

TAREFA BASICA SISTEMAS LINEARES

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$$\textcircled{1} \quad \textcircled{A} \quad \begin{cases} 2x - y = 2 \\ -x + 3y = -3 \end{cases} \quad \begin{array}{r} 2 -1 : 2 \\ -1 \quad 3 : -3 \\ -1 \quad 3 \\ -1 \quad 6 -1 \\ D = 6 + 2 = 8 \\ D = 8 \end{array}$$

$$D_x = 6 - 3 = 3$$

$$x = \frac{3}{3} = 1$$

$$\begin{pmatrix} 2 & 2 \\ -1 & 3 \\ -2 & -6 \end{pmatrix} \quad D_y = -6 + 2 = 4 \quad y = \frac{4}{8} = \frac{1}{2}$$

$$V = \left\{ \left(\frac{3}{3}, \frac{4}{5} \right) \right\}$$

$$\textcircled{B} \quad \begin{cases} 3x - y + z = 1 \\ 2x + 3z = -1 \\ 4x + y - 2z = 7 \end{cases} \quad \begin{array}{r} 3 -1 \quad 1 \\ 2 \quad 0 \quad 3 \\ 4 \quad 1 \quad -2 \\ 0 + 3 + 2 = 9 \\ 0 - 12 + 2 = -10 \end{array} \quad D = -10$$

$$\begin{pmatrix} 1 & -1 & 1 \\ -1 & 0 & 3 \\ 1 & 1 & -2 \end{pmatrix} \quad \begin{pmatrix} 1 & -1 \\ -1 & 0 \\ 1 & 1 \end{pmatrix}$$

$$D_x = -22 - 1 = -23$$

$$\begin{pmatrix} 3 & -1 & 1 \\ 2 & 0 & 1 \\ 1 & 1 & 2 \end{pmatrix}$$

$$\textcircled{1} \quad \textcircled{A} \quad \begin{cases} 2x - y = 2 \\ -x + 3y = -3 \end{cases} \quad \begin{array}{r} \left(\begin{array}{cc|c} 2 & -1 & 2 \\ -1 & 3 & -3 \end{array} \right) \\ \xrightarrow{-1} \left(\begin{array}{cc|c} 2 & -1 & 2 \\ 0 & 4 & -1 \end{array} \right) \\ \xrightarrow{\text{DEI}} 6+2=5 \end{array}$$

$$\begin{pmatrix} 2 & -1 \\ -1 & 3 \end{pmatrix} \quad D = 5$$

$$D_x = 6 - 3 = 3 \quad X = \frac{3}{5}$$

$$\begin{pmatrix} 2 & 2 \\ -1 & -2 \end{pmatrix} \quad D_y = -6 + 2 = 4 \quad Y = \frac{4}{5}$$

$$\begin{pmatrix} 2 & 2 \\ -1 & -2 \end{pmatrix} \quad D_z = 0 + 9 + 4 = 13$$

$$\textcircled{B} \quad \begin{cases} 3x - y + z = 1 \\ 2x + 3z = -1 \\ 4x + y - 2z = 7 \end{cases} \quad \begin{array}{r} \left(\begin{array}{ccc|c} 3 & -1 & 1 & 1 \\ 2 & 0 & 3 & -1 \\ 4 & 1 & -2 & 7 \end{array} \right) \\ \xrightarrow{R1-R3} \left(\begin{array}{ccc|c} 3 & -1 & 1 & 1 \\ 2 & 0 & 3 & -1 \\ 0 & 1 & -3 & 6 \end{array} \right) \\ \xrightarrow{R2-2R1} \left(\begin{array}{ccc|c} 3 & -1 & 1 & 1 \\ 0 & 2 & 1 & -3 \\ 0 & 1 & -3 & 6 \end{array} \right) \\ \xrightarrow{R3-\frac{1}{2}R2} \left(\begin{array}{ccc|c} 3 & -1 & 1 & 1 \\ 0 & 2 & 1 & -3 \\ 0 & 0 & -\frac{5}{2} & 7 \end{array} \right) \\ \xrightarrow{R3 \cdot -\frac{2}{5}} \left(\begin{array}{ccc|c} 3 & -1 & 1 & 1 \\ 0 & 2 & 1 & -3 \\ 0 & 0 & 1 & -\frac{14}{5} \end{array} \right) \\ \xrightarrow{R1-R3} \left(\begin{array}{ccc|c} 3 & -1 & 1 & \frac{19}{5} \\ 0 & 2 & 1 & -3 \\ 0 & 0 & 1 & -\frac{14}{5} \end{array} \right) \\ \xrightarrow{R2-R1} \left(\begin{array}{ccc|c} 3 & -1 & 1 & \frac{19}{5} \\ 0 & 1 & 0 & -\frac{28}{5} \\ 0 & 0 & 1 & -\frac{14}{5} \end{array} \right) \\ \xrightarrow{R1+R2} \left(\begin{array}{ccc|c} 3 & 0 & 1 & -\frac{9}{5} \\ 0 & 1 & 0 & -\frac{28}{5} \\ 0 & 0 & 1 & -\frac{14}{5} \end{array} \right) \end{array} \quad D = 10 - 11 = -1$$

$$0+3-2=1 \quad 0-12+2=-10$$

$$\begin{pmatrix} 1 & -1 & 1 \\ -1 & 0 & 3 \\ 2 & 1 & -2 \end{pmatrix} \quad \begin{array}{l} 1-1 \\ 1-0 \\ 2+1-1 \end{array} \quad D_x = 22-1 \quad \begin{pmatrix} 3 & -1 & 1 \\ 2 & 0 & 1 \\ 4 & 1 & -2 \end{pmatrix} \quad \begin{array}{l} 3-1 \\ 2-0 \\ 4+1 \end{array} \quad D = 0+3-14=-11$$

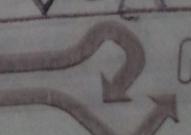
$$\begin{pmatrix} 1 & -1 & 1 \\ -1 & 0 & 3 \\ 2 & 1 & -2 \end{pmatrix} \quad \begin{array}{l} 1-1 \\ 1-0 \\ 2+1-1 \end{array} \quad D_x = 22-1 \quad \begin{pmatrix} 3 & -1 & 1 \\ 2 & 0 & 1 \\ 4 & 1 & -2 \end{pmatrix} \quad \begin{array}{l} 3-1 \\ 2-0 \\ 4+1 \end{array} \quad D = 0+3-14=-11$$

$$0-21+7=-22 \quad D_z = 6+7=13 \quad D_y = 0+14=14 \quad D = 0+14-12=0$$

$$-4+63-4=55$$

$$\begin{pmatrix} 3 & 1 & 1 & 3 & 1 \\ 2 & -1 & 3 & 2 & -1 \\ 4 & 7 & 2 & 4 & 7 \end{pmatrix} \quad \begin{array}{l} 3+1 \\ 2-1 \\ 4+7-2 \end{array} \quad D_x = 72+55 \quad X = -23+7 = -16 \quad Y = 23-1 = 22 \quad Z = -23 = -1$$

$$-6+12+14=32$$

$$Z = \frac{-23}{2} = -11 \quad V = \{1, 1, -1\}$$


DSTQQSS

$$\textcircled{2} \quad \begin{cases} 3x + 4y - z = 7 \\ 4x + 5y + 2z = 12 \\ x - 2y + 3z = 8 \end{cases} \quad \left(\begin{array}{ccc|c} 3 & 4 & -1 & 7 \\ 4 & 5 & 2 & 12 \\ 1 & -2 & 3 & 8 \end{array} \right) \quad \begin{array}{l} -5x - 12 + 4y - z = 7 \\ 4x + 5y + 2z = 12 \\ x - 2y + 3z = 8 \end{array}$$

$$45 + 8 + 8 = 61$$

$$-72 + 148 - 12 = D = 61 - 31 = 30$$

$$\left(\begin{array}{ccc|c} 3 & 1 & -1 & 7 \\ 4 & 12 & 2 & 12 \\ 1 & 8 & 3 & 8 \end{array} \right) \quad \begin{array}{l} 3 \cdot 7 - 48 \\ 4 \cdot 12 - 12 \\ 1 \cdot 8 - 8 \end{array} \quad D_x = 78 - 48 = 30 \quad y = \frac{30}{30} = 1$$

$$108 + 12 - 32 = 78$$

ALTERNATIVA A

$$2 - 33 - 6 = -37$$

$$\textcircled{3} \quad \begin{cases} x + 2y + z = 7 \\ 3x + y - 11z = -2 \\ 2x + 3y - z = 1 \end{cases} \quad \left(\begin{array}{ccc|c} 1 & 2 & 1 & 7 \\ 3 & 1 & -11 & -2 \\ 2 & 3 & -1 & 1 \end{array} \right) \quad \begin{array}{l} 7 - 29 + 28 = -2 \\ 3 - 11 - 1 = -11 \\ 2 - 3 + 1 = 0 \end{array}$$

$$-1 - 44 + 9 = -36$$

$$7 - 33 + 4 = 28 \quad D = -36 + 37 = 1$$

$$\left(\begin{array}{ccc|c} 1 & 2 & 1 & 7 \\ -2 & 1 & -11 & -2 \\ 1 & 3 & -1 & 1 \end{array} \right) \quad \begin{array}{l} 1 \cdot 2 \\ -2 \cdot 1 \\ 1 \cdot 3 \end{array} \quad D_x = -29 + 28 = -1 \quad x = \frac{-1}{-1} = 1$$

$$-1 - 22 - 6 = -29 \quad y = \frac{-1}{-1} = 1$$

$$-4 - 11 - 3 = -18 \quad z = \frac{-1}{-1} = 1$$

$$\left(\begin{array}{ccc|c} 1 & 1 & 1 & 1 \\ 3 & -2 & -11 & -2 \\ 2 & 1 & -1 & 1 \end{array} \right) \quad \begin{array}{l} 1 \cdot 1 \\ 3 \cdot -2 \\ 2 \cdot 1 \end{array} \quad D_y = -18 + 19 = -1 + 1 = 0 \quad x + y + z = 0$$

$$2 - 22 + 3 = -19 \quad -1 + 1 + 0 = 0$$

$$2 - 6 + 6 = 2$$

ALTERNATIVA C

$$\left(\begin{array}{ccc|c} 1 & 2 & 1 & 7 \\ 3 & 1 & -2 & -2 \\ 2 & 3 & 1 & 2 \end{array} \right) \quad \begin{array}{l} 1 \cdot 2 \\ 3 \cdot 1 \\ 2 \cdot 3 \end{array} \quad D_z = 2 - 2 = 0$$

$$(4) \begin{cases} x+2y-3z=29 \\ x+3y-2z=4 \\ x-y-2z=8 \end{cases} \quad \begin{pmatrix} 1 & 2 & -3 \\ 1 & 3 & -2 \\ 1 & -1 & -2 \end{pmatrix} \begin{matrix} 1 & 2 \\ 1 & 3 \\ 1 & -7 \end{matrix}$$

$$\begin{matrix} -9+2-4 \\ -9-2 \\ -11 \end{matrix} \quad \begin{matrix} 1 & 2 \\ 1 & 3 \\ 1 & -7 \end{matrix} \quad \begin{matrix} 1 & 2 \\ 1 & 3 \\ 1 & -7 \end{matrix}$$

$$-6-4+3=-7$$

$$D = -7+11=4$$

$$-72+58-16=-30$$

$$\begin{pmatrix} 29 & 2 & -3 \\ 4 & 3 & -2 \\ 8 & -1 & -2 \end{pmatrix} \begin{matrix} 29 & 2 \\ 4 & 3 \\ 8 & -1 \end{matrix} \quad D_x = -194+30 = -164$$

$$-174-32+72 = -194$$

$$-72-76-58 = -86$$

$$\begin{pmatrix} 1 & 29 & -3 \\ 1 & 4 & -2 \\ 1 & 8 & -2 \end{pmatrix} \begin{matrix} 1 & 29 \\ 1 & 4 \\ 1 & 8 \end{matrix} \quad D_y = -90+86 = -4$$

$$-8-58-24 = -90$$

$$8-4+16 = +99$$

$$\begin{pmatrix} 1 & 2 & 29 \\ 1 & 3 & 4 \\ 1 & -1 & 8 \end{pmatrix} \begin{matrix} 1 & 2 \\ 1 & 3 \\ 1 & -1 \end{matrix} \quad D_z = 3-99 = -96$$

$$24+8-29 = 3$$

$$x = \frac{164}{164} = 1 \quad x+6y+2z=1$$

$$47+1-24=1$$

$$y = +4 = -1$$

$$+4$$

$$z = \frac{-96}{-96} = -24$$

$$\textcircled{5} \quad \begin{cases} 2x + y = 5 \\ 2y + x = 3 \\ 3x + 2y + z = 7 \end{cases}$$

$$\begin{pmatrix} 2 & 1 & 0 \\ 0 & 2 & 1 \\ 3 & 3 & 1 \end{pmatrix} \begin{matrix} 0+4=4 \\ 6-2=3 \\ 3-3=0 \end{matrix}$$

$$0+10+0=10$$

$$4+3+0=7$$

$$\begin{pmatrix} 5 & 1 & 0 \\ 1 & 2 & 1 \\ 1 & 2 & 1 \end{pmatrix} \begin{matrix} 18+0=18 \\ 3-2=1 \\ 7-3=4 \end{matrix}$$

$$10+7+0=17$$

$$0+14+0=14$$

$$\begin{pmatrix} 2 & 5 & 0 \\ 0 & 3 & 1 \\ 1 & 7 & 1 \end{pmatrix} \begin{matrix} 2-5= -3 \\ 0-3= -3 \\ 3-7= -4 \end{matrix}$$

$$6+15+0=21$$

$$30+12+0=42$$

$$\begin{pmatrix} 1 & 1 & 5 \\ 0 & 2 & 3 \\ 3 & 2 & 7 \end{pmatrix} \begin{matrix} 2-1=1 \\ 0-2=-2 \\ 3-7=-4 \end{matrix} \begin{matrix} 5-4=1 \\ 1-2=-1 \\ 7-3=4 \end{matrix}$$

$$28+9+0=37$$

$$V = \left\{ \begin{pmatrix} 4 & 7 & 5 \\ 3 & 3 & 3 \end{pmatrix} \right\} \text{ ALTERNATIVA D}$$

$$\textcircled{6} \quad \begin{bmatrix} 1 & 0 & 0 \\ 2 & 1 & 0 \\ -1 & 2 & 2 \end{bmatrix} \cdot \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 3 \\ 2 \\ -1 \end{bmatrix} \quad D \begin{pmatrix} 1x & 0y & 0z \\ 2x & 1y & 0z \\ -1x & 2y & 2z \end{pmatrix} : 3$$

$$D = \begin{pmatrix} 1 & 0 & 0 \\ 2 & 1 & 0 \\ -1 & 2 & 2 \end{pmatrix}$$

ALTERNATIVA E, pois $Z=0$

$$D \geq 1, 1, 2 = 2$$

$$0+0+0$$

$$D \begin{pmatrix} 3 & 0 & 0 \end{pmatrix} \begin{pmatrix} 3 \\ 0 \\ 0 \end{pmatrix}$$

$$\begin{array}{c|cc} 7 & 1 & 0 \\ -1 & 2 & 2 \end{array} \begin{array}{c|cc} 3 & 1 & D_x = 6 \\ 1 & 2 & \bar{2} \end{array} \quad X = 6 = 3$$

$$6 + 0 + 0 = 6$$

$$0+0+0=0$$

$$\begin{array}{c|cc} 1 & 3 & 0 \\ -1 & 7 & 2 \end{array} \begin{array}{c|cc} 1 & 3 \\ -1 & 7 & \bar{2} \end{array} \quad D_y = 14 - 12 = 2 \quad Y = 2 = 7$$

$$14 + 0 + 0 = 14$$

$$-3 + 14 + 0 = 11$$

$$\begin{array}{c|cc} 1 & 0 & 3 \\ -1 & 2 & 1 \end{array} \begin{array}{c|cc} 1 & 0 \\ -1 & 2 & \bar{1} \end{array} \quad D_z = 11 - 11 = 0 \quad Z = 0 = 0$$

$$-1 + 0 + 12 = 11$$

TAREFA BÁSICA PARTE 2: ESCALONAMENTO

$$\textcircled{1} \quad \left\{ \begin{array}{l} 2x - y - 3z = -5 \\ x + 3y - z = 17 \\ x - 5z = 3 \end{array} \right. \quad \left(\begin{array}{ccc|c} 2 & -1 & -3 & -5 \\ 1 & 3 & -1 & 17 \\ 1 & 0 & -5 & 3 \end{array} \right) \quad \left(\begin{array}{ccc|c} 2 & -1 & -3 & -5 \\ 1 & 3 & -1 & 17 \\ 1 & 0 & -5 & 3 \end{array} \right) \quad \left(\begin{array}{ccc|c} 2 & -1 & -3 & -5 \\ 1 & 3 & -1 & 17 \\ 1 & 0 & -5 & 3 \end{array} \right)$$

$$-9 - 0 + 5 = -4$$

$$-30 + 760 = -29$$

$$D = -2964 = -25$$

$$-26 + 0 + 55 = 28$$

$$D_x \left(\begin{array}{ccc|c} -5 & -1 & -3 & -5 \\ 11 & 3 & -1 & 17 \\ 3 & 0 & -5 & 3 \end{array} \right) \quad D_x = 78 - 18 = 60 \quad x: 60 = -2$$

$$-25$$

$$78 + 3 - 0 = 78$$

$$-13 - 6 + 25 = -4$$

$$D_y \left(\begin{array}{ccc|c} 2 & -5 & -3 & 2 \\ 1 & 17 & -1 & 1 \\ 1 & 3 & -5 & 3 \end{array} \right) \quad D_y = -194 + 14 = -180 \quad y: -180 = 4$$

$$4 = 5 + x + 25$$

$$-170 + 5 - 9 = -114$$

$$-15 + 0 - 3 = -18$$

$$V = \{-2, 4, -1\}$$

$$D_z \left(\begin{array}{ccc|c} 2 & -1 & -5 & 2 \\ 1 & 3 & 11 & 1 \\ 1 & 0 & 3 & 0 \end{array} \right) \quad D_z = 7 + 18 = 25 \quad z: 25 = -1$$

$$-25$$

$$18 - 17 + 0 = 1$$

$$\textcircled{2} \quad \left\{ \begin{array}{l} x = 2y \\ 2y = 32 \\ x + y + z = 11 \end{array} \right. \quad \left| \begin{array}{c|cc|c} & 1 & -2 & 0 \\ & 0 & 2 & -3 \\ & 1 & 1 & 1 \end{array} \right. \quad \begin{array}{l} 0 - 3 + 0 = -3 \\ 1 - 2 + 0 = -1 \\ 0 + 2 - 3 = -1 \end{array} \quad \begin{array}{l} 1 \times 02 \\ 1 \times 02 \\ 1 \times 1 \end{array} \quad \begin{array}{l} 02 \\ 02 \\ 11 \end{array} \quad \begin{array}{l} 0 = 8 + 3 = 11 \\ 11 \end{array}$$

$$0 + 0 + 0 = 0 \quad 2 + 6 + 0 = 8$$

$$Dz \left| \begin{array}{c|cc|c} 1 & -2 & 0 \\ 0 & 2 & 0 \\ 1 & 1 & 1 \end{array} \right. \quad \begin{array}{l} 1 - 2 \\ 02 \\ 11 \end{array} \quad Dz = 22 \quad Z = 22 : 2 \quad \begin{array}{l} 1 \\ 11 \end{array} \quad 22 + 0 = 22$$

$$2y = 32$$

$$x = 2y$$

$$x + 2y + 3z$$

$$2y = 3,2$$

$$x = 2,3$$

$$6 + (2,3) + (3,2)$$

$$y = 6 - 3$$

$$x = 6$$

$$6 + 6 = 6$$

$$\frac{2}{2}$$

$$18$$

ALTERNATIVA (B)

$$0 - 12 + 6 = -6$$

$$\textcircled{3} \quad \left\{ \begin{array}{l} x + y + z = 0 \\ 2x - y - 2z = 1 \\ 6y + 3z = -12 \end{array} \right. \quad \left| \begin{array}{c|cc|c} & 1 & 1 & 1 \\ & 2 & -1 & -2 \\ & 0 & 6 & 3 \end{array} \right. \quad \begin{array}{l} 111 \\ 2 -1 -2 \\ 063 \end{array} \quad \begin{array}{l} 11 \\ 2 -1 \\ 06 \end{array} \quad \begin{array}{l} 1 \\ 1 \\ 15 \end{array} \quad \begin{array}{l} 0 - 12 + 6 = -6 \\ 0 + 6 + 24 = 30 \\ -3 + 0 + 12 \end{array}$$

$$Dz \left| \begin{array}{c|cc|c} 1 & 1 & 0 \\ 2 & -1 & 1 \\ 0 & 6 & -12 \end{array} \right. \quad \begin{array}{l} 11 \\ 2 -1 \\ 06 \end{array} \quad Dz = 12 + 18 = 30 \quad Z = 30 : 2 \quad \begin{array}{l} 1 \\ 1 \\ 15 \end{array} \quad 12 + 0 + 0 = 12 \quad \text{ALTERNATIVA D}$$