

1. $C \rightarrow D, C \rightarrow A, B \rightarrow C$.

a) Identify the candidate keys.

Rewrite the relations: $B \rightarrow C, C \rightarrow A, C \rightarrow D$.

Transitive rule 3: $B \rightarrow C, B \rightarrow A, B \rightarrow D$.

$B \rightarrow$ all: A, B, C, D.

B is a key.

b) Identify the best normal form.

$R = \underline{A}BCD$

$B \rightarrow ACD$.

R is a BCNF.

c) Decompose to set of BCNF

R is in BCNF form.

2. $B \rightarrow C, D \rightarrow A$.

a) Identify the candidate keys.

$BD \rightarrow A, BD \rightarrow C$.

BD is a key.

b) Identify the best normal form.

$R = \underline{BD}CA$

$BD \rightarrow A, BD \rightarrow C$.

R is a BCNF.

c) Decompose to set of BCNF

R is in BCNF form.

3. $ABC \rightarrow D, D \rightarrow A.$

a) Identify the candidate keys.

$BC \rightarrow A, BC \rightarrow D, A \rightarrow D, D \rightarrow A.$

BC is a key.

b) Identify the best normal form.

$R = \underline{BC}DA$

R is a BCNF, and also 2NF.

c) Decompose to set of BCNF

$BC \rightarrow A, BC \rightarrow D, A \rightarrow D, D \rightarrow A$

$\Rightarrow BC \rightarrow A, BC \rightarrow D.$

4. $A \rightarrow B, BC \rightarrow D, A \rightarrow C.$

a) Identify the candidate keys.

$A \rightarrow B, A \rightarrow C, BC \rightarrow D.$

Transitivity: $A \rightarrow B, A \rightarrow C, A \rightarrow D, BC \rightarrow D.$

A is a key.

b) Identify the best normal form.

$R = \underline{A}BCD$

R is a BCNF, and also a 2NF.

c) Decompose to set of BCNF

$A \rightarrow B, A \rightarrow C, A \rightarrow D.$

5. $AB \rightarrow C, AB \rightarrow D, A \rightarrow C, C \rightarrow A.$

a) Identify the candidate keys.

AB is a key.

b) Identify the best normal form.

$R = \underline{A}BCD$

R is a 3NF.

c) Decompose to set of BCNF

There is no possible BCNF.