Exp. 3: Demonstrate Matrix operations in R

Aim: To experiment with matrices, a two-dimensional data type/objects of R.

- Matrices are the R objects in which the elements are arranged in a two-dimensional rectangular layout.

- They contain elements of the same atomic types.

$$\mathbf{A} = \begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{bmatrix}$$

Exp. 3: Demonstrate Matrix operations in R

- A Matrix is created using the **matrix()** function.

Syntax: The basic syntax for creating a matrix in R is −

matrix(data, nrow, ncol, byrow, dimnames)

Following is the description of the parameters used −

- **data** is the input vector which becomes the data elements of the matrix.
- **nrow** is the number of rows to be created.
- **ncol** is the number of columns to be created.
- **byrow** is a logical clue. If TRUE then the input vector elements are arranged by row.
- **dimname** is the names assigned to the rows and columns.

Exp. 3: Demonstrate Matrix operations in R

Example: Create a matrix taking a vector of numbers as input.

 # Elements are arranged sequentially by row:

```
M <- matrix(c(3:14), nrow = 4, ncol=3, byrow = TRUE)
print(M)
```

 # it produces the following result :

```
     [,1] [,2] [,3]
[1,]    3    4    5
[2,]    6    7    8
[3,]    9   10   11
[4,]   12   13   14
```

Exp. 3: Demonstrate Matrix operations in R

Example: Create a matrix taking a vector of numbers as input.

```
# Elements are arranged sequentially by column:
M      N <- matrix(c(3:14), nrow = 4, ncol=3,byrow = FALSE)
       print(N)

# it produces the following result :
     [,1] [,2] [,3]
[1,]    3    7   11
[2,]    4    8   12
[3,]    5    9   13
[4,]    6   10   14
```

Exp. 3: Demonstrate Matrix operations in R

Example: Create a matrix taking a vector of numbers as input.

```
# Define the column and row names.
        rownames = c("row1", "row2", "row3", "row4")
        colnames = c("col1", "col2", "col3")

        P <- matrix(c(3:14), nrow =4, byrow = TRUE, dimnames = list(rownames, colnames))
        print(P)

# it produces the following result :
        col1    col2    col3
row1     3       4       5
row2     6       7       8
row3     9       10      11
row4     12      13      14
```

Exp. 3: Demonstrate Matrix operations in R

Example: Create a matrix taking a vector of numbers as input.

Accessing Elements of a Matrix:

- Elements of a matrix can be accessed by using the column and row index of the element.

- Use the **indexes (starting with 1) to access a row or a column** or an element.

Exp. 3: Demonstrate Matrix operations in R

Example: Create a matrix taking a vector of numbers as input.

```
# Define the column and row names.
        rownames = c("row1", "row2", "row3", "row4")
        colnames = c("col1", "col2", "col3")

# Create the matrix.
        P <- matrix(c(3:14), nrow =4, byrow = TRUE, dimnames = list(rownames, colnames))

# Access the element at 1st row and 3rd column.
     print(P[1,3])

# it produces the following result :
        5
```

Exp. 3: Demonstrate Matrix operations in R

Example: Create a matrix taking a vector of numbers as input.

 # Access the element at 4th row and 2nd column.

```
print(P[4,2])
```

 # it produces the following result :

```
13
```

 # Access the only the 2nd row .

```
print(P[2,])
```

 # it produces the following result :

```
col1 col2 col3
   6    7    8
```

Exp. 3: Demonstrate Matrix operations in R

Example: Create a matrix taking a vector of numbers as input.

 # Access the only the 3rd column.

```
print(P[,3])
```

 # it produces the following result :

```
row1 row2 row3 row4
5    8    11   14
```

Exp. 3: Demonstrate Matrix operations in R

Example: Create a matrix taking a vector of numbers as input.

Creating a Matrix by joining multiple vectors:

- **cbind()** **and** **rbind()** both create matrices by combining several vectors of the same length.

- **cbind()** combines vectors as columns, while **rbind()** combines them as rows.

Exp. 3: Demonstrate Matrix operations in R

 # Example:

```
x <- 1:5
y <- 6:10
z <- 11:15
```

 # Create a matrix where x, y and z are columns

cbind(x, y, z)

 # it produces the following result :

	x	y	z
[1,]	1	6	11
[2,]	2	7	12
[3,]	3	8	13
[4,]	4	9	14
[5,]	5	10	15

 # Create a matrix where x, y and z are rows

rbind(x, y, z)

 # it produces the following result :

	[,1]	[,2]	[,3]	[,4]	[,5]
x	1	2	3	4	5
Y	6	7	8	9	10
z	11	12	13	14	15

Exp. 3: Demonstrate Matrix operations in R

Example: Create a matrix taking a vector of numbers as input.

Matrix Computations:

- Various mathematical operations are performed on the matrices using the R operators. The result of the operation is also a matrix.

- The **dimensions (number of rows and columns) should be same** for the matrices involved in the operation.

- **Operations on Matrix:**
  - Addition
  - Subtraction
  - Division
  - Multiplication
  - Transpose of a Matrix
  - Creating an Identity Matrix
  - Returns the diagonal elements of Matrix
  - Dimensions of a Matrix
  - Determinant of a Matrix
  - Inverse of a Matrix

Exp. 3: Demonstrate Matrix operations in R

Example: Create a matrix taking a vector of numbers as input.

```
#Matrix Addition:
        m=matrix(rep(2,9),nrow=3)
        n=matrix(rep(3,9),nrow=3)
        p=m+n
        cat("Result of addition","\n")
        print(p)

# it produces the following result :

     [,1] [,2] [,3]
[1,]    5    5    5
[2,]    5    5    5
[3,]    5    5    5
```

Exp. 3: Demonstrate Matrix operations in R

Example: Create a matrix taking a vector of numbers as input.

```
#Matrix Subtraction:
        m=matrix(rep(2,9),nrow=3)
        n=matrix(rep(3,9),nrow=3)
        p=m-n
        cat("Result of subtraction is","\n")
        print(p)

# it produces the following result :

     [,1] [,2] [,3]
[1,]   -1   -1   -1
[2,]   -1   -1   -1
[3,]   -1   -1   -1
```

Exp. 3: Demonstrate Matrix operations in R

Example: Create a matrix taking a vector of numbers as input.

```
#Matrix Multiplication:
        m=matrix(rep(2,9),nrow=3)
        n=matrix(rep(3,9),nrow=3)
        p=m*n
        cat("Result of Multiplication is","\n")
        print(p)
```

 # it produces the following result :

```
     [,1] [,2] [,3]
[1,]    6    6    6
[2,]    6    6    6
[3,]    6    6    6
```

Exp. 3: Demonstrate Matrix operations in R

Example: Create a matrix taking a vector of numbers as input.

```
#Matrix Division:
        m=matrix(rep(2,9),nrow=3)
        n=matrix(rep(3,9),nrow=3)
        p=m/n
        cat("Result of Division is","\n")
        print(p)

# it produces the following result :
```

	[,1]	[,2]	[,3]
[1,]	0.6666667	0.6666667	0.6666667
[2,]	0.6666667	0.6666667	0.6666667
[3,]	0.6666667	0.6666667	0.6666667

Exp. 3: Demonstrate Matrix operations in R

Example: Create a matrix taking a vector of numbers as input.

```
#Check the Matrix Equality:
        m=matrix(c(1:9),nrow=3)
        n=matrix(rep(3,9),nrow=3)
        p=(m==n)
        cat("Result of Division is","\n")
        print(p)

# it produces the following result :
```

	[,1]	[,2]	[,3]
[1,]	FALSE	FALSE	FALSE
[2,]	FALSE	FALSE	FALSE
[3,]	TRUE	FALSE	FALSE

Exp. 3: Demonstrate Matrix operations in R

Example: Create a matrix taking a vector of numbers as input.

#To create an identity matrix

```
p=diag(x,nrows, ncols)
p=diag(3)
print(p)
```

 # it produces the following result :

```
     [,1] [,2] [,3]
[1,]    1    0    0
[2,]    0    1    0
[3,]    0    0    1
```

Exp. 3: Demonstrate Matrix operations in R

#To create an identity matrix

```
p=diag(3)
print(p)
```

it produces the following result :

```
     [,1] [,2] [,3]
[1,]    1    0    0
[2,]    0    1    0
[3,]    0    0    1
```

#To find the determinant of a square matrix

```
p=diag(3)
print(p)
print(det(p))
```

it produces the following result :

```
1
```

#Dimension of a matrix

```
m=matrix(c(1:9),nrow=3)
y=dim(m)
print(y)
```

it produces the following result :

```
[1] 3 3
```