

# F5: BAGS, QUEUES, AND STACKS

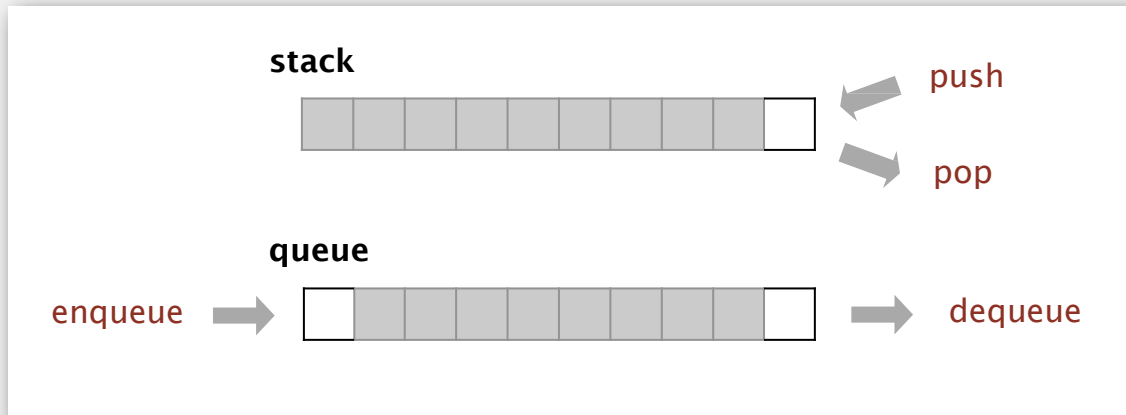


- stacks
- resizing arrays
- generics
- iterators
- applications
- queues

# Stacks and queues

## Fundamental data types.

- Value: collection of objects.
- Operations: **insert**, **remove**, **iterate**, test if empty.
- Intent is clear when we insert.
- Which item do we remove?



**Stack.** Examine the item most recently added. ← LIFO = "last in first out"

**Queue.** Examine the item least recently added. ← FIFO = "first in first out"

## Client, implementation, interface

### Separate interface and implementation.

Ex: stack, queue, bag, priority queue, symbol table, union-find, ....

### Benefits.

- Client can't know details of implementation  $\Rightarrow$  client has many implementation from which to choose.
- Implementation can't know details of client needs  $\Rightarrow$  many clients can re-use the same implementation.
- **Design:** creates modular, reusable libraries.
- **Performance:** use optimized implementation where it matters.

**Client:** program using operations defined in interface.

**Implementation:** actual code implementing operations.

**Interface:** description of data type, basic operations.

- stacks
- resizing arrays
- generics
- iterators
- applications
- queues

# Stack API

Warmup API. Stack of strings data type.

```
public class StackOfStrings
```

```
    StackOfStrings()           create an empty stack
```

```
    void push(String s)       insert a new item onto stack
```

```
    String pop()              remove and return the item  
                             most recently added
```

```
    boolean isEmpty()         is the stack empty?
```

```
    int size()                number of items on the stack
```

push pop



## Stack test client

Read strings from standard input.

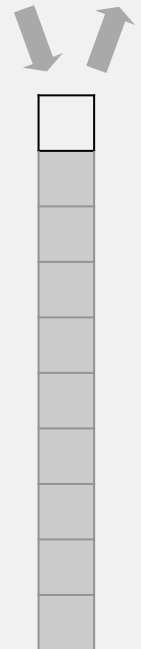
- If string equals "-", pop string from stack and print.
- Otherwise, push string onto stack.

```
public static void main(String[] args)
{
    StackOfStrings stack = new StackOfStrings();
    while (!StdIn.isEmpty())
    {
        String item = StdIn.readString();
        if (item.equals("-")) StdOut.print(stack.pop());
        else                  stack.push(item);
    }
}
```

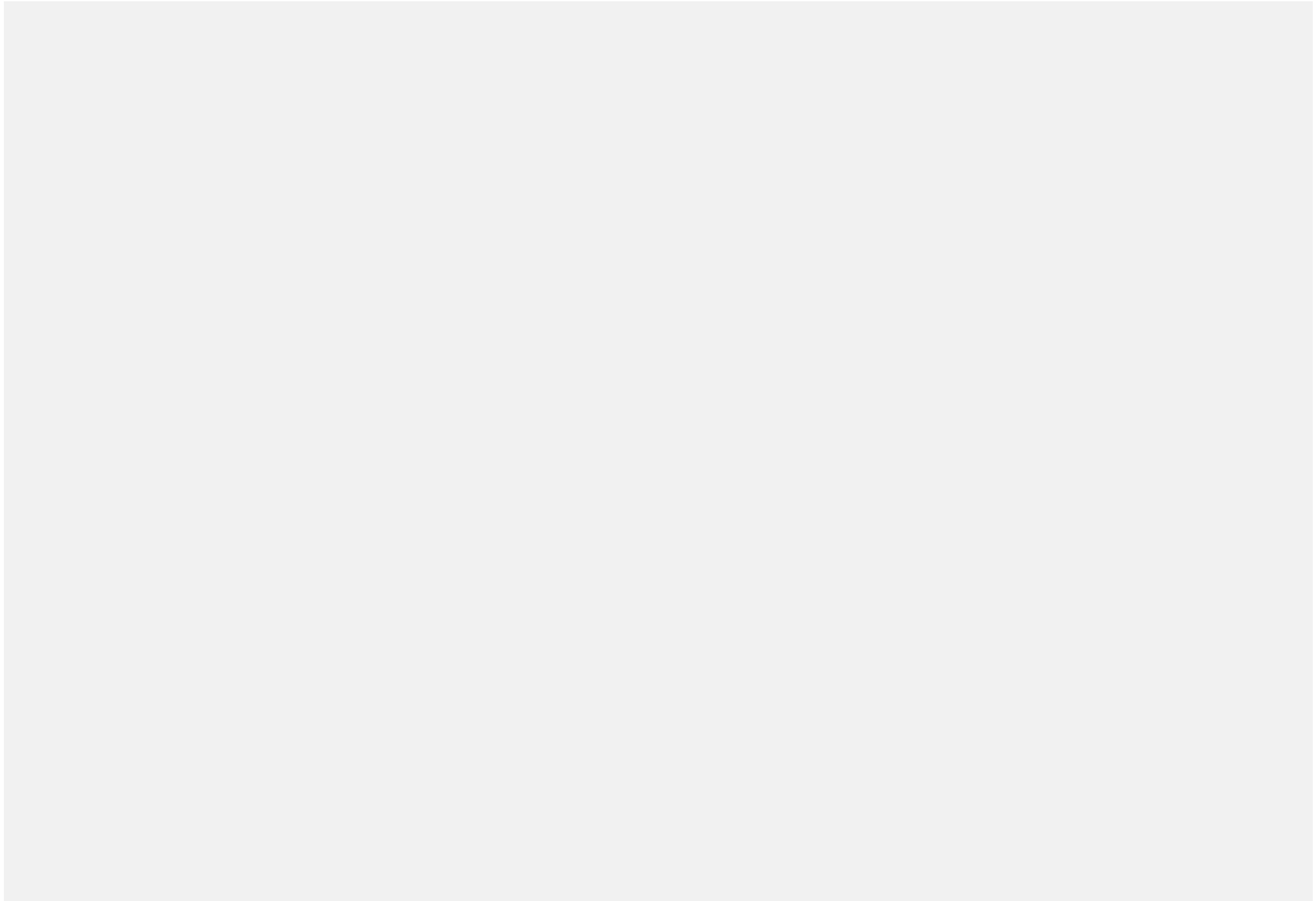
```
% more tobe.txt
to be or not to - be - - that - - - is

% java StackOfStrings < tobe.txt
to be not that or be
```

push pop



## Stack: linked-list representation







## Stack **pop**: linked-list implementation

### inner class

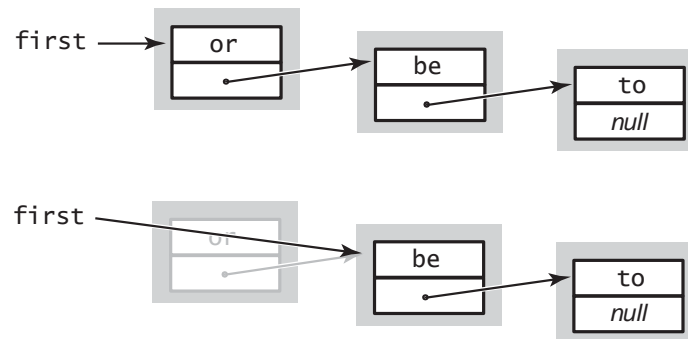
```
private class Node
{
    String item;
    Node next;
}
```

### save item to return

```
String item = first.item;
```

### delete first node

```
first = first.next;
```



### return saved item

```
return item;
```

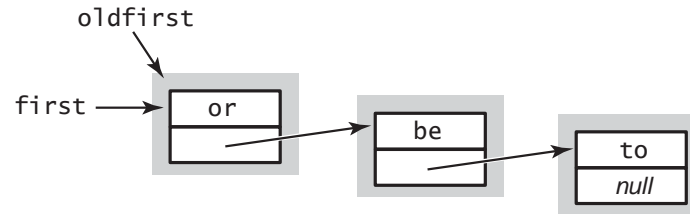
## Stack push: linked-list implementation

### inner class

```
private class Node
{
    String item;
    Node next;
}
```

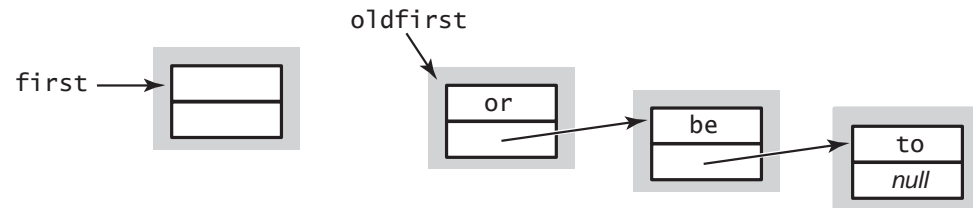
### save a link to the list

```
Node oldfirst = first;
```



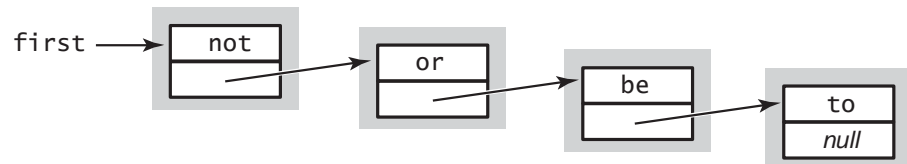
### create a new node for the beginning

```
first = new Node();
```



### set the instance variables in the new node

```
first.item = "not";
first.next = oldfirst;
```



## Stack: linked-list implementation in Java

```
public class LinkedStackOfStrings
{
    private Node first = null;
```

```
    private class Node
    {
        String item;
        Node next;
    }
```

← inner class

```
    public boolean isEmpty()
    { return first == null; }
```

```
    public void push(String item)
    {
        Node oldfirst = first;
        first = new Node();
        first.item = item;
        first.next = oldfirst;
    }
```

```
    public String pop()
    {
        String item = first.item;
        first = first.next;
        return item;
    }
}
```

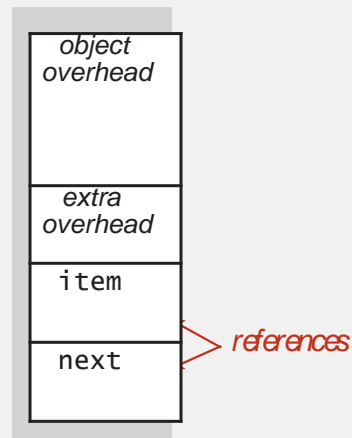
## Stack: linked-list implementation performance

**Proposition.** Every operation takes constant time in the worst case.

**Proposition.** A stack with  $N$  items uses  $\sim 40 N$  bytes.

### inner class

```
private class Node
{
    String item;
    Node next;
}
```



16 bytes (object overhead)

8 bytes (inner class extra overhead)

8 bytes (reference to String)

8 bytes (reference to Node)

---

40 bytes per stack node

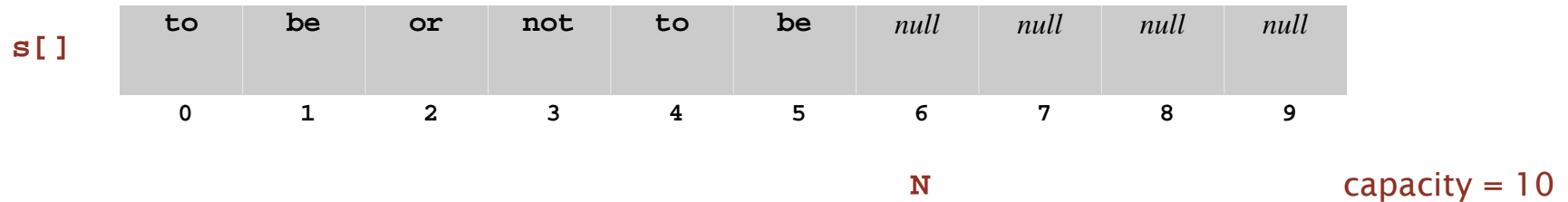
**Remark.** Analysis includes memory for the stack  
(but not the strings themselves, which the client owns).

## Stack: array implementation

## Stack: array implementation

### Array implementation of a stack.

- Use array `s[]` to store `N` items on stack.
- `push()`: add new item at `s[N]`.
- `pop()`: remove item from `s[N-1]`.

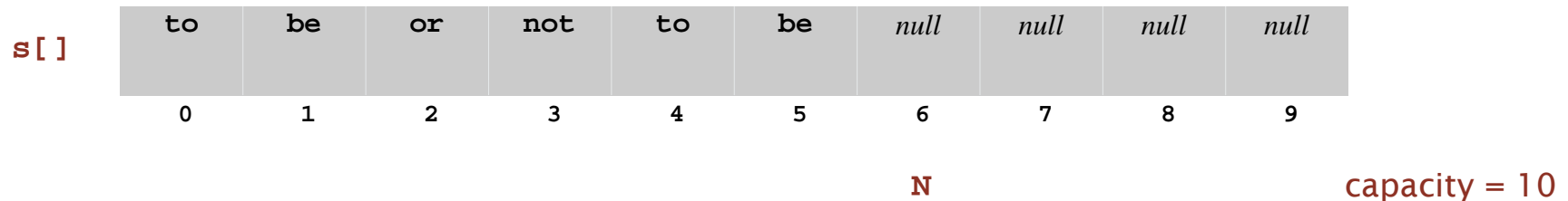


Defect. ???

## Stack: array implementation

### Array implementation of a stack.

- Use array  $s[]$  to store  $N$  items on stack.
- `push()`: add new item at  $s[N]$ .
- `pop()`: remove item from  $s[N-1]$ .



**Defect.** Stack overflows when  $N$  exceeds capacity. [stay tuned]

## Stack: array implementation

```
public class FixedCapacityStackOfStrings
{
    private String[] s;
    private int N = 0;

    public FixedCapacityStackOfStrings(int capacity)
    { s = new String[capacity]; }

    public boolean isEmpty()
    { return N == 0; }

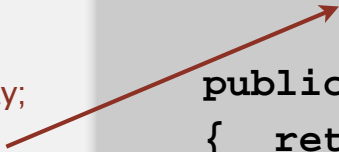
    public void push(String item)
    { s[N++] = item; }

    public String pop()
    { return s[--N]; }
}
```

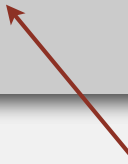
a cheat  
(stay tuned)



use to index into array;  
then increment N



decrement N;  
then use to index into array





## Stack considerations

### Overflow and underflow.

- Underflow: throw exception if pop from an empty stack.
- Overflow: use resizing array for array implementation. [stay tuned]

**Loitering.** Holding a reference to an object when it is no longer needed.

```
public String pop()
{ return s[--N]; }
```

loitering

```
public String pop()
{
    String item = s[--N];
    s[N] = null;
    return item;
}
```

this version avoids "loitering":  
garbage collector can reclaim memory  
only if no outstanding references

**Null items.** We allow null items to be inserted.

- stacks
- **resizing arrays**
- generics
- iterators
- applications
- queues

## Stack: resizing-array implementation

**Problem.** Requiring client to provide capacity does not implement API!

**Q.** How to grow and shrink array?

**First try.**

- `push()`: increase size of array `s[]` by 1.
- `pop()`: decrease size of array `s[]` by 1.

## Stack: resizing-array implementation

**Problem.** Requiring client to provide capacity does not implement API!

**Q.** How to grow and shrink array?

**First try.**

- `push()`: increase size of array `s[]` by 1.
- `pop()`: decrease size of array `s[]` by 1.

**Too expensive.**

- Need to copy all item to a new array.
- Inserting first  $N$  items takes time proportional to  $1 + 2 + \dots + N \sim N^2 / 2$ .

↑  
infeasible for large  $N$

**Challenge.** Ensure that array resizing happens infrequently.

## Stack: resizing-array implementation

Q. How to grow array?

A. If array is full, create a new array of **twice** the size, and copy items.

"repeated doubling"



```
public ResizingArrayStackOfStrings()
{
    s = new String[1];
}

public void push(String item)
{
    if (N == s.length) resize(2 * s.length);
    s[N++] = item;
}

private void resize(int capacity)
{
    String[] copy = new String[capacity];
    for (int i = 0; i < N; i++)
        copy[i] = s[i];
    s = copy;
}
```

see next slide



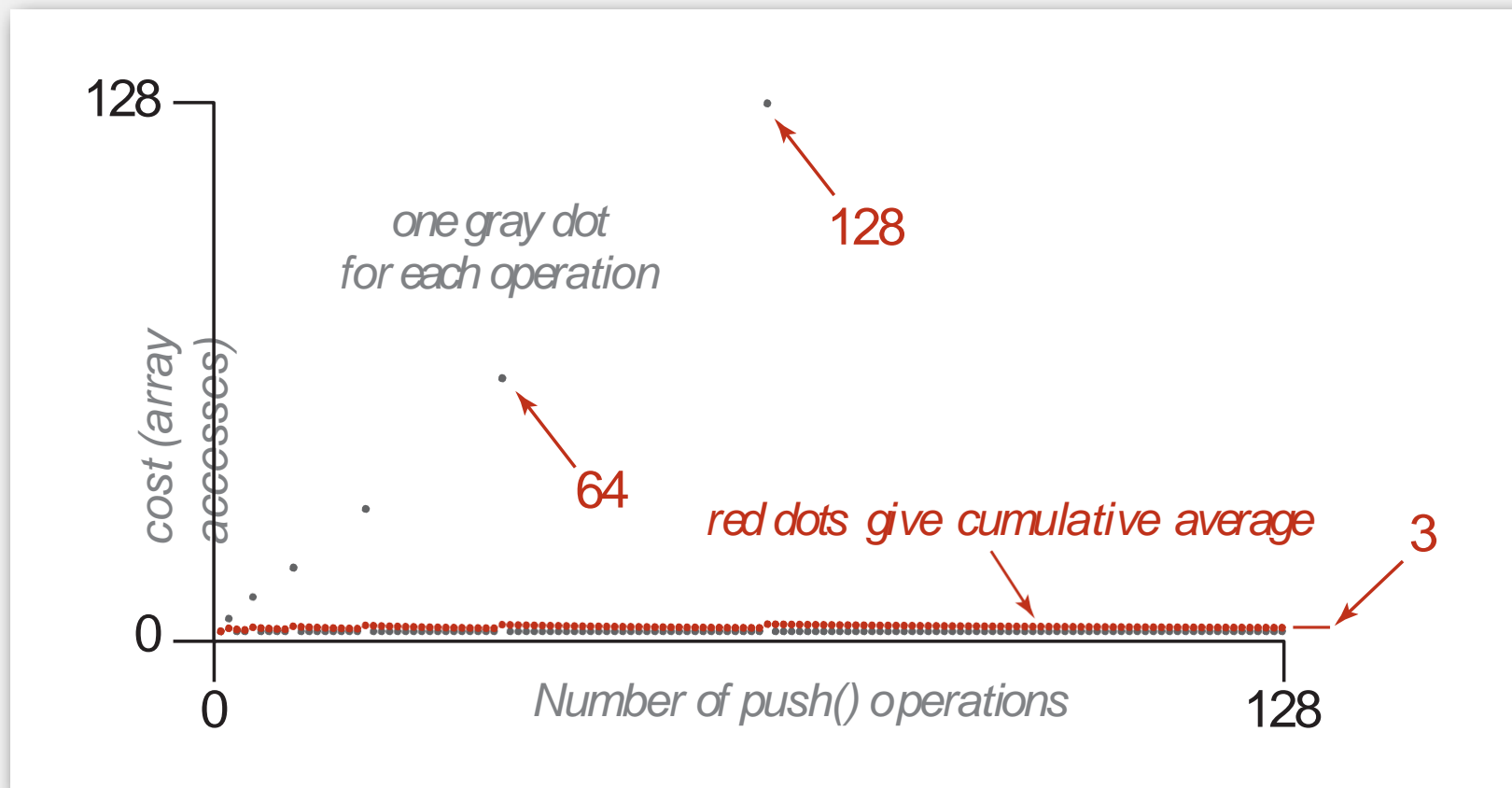
**Consequence.** Inserting first  $N$  items takes time proportional to  $N$  (not  $N^2$ ).

## Stack: amortized cost of adding to a stack

Cost of inserting first  $N$  items.  $N + (2 + 4 + 8 + \dots + N) \sim 3N$ .

↑  
1 array accesses  
per push

↑  
k array accesses  
to double to size  
k  
(ignoring cost to create new array)



## Stack: resizing-array implementation

Q. How to shrink array?

First try.

- `push()`: double size of array `s[]` when array is full.
- `pop()`: halve size of array `s[]` when array is **one-half full**.

## Stack: resizing-array implementation

Q. How to shrink array?

First try.

- `push()`: double size of array `s[]` when array is full.
- `pop()`: halve size of array `s[]` when array is **one-half full**.

Too expensive in worst case.

- Consider push-pop-push-pop-... sequence when array is full.
- Each operation takes time proportional to  $N$ .

"thrashing"



$N = 5$	to	be	or	not	to	null	null	null
$N = 4$	to	be	or	not				
$N = 5$	to	be	or	not	to	null	null	null
$N = 4$	to	be	or	not				



## Stack: resizing-array implementation

Q. How to shrink array?

Efficient solution.

- `push()`: double size of array `s[]` when array is full.
- `pop()`: halve size of array `s[]` when array is **one-quarter full**.

```
public String pop()
{
    String item = s[--N];
    s[N] = null;
    if (N > 0 && N == s.length/4) resize(s.length/2);
    return item;
}
```

**Invariant.** Array is between 25% and 100% full.

## Stack: resizing-array implementation trace

push()	pop()	N	a.length	a[]								
				0	1	2	3	4	5	6	7	
to		0	1	null								
		1	1	to								
be		2	2	to	be							
or		3	4	to	be							or
not		4	4	to	be	or	not					
to		5	8	to	be	or	not					to
-	to	4	8	to	be	or	not	null	null	null	null	
be		5	8	to	be	or	not	be	null	null	null	
-	be	4	8	to	be	or	not	null	null	null	null	
-	not	3	8	to	be	or	null	null	null	null	null	
that		4	8	to	be	or	that	null	null	null	null	
-	that	3	8	to	be	or	null	null	null	null	null	
-	or	2	4	to	be	null	null					
-	be	1	2	to	null							
is		2	2	to	is							

Trace of array resizing during a sequence of push() and pop() operations

## Stack resizing-array implementation: performance

**Amortized analysis.** Average running time per operation over a worst-case sequence of operations.

**Proposition.** Starting from an empty stack, any sequence of  $M$  push and pop operations takes time proportional to  $M$ .

	best	worst	amortized
construct	1	1	1
push	1	N	1
pop	1	N	1
size	1	1	1

doubling and  
halving operations

order of growth of running time  
for resizing stack with  $N$  items

## Stack resizing-array implementation: memory usage

**Proposition.** Uses between  $\sim 8 N$  and  $\sim 32 N$  bytes to represent a stack with  $N$  items.

- $\sim 8 N$  when full.
- $\sim 32 N$  when one-quarter full.

```
public class ResizingArrayStackOfStrings
{
    private String[] s;
    private int N = 0;
    ...
}
```

8 bytes (reference to array)

24 bytes (array overhead)

8 bytes  $\times$  array size

4 bytes (int)

4 bytes (padding)

**Remark.** Analysis includes memory for the stack (but not the strings themselves, which the client owns).

## Stack implementations: resizing array vs. linked list

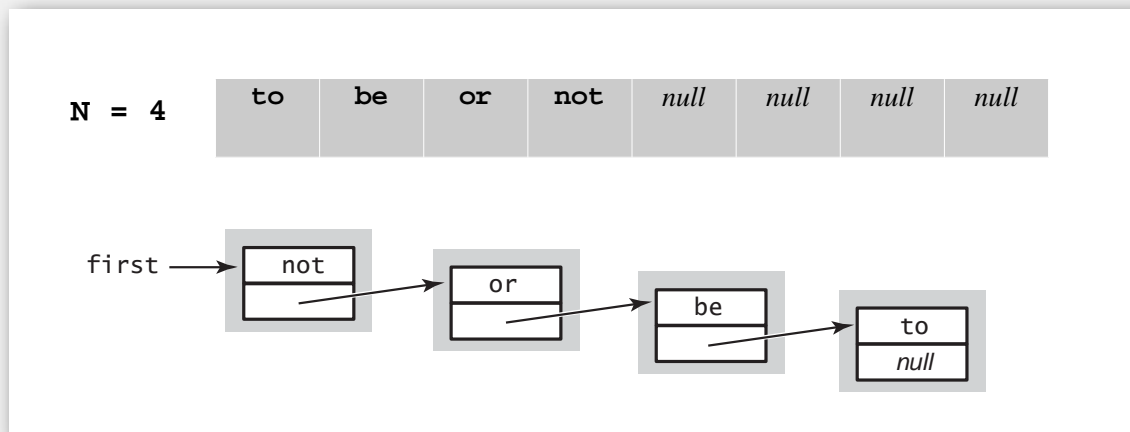
**Tradeoffs.** Can implement a stack with either a resizing array or a linked list; client can use interchangeably. Which one is better?

### Linked-list implementation.

- Every operation takes constant time in the **worst case**.
- Uses extra time and space to deal with the links.

### Resizing-array implementation.

- Every operation takes constant **amortized** time.
- Less wasted space.



Tölvuorðasafn:

**generic** : *stofnrænn*

Sem er notaður sem [sniðmát](#) til að mynda raunverulega máleiningu fyrir viðeigandi [gagnatög](#) í samræmi við reglur um [rammtögun](#).

- stacks
- resizing arrays
- **generics**
- iterators
- applications
- queues

## Parameterized stack

We implemented: `StackOfStrings`.

We also want: `StackOfURLs`, `StackOfInts`, `StackOfVans`, ....

**Attempt 1.** Implement a separate stack class for each type.

- Rewriting code is tedious and error-prone.
- Maintaining cut-and-pasted code is tedious and error-prone.

@#\*\$! most reasonable approach until Java 1.5.



## Parameterized stack

We implemented: `StackOfStrings`.

We also want: `StackOfURLs`, `StackOfInts`, `StackOfVans`, ....

**Attempt 2.** Implement a stack with items of type object.

- Casting is required in client.
- Casting is error-prone: run-time error if types mismatch.

```
StackOfObjects s = new StackOfObjects();  
Apple a = new Apple();  
Orange b = new Orange();  
s.push(a);  
s.push(b);  
a = (Apple) (s.pop());
```

run-time error





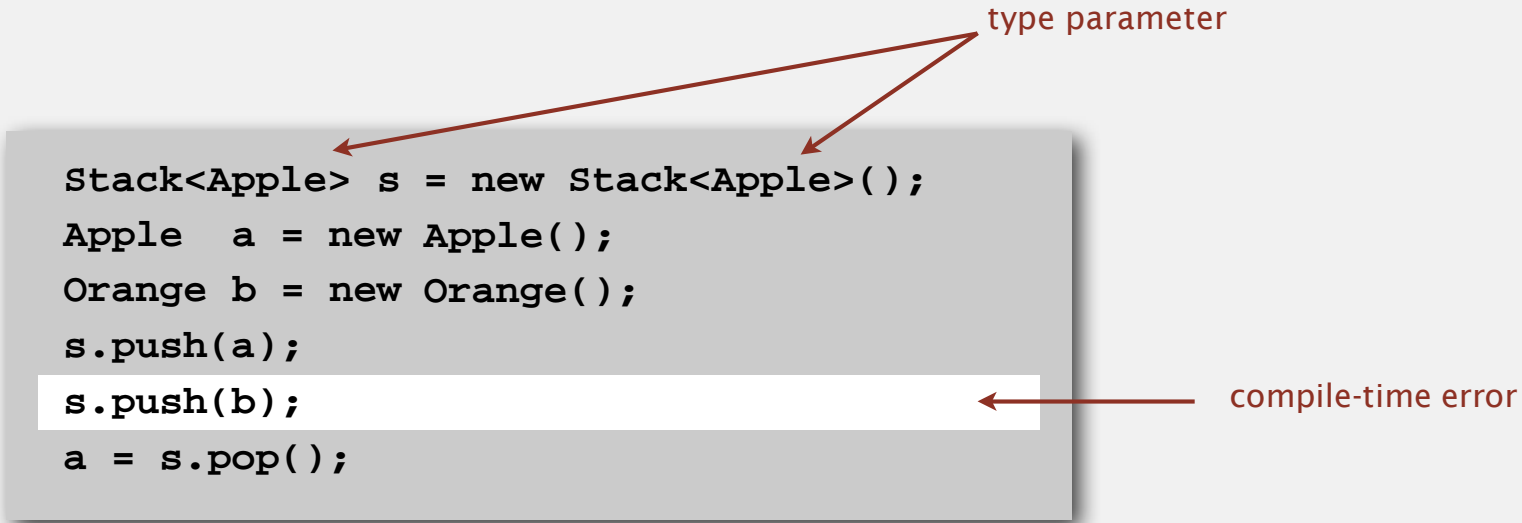
## Parameterized stack

We implemented: `StackOfStrings`.

We also want: `StackOfURLs`, `StackOfInts`, `StackOfVans`, ....

Attempt 3. Java generics.

- Avoid casting in client.
- Discover type mismatch errors at compile-time instead of run-time.



```
Stack<Apple> s = new Stack<Apple>();  
Apple a = new Apple();  
Orange b = new Orange();  
s.push(a);  
s.push(b);  
a = s.pop();
```

Guiding principles. Welcome compile-time errors; avoid run-time errors.

## Generic stack: linked-list implementation

```
public class
LinkedStackOfStrings
{
    private Node first = null;

    private class Node
    {
        String item;
        Node next;
    }

    public boolean isEmpty()
    { return first == null; }

    public void push(String item)
    {
        Node oldfirst = first;
        first = new Node();
        first.item = item;
        first.next = oldfirst;
    }

    public String pop()
    {
        String item = first.item;
        first = first.next;
        return item;
    }
}
```

```
public class Stack<Item>
{
    private Node first = null;

    private class Node
    {
        Item item
        Node next
    }

    public boolean isEmpty()
    { return first == null; }

    public void push(Item item)
    {
        Node oldfirst = first;
        first = new Node();
        first.item = item;
        first.next = oldfirst;
    }

    public Item pop()
    {
        Item item = first.item;
        first = first.next;
        return item;
    }
}
```

generic type name



## Generic stack: array implementation

```
public class FixedCapacityStackOfStrings
{
    private String[] s;
    private int N = 0;

    public ..StackOfStrings(int capacity)
    { s = new String[capacity]; }

    public boolean isEmpty()
    { return N == 0; }

    public void push(String item)
    { s[N++] = item; }

    public String pop()
    { return s[--N]; }
}
```

the way it should be

```
public class FixedCapacityStack<Item>
{
    private Item[] s;
    private int N = 0;

    public FixedCapacityStack(int capacity)
    { s = new Item[capacity]; }

    public boolean isEmpty()
    { return N == 0; }

    public void push(Item item)
    { s[N++] = item; }

    public Item pop()
    { return s[--N]; }
}
```

@#\$\*! generic array creation not allowed in Java

## Generic stack: array implementation

```
public class FixedCapacityStackOfStrings
{
    private String[] s;
    private int N = 0;

    public ..StackOfStrings(int capacity)
    { s = new String[capacity]; }

    public boolean isEmpty()
    { return N == 0; }

    public void push(String item)
    { s[N++] = item; }

    public String pop()
    { return s[--N]; }
}
```

the way it is

```
public class FixedCapacityStack<Item>
{
    private Item[] s;
    private int N = 0;

    public FixedCapacityStack(int capacity)
    { s = (Item[]) new Object[capacity]; }

    public boolean isEmpty()
    { return N == 0; }

    public void push(Item item)
    { s[N++] = item; }

    public Item pop()
    { return s[--N]; }
}
```

the ugly cast



## Generic data types: autoboxing

Q. What to do about primitive types?

## Generic data types: autoboxing

Q. What to do about primitive types?

Wrapper type.

- Each primitive type has a **wrapper** object type.
- Ex: `Integer` is wrapper type for `int`.

**Autoboxing.** Automatic cast between a primitive type and its wrapper.

„Syntactic sugar“. Behind-the-scenes casting.

```
Stack<Integer> s = new Stack<Integer>();  
  
s.push(17);           // s.push(new Integer(17));  
int a = s.pop();      // int a = s.pop().intValue();
```

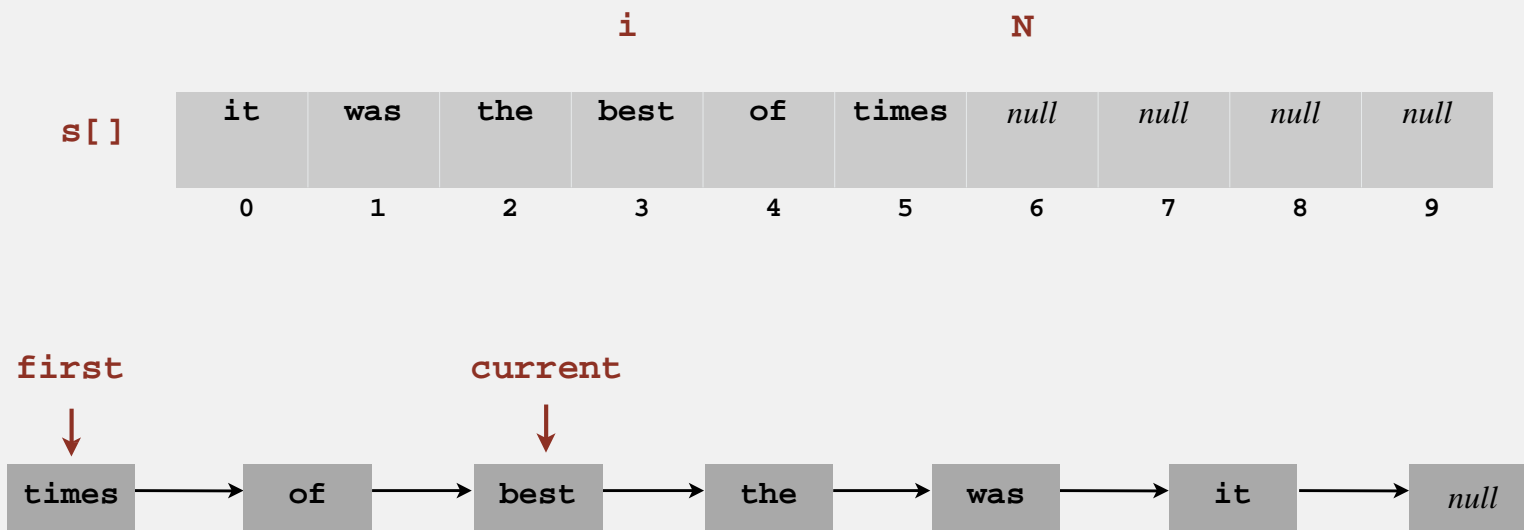
**Bottom line.** Client code can use generic stack for **any** type of data.

- stacks
- resizing arrays
- queues
- generics
- **iterators**
- applications

ísl.: Ítrrarar, ítrekarar

## Iteration

**Design challenge.** Support iteration over stack items by client, without revealing the internal representation of the stack.



**Java solution.** Make stack implement the `Iterable` interface.



## Java Interfaces

### Restricted form of multiple inheritance.

Java doesn't allow a class to inherit from multiple parents. Interfaces are a way around it.

### Interface inheritance (subtyping).

- Java provides the interface construct for declaring a relationship between otherwise unrelated classes, by specifying a common set of methods that each implementing class must include.
- Interfaces enable us to write client programs that can manipulate objects of varying types, by invoking common methods from the interface.

### Built-in interfaces

- `java.util.Comparable` (see Chapter 2 on Sorting)
- `java.util.Iterable` and `java.util.Iterator` ([Here](#))

# Iterators

Q. What is an `Iterable` ?

A. Has a method that returns an `Iterator`.

Q. What is an `Iterator` ?

A. Has methods `hasNext()` and `next()`.

Q. Why make data structures `Iterable` ?

A. Java supports elegant client code.

## Iterable interface

```
public interface Iterable<Item>
{
    Iterator<Item> iterator();
}
```

## Iterator interface

```
public interface Iterator<Item>
{
    boolean hasNext();
    Item next();
    void remove(); ← optional; use
                    at your own risk
}
```

## “foreach” statement

```
for (String s : stack)
    StdOut.println(s);
```

## equivalent code

```
Iterator<String> i = stack.iterator();
while (i.hasNext())
{
    String s = i.next();
    StdOut.println(s);
}
```

## Stack iterator: linked-list implementation

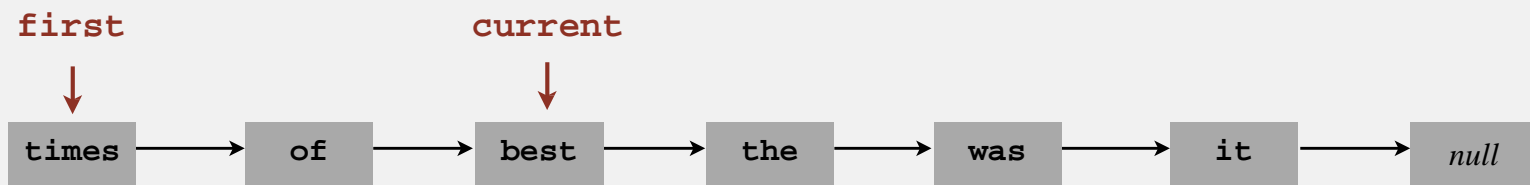
```
import java.util.Iterator;

public class Stack<Item> implements Iterable<Item>
{
    ...

    public Iterator<Item> iterator() { return new ListIterator(); }

    private class ListIterator implements Iterator<Item>
    {
        private Node current = first;

        public boolean hasNext() { return current != null; }
        public void remove()     { /* not supported */ }
        public Item next()
        {
            Item item = current.item;
            current = current.next;
            return item;
        }
    }
}
```



## Stack iterator: array implementation

```
import java.util.Iterator;

public class Stack<Item> implements Iterable<Item>
{
    ...

    public Iterator<Item> iterator()
    { return new ReverseArrayIterator(); }

    private class ReverseArrayIterator implements Iterator<Item>
    {
        private int i = N;

        public boolean hasNext() { return i > 0; }
        public void remove()    { /* not supported */ }
        public Item next()      { return s[--i]; }
    }
}
```

	<i>i</i>					<i>N</i>				
<i>s[ ]</i>	it	was	the	best	of	times	<i>null</i>	<i>null</i>	<i>null</i>	<i>null</i>
	0	1	2	3	4	5	6	7	8	9

## Bag API

**Main application.** Adding items to a collection and iterating (when order doesn't matter).

```
public class Bag<Item> implements Iterable<Item>
```

```
    Bag()
```

*create an empty bag*

```
    void add(Item x)
```

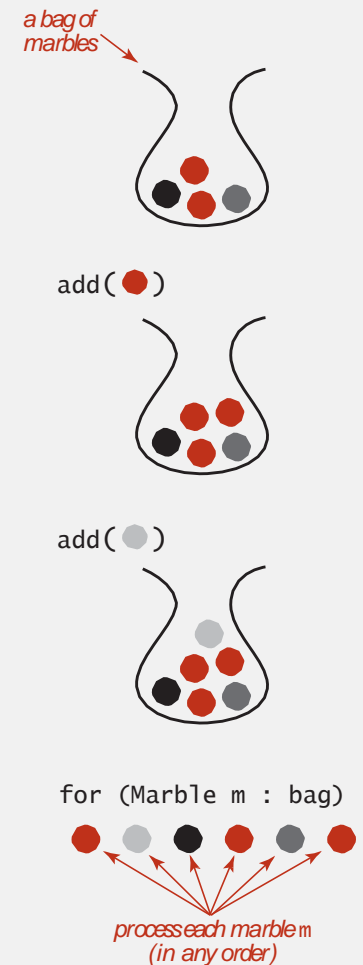
*insert a new item onto bag*

```
    int size()
```

*number of items in bag*

```
    Iterable<Item> iterator()
```

*iterator for all items in bag*



**Implementation.** Stack (without pop) or queue (without dequeue).

- stacks
- resizing arrays
- queues
- generics
- iterators
- applications

## Java collections library

**List interface.** `java.util.List` is API for ordered collection of items.

```
public interface List<Item> implements Iterable<Item>
```

```
    List() create an empty list
```

```
    boolean isEmpty() is the list empty?
```

```
    int size() number of items
```

```
    void add(Item item) append item to the end
```

```
    Item get(int index) return item at given index
```

```
    Item remove(int index) return and delete item at given index
```

```
    boolean contains(Item item) does the list contain the given item?
```

```
    Iterator<Item> iterator() iterator over all items in the list
```

```
    ...
```

**Implementations.** `java.util.ArrayList` uses resizing array;

`java.util.LinkedList` uses linked list.

## Java collections library

### `java.util.Stack`.

- Supports `push()`, `pop()`, `size()`, `isEmpty()`, and iteration.
- Also implements `java.util.List` interface from previous slide, including, `get()`, `remove()`, and `contains()`.
- Bloated and poorly-designed API (why?)  $\Rightarrow$  don't use.

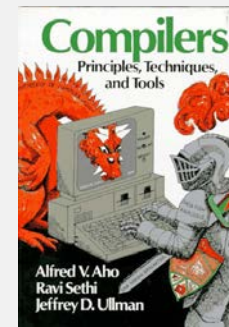
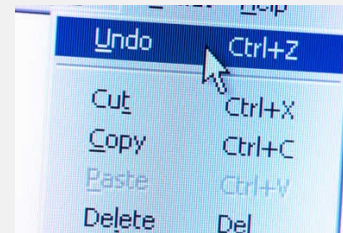
`java.util.Queue`. An interface, not an implementation of a queue.

**Best practices.** Use our implementations of `stack`, `queue`, and `Bag`.



## Stack applications

- Parsing in a compiler.
- Java virtual machine.
- Undo in a word processor.
- Back button in a Web browser.
- PostScript language for printers.
- Implementing function calls in a compiler.
- ...



## Function calls

How a compiler implements a function.

- Function call: **push** local environment and return address.
- Return: **pop** return address and local environment.

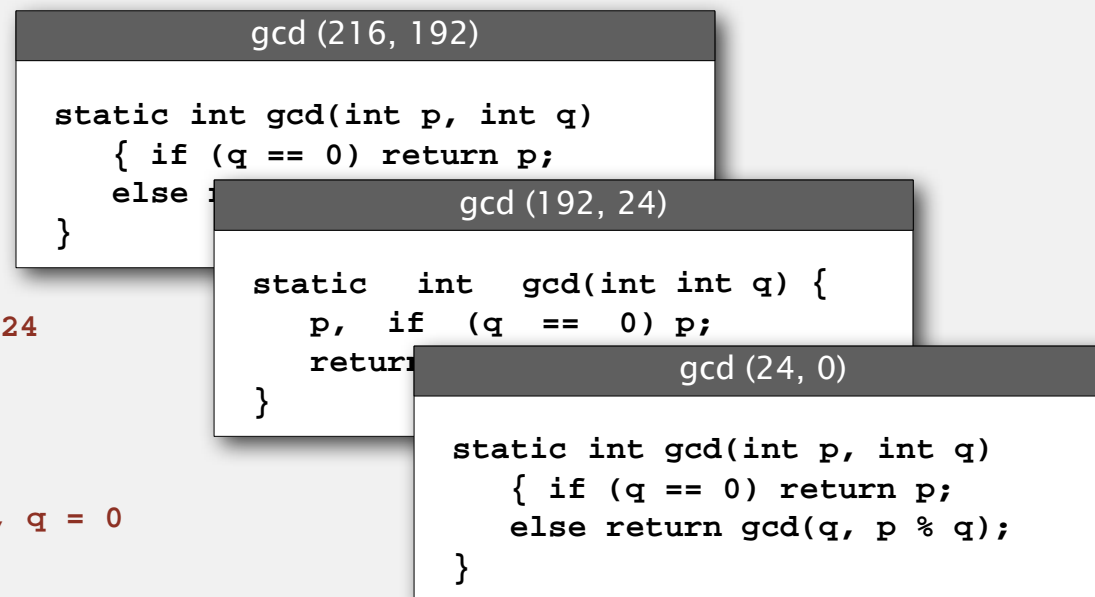
**Recursive function.** Function that calls itself.

**Note.** Can always use an explicit stack to remove recursion.

`p = 216, q = 192`

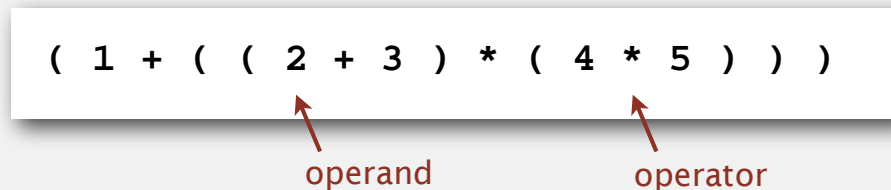
`p = 192, q = 24`

`p = 24, q = 0`



# Arithmetic expression evaluation

**Goal.** Evaluate infix expressions.

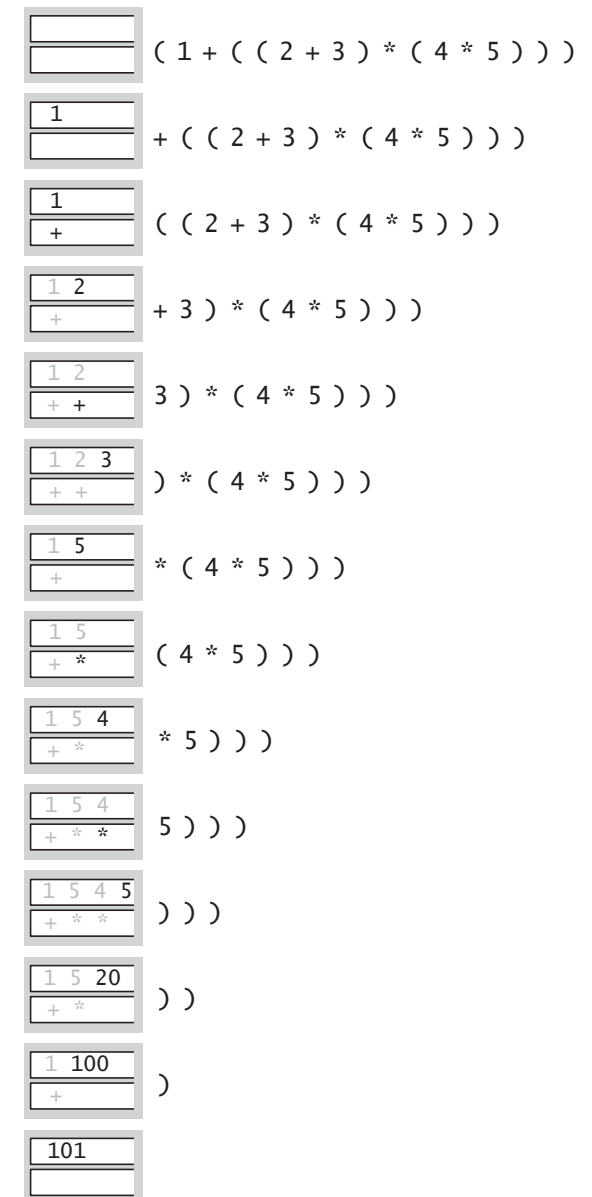


value stack  
operator  
stack

**Two-stack algorithm.** [E. W. Dijkstra]

- Value: push onto the value stack.
- Operator: push onto the operator stack.
- Left parenthesis: ignore.
- Right parenthesis: pop operator and two values; push the result of applying that operator to those values onto the operand stack.

**Context.** An interpreter!



## Arithmetic expression evaluation demo

## Arithmetic expression evaluation

```
public class Evaluate
{
    public static void main(String[] args)
    {
        Stack<String> ops  = new Stack<String>();
        Stack<Double> vals = new Stack<Double>();
        while (!StdIn.isEmpty()) {
            String s = StdIn.readString();
            if      (s.equals("("))                ;
            else if (s.equals("+"))      ops.push(s);
            else if (s.equals("*"))      ops.push(s);
            else if (s.equals(")"))
            {
                String op = ops.pop();
                if      (op.equals("+")) vals.push(vals.pop() + vals.pop());
                else if (op.equals("*")) vals.push(vals.pop() * vals.pop());
            }
            else vals.push(Double.parseDouble(s));
        }
        StdOut.println(vals.pop());
    }
}
```

```
% java Evaluate
( 1 + ( ( 2 + 3 ) * ( 4 * 5 ) ) )
101.0
```

## Correctness

Q. Why correct?

A. When algorithm encounters an operator surrounded by two values within parentheses, it leaves the result on the value stack.

```
( 1 + ( ( 2 + 3 ) * ( 4 * 5 ) ) )
```

as if the original input were:

```
( 1 + ( 5 * ( 4 * 5 ) ) )
```

Repeating the argument:

```
( 1 + ( 5 * 20 ) )  
( 1 + 100 )  
101
```

Extensions. More ops, precedence order, associativity.

## Stack-based programming languages

**Observation 1.** The 2-stack algorithm computes the same value if the operator occurs **after** the two values.

```
( 1 ( ( 2 3 + ) ( 4 5 * ) * ) + )
```

**Observation 2.** All of the parentheses are redundant!

```
1 2 3 + 4 5 * * +
```



Jan Lukasiewicz

**Bottom line.** Postfix or "reverse Polish" notation.

**Applications.** Postscript, Forth, calculators, Java virtual machine, ...

- stacks
- resizing arrays
- generics
- iterators
- applications
- **queues**



# Queue API

```
public class QueueOfStrings
```

```
    QueueOfStrings()
```

*create an empty queue*

```
    void enqueue(String s)
```

*insert a new item onto queue*

```
    String dequeue()
```

*remove and return the item  
least recently added*

```
    boolean isEmpty()
```

*is the queue empty?*

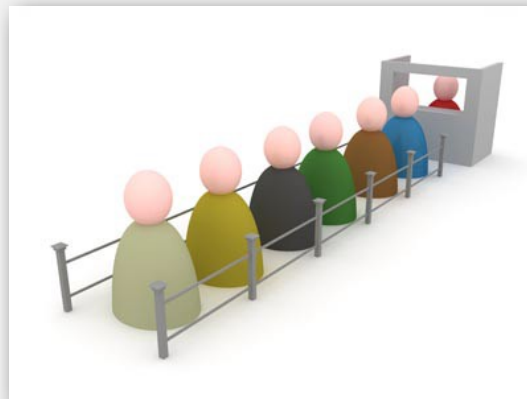
```
    int size()
```

*number of items on the queue*

enqueue

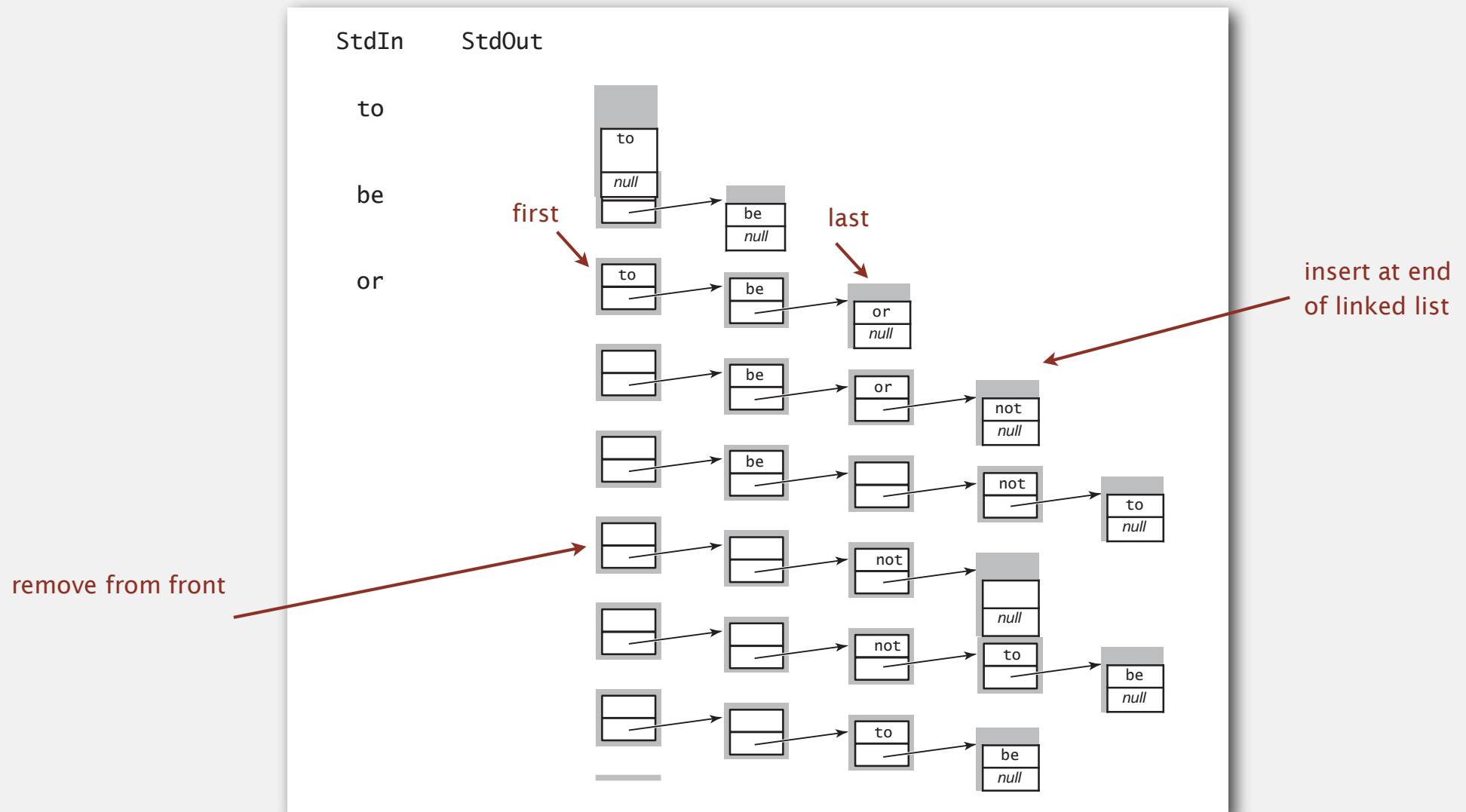


dequeue



## Queue: linked-list representation

Maintain pointer to first and last nodes in a linked list;  
insert/remove from opposite ends.



## Queue dequeue: linked-list implementation

### inner class

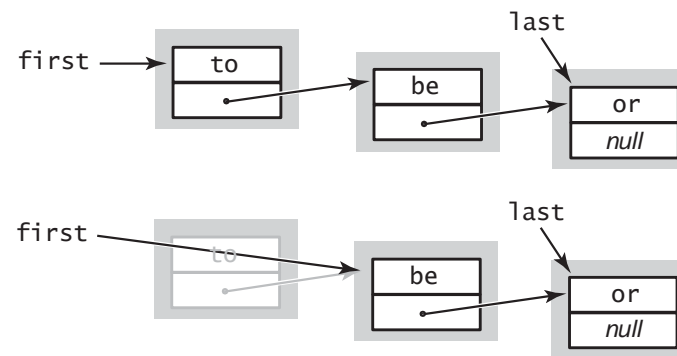
```
private class Node
{
    String item;
    Node next;
}
```

### save item to return

```
String item = first.item;
```

### delete first node

```
first = first.next;
```



### return saved item

```
return item;
```

**Remark.** Identical code to linked-list stack `pop()`.

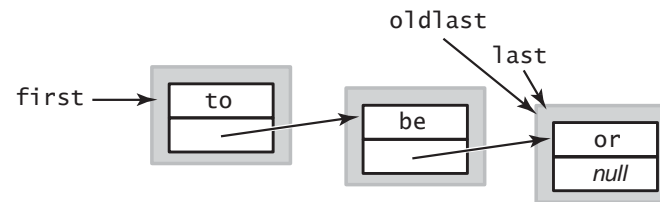
## Queue enqueue: linked-list implementation

### inner class

```
private class Node
{
    String item;
    Node next;
}
```

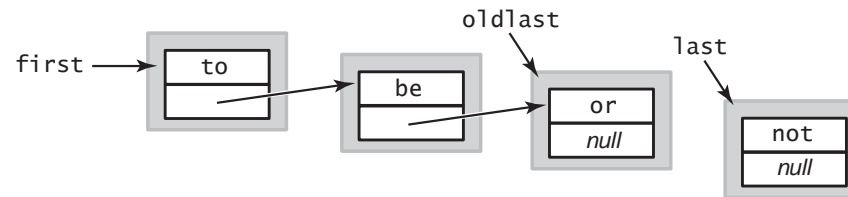
### save a link to the last node

```
Node oldlast = last;
```



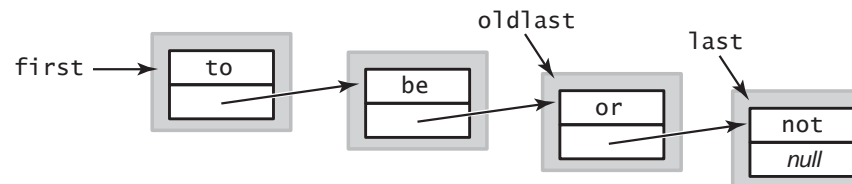
### create a new node for the end

```
Node last = new Node();
last.item = "not";
last.next = null;
```



### link the new node to the end of the list

```
oldlast.next = last;
```



## Queue: linked-list implementation in Java

```
public class LinkedQueueOfStrings
{
    private Node first, last;

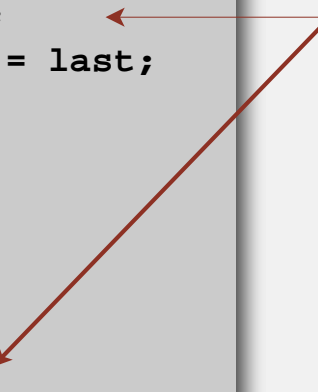
    private class Node
    { /* same as in StackOfStrings */ }

    public boolean isEmpty()
    { return first == null; }

    public void enqueue(String item)
    {
        Node oldlast = last;
        last = new Node();
        last.item = item;
        last.next = null;
        if (isEmpty()) first = last;
        else            oldlast.next = last;
    }

    public String dequeue()
    {
        String item = first.item;
        first       = first.next;
        if (isEmpty()) last = null;
        return item;
    }
}
```

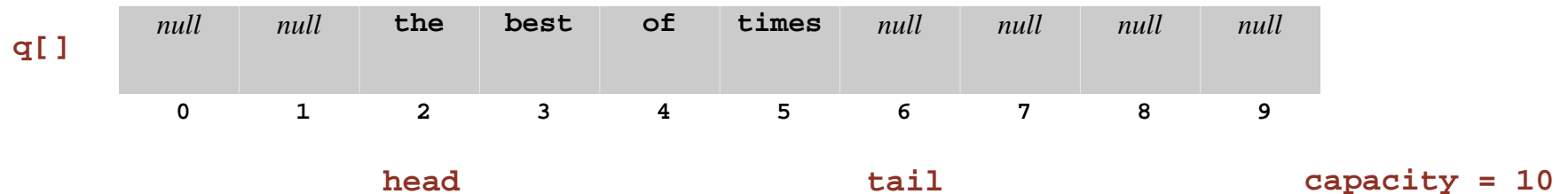
special cases for  
empty queue



## Queue: resizing array implementation

### Array implementation of a queue.

- Use array `q[]` to store items in queue.
- `enqueue()`: add new item at `q[tail]`.
- `dequeue()`: remove item from `q[head]`.
- Update `head` and `tail` modulo the capacity.
- Add resizing array.



# Queue applications

## Familiar applications.

- iTunes playlist.
- Data buffers (iPod, TiVo).
- Asynchronous data transfer (file IO, pipes, sockets).
- Dispensing requests on a shared resource (printer, processor).

## Simulations of the real world.

- Traffic analysis.
- Waiting times of customers at call center.
- Determining number of cashiers to have at a supermarket.

