# 1.1\_Cutting\_Pattern\_Synthetic

July 20, 2022

### 1 Cutting pattern

Extracting diffraction orders from Echelle spectrometer spectral image of an incandescent lamp.

#### 1.1 Imports and Setup

```
[1]: %matplotlib inline

[2]: from scipy.signal import savgol_filter
  import matplotlib.pyplot as plt
  import matplotlib as mpl
  import numpy as np
  import peakutils
```

# 2 Generate test image

A typical Echelle spectrometer image with several diffraction orders. Each diffraction order is a band with a parabolic shape. Intensity for each order has a maximum in the center. With increasing diffraction order number, the intensity usually decreases. Spacing between orders and their shape will depend on the setup. The synthetic image is helpful to demonstrate the extraction procedure of the diffraction orders.

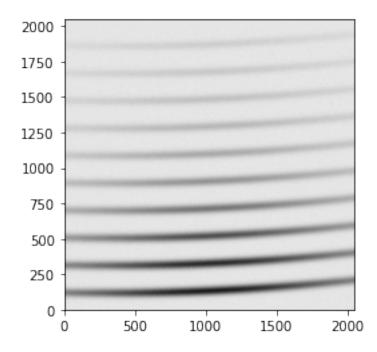
```
[3]: def gauss_fn(x, height, position, width):
    """Gaussian function"""
    return height * np.exp(-((x - position) / width) ** 2)
```

```
[12]: # image size in pixels
nx, ny = [2048, 2048]
image = np.zeros((nx, ny))

# generating order pattern
x = np.arange(nx)
o = np.arange(10) # order numbers represented by individual curves
c = 3e-5 # curvature of each curve
x_c = 300 # central symmetry point in x
y_b = 120 # bottom point of the first curve in y
y_s = 193 # spread of individual curves in y
```

```
pt = np.array([(c * (x - x_c - i ** 2) ** 2 + y_b + i * y_s) for i in o]).
 →astype(int)
# add Gaussian profiles along the generated order lines
width = 200
profy = np.linspace(0, 2, width)
# add intensity attenuation
intensity = 1 / ((x - nx / 2) ** 2 + 1e6)
intensity = intensity / intensity.max()
xx = np.arange(10)
vv = 1 / ((xx - 0.1) ** 2 + 10)
vv = vv / vv.max() * 20
# add bands
for j, p in enumerate(pt):
   for i, y in enumerate(p):
        image[y - width // 2 : y + width // 2 + width % 2, i] = \
            gauss_fn(profy, vv[j] * intensity[i], 1, 0.3)
# add noise
image += np.random.rand(nx, ny) * 5
scale = 1
plt.imshow(image, origin="lower", cmap="binary")
# norm=mpl.colors.LogNorm(image.min(), image.max() * scale))
```

#### [12]: <matplotlib.image.AxesImage at 0x1ae7ab78e50>



# 3 Extract peak positions

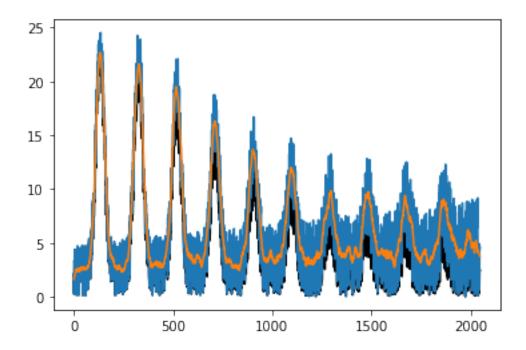
## 3.1 Check signal, select amplifier

Because intensity for higher orders may drop significantly, for best peak detection it is better to amplify weak intensities. Here, select this amplifier function.

## 3.1.1 Smooth signal

```
[5]: x = np.arange(nx)
y = image[:, 1000]
ysm = savgol_filter(y, 21, 1)
amp = np.exp(3e-4 * x) # amplify weak signal for higher orders
plt.plot(y, 'k')
plt.plot(y * amp)
plt.plot(ysm * amp)
```

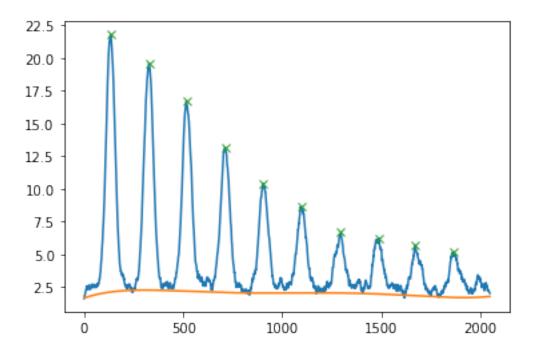
#### [5]: [<matplotlib.lines.Line2D at 0x1ae75b829d0>]



#### 3.1.2 Check

```
[6]: # calculate baseline
base = peakutils.baseline(ysm, 6)
# adjust parameters for correct peak detection
ind = peakutils.indexes(ysm-base, thres=.1, min_dist=80)
plt.plot(ysm)
plt.plot(base)
plt.plot(ind, ysm[ind], 'x')
```

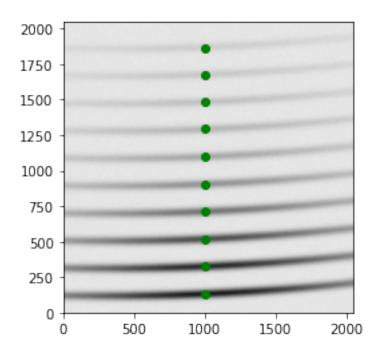
#### [6]: [<matplotlib.lines.Line2D at 0x1ae75bfd670>]



## 3.2 Peak positions over image

```
[7]: plt.imshow(image, origin="lower", cmap="binary")
# norm=mpl.colors.LogNorm(image.min(), image.max() * scale))
x = np.ones(ind.shape[0]) * 1000
plt.plot(x, ind, 'og')
```

[7]: [<matplotlib.lines.Line2D at 0x1ae75c6b670>]



#### 3.3 Detect all and plot

Define positions for peak selection. Even distribution from center, which is the brightest.

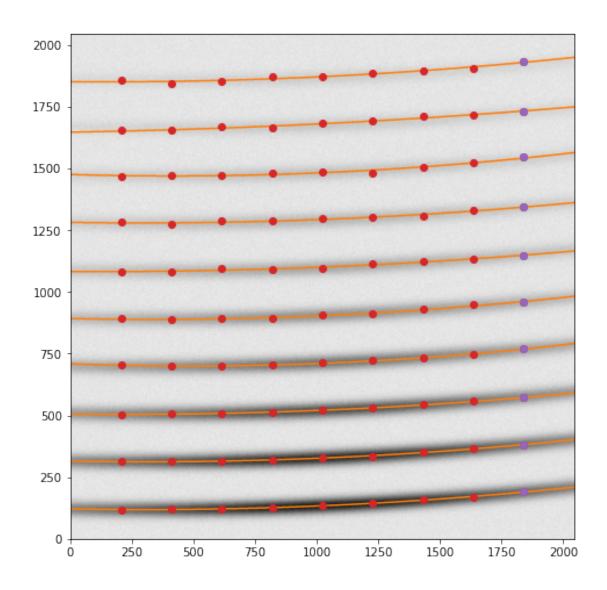
If not all peaks are detected correctly, there will be different number of results for each x pixel in xselec. If so, no fitting is done. Adjust peak finding parameters thres and  $min_dist$  to get all peaks, and no extra.

```
[8]: dx = nx // 10
    n = 4
     xselect = np.arange(nx // 2 - dx * n, nx // 2 + dx * n + 1, dx, dtype=int)
     peaks = []
     pvals = []
     for xind in xselect:
         y=image[:, xind]
         ysm = savgol_filter(y, 21, 1)
         base = peakutils.baseline(ysm, 6)
         ind = peakutils.indexes(ysm - base, thres=.1, min_dist=180)
         peaks.append(ind)
         pvals.append(ysm[ind])
     # check if all peaks were detected
     uniques = np.unique([len(i) for i in peaks])
     if uniques.shape[0] > 1:
         print("Adjust peak finding parameters,", uniques)
```

```
else:
    print("Shape's good!\nBut check the image, did we get everything?")
    pat_y = np.array(peaks)
    # fit quadratics
   fits = [np.poly1d(np.polyfit(xselect, i, 2)) for i in pat_y.T]
    x = np.arange(nx)
    pattern = np.array([f(x) for f in fits], dtype=int)
    # plot fits
    for p in pattern:
       plt.plot(p, 'C1')
plt.imshow(image, origin="lower", cmap="binary")
# norm=mpl.colors.LogNorm(image.min(), image.max() * scale))
# plot peaks
for ind,px in zip(peaks, xselect):
    x = np.ones(ind.shape[0]) * px
    plt.plot(x, ind, 'oC3')
plt.plot(x, ind, 'oC4')
plt.gcf().set_size_inches([8, 8])
```

Shape's good!

But check the image, did we get everything?



# 4 Save current image and pattern

```
[9]: if uniques.shape[0] == 1:
    np.savetxt('pattern_image_synthetic.txt', image)
    np.savetxt('pattern.txt', pattern.T, fmt='%.d')
```