



Digital Image Processing

Image Segmentation:

Point, Line and Edge Detection

By: Dr. Hafeez

Contents

So far we have been considering image processing techniques used to transform images for **human interpretation**

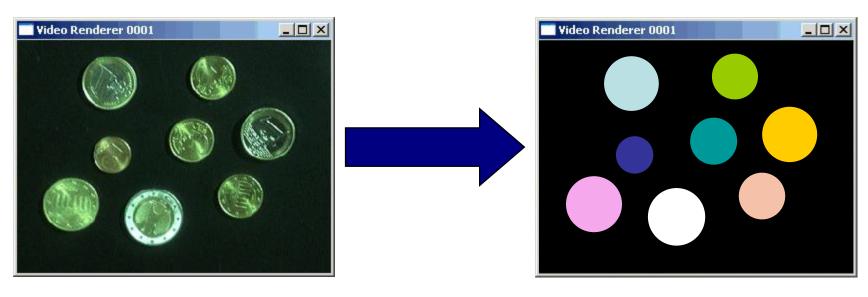
Today we will begin looking at automated image analysis by examining the thorny issue of **image segmentation**:

- The segmentation problem
- Finding points, lines and edges

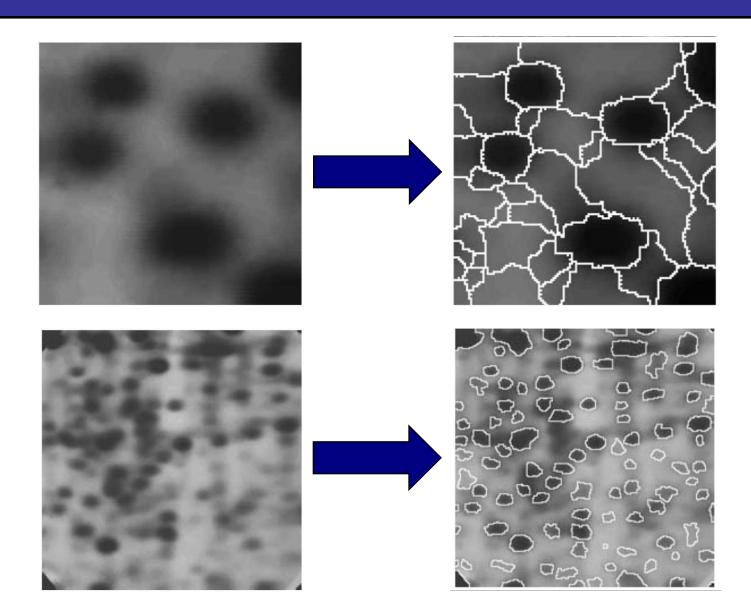
The Segmentation Problem

Segmentation attempts to partition the pixels of an image into groups that strongly correlate with the objects in an image

Typically the first step in any automated computer vision application



Segmentation Examples





Detection Of Discontinuities

There are three basic types of grey level discontinuities that we tend to look for in digital images:

- Points
- Lines
- Edges

We typically find discontinuities using masks and correlation

Point Detection

Point detection can be achieved simply using the mask below:

Output 1 if:

$$R = \sum_{i=1}^{9} w_i z_i \qquad |R| \ge T$$

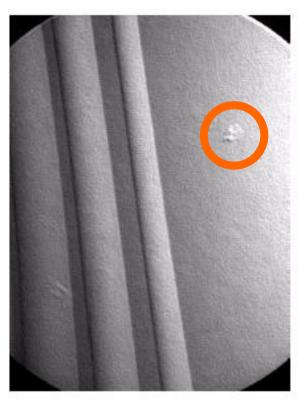
Else output 0.

-1	-1	-1	
-1	8 🛧	-1	R is called Response of
-1	-1	-1	the filter.

Points are detected at those pixels in the subsequent filtered image that are above a set threshold



Point Detection (cont...)



X-ray image of a turbine blade



Result of point detection



Result of thresholding



Line Detection

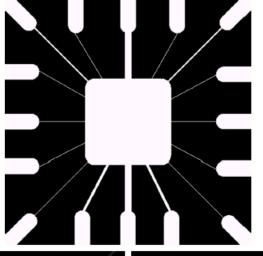
The next level of complexity is to try to detect lines

The masks below will extract lines that are one pixel thick and running in a particular direction

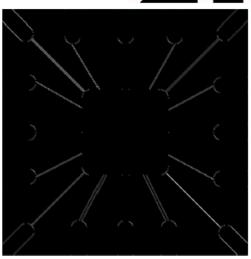
-1	-1 orizon	-1	2	-1 +45°	-1	-1	2 Vertica	-1	-1	-1 -45°	2
2	2	2	-1	2	-1	-1	2	-1	-1	2	-1
-1	-1	-1	-1	-1	2	-1	2	-1	2	-1	-1

Line Detection (cont...)

Binary image of a wire bond mask



After processing with -45° line detector



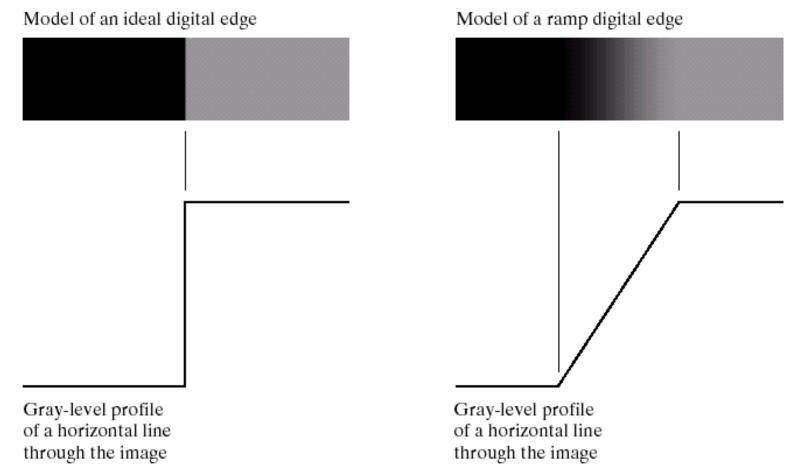


Result of thresholding filtering result



Edge Detection

An edge is a set of **connected pixels that lie on the boundary** between two regions



Edge Point

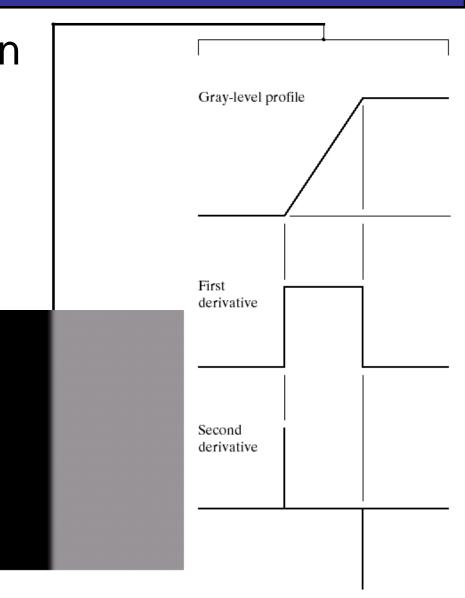
We define a point in an image as being an <u>edge point</u> if its 2-D 1st order derivative is greater than a specified threshold.

A **set** of **such points** that are connected according to a <u>predefined</u> <u>criterion</u> of <u>connectedness</u> is by definition an <u>edge</u>.

Edges & Derivatives

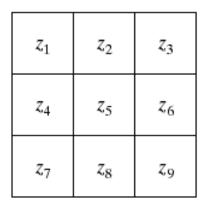
We have already spoken about how derivatives are used to find discontinuities 1st derivative tells us where an edge is 2nd derivative show double

response with thin



Common Edge Detectors

Given a 3*3 region of an image the following edge detection filters can be used



-1	0	0	-1
0	1	1	0

Roberts

-1	-1	-1
0	0	0
1	1	1

-1	0	1
-1	0	1
-1	0	1

Prewitt

-1	-2	-1
0	0	0
1	2	1

-1	0	1
-2	0	2
-1	0	1



Original Image

Horizontal Gradient Component



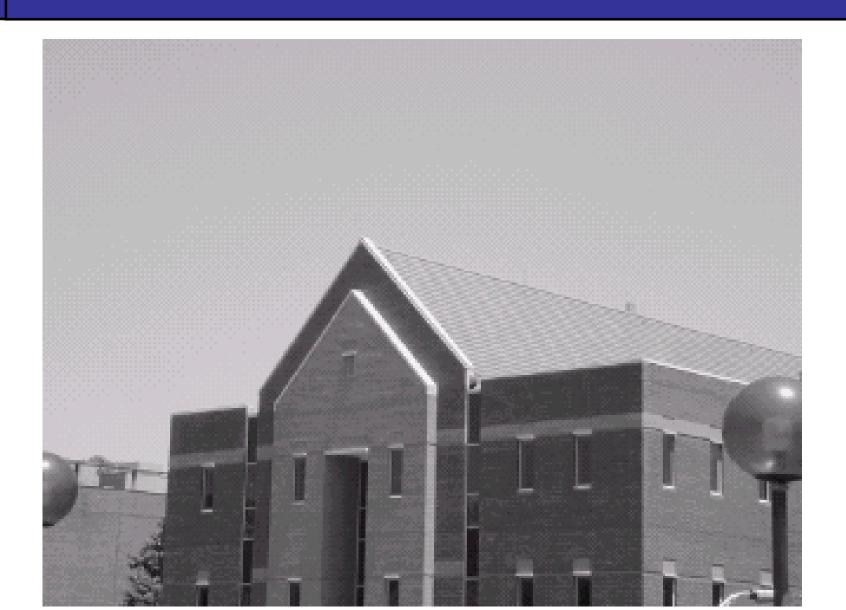




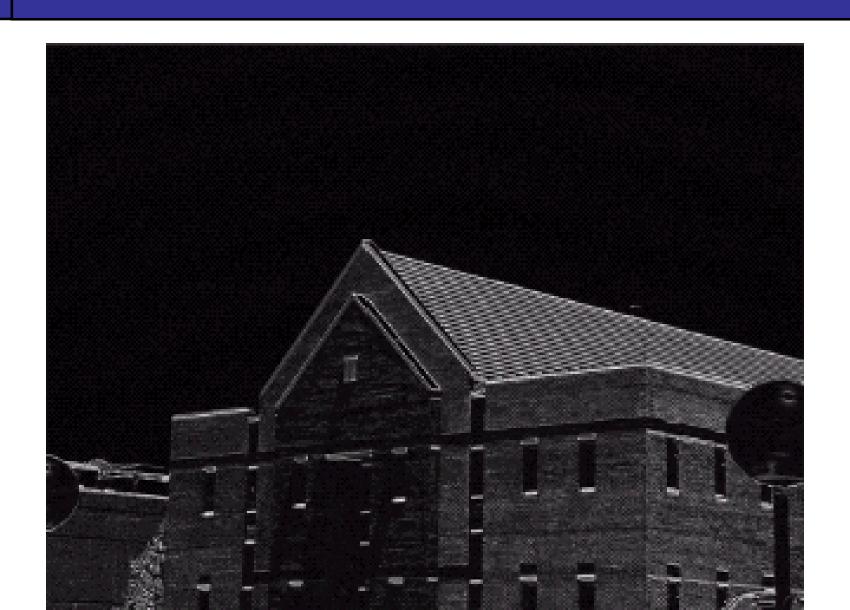


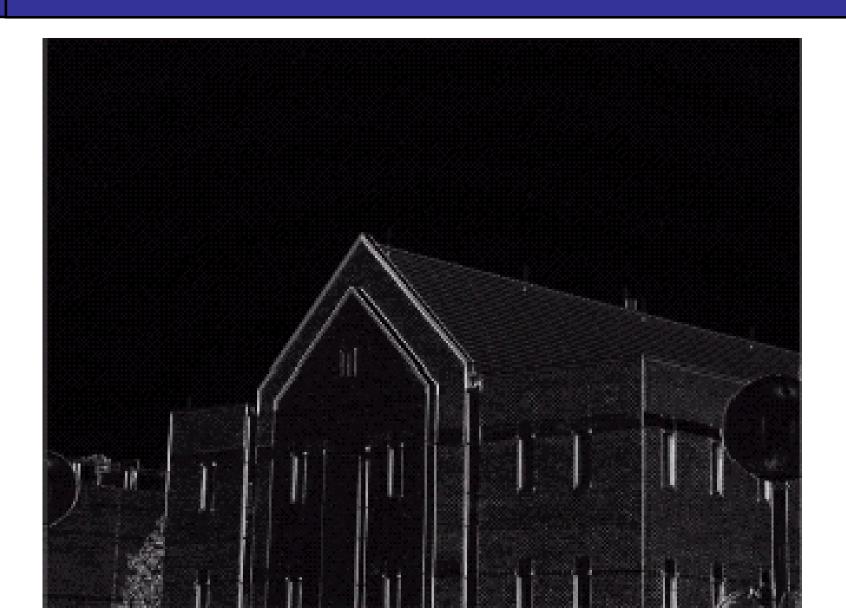


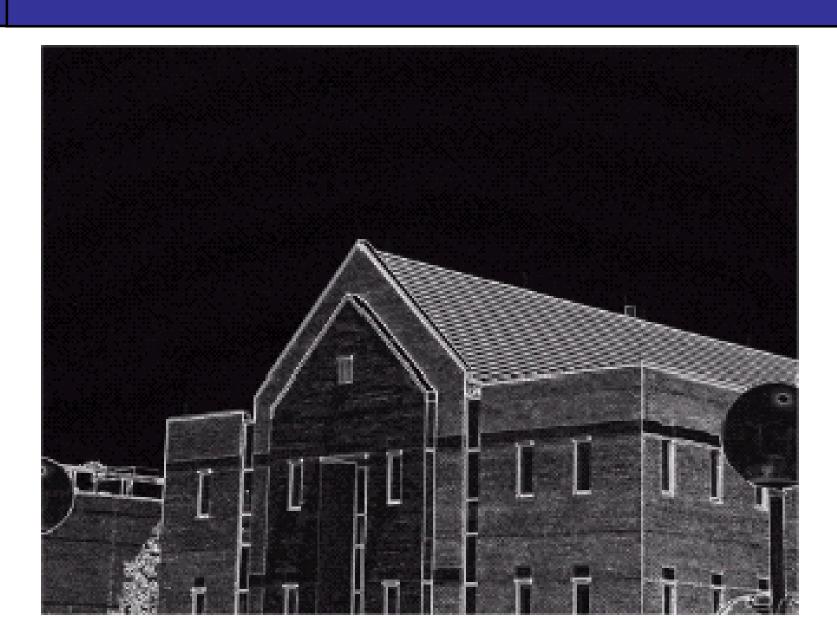
Combined Edge Image









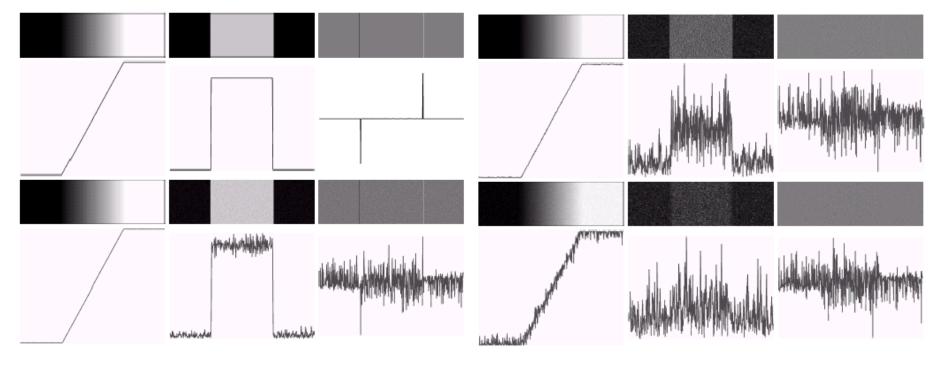




Derivatives & Noise

Derivative based edge detectors are extremely sensitive to noise

We need to keep this in mind





Edge Detection Problems

Often, problems arise in **edge detection** in that there is **too much detail**

For example, the brickwork in the previous example

One way to **overcome this** is to **smooth images** prior to edge detection

Laplacian Edge Detection

We encountered the 2nd-order derivative based Laplacian filter already

0	-1	0	-1	-1	-1
-1	4	-1	-1	8	-1
0	-1	0	-1	-1	-1

The Laplacian is typically not used by itself as it is too sensitive to noise

Usually used for edge detection the Laplacian is combined with a smoothing Gaussian filter



Laplacian Of Gaussian

The Laplacian of Gaussian (or Mexican hat) filter uses the Gaussian for noise removal and the Laplacian for edge detection

$$G(x, y) = e^{-\frac{x^2 + y^2}{2\sigma^2}}$$
 The Gaussian function

 $\nabla^2 G(x, y) = \frac{\partial^2 G(x, y)}{\partial x^2} + \frac{\partial^2 G(x, y)}{\partial y^2}$ The Laplacian of Gaussian function

$$\nabla^2 G(x, y) = \frac{\partial}{\partial x} \left(\frac{-x}{\sigma^2} e^{-\frac{x^2 + y^2}{2\sigma^2}} \right) + \frac{\partial}{\partial y} \left(\frac{-y}{\sigma^2} e^{-\frac{x^2 + y^2}{2\sigma^2}} \right)$$

$$\nabla^2 G(x, y) = \left(\frac{x^2}{\sigma^4} - \frac{1}{\sigma^2}\right) e^{-\frac{x^2 + y^2}{2\sigma^2}} + \left(\frac{y^2}{\sigma^4} - \frac{1}{\sigma^2}\right) e^{-\frac{x^2 + y^2}{2\sigma^2}}$$

$$\nabla^{2}G(x,y) = \left(\frac{x^{2} + y^{2} - 2\sigma^{2}}{\sigma^{4}}\right)e^{-\frac{x^{2} + y^{2}}{2\sigma^{2}}}$$

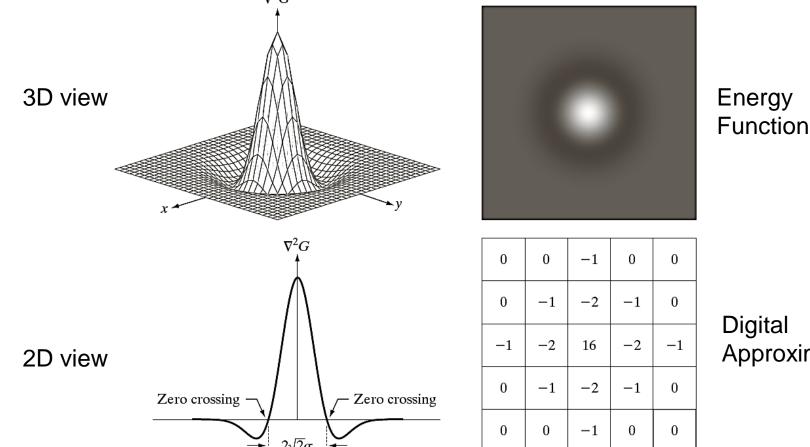
0	0	-1	0	0
0	-1	-2	-1	0
-1	-2	16	-2	-1
0	-1	-2	-1	0
0	0	-1	0	0

Digital approximation of LoG

This expression is called Laplacian of a Gaussion (LoG)

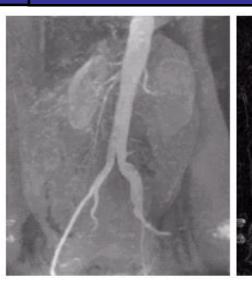
Laplacian Of Gaussian

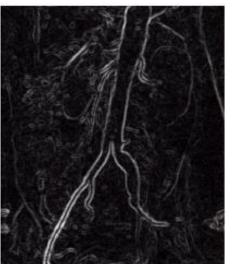
The Laplacian of Gaussian (or Mexican hat) filter's shape in 2D and 3D is given below:

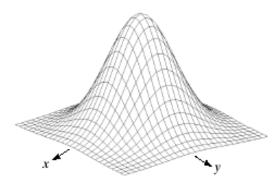


Digital Approximation

Laplacian Of Gaussian Example







-1	-1	-1
-1	8	-1
-1	-1	-1









Thresholding

Thresholding is usually the first step in any segmentation approach

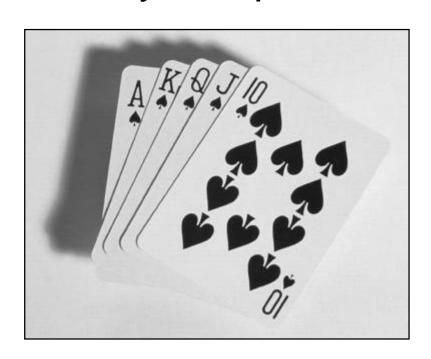
We have talked about simple single value thresholding already

Single value thresholding can be given mathematically as follows:

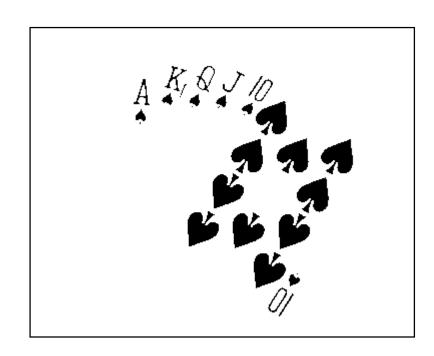
$$g(x, y) = \begin{cases} 1 & \text{if } f(x, y) > T \\ 0 & \text{if } f(x, y) \le T \end{cases}$$

Thresholding Example

Imagine a poker playing robot that needs to visually interpret the cards in its hand



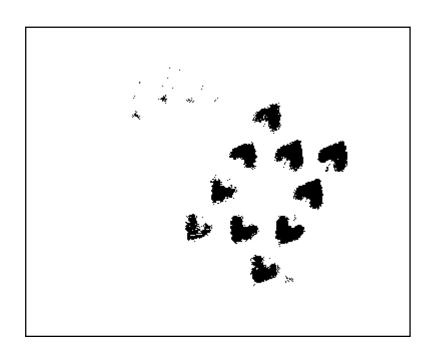
Original Image



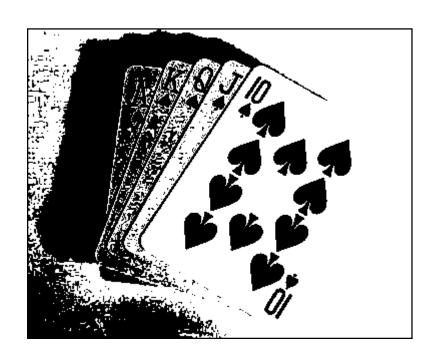
Thresholded Image

But Be Careful

If you get the threshold wrong the results can be disastrous



Threshold Too Low



Threshold Too High

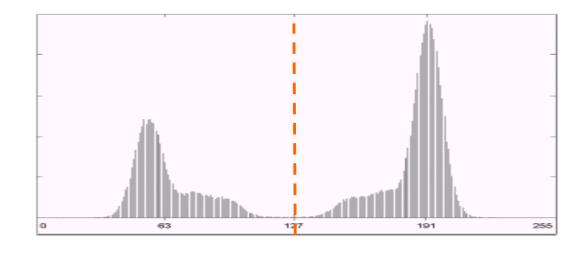
Basic Global Thresholding

Based on the histogram of an image

Partition the image histogram using a single global threshold

The success of this technique very strongly depends on how well the histogram can be

<u>partitioned</u>



Basic Global Thresholding Algorithm

The basic global threshold, T, is calculated as follows:

- 1. Select an initial estimate for T (typically the average grey level in the image)
- 2. Segment the image using T to produce two groups of pixels: G₁ consisting of pixels with grey levels >T and G₂ consisting pixels with grey levels ≤ T
- 3. Compute the average grey levels of pixels in G_1 to give μ_1 and G_2 to give μ_2

Basic Global Thresholding Algorithm

4. Compute a new threshold value:

$$T = \frac{\mu_1 + \mu_2}{2}$$

5. Repeat steps 2-4 until the difference in T in successive iterations is less than a predefined limit ΔT

This algorithm works very well for finding thresholds when the histogram is suitable; however, it is required to be processed on the entire image and not the histogram.

Otsu's Optimum Global Thresholding Method

The Otsu's method operates on image histogram which makes it faster algorithm to find global threshold.

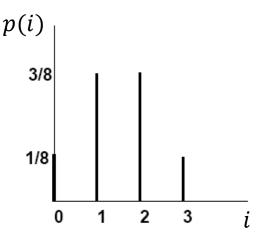
Consider an image with *L* gray levels and its normalized histogram

- p(i) is the normalized frequency of gray level i.

Assuming that we have set the threshold at *T*, the normalized fraction of pixels that will be classified as background and object will be:

background T object
$$q_b(T) = \sum_{i=0}^T p(i) \qquad q_o(T) = \sum_{i=T+1}^{L-1} p(i)$$

$$q_b(T) + q_o(T) = 1$$



Otsu's Method (2)

The mean gray-level value of the background and the object pixels will be:

$$\mu_o(T) = \frac{\sum_{i=T+1}^{L} iP(i)}{\sum_{i=T+1}^{L} P(i)} = \frac{1}{q_o(T)} \sum_{i=T+1}^{L} iP(i)$$

The mean gray-level value over the whole image ("grand" mean) is:

$$\mu = \frac{\sum_{i=1}^{L} iP(i)}{\sum_{i=1}^{L} P(i)} = \sum_{i=1}^{L} iP(i)$$

Otsu's Method (3)

The variance of the background and the object

pixels will be:
$$\sigma_b^2(T) = \frac{\sum_{i=1}^{T} (i - \mu_b)^2 P(i)}{\sum_{i=1}^{T} P(i)} = \frac{1}{q_b(T)} \sum_{i=1}^{T} (i - \mu_b)^2 P(i)$$

$$\sigma_o^2(T) = \frac{\sum_{i=T+1}^{L} (i - \mu_o)^2 P(i)}{\sum_{i=T+1}^{L} P(i)} = \frac{1}{q_o(T)} \sum_{i=T+1}^{L} (i - \mu_o)^2 P(i)$$

The variance of the whole image is:

$$\sigma^2 = \sum_{i=1}^{L} (i - \mu)^2 P(i)$$

Otsu's Method (4)

It can be shown that the variance of the whole image can be written as follows:

$$\sigma^2 = q_b(T)\sigma_b^2(T) + q_o(T)\sigma_o^2(T) + q_b(T)(\mu_b(T) - \mu)^2 + q_o(T)(\mu_o(T) - \mu)^2$$
 Within-class variance between-class variance
$$\sigma^2_W(T)$$

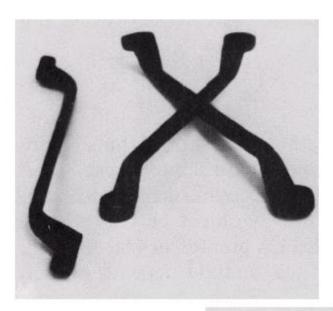
$$\sigma^2_B(T)$$
 should be minimized! should be maximized!

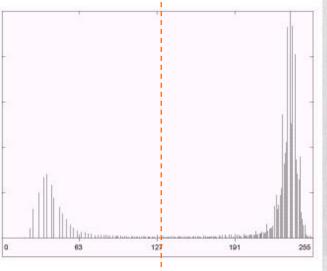
Another way to write between-class variance is:

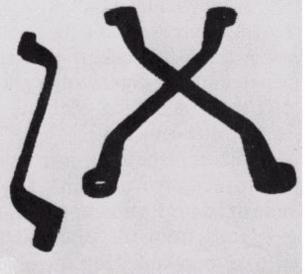
$$\sigma_B^2(T) = q_b(T) q_o(T) [\mu_b(T) - \mu_o(T)]^2$$

The Otsu's optimum T is a threshold that either minimizes the within class variance or maximizes the between-class variance.

Thresholding Example 1



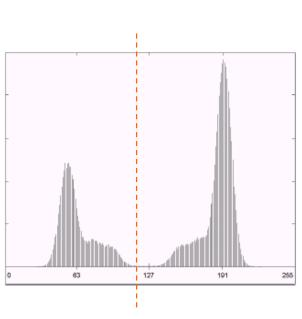






Thresholding Example 2



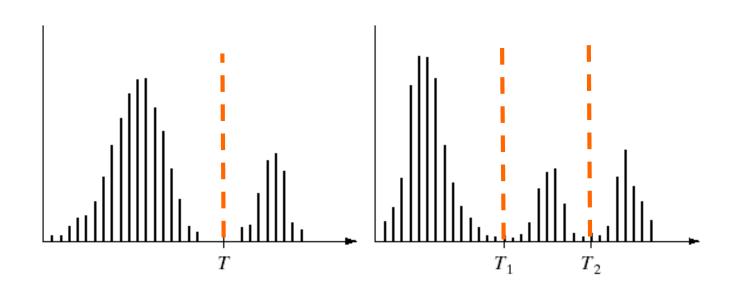




Problems With Single Value Thresholding

Single value thresholding only works for bimodal histograms

Images with other kinds of histograms need more than a single threshold

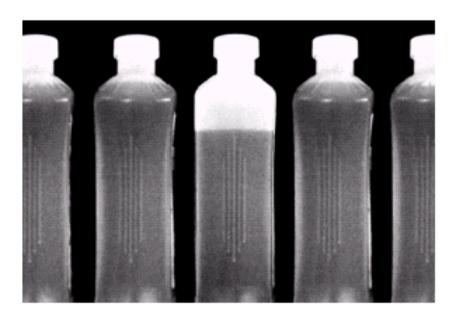




Problems With Single Value Thresholding (cont...)

Let's say we want to isolate the contents of the bottles

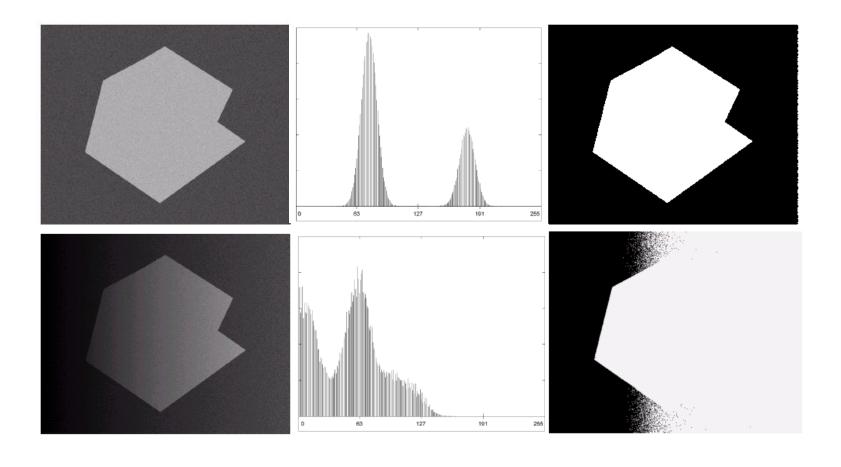
Think about what the histogram for this image would look like



What would happen if we used a single threshold value?



Single Value Thresholding and Illumination



Uneven illumination can really upset a single valued thresholding scheme

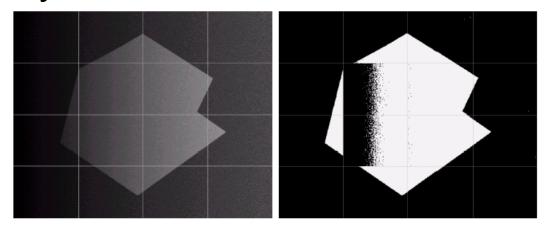
Basic Adaptive Thresholding

An approach to handling situations in which single value thresholding will not work is to divide an image into sub images and threshold these individually

Since the threshold for each pixel depends on its location within an image this technique is said to be *adaptive*

Basic Adaptive Thresholding Example

The image below shows an example of using adaptive thresholding with the image shown previously



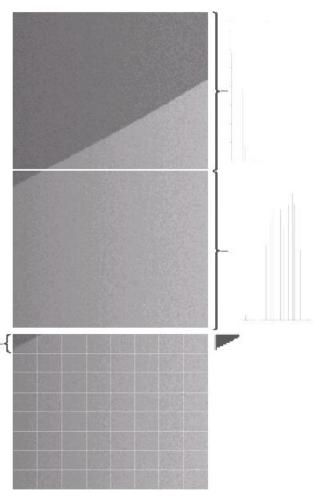
As can be seen success is mixed

But, we can further subdivide the troublesome sub images for more success

Basic Adaptive Thresholding Example (cont...)

These images show the troublesome parts of the previous problem further subdivided

After this sub division successful thresholding can be achieved



Summary

In this lecture we have begun looking at segmentation, and in particular edge detection

Edge detection is massively important as it is in many cases the first step to object recognition

We have also looked at the very basic type of segmentation i.e., Thresholding and what it offers.