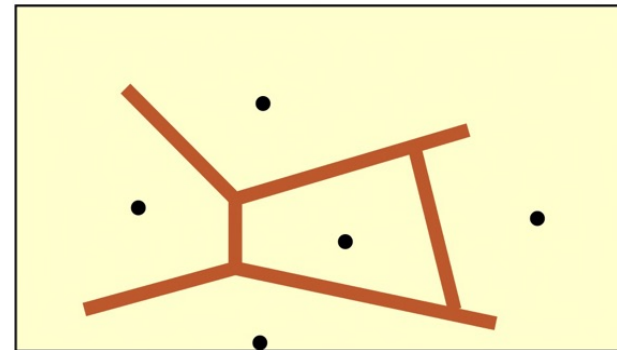
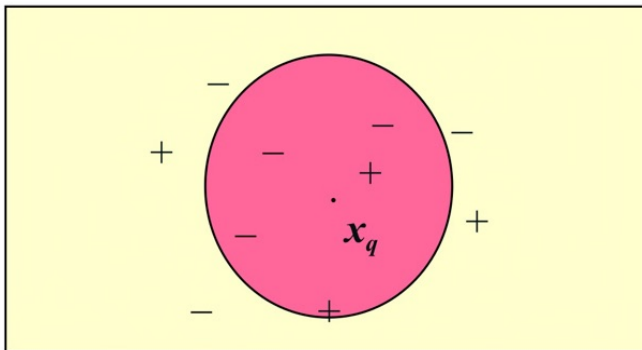
เลซี่ เลิร์นนิง Lazy Learner: Instance-Based Methods

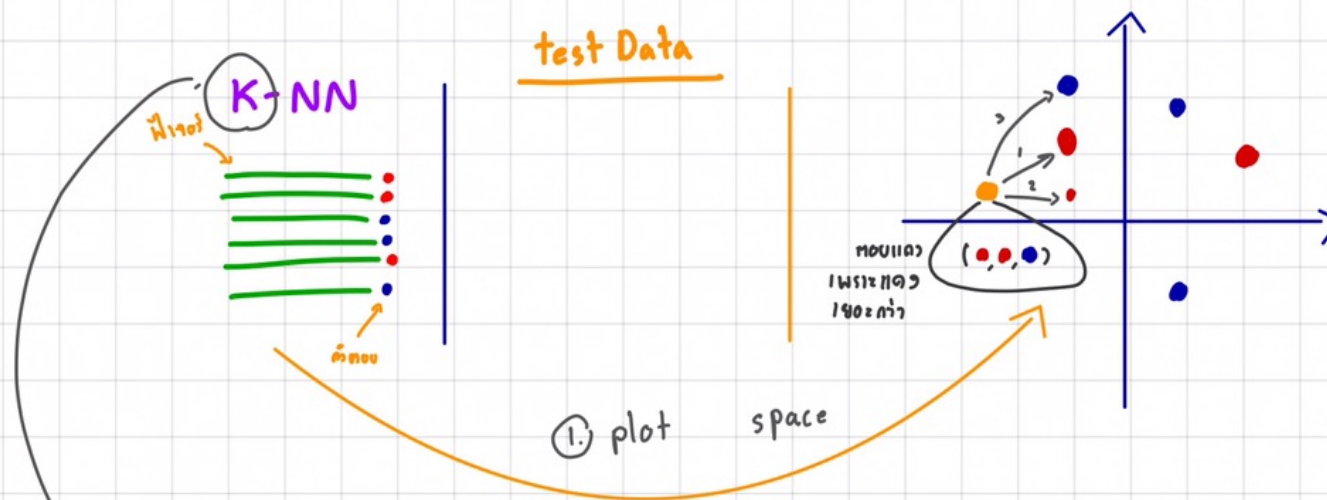
เมื่อได้ข้อมูล train มา เก็บเอาไว้เฉยๆ เมื่อมี data ที่มาจริงๆ | เก็บไว้จนสุดท้ายจริงๆ ค่อยทำ

- ❑ Instance-based learning:
 - ❑ Store training examples and delay the processing (“lazy evaluation”) until a new instance must be classified
- ❑ Typical approaches
 - ❑ k-nearest neighbor approach
 - ❑ Instances represented as points in a Euclidean space.
 - ❑ Locally weighted regression
 - ❑ Constructs local approximation
 - ❑ Case-based reasoning
 - ❑ Uses symbolic representations and knowledge-based inference

The ~~k~~-Nearest Neighbor Algorithm

- ❑ All instances correspond to points in the n-D space
- ❑ The nearest neighbor are defined in terms of Euclidean distance, $\text{dist}(\mathbf{x}_1, \mathbf{x}_2)$
- ❑ Target function could be discrete- or real- valued
- ❑ For discrete-valued, k -NN returns the most common value among the k training examples nearest to \mathbf{x}_q
- ❑ Voronoi diagram: the decision surface induced by 1-NN for a typical set of training examples





ถาม 3 คนได้โหวต
 5 คนได้ หน้าเว็บ
 เชนชิกับค่า k อยกๆ
 ชื่อเพื่อนบ้านที่อยู่ใกล้ก่อน

2. ถามเพื่อนบ้าน

k คน

คนที่ 1 โหวต

คนที่ 2 โหวต

คนที่ 3 หน้าเว็บ