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ASSIGNMENT 7

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Download all python codes from

https://github.com/Atlakeerthana/Assignment7/tree/main/Assignment7

and latex-tikz codes from

https://github.com/Atlakeerthana/Assignment7/tree/main/Assignment7

1 Question No 2.25(vector forms)

Find the equation of set of points P such that

$$(\mathbf{PA})^2 + (\mathbf{PB})^2 = 2k^2;$$
 (1.0.1)

$$\mathbf{A} = \begin{pmatrix} 3 \\ 4 \\ 5 \end{pmatrix}; \tag{1.0.2}$$

$$\mathbf{B} = \begin{pmatrix} -1\\3\\-7 \end{pmatrix}; \tag{1.0.3}$$

respectively.

2 SOLUTION

Given,

$$\mathbf{A} = \begin{pmatrix} 3\\4\\5 \end{pmatrix}; \tag{2.0.1}$$

$$\mathbf{B} = \begin{pmatrix} -1\\3\\-7 \end{pmatrix}; \tag{2.0.2}$$

Let

$$\mathbf{P} = \begin{pmatrix} x \\ y \\ z \end{pmatrix}; \tag{2.0.3}$$

so,

$$(\mathbf{PA})^{2} = \left\| \begin{pmatrix} \mathbf{X} \\ \mathbf{Y} \\ \mathbf{Z} \end{pmatrix} - \begin{pmatrix} 3 \\ 4 \\ 5 \end{pmatrix} \right\|^{2}$$

$$= \left\| \begin{pmatrix} \mathbf{X} \\ \mathbf{Y} \\ \mathbf{Z} \end{pmatrix} \right\|^{2} + \left\| \begin{pmatrix} 3 \\ 4 \\ 5 \end{pmatrix} \right\|^{2} - 2 \begin{pmatrix} 3 & 4 & 5 \end{pmatrix} \begin{pmatrix} \mathbf{X} & \mathbf{Y} & \mathbf{Z} \end{pmatrix}$$

$$= \mathbf{X}^{2} + \mathbf{Y}^{2} + \mathbf{Z}^{2} - 6\mathbf{X} - 8\mathbf{Y} - 10\mathbf{Z} + 50$$

$$(2.0.6)$$

and

$$(\mathbf{PB})^{2} = \left\| \begin{pmatrix} \mathbf{X} \\ \mathbf{Y} \\ \mathbf{Z} \end{pmatrix} - \begin{pmatrix} -1 \\ 3 \\ -7 \end{pmatrix} \right\|^{2}$$

$$= \left\| \begin{pmatrix} \mathbf{X} \\ \mathbf{Y} \\ \mathbf{Z} \end{pmatrix} \right\|^{2} + \left\| \begin{pmatrix} -1 \\ 3 \\ -7 \end{pmatrix} \right\|^{2} - 2 \begin{pmatrix} -1 & 3 & -7 \end{pmatrix} \begin{pmatrix} \mathbf{X} & \mathbf{Y} & \mathbf{Z} \end{pmatrix}$$

$$= \mathbf{X}^{2} + \mathbf{Y}^{2} + \mathbf{Z}^{2} + 2\mathbf{X} - 6\mathbf{Y} + 14\mathbf{Z} + 59$$

$$(2.0.8)$$

$$= \mathbf{X}^{2} + \mathbf{Y}^{2} + \mathbf{Z}^{2} + 2\mathbf{X} - 6\mathbf{Y} + 14\mathbf{Z} + 59$$

$$(2.0.9)$$

The given equation is

$$(\mathbf{PA})^2 + (\mathbf{PB})^2 = 2k^2$$
 (2.0.10)

Sub (2.0.7) and (2.0.10) values in (2.0.11)

: the required equation is

$$2X^2 + 2Y^2 + 2Z^2 - 4X - 14Y + 4Z + 109 = 2k^2$$
(2.0.11)