University of Cincinnati



GEOL 6024: GroundWater Modeling

Calibrating Model using Flopy Project Report

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April 25, 2022

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1. Introduction

Planning to install a new 250 GPM well at their main facility, a small manufacturer hires you to determine whether their proposed well (see above) will cause any problems with the stream and an existing well and whether the new well or the existing well would likely become contaminated by a nearby TCE plume as a result of the operation of the new well. The new well will be operated continuously.

Geologic data indicate a water table aquifer with bottom elevation of –100ft in this area. The aquifer abruptly pinches out at west and southern boundaries. Ground surface elevation in the area is approximately 3m. A 1st-order stream (average depth=1m) flowing through the area empties into the deep lake (water surface elevation 0.00m) in the NE corner of the map. The stream is predominantly fed by groundwater, meaning the streamflow is essentially baseflow.

Although there has been no study of actual recharge rates to this aquifer, long term average recharge from precipitation in this part of the state varies between 10 and 18 inches/yr depending on the location of the aquifer.

Only one well in the vicinity currently pumps (200 GPM) from this aquifer. This well has been operating continuously for the past 15 years.

This past August, in anticipation of the need to understand this aquifer better, 45 piezometers were installed to determine the water table variation throughout the area. In addition, stream water levels and stream discharges were measured. Average stream discharge measured at a cross section approaching the lake was 1486.65 m³/d (272.73 GPM). The streambed leakance (hydraulic conductivity per unit thickness of the streambed) is unknown and must be calibrated. Annual average water table elevations and stream water levels are provided.

2. Codes

2.1 Importing libraries

Same as in other exercises few python libraries are loaded, this one here has many libraries as we're using more and more advanced features.

matplotlib.gridspec is for plotting multiple plots in a grid. pandas is for loading river head values from csv file, and scipy.interpolate is being used to interpolate the head values from river nodes into each cell.

```
import math
import flopy
import matplotlib.pyplot as plt
import matplotlib.gridspec as gridspec
import numpy as np
import pandas as pd
from scipy.interpolate import interp2d

from shapely import geometry
```

This function here makes a shapely.geometry shape from csv file. We'll later use this to load lake and river from their co-ordinates.

2.2 Simulation Parameters

Simulation grid specifications.

```
_ code: python
    X0 = 0
    XN = 3000
2
    NC = 100
3
    \Delta X = XN/NC
4
5
    Y0 = 0
6
    YN = 2230
    NR = 75
    \Delta Y = YN/NR
10
    Top = 3
                                             # m
11
    Height = 100 * 0.3048
12
    Bottom = Top-Height
13
```

There is only one geolayer for this simulation.

```
geolyr_thickness = [Height]
geolyr_subdivisions = [50]
```

This parameters is used to determine whether to include second well in the simulation or not. For now it's false for calibration purposes.

```
SECOND_WELL_ON = False code: python _____
```

Let's define the grid points for later use.

Domain and lake geometry definitions along with lake parameters.

```
code: python

domain = geometry.box(X0, Y0, XN, YN)

lake = csv_2_shape('./data/4_lake.csv', geometry.Polygon)

lake_top = 0

lake_height = Height

lake_bottom = lake_top - lake_height

lake_bed_thickness = 1  # m

lake_conductance = 5 #* ΔX * ΔY / lake_bed_thickness # leakance

to conductance how?
```

Here we'll define river geometry from the csv, and we'll also use the csv data to define a function get_river_head which we can pass (x, y) co-ordinate to and get the head value interpolated from river nodes.

Now other parameters for the river.

```
river_top = 0
river_height = Height
river_bottom = river_top - river_height
```

```
river_width = 1
riverbed_thickness = 1
```

Well definitions.

```
code: python
well1 = geometry.Point((2373.8920225624497, 1438.255033557047))
well1_top = 0
well1_bottom = Bottom
well1_rate = -200 * 5.451 # GPM → m³/day

well2 = geometry.Point((1871.071716357776, 1030.7494407158838))
well2_top = 0
well2_bottom = Bottom
well2_rate = -250 * 5.451 # GPM → m³/day
```

2.3 Calibration Parameters

Here the parameters defined can be changed to get different results and these parameters are unknown. The current values are obtained after running batch process with a ton of parameters and selecting the best one.

```
code: python

Kh = 4.48

riv_cond = .01

# between 10-18 inch/year

Rch = 18 # inch/year

rech = Rch * 0.0254 / 365 # m/day
```

2.4 Utility Functions

This function here can be used to find the conductance of river cell, it'll use the intersection length of river with the cell to calculate the equivalent conductance. For now, river width and riverbed thickness are put in arbitrarily, but since we're calibrating it anyway, it should be fine.

```
code: python

def get_riv_conductance (intersect_length):

"Give conductance based on river intersection on grid."

return (riv_cond *

intersect_length * river_width / (ΔX*ΔY) # factor of

area covered

/ riverbed_thickness)
```

Now the same function to get the layers as in the previous models.

```
code: python

def get_layers(top=Top, bottom=Bottom):
   all_layers = [(i, b) for i, b in enumerate(bot) if b < top]</pre>
```

```
b = top
for i, b in all_layers:
    if b > bottom:
        yield i, top, b

else:
        break
        top = b

if b <= bottom:
        yield i, top, bottom</pre>
```

Similarly, a function to get the grid points. This one is a little more complex than the ones in the previous ones as we needed to calculate the conductance for each grid cell so it now returns the intersection length for linestring and intersection area for polygons.

You can provide a shape and it'll give you the grid points, shape can only be geometry. Point, geometry. Polygon or geometry. LineString.

```
___ code: python _
   def get_grid_points(shape, /, xy_grid_points, layers=None):
        if not layers:
2
            layers = [0]
3
        else:
4
            layers = list(layers)
        grid_pts = enumerate(map(geometry.Point, xy_grid_points))
        grid_boxes = enumerate(map(lambda x: geometry.box(
                 x[0] - \Delta X/2, x[1] - \Delta Y/2, x[0] + \Delta X/2, x[1] + \Delta Y/2),
                                  xy_grid_points))
10
11
        if isinstance(shape, geometry.Polygon):
12
            points = filter(lambda gp: shape.contains(gp[1]),
13

    grid_boxes)

            points = map(lambda gp: (gp[0],
14
             ⇒ shape.intersection(gp[1]).area), points)
        elif isinstance(shape, geometry.Point):
15
            nearest = min(grid_pts, key=lambda gp:
16
             ⇒ shape.distance(gp[1]))
            points = [(nearest[0], nearest[1].area)]
        elif isinstance (shape, geometry.LineString):
18
            points = filter(lambda gp: shape.intersects(gp[1]),
19

    grid_boxes)

            points = map(lambda gp: (gp[0],
20
                shape.intersection(gp[1]).length), points)
21
        for i, insec in points:
            col = i // (NR)
23
            row = i % (NR)
24
            for j in layers:
25
```

```
yield (j, row, col), xy_grid_points[i], insec
```

2.5 Calibration Data

We'll also load the calibration data for the observation wells, we'll get the grid points for all those wells so we can use that to extract the model heads at those wells later.

Here we can see how our calibration data is:

```
calib_wells.head()
```

```
output -
   well
                                           h
                                               weight
                     Х
                                   У
0
      1
        1138.014528
                        1776.654749
                                     12.10
                                                     1
                                                     1
1
      2
          571.428571
                         766.212291
                                      14.95
2
      3
          479.418886
                        1896.375419 14.79
                                                     1
3
      4
         1452.784504
                         680.013408 12.14
                                                     1
4
           479.418886
                         713.535196
                                    15.13
      5
                                                     1
```

And the grid points for the well that are obtained. The layer is not useful as we'll look at the watertable data which is 2 dimensional.

```
calib_wells_grid_pts[:5]
```

2.6 Calibration Dependent Simulation Parameters

Using the geolayer information we'll make the computational layers and use same hydraulic conductivity for all layers. So first we'll define a lookup table and geolayer characteristics.

Here we'll calculate the bottom elevation for all the layers that we'll need for descritization package.

```
thickness = np.zeros(NLay)

k_hz = [0 for i in range(NLay)]

k_vt = [0 for i in range(NLay)]

bot = np.ones(NLay)
```

Now we'll populate the values for the arrays we defined above.

2.7 Stress Period Functions

The function gives the river stress period data for river package. It'll use the grid points that intersect with the river, and then calculate conductivity based on that intersection to finally return it. Head and conductance as well as grid points are calculated using the functions defined earlier.

Similarly for constant head boundaries, we'll also add the lake heads.

```
for lay, thk, bottom in layers_tuple:
                # cellid, head
                yield ((lay, grid_pt[1], grid_pt[2]), lake_top)
       for grid_pt, pt, _ in get_grid_points(river,

    xy_grid_points=xy_grid_points):
           # cellid, head
10
           stage = get_river_head(pt[0], pt[1])[0]
           rbot = stage-1
12
            lyrs = get_layers(stage, rbot)
13
            for 1, t, b in lyrs:
14
                yield ((1, grid_pt[1], grid_pt[2]), stage)
15
```

Now the stress period data for wells. Second well stress period data is only added if the variable SECOND_WELL_ON is True.

```
code: python
   def get_well_stress_period():
       well1_layers = [1[0] for 1 in get_layers(well1_top,
2

    well1_bottom)]

       well1_pts = get_grid_points(well1,
3

→ xy_grid_points=xy_grid_points,

                                    layers=well1_layers)
4
       rate1 = well1_rate/len(well1_layers)
       spd = [(wpt, rate1) for wpt, _, _ in well1_pts]
       if SECOND_WELL_ON:
           well2_layers = [1[0] for 1 in get_layers(well2_top,
            → well2_bottom)]
           well2_pts = get_grid_points(well2,

→ xy_grid_points=xy_grid_points,

                                        layers=well2_layers)
10
            rate2 = well2_rate/len(well2_layers)
11
            spd += [(wpt, rate2) for wpt, _, _ in well2_pts]
12
       return {0: spd}
```

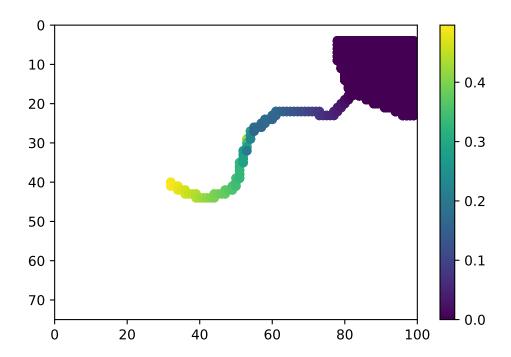
To see the stress period heads are correct we can plot it.

```
code: python

sp = list(get_chd_stress_period())

x = [l[0][2] for l in sp]+[0]
y = [l[0][1] for l in sp]+[0]
c = [l[1] for l in sp] + [None]
```

```
plt.scatter(x, y, c=c)
plt.xlim(left=0, right=NC)
plt.ylim(bottom=NR, top=0)
plt.colorbar()
filename="./images/4_calib_input.pdf"
plt.savefig(filename)
plt.show()
```



2.8 Flopy Model

Let's define the paths and the executable for simulation.

The time descritization will use default parameters as we want steady state. We'll use days as time unit.

```
tdis = flopy.mf6.ModflowTdis(sim,
time_units='days')
ims = flopy.mf6.ModflowIms(sim)
```

```
gwf = flopy.mf6.ModflowGwf(sim, modelname=name, save_flows=True)
```

Now using the previously defined parameters let's define the descritization package to define our model grid.

```
code: python

dis = flopy.mf6.ModflowGwfdis(gwf,

length_units='METERS',

nlay=NLay,

nrow=NR,

ncol=NC,

delc=ΔX,

delr=ΔY,

top=Top,

botm=bot)
```

We'll use the top elevation as the initial head for all the cells except for the cells that belongs to the constant head boundaries.

```
code: python
initial_head = np.ones((NLay, NR, NC)) * Top
for gp, head in get_chd_stress_period():
    initial_head[gp] = head

ic = flopy.mf6.ModflowGwfic(gwf, strt=initial_head)
```

For recharge we'll use the parameter defined above.

```
recharge = flopy.mf6.ModflowGwfrcha(gwf, recharge=rech)
```

We'll modify the cells that are on the river extent to have the same vertical conductance as that of the river bed. It'll simulate the river bed leakance for us.

```
code: python

k_vt_new = np.ones(shape=(NLay, NR, NC)) *Kh

for gp, _, cond, _ in get_riv_stress_period():
    k_vt_new[gp] = cond
```

We'll use the modified vertical conductance for the k33 variable and constant value for horizontal one.

```
k33=k_vt_new,
save_specific_discharge=True)
```

Now we'll define the chd package.

```
code: python

chd = flopy.mf6.ModflowGwfchd(
    gwf,
    stress_period_data=list(get_chd_stress_period()))
```

The riv package.

```
rivers = flopy.mf6.ModflowGwfriv(
gwf,
stress_period_data=list(get_riv_stress_period()))
```

Now the well stress period.

```
code: python

wells = flopy.mf6.ModflowGwfwel(
    gwf,
    stress_period_data=get_well_stress_period())
```

Files to save the output data.

```
budget_file = name + '.bud'
head_file = name + '.hds'
oc = flopy.mf6.ModflowGwfoc(gwf,

budget_filerecord=budget_file,
head_filerecord=head_file,
saverecord=[('HEAD', 'ALL')],
('BUDGET', 'ALL')])
```

Now finally we can save the files and run modflow simulation.

```
code: python
sim.write_simulation()
result,_ = sim.run_simulation()
result
```

```
False
```

This part here is not needed for the notebook, I'm putting it here so the tangled python script will end if simulation fails.

```
code: python

if not result:
   print("Error in Simulation")
   exit(1)
```

2.9 Simulation Post Processing

We can extract the simulation output from the simulation.

```
head_arr = gwf.output.head().get_data()
bud = gwf.output.budget()
```

And use the postprocessing tools to get the watertable as well as the specific discharges.

Now we can get the head value from the watertable for all the well grid points.

```
model_heads = map(lambda x: watertable[(x[1], x[2])],

calib_wells_grid_pts)
```

By doing some calculations we can calculate the errors for individual wells. Let's also calculate the size and color for the wells based on the absolute error and is it below or above the predicted value.

The RMSE and NSE values can be calculated from the individual error values.

```
code: python

rmse = math.sqrt(calib_wells.sq_err.sum())

nse = 1 - calib_wells.sq_err.sum()/(calib_wells.h -

calib_wells.h.mean()).map(lambda x: x**2).sum()
```

```
print(f'Rch={Rch} inch/year; K={Kh} m/day; RK={riv_cond};

RMSE={rmse}; NSE={nse}')
```

```
output

Rch=18 inch/year; K=4.48 m/day; RK=0.01 ; RMSE=10.076239940964998;

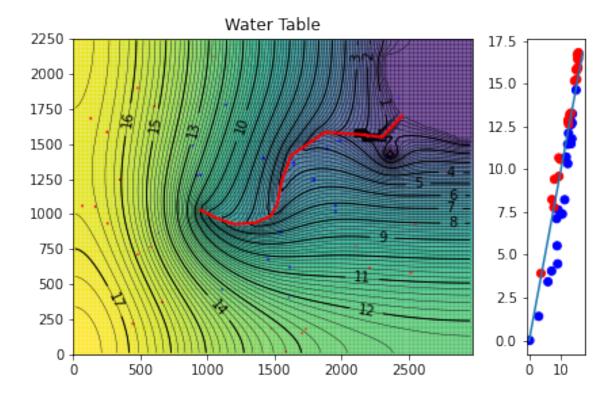
→ NSE=0.8301897496017947
```

2.10 Plots

```
code: python
   qs = qs = qridspec.GridSpec(1, 5)
   fig = plt.figure(constrained layout=True)
2
   ax1 = fig.add\_subplot(gs[0, :4])
3
   ax1.set_title('Water Table')
5
   pmv = flopy.plot.PlotMapView(gwf, ax=ax1)
   pmv.plot_array(watertable)
   pmv.plot_grid(colors='white', linewidths=0.3)
   contours = pmv.contour_array(watertable,
                                   levels=np.arange(0, 100, 1),
10
                                   linewidths=1.,
11
                                   colors='black')
12
   ax1.clabel(contours, fmt="%.0f")
13
   pmv.contour_array(watertable,
                       levels=np.arange(0, 100, .2),
15
                       linewidths=.4,
16
                       colors='black')
17
   ax1.plot(river_df.x, river_df.y, linewidth=2, color='red')
18
19
   ax1.scatter(calib_wells.x, calib_wells.y,
20
               s=calib_wells.pt_size,
21
               c=calib_wells.pt_color)
22
23
24
   ax2 = fig.add\_subplot(gs[0, 4])
25
   ax2.scatter(calib_wells.h, calib_wells.model_h,
26

    c=calib_wells.pt_color)

   max_h = max(calib_wells.h.max(), calib_wells.model_h.max())
27
   plt.plot([0, max_h], [0, max_h])
   fig.tight_layout()
29
   plt.savefig("./images/4_calibration.png")
30
   plt.show()
31
```

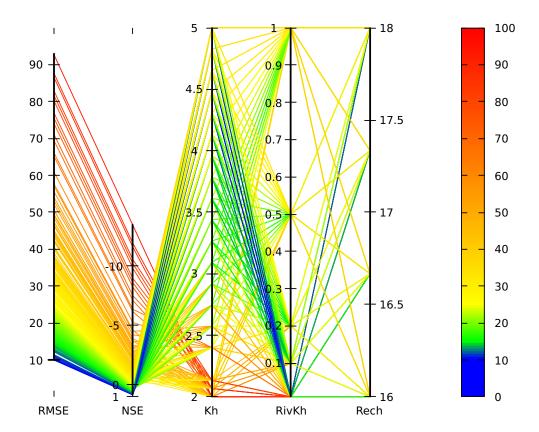


Here in the plot we can see the points above and below the model lines with red and blue color respectively. Seeing the distribution of errors we can adjust the values of Kh and RivKh as well as recharge to get the model calibrated.

3. Summary of Calibration Trials

There were a lot of calibration trials done for the parameters to reach the current value they have.

Here is the summary of final trial where the blue region shows the models which resulted in good NSE values.

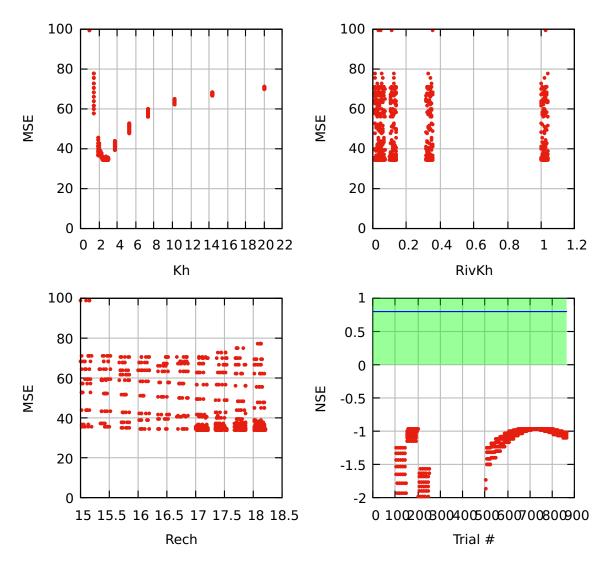


The models with ¿.8 NSE are tabulated below:

Kh	RivKh	Rech	RMSE	NSE
3.96	0.01	16.00	10.14	0.828
3.96	0.01	16.67	10.92	0.801
4.13	0.01	16.00	10.42	0.818
4.13	0.01	16.67	10.10	0.830
4.13	0.01	17.33	10.82	0.804
4.31	0.01	16.67	10.31	0.822
4.31	0.01	17.33	10.03	0.832
4.31	0.01	18.00	10.74	0.807
4.48	0.01	17.33	10.25	0.824
4.48	0.01	18.00	9.99	0.833
4.65	0.01	18.00	10.16	0.827

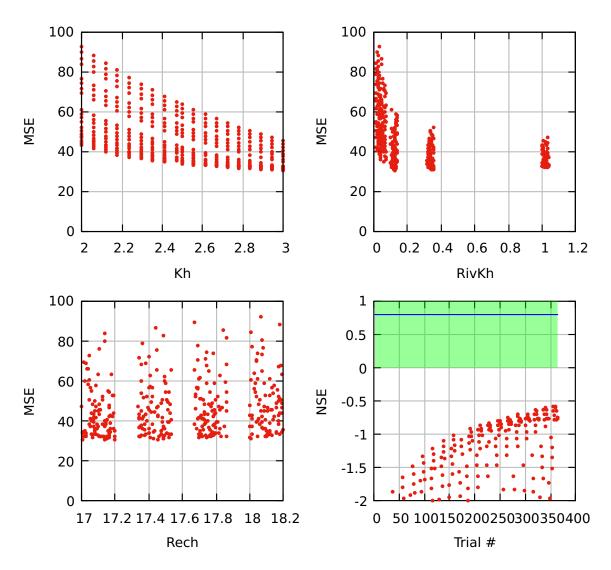
It took a lot of trials and errors to even get the model right at first, I'd like to show these in an attempt to convey how important calibration is in modeling. Before this model, we didn't calibrate any so we don't know they're doing well, giving good results or not.

For example, first batch processing on this problem couldn't find any good values for the calibration parameters.

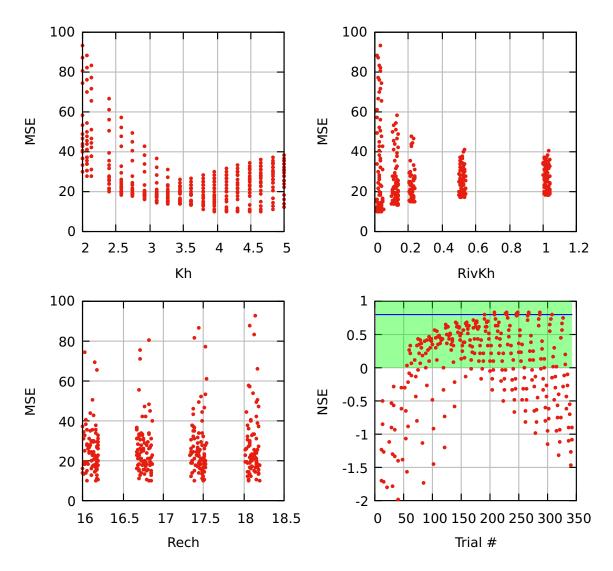


As shown in the last plot, the green area is the area with Positive NSE values, so all of our 900 trials fell under the "worse than just averaging the data" level of calibration. Which let us know something was either wrong with the model, or wrong with calculation of errors (or sampling of model head on well locations).

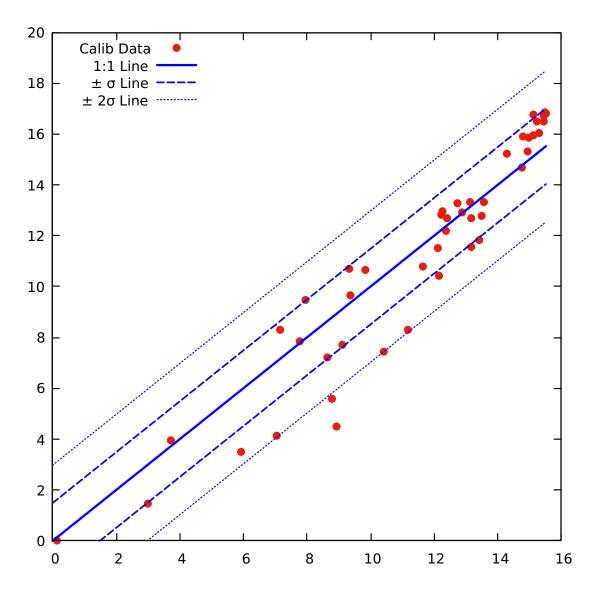
And model was improved and again we ran into same problem.



Previously we could see the Trend of K value for optimization, but here before we reached that value, it was apparent that the points were not going towards the Positive NSE values. And this made me check the sampling of wells and turns out our calculation of grid point was off, then I modified the $get_grid_points()$ and used that to get grid points instead of manually calculating it using the ΔX , ΔY myself. And finally I was able to solve this mystery and the final trials looked good.



This time the calibration looked good. I also looked at the residuals.



Most points are within 1σ of the 1:1 line, and all but 2 points are within the 2σ range. Hence I concluded the calibration.

This overall process and this model was extremely important on understanding the need of calibrating a model as a model is only good enough if it matches the observed data, and even then we can't trust the same model for other data that is wasn't calibrated for.

4. Export to vtk format

We can also export the heads data we obtained from the simulation and then visualize it using external tools like Paraview.

After running the code we get a .vtk file in the same directory as the model files, after that we can load it in Paraview, as seen in figure below.