

UNIT II: Regular Expressions, Finite Automata, Grammars & Chomsky Hierarchy

Complete Study Guide with Sudhakar Atchala YouTube Resources

1. Regular Expressions (RE)

Definition and Basics

Regular expressions are symbolic notations used to define search patterns in strings and represent languages accepted by Finite Automata. They are the most concise method to describe regular languages[1].

Formal Definition: A regular expression over an alphabet Σ is defined recursively:

- \emptyset (empty set) is a regular expression
- ϵ (empty string) is a regular expression
- For every $a \in \Sigma$, a is a regular expression
- If r and s are regular expressions, then:
 - $(r + s)$ [Union]
 - $(r \cdot s)$ [Concatenation]
 - (r^*) [Kleene closure]
 - (r^+) [Positive closure]are also regular expressions[1]

Operations on Regular Expressions

- **Union ($r + s$):** Combines two expressions; accepts strings from either expression
- **Concatenation (rs):** Combines two expressions in sequence
- **Kleene Closure (r^*):** Zero or more repetitions of the expression
- **Positive Closure (r^+):** One or more repetitions ($r^+ = rr^*$)
- **Complement (\bar{r}):** Accepts all strings not in the language of r

Reference: Sudhakar Atchala - Algebraic Laws of Regular Expression

- Video Link: <https://www.youtube.com/watch?v=FFxr18CXyeM>
 - Duration: 10:59
 - Topics Covered: Identity rules, algebraic properties of RE
-

2. Identity Rules (Algebraic Laws of Regular Expressions)

Identity rules are fundamental algebraic properties that help simplify and manipulate regular expressions[2].

Law	Expression	Meaning
Idempotence	$r + r = r$	Union of same expression
Associativity	$(r + s) + t = r + (s + t)$	Grouping of unions
Commutativity	$r + s = s + r$	Order of union
Identity (Union)	$r + \emptyset = r$	Union with empty set
Identity (Concatenation)	$r \cdot \varepsilon = \varepsilon \cdot r = r$	Concatenation with empty string
Annihilation	$r \cdot \emptyset = \emptyset \cdot r = \emptyset$	Concatenation with empty set
Closure	$r^{**} = r^*$	Idempotence of Kleene star
Distributivity	$r(s + t) = rs + rt$	Over union

Table 1: Algebraic Laws and Identity Rules for Regular Expressions

Importance: These rules help in:

- Simplifying complex regular expressions
- Proving equivalence between different expressions
- Converting between different representations

3. Equivalence of Two Regular Expressions

Two regular expressions r and s are equivalent if they represent the same language, i.e., $L(r) = L(s)$ [1][2].

Methods to Prove Equivalence

1. **Using Identity Rules:** Apply algebraic laws to transform one expression into another
2. **Converting to Finite Automata:** Both expressions should accept the same language
3. **Constructing Equivalent DFAs:** Create DFAs for both expressions and check if they are equivalent
4. **Direct Comparison:** Compare the accepted strings directly

Example

- Expression 1: $(a + b)^* = a + b + aa + ab + ba + bb + \dots$
- Expression 2: $a^*(ba^*)^* = \varepsilon + a + b + aa + ab + ba + bb + \dots$

Both expressions accept the same language, hence they are equivalent[2].

4. Manipulations of Regular Expressions

Regular expression manipulations involve transforming expressions while maintaining language equivalence[2].

Common Manipulation Techniques

- **Factoring:** Extract common parts; $ab + ac = a(b + c)$
- **Expansion:** $r(s + t) = rs + rt$
- **Substitution:** Replace sub-expressions with equivalent ones
- **Reversal:** Reversing all strings in the language
- **Homomorphism:** Mapping symbols according to a substitution function

Practical Applications

- Pattern matching in text
 - Compiler design (lexical analysis)
 - String searching in text editors
 - Data validation
-

5. Finite Automata and Regular Expressions

Finite Automata (FA) are computing machines that can be in one of a finite number of states. Regular expressions and Finite Automata are equivalent in their expressive power[1].

Types of Finite Automata

Deterministic Finite Automata (DFA):

- For each state and input symbol, there is exactly one transition
- Formally: $\delta: Q \times \Sigma \rightarrow Q$
- Easier to implement but may require more states

Non-deterministic Finite Automata (NFA):

- For each state and input symbol, there can be zero, one, or multiple transitions
- Formally: $\delta: Q \times \Sigma \rightarrow P(Q)$ (power set of Q)
- More concise but harder to implement

ϵ -NFA (NFA with epsilon transitions):

- Allows transitions without consuming any input symbol
- Simplifies expression to automata conversion

Formal Definition of FA

A Finite Automaton is a 5-tuple $M = (Q, \Sigma, \delta, q_0, F)$ where:

- Q is a finite set of states
- Σ is a finite alphabet (input symbols)
- δ is the transition function
- $q_0 \in Q$ is the initial state

- $F \subseteq Q$ is the set of final/accepting states[1]
-

6. Inter-conversion: Regular Expression to Finite Automata

Method 1: Direct Method (Thompson's Construction)

The direct method constructs an ϵ -NFA from a regular expression by decomposing the expression recursively.

Steps:

1. For each atom in the regular expression, create a simple automaton
2. Combine automata according to the operations (+, , *)
3. The resulting automaton accepts the same language as the expression[1]

Video Resource: Sudhakar Atchala - Converting Regular Expression to Finite Automata using Direct Method

- Video Link: <https://www.youtube.com/watch?v=1gxDtBOhKJE>
- Duration: 38:21
- Topics: Thompson's construction, detailed examples with complex expressions

Method 2: Subset Construction Method

This method converts a regular expression to NFA first, then NFA to DFA.

Steps:

1. Construct ϵ -NFA from regular expression using Thompson's method
2. Convert ϵ -NFA to NFA by eliminating ϵ -transitions
3. Convert NFA to DFA using subset construction algorithm
4. Minimize the DFA if needed[1]

Video Resource: Sudhakar Atchala - Converting Regular Expression to Finite Automata using Subset Method

- Video Link: <https://www.youtube.com/watch?v=nlbmngDw8Dg>
 - Duration: 12:48
 - Topics: Epsilon-NFA elimination, subset construction, practical examples
-

7. Inter-conversion: Finite Automata to Regular Expression

Arden's Theorem (Arden's Method)

Arden's Theorem is used to convert a Finite Automaton (DFA or NFA) into a regular expression.

Theorem Statement:

If R is a regular expression and does not contain ϵ , then the equation $X = RX + S$ has a unique

solution: $X = R^*S[2]$

Algorithm Steps:

1. Create state equations for each state based on incoming transitions
2. Add ϵ to the initial state equation
3. For each non-final state, substitute its equation into the equations of states that have incoming edges from it
4. Repeatedly eliminate states until only the final state equation remains
5. The resulting expression is the regular expression for the FA[2]

Video Resources:

1. Sudhakar Atchala - Conversion of Finite Automata to Regular Expression using Arden's Method
 - Video Link: <https://www.youtube.com/watch?v=OsTphhnaXio>
 - Duration: 10:52
 - Topics: Arden's theorem concept, step-by-step solution
2. Sudhakar Atchala - Conversion of Finite Automata(DFA) to Regular Expression using Arden's Theorem
 - Video Link: <https://www.youtube.com/watch?v=S5uGHkhM5Dc>
 - Duration: 19:35
 - Topics: Complete construction with multiple examples
3. Sudhakar Atchala - Arden's Theorem - Complete Explanation with Examples
 - Extended discussion of applications and complex cases

8. Equivalence between FA and RE

Theorem: A language is regular if and only if it is accepted by some Finite Automaton (DFA or NFA).

This equivalence means:

- Every regular expression can be converted to a Finite Automaton
- Every Finite Automaton can be converted to a regular expression
- Therefore, FA and RE have the same expressive power[2]

Proof Sketch:

- Given a regular expression, construct an ϵ -NFA using Thompson's construction (RE \rightarrow FA)
- Given a finite automaton, use Arden's theorem to construct a regular expression (FA \rightarrow RE)
- Both conversions preserve the language accepted/represented

Video Resource: Sudhakar Atchala - Equivalence of DFA and Regular Expression

- Video Link: <https://www.youtube.com/watch?v=Lf7lS4XFXKw>
 - Duration: Related to Arden's method
 - Topics: Proving equivalence through conversion
-

9. Pumping Lemma for Regular Sets

Statement of Pumping Lemma

If L is a regular language, then there exists a constant n (pumping length) such that for every string $w \in L$ with $|w| \geq n$, we can write $w = xyz$ such that:

1. $y \neq \varepsilon$ (y is non-empty)
2. $|xy| \leq n$
3. For all $k \geq 0$, $xy^kz \in L$ (the middle part can be repeated any number of times)[2]

Intuition

The pumping lemma states that sufficiently long strings in a regular language must have a repeating segment that can be "pumped" (repeated arbitrarily many times) while remaining in the language.

Proof Technique (Contradiction Method)

1. Assume language L is regular
2. Choose an appropriate string $w \in L$ with $|w| \geq n$
3. Express $w = xyz$ according to pumping lemma conditions
4. Show that $xy^kz \notin L$ for some k (usually $k = 0$ or $k = 2$)
5. This contradicts the assumption that L is regular
6. Therefore, L is not a regular language[2]

Classic Examples of Non-regular Languages

- $L = \{a^n b^n : n \geq 0\}$ (equal number of a's and b's)
- $L = \{a^n : n \text{ is prime}\}$ (prime powers of a)
- $L = \{0^{n^2}\}$ (perfect squares)

Video Resources:

1. Sudhakar Atchala - Pumping Lemma for Regular Languages with an example
 - Video Link: https://www.youtube.com/watch?v=BKIUSHYpq_Y
 - Duration: 8:58
 - Topics: Basic concept, example proof
 2. Sudhakar Atchala - Prove that $L = \{a^p \mid p \text{ is prime}\}$ is not regular
 - Video Link: https://www.youtube.com/watch?v=aw6Akr6_e5k
 - Duration: 8:56
 - Topics: Pumping lemma application
 3. Sudhakar Atchala - Show that $L = \{0^{n^2}\}$ is not regular
 - Video Link: <https://www.youtube.com/watch?v=ccdsYbgQUHY>
 - Duration: 8:09
 - Topics: Perfect square example, detailed proof
-

10. Closure Properties of Regular Sets

Closure properties describe which operations, when applied to regular languages, produce regular languages[2].

Fundamental Closure Properties

Property	Operation	Result
Union	$L1 \cup L2$	Regular (closed)
Concatenation	$L1 \cdot L2$	Regular (closed)
Kleene Closure	L^*	Regular (closed)
Complement	$L^c = \Sigma^* - L$	Regular (closed)
Intersection	$L1 \cap L2$	Regular (closed)
Difference	$L1 - L2$	Regular (closed)
Reversal	L^R	Regular (closed)
Homomorphism	$h(L)$	Regular (closed)
Inverse Homomorphism	$h^{-1}(L)$	Regular (closed)

Table 2: Closure Properties of Regular Languages

Proof Techniques

For Union: If $M1$ and $M2$ are DFAs accepting $L1$ and $L2$, construct product automaton with accepting states being any combination of accepting states from both machines.

For Concatenation: Create composite automaton where accepting states of first automaton have ϵ -transitions to start state of second automaton.

For Complement: In a DFA, swap accepting and non-accepting states.

For Intersection: Use De Morgan's law: $L1 \cap L2 = (L1^c \cup L2^c)^c$

Video Resources:

1. Sudhakar Atchala - Closure properties of Regular Languages
 - o Video Link: <https://www.youtube.com/watch?v=UoFrOT7T7ns>
 - o Duration: 9:47
 - o Topics: Union, concatenation, closure, complement, intersection, reversal
 2. Sudhakar Atchala - Closure Properties of Regular Languages (with proof)
 - o Video Link: <https://www.youtube.com/watch?v=WwliYxbcamw>
 - o Duration: 13:47
 - o Topics: Detailed proofs for each property
-

11. Grammars and Context-Free Grammars

Definition of Grammar

A grammar G is a 4-tuple (N, Σ, P, S) where:

- N is a finite set of non-terminals (variables)
- Σ is a finite set of terminals (alphabet)
- P is a finite set of production rules
- $S \in N$ is the start symbol[3]

Production Rule Format: $A \rightarrow \alpha$

- A is a non-terminal (left-hand side)
- α is a string of terminals and non-terminals (right-hand side)

Language Generated by Grammar

$$L(G) = \{w \in \Sigma^* : S \Rightarrow^* w\}$$

The language consists of all strings of terminals that can be derived from the start symbol through repeated application of production rules[3].

Types of Derivations

- **Leftmost Derivation:** Replace leftmost non-terminal at each step
- **Rightmost Derivation:** Replace rightmost non-terminal at each step
- **Sentential Form:** Any intermediate string during derivation containing terminals and/or non-terminals

12. Classification of Grammars: Chomsky Hierarchy

The Chomsky Hierarchy classifies grammars into four types based on the form of production rules[3].

Type 0: Unrestricted Grammars

Production Rule Form: $\alpha \rightarrow \beta$ (no restrictions)

- α can be any string with at least one non-terminal
- β can be any string of terminals and non-terminals

Language: Recursively Enumerable Languages (RE)

Automaton: Turing Machine

Properties:

- Most powerful grammar
- Undecidable language properties
- Capable of describing any computable language

Type 1: Context-Sensitive Grammars (CSG)

Production Rule Form: $\alpha A \beta \rightarrow \alpha \gamma \beta$ (where $|\gamma| \geq 1$)

- Length of right-hand side \geq length of left-hand side (non-contracting)
- A is a single non-terminal with context α and β

Language: Context-Sensitive Languages (CSL)

Automaton: Linear Bounded Automaton (LBA)

Properties:

- The symbol A can be replaced only in the context of α and β
- All derivations never decrease the string length
- Recognition is decidable

Type 2: Context-Free Grammars (CFG)

Production Rule Form: $A \rightarrow \alpha$ (where A is a single non-terminal)

- A is a non-terminal
- α is any string of terminals and non-terminals

Language: Context-Free Languages (CFL)

Automaton: Pushdown Automaton (PDA)

Properties:

- Most commonly used in programming languages
- Used for syntax analysis in compilers
- Recognition is decidable and efficient ($O(n^3)$)
- Ambiguity possible

Type 3: Regular Grammars (RG)

Production Rule Forms:

- Right Linear: $A \rightarrow aB$ or $A \rightarrow a$ or $A \rightarrow \epsilon$
- Left Linear: $A \rightarrow Ba$ or $A \rightarrow a$ or $A \rightarrow \epsilon$
- Where $a \in \Sigma, A, B \in N$

Language: Regular Languages

Automaton: Finite Automaton (DFA/NFA)

Properties:

- Most restrictive grammar
- Equivalent to regular expressions
- Used for lexical analysis
- No ambiguity if deterministic

Hierarchy Diagram

Type	Grammar	Language	Automaton	Complexity
Type 0	Unrestricted	Recursively Enumerable	Turing Machine	Undecidable
Type 1	Context-Sensitive	CSL	Linear Bounded Automaton	NP-complete
Type 2	Context-Free	CFL	Pushdown Automaton	Polynomial
Type 3	Regular	Regular	Finite Automaton	Linear

Table 3: Chomsky Hierarchy Classification

Video Resources:

1. Sudhakar Atchala - Types of Grammar | Chomsky Hierarchy | Regular | Context Free | Context Sensitive
 - Video Link: <https://www.youtube.com/watch?v=srPezAciSVw>
 - Duration: 15:37
 - Topics: Complete Chomsky hierarchy explanation with all four types
2. Sudhakar Atchala - Chomsky Hierarchy - Explained in Detail with examples
 - Video Link: <https://www.youtube.com/watch?v=b4ThUo3epeA>
 - Duration: Comprehensive coverage
 - Topics: Classification, examples, automata comparison
3. Sudhakar Atchala - Types of languages || TOC || FLAT || Theory of Computation
 - Video Link: <https://www.youtube.com/watch?v=b4ThUo3epeA>
 - Topics: Language types and hierarchy visualization

13. Right Linear Regular Grammars (RLG)

Definition

A Right Linear Grammar (RLG) has production rules of the form:

- $A \rightarrow aB$ (terminal followed by non-terminal)
- $A \rightarrow a$ (only terminal)
- $A \rightarrow \epsilon$ (epsilon production)

Where $A, B \in N$, $a \in \Sigma[3]$

Characteristics

- **Linear:** At most one non-terminal on the right side
- **Right:** The non-terminal always appears at the rightmost position
- **Regular:** Generates regular languages exactly
- **Equivalent to RG:** Can be converted bidirectionally with DFA/NFA

Example

Grammar G (RLG):

- $S \rightarrow aS \mid bA \mid \varepsilon$
- $A \rightarrow aA \mid b$

Language: $\{ab(ab)^*\}$: strings with at least one 'b', 'a' only before 'b'}

Properties

- Every RLG generates a regular language
 - Every regular language can be generated by some RLG
 - Recognition is linear time $O(n)$
 - Deterministic when no ambiguity exists
-

14. Left Linear Regular Grammars (LLG)

Definition

A Left Linear Grammar (LLG) has production rules of the form:

- $A \rightarrow Ba$ (non-terminal followed by terminal)
- $A \rightarrow a$ (only terminal)
- $A \rightarrow \varepsilon$ (epsilon production)

Where $A, B \in N$, $a \in \Sigma$ [3]

Characteristics

- **Linear:** At most one non-terminal on the right side
- **Left:** The non-terminal always appears at the leftmost position
- **Regular:** Generates regular languages exactly
- **Mirror of RLG:** LLG for L equals RLG for L^R (reverse)

Example

Grammar G (LLG):

- $S \rightarrow Sa \mid Ab \mid \varepsilon$
- $A \rightarrow Aa \mid b$

Language: Similar to RLG but builds strings from right to left

Relationship between RLG and LLG

- **RLG** generates strings by appending symbols to the right
- **LLG** generates strings by prepending symbols to the left
- A language is RLG iff its reverse is LLG
- Both generate exactly the regular languages[3]

Conversion between RLG and LLG

To convert RLG to equivalent LLG:

1. Take the reverse of all productions
2. Swap the direction of symbol placement

Example Conversion:

- RLG: $S \rightarrow aA, A \rightarrow b$
 - LLG (equivalent): $S \rightarrow Ab, A \rightarrow a$
-

15. Equivalence between Regular Grammars (RG) and Finite Automata (FA)

Theorem

A language is regular if and only if it can be generated by a regular grammar (RG) AND accepted by a Finite Automaton (FA).

Formally: $L(RG) = L(FA)$ for regular languages[3]

Proof of Equivalence

Direction 1: RG \rightarrow FA

Given a right linear grammar $RG = (N, \Sigma, P, S)$:

1. Create states: One for each non-terminal, plus a new accepting state
2. For each production $A \rightarrow aB$, create transition $\delta(A, a) = B$
3. For each production $A \rightarrow a$, create transition $\delta(A, a) = \text{accepting state}$
4. For each production $A \rightarrow \epsilon$, add ϵ -transition from A to accepting state
5. Initial state is S
6. The resulting automaton accepts $L(RG)$ [3]

Direction 2: FA \rightarrow RG

Given a DFA $M = (Q, \Sigma, \delta, q_0, F)$:

1. For each state q and input a , if $\delta(q, a) = p$, add production $q \rightarrow ap$
2. For each final state f , add production $f \rightarrow \epsilon$
3. Start symbol is q_0
4. The resulting grammar generates $L(M)$ [3]

Formal Statement

If G is a right linear grammar, then there exists a DFA M such that $L(G) = L(M)$.
If M is a DFA, then there exists a right linear grammar G such that $L(M) = L(G)$.

16. Inter-conversion: RG to FA

Conversion Algorithm

1. **Create States:** Create a state for each non-terminal in the grammar. Create an additional state (final state) labeled F.
2. **Set Initial State:** The state corresponding to the start symbol S is the initial state.
3. **Create Transitions:**
 - For production $A \rightarrow aB$: Create transition $\delta(A, a) = B$
 - For production $A \rightarrow a$: Create transition $\delta(A, a) = F$
 - For production $A \rightarrow \epsilon$: Add ϵ -transition to F
4. **Define Accepting States:** Set F and any states with ϵ -productions as accepting states.
5. **Optimize:** Remove unreachable states and redundant transitions if needed.

Example Conversion

Given RG:

- $S \rightarrow aA \mid bB$
- $A \rightarrow aS \mid b$
- $B \rightarrow c$

Conversion Steps:

1. States: {S, A, B, F}
2. Initial state: S
3. Transitions:
 - $\delta(S, a) = A$
 - $\delta(S, b) = B$
 - $\delta(A, a) = S$
 - $\delta(A, b) = F$
 - $\delta(B, c) = F$
4. Accepting state: {F}

Resulting FA: DFA with above transitions and states

Video Resource: Sudhakar Atchala - Converting Regular Grammar to Finite Automata

- Video Link: https://www.youtube.com/watch?v=frzs_IWiiqQ
- Duration: Comprehensive coverage
- Topics: Conversion procedure with examples

17. Inter-conversion: FA to RG

Conversion Algorithm

1. **Create Non-terminals:** Create a non-terminal for each state in the FA.
2. **Set Start Symbol:** The non-terminal corresponding to the initial state is the start symbol.
3. **Create Productions:**
 - For each transition $\delta(q_i, a) = q_j$: Create production $Q_i \rightarrow aQ_j$ (Right Linear)

- For each transition $\delta(q_i, a) = q_j$: Create production $Q_j \rightarrow aQ_i$ (Left Linear for reverse)
4. **Add Final Productions:** For each accepting state q_f , add production $Q_f \rightarrow \epsilon$
 5. **Simplify:** Remove unreachable productions if any.

Example Conversion

Given DFA:

- States: $\{q_0, q_1, q_2\}$
- Initial: q_0
- Accepting: $\{q_2\}$
- Transitions:
 - $\delta(q_0, a) = q_1, \delta(q_0, b) = q_0$
 - $\delta(q_1, a) = q_2, \delta(q_1, b) = q_0$
 - $\delta(q_2, a) = q_2, \delta(q_2, b) = q_2$

Resulting RG:

- $S \rightarrow aA \mid bS$
- $A \rightarrow aB \mid bS$
- $B \rightarrow aB \mid bB \mid \epsilon$

Where: $S = Q_0, A = Q_1, B = Q_2$

18. Summary of Key Concepts

Key Relationships

Concept	Representation	Equivalence
Regular Languages	Regular Expressions	Equivalent
Regular Languages	Finite Automata (DFA/NFA)	Equivalent
Regular Languages	Right/Left Linear Grammars	Equivalent
Context-Free Languages	Context-Free Grammars	Equivalent
Context-Free Languages	Pushdown Automata	Equivalent

Table 4: Equivalence Relationships in Formal Language Theory

Decision Procedure Summary

- **To prove a language is regular:** Convert to FA, RE, or RG; or show finite states suffice
- **To prove a language is NOT regular:** Use pumping lemma for contradiction
- **To check equivalence:** Convert to same representation; compare or minimize
- **To convert between representations:** Use specific algorithms (Thompson's, Arden's, conversion procedures)

19. Practice Problems Summary

Regular Expressions & FA Conversion

- Convert $(a + b)^*$ to ϵ -NFA
- Convert $(ab + ba)^*$ to DFA
- Convert given DFA to regular expression using Arden's method

Pumping Lemma Applications

- Prove $L = \{a^n b^n : n \geq 0\}$ is not regular
- Prove $L = \{a^n : n \text{ is prime}\}$ is not regular
- Prove $L = \{0^{n^2} : n \geq 0\}$ is not regular

Grammar Conversions

- Convert RG to DFA
- Convert DFA to RLG
- Classify grammar into Chomsky hierarchy

Closure Properties

- Show union of two regular languages is regular
- Show complement of regular language is regular
- Show intersection of regular languages is regular

20. Important Video Playlist - Sudhakar Atchala

Main Theory of Computation Playlist

Link: https://www.youtube.com/playlist?list=PLXj4XH7LcRfBkMIS_9aebcY78NLFwhE4M

Complete Collection of Relevant Videos:

1. Regular Expressions & Identity Rules

- Video: Algebraic Laws of Regular Expression || Identity Rules
- Link: <https://www.youtube.com/watch?v=FFxr18CXyeM>
- Duration: 10:59

2. RE to FA Conversion

- Direct Method: <https://www.youtube.com/watch?v=1gxDtBOhKJE> (38:21)
- Subset Method: <https://www.youtube.com/watch?v=nlbmimgDw8Dg> (12:48)

3. FA to RE Conversion (Arden's Method)

- Basic: <https://www.youtube.com/watch?v=OsTphhnaXio> (10:52)
- Complete: <https://www.youtube.com/watch?v=S5uGHkhM5Dc> (19:35)

4. Pumping Lemma

- Basic Concept: https://www.youtube.com/watch?v=BKIUSHYpq_Y (8:58)
- Prime Example: https://www.youtube.com/watch?v=aw6Akr6_e5k (8:56)
- Perfect Square: <https://www.youtube.com/watch?v=ccdsYbgQUHY> (8:09)

5. Closure Properties

- Overview: <https://www.youtube.com/watch?v=UoFrOT7T7ns> (9:47)
- With Proofs: <https://www.youtube.com/watch?v=WwliYxbcamw> (13:47)

6. Chomsky Hierarchy & Grammars

- Types of Grammar: <https://www.youtube.com/watch?v=srPezAciSVw> (15:37)
 - Language Classification: <https://www.youtube.com/watch?v=b4ThUo3epeA>
- 7. Regular Grammar to FA**
- Conversion Procedure: https://www.youtube.com/watch?v=frzs_IWiiqQ
-

References

- [1] Sudhakar Atchala. (2022, October 30). Converting Regular Expression to Finite Automata using Direct Method || Theory of computation. YouTube. Retrieved from <https://www.youtube.com/watch?v=1gxDtBOhKJE>
- [2] Sudhakar Atchala. (2022, October 27). Conversion of Finite Automata to Regular Expression using Arden's Method. YouTube. Retrieved from <https://www.youtube.com/watch?v=OsTphhnaXio>
- [3] Sudhakar Atchala. (2022, September 9). Automata Theory - Chomsky Classification of Languages. YouTube. Retrieved from <https://www.youtube.com/watch?v=srPezAciSVw>
- [4] Sudhakar Atchala. (2022, October 31). Pumping Lemma for Regular Languages with an example. YouTube. Retrieved from https://www.youtube.com/watch?v=BKIUSHYpq_Y
- [5] Sudhakar Atchala. (2022, November 15). Closure properties of Regular Languages. YouTube. Retrieved from <https://www.youtube.com/watch?v=UoFrOT7T7ns>
- [6] Sudhakar Atchala. (2022, June 23). Algebraic Laws of Regular Expression || Identity Rules. YouTube. Retrieved from <https://www.youtube.com/watch?v=FFxr18CXyeM>
- [7] Sudhakar Atchala. (2024, September 2). Converting Regular Grammar to Finite Automata || Procedure. YouTube. Retrieved from https://www.youtube.com/watch?v=frzs_IWiiqQ
-

Study Tips:

1. **Watch videos first** to understand concepts visually
 2. **Take notes** on key definitions and theorems
 3. **Work through examples** step-by-step
 4. **Practice conversions** between $RE \leftrightarrow FA \leftrightarrow RG$
 5. **Memorize closure properties** and Chomsky hierarchy
 6. **Practice pumping lemma proofs** with different languages
 7. **Create summary tables** for quick reference
 8. **Review identity rules** regularly for RE manipulation
 9. **Understand the equivalence relationships** between all representations
 10. **Work through past exam questions** from your institution
-

Last Updated: November 2025

Resource Compilation: Based on Sudhakar Atchala YouTube Channel Videos

Suitable for: B.Tech Computer Science students studying Formal Languages and Automata Theory (FLAT) / Theory of Computation (TOC)