中国科学院大学

2022 年招收攻读硕士学位研究生入学统一考试试题答案

——公式参考中科大信号与系统

试题答案仅供参考

一、选择

解析:

$$u[n-1] = \sum_{k=1}^{\infty} \delta[n-k] \quad \sum_{k=-\infty}^{\infty} \delta[k-1] = 1$$

解析:

$$f(-2t+3) = f[-2(t-\frac{3}{2})] \Leftrightarrow f(-2t)$$
右移 $\frac{3}{2}$ $f(-2t)$ 看成一个整体

二、判断

解析:未指明系统是 LTI 系统,且初始状态必须为 0

2 🗸

解析: 稳定系统才存在频率响应

3. **x**

解析: 若系统因果, 则正确, 若反因果, 则错误

4. **x**

解析:

$$\delta(at) = \frac{1}{|a|} \delta(t)$$

解析:

$$F(jw) = \frac{1}{2}F(\frac{jw}{2})e^{-\frac{5}{2}jw}$$

解析:

$$E\{A\cos wtA\cos w(t-\tau)\} = \frac{A^2}{2}E\{\cos(w\tau) + \cos(2wt - w\tau)\} = \frac{A^2}{2}\cos(w\tau)$$

9. ✓

10. 🗸

解析:

$$y[n] = \sum_{m=-\infty}^{n} x[m] = \sum_{m=-\infty}^{n} x[m]u[-m+n] = x[n] * u[n]$$

三、填空

1. 10

解析:

$$f(t) = 4\cos 20\pi t + 2\cos 30\pi t$$

$$T_1 = \frac{1}{10}$$
 $T_2 = \frac{1}{15}$ $T = \frac{1}{5}$

基频:
$$w_0 = \frac{2\pi}{T} = 10\pi$$
 $w_2 = 20\pi$ $w_3 = 30\pi$ 谐波之间是正交的

$$x(t) = A \sin wt / A \cos wt \quad P = \frac{A^2}{2}$$

$$\therefore P = \frac{1}{2}(4^2 + 2^2) = 10$$

$$2. \quad \frac{4\pi}{w_m} s$$

解析:

$$f(t/4) \longleftrightarrow 4F(4w) \quad 4w = w_m \quad w_m' = w_m/4 \quad T_s = \frac{2\pi}{w_s} = \frac{2\pi}{2w_m'} = \frac{\pi}{w_m/4} = \frac{4\pi}{w_m} s$$

3.
$$\int_{-\infty}^{\infty} f(t)dt \qquad \frac{1}{2\pi} \int_{-\infty}^{\infty} f(t)dw$$

解析:

$$F(w) = \int_{-\infty}^{\infty} f(t)e^{-jwt}dt \quad F(0) = \int_{-\infty}^{\infty} f(t)dt$$

$$f(t) = \frac{1}{2\pi} \int_{-\infty}^{\infty} f(t)e^{jwt} dw \quad f(0) = \frac{1}{2\pi} \int_{-\infty}^{\infty} f(t) dw$$

4. 4

5. 不稳定

解析

$$H(z) = \frac{1}{1+z^{-1}} \cdot \frac{1}{2-z^{-1}}$$
 极点 $\frac{1}{2}$,-1 单位圆上存在极点不稳定

解析:

$$7. \quad \frac{1}{2}y(2t)$$

解析:

$$y(t) = f(t) * h(t) \longleftrightarrow Y(w) = F(w) \cdot H(w) \quad Y(\frac{w}{2}) = F(\frac{w}{2}) \cdot H(\frac{w}{2})$$

$$f(2t) \longleftrightarrow \frac{CFT}{2} \to \frac{1}{2} F(\frac{w}{2}) \quad h(2t) \longleftrightarrow \frac{CFT}{2} \to \frac{1}{2} H(\frac{w}{2})$$

$$f(2t) * h(2t) \longleftrightarrow \frac{CFT}{2} \to \frac{1}{2} F(\frac{w}{2}) \cdot \frac{1}{2} H(\frac{w}{2}) = \frac{1}{2} \cdot \frac{1}{2} Y(\frac{w}{2})$$

$$\frac{1}{2} \cdot \frac{1}{2} Y(\frac{w}{2}) \longleftrightarrow \frac{ICFT}{2} \to \frac{1}{2} y(2t)$$

四、计算

$$y_{uzi}[n] = 8 \cdot (-1)^{n} u[n] - 20(-2)^{n} u[n]$$
1.
$$y_{uzs}[n] = -\frac{1}{2} \cdot (-1)^{n} u[n] + \frac{4}{3} (-2)^{n} u[n] + \frac{1}{6} u[n]$$

2.
$$H(z) = \frac{2}{1 + 2z^{-1}} - \frac{1}{1 + z^{-1}}$$
$$h[n] = 2 \cdot (-2)^{n} u[n] - (-1)^{n} u[n]$$

3.
$$y[n] = y_{uzi}[n] + \{y_{uzs}[n] - y_{uzs}[n-5]\}$$

五、计算

1

$$f_1(t) = Sa(100\pi t)$$
 $f_2(t) = Sa(200\pi t)$
 $f(t) = f_1(t) * f_2(t)$

$$w_{m1} = 100\pi$$
 $w_{m2} = 200\pi$ $w_m = 300\pi$ $T_s = \frac{\pi}{w_m} = \frac{1}{300}s$

2.

$$\begin{split} Sa(Wt) & \stackrel{CFT}{\longleftrightarrow} \frac{\pi}{W} R_{2W}(w) \\ f_1(t) & \stackrel{CFT}{\longleftrightarrow} \frac{1}{100} R_{2\times 100}(w) \quad f_2(t) & \stackrel{CFT}{\longleftrightarrow} \frac{1}{200} R_{2\times 200}(w) \\ f(t) & = f_1(t) * f_2(t) & \stackrel{CFT}{\longleftrightarrow} F(w) = \frac{1}{2\pi} \cdot \frac{1}{20000} R_{2\times 100}(w) * R_{2\times 200}(w) \end{split}$$

$$F(w) = \begin{cases} \frac{1}{200} (w + 300\pi) & -300\pi \le w \le -100\pi \\ \frac{1}{200} & |w| \le 100\pi \\ \frac{1}{200} (-w + 300\pi) & 100\pi \le w \le 300\pi \end{cases}$$

$$f_{s}(t) = f(t) \cdot p(t) \longleftrightarrow \frac{1}{2\pi} F_{s}(w) * \frac{2\pi}{T} \sum_{k=-\infty}^{\infty} \delta(w - k \frac{2\pi}{T}) = \frac{1}{T} \sum_{k=-\infty}^{\infty} F(w - k \frac{2\pi}{T}) = 300 \sum_{k=-\infty}^{\infty} F(w - k 600\pi)$$

六、计算

/

七、计算

1. 功率信号

2

$$\begin{split} R_f(\tau) &= E\{A\cos 100\pi t \cos 1000\pi t A \cos 100\pi (t-\tau) \cos 1000\pi (t-\tau)\} \\ &= \frac{A^2}{4} E\{[\cos 100\pi \tau + \cos(200\pi t - 100\pi\tau)][\cos 1000\pi \tau + \cos(2000\pi t - 1000\pi\tau)]\} \\ &= \frac{A^2}{4} E\{\cos 100\pi \tau \cdot \cos 1000\pi \tau \cdot \cos 1000\pi \tau \cdot \cos(2000\pi t - 1000\pi\tau) + \cos(200\pi t - 100\pi\tau) \cdot \cos 1000\pi \tau + \cos(200\pi t - 100\pi\tau) \cdot \cos(2000\pi t - 1000\pi\tau)\} \\ &= \frac{A^2}{4} E\{\cos 100\pi \tau \cdot \cos 1000\pi \tau + \cos(200\pi t - 100\pi\tau) \cdot \cos(2000\pi t - 1000\pi\tau)\} \\ &= \frac{A^2}{4} \cos 100\pi \tau \cdot \cos 1000\pi \tau + \frac{A^2}{4} E\{\cos(200\pi t - 100\pi\tau) \cdot \cos(2000\pi t - 1000\pi\tau)\} \\ &= \frac{A^2}{8} [\cos 900\pi \tau + \cos 1100\pi\tau] + \frac{A^2}{4} E\{\frac{\cos(1800\pi t - 900\pi\tau) + \cos(2200\pi t - 1100\pi\tau)}{2}\} \\ &= \frac{A^2}{8} [\cos 900\pi \tau + \cos 1100\pi\tau] + \frac{A^2}{4} E\{\frac{\cos(1800\pi t - 900\pi\tau) + \cos(2200\pi t - 1100\pi\tau)}{2}\} \\ &= \frac{A^2}{8} [\cos 900\pi \tau + \cos 1100\pi\tau] + \frac{A^2}{4} E\{\frac{\cos(1800\pi t - 900\pi\tau) + \cos(2200\pi t - 1100\pi\tau)}{2}\} \\ &= \frac{A^2}{8} [\cos 900\pi \tau + \cos 1100\pi\tau] + \frac{A^2}{4} E\{\frac{\cos(1800\pi t - 900\pi\tau) + \cos(2200\pi t - 1100\pi\tau)}{2}\} \\ &= \frac{A^2}{8} [\cos 900\pi \tau + \cos 1100\pi\tau] + \frac{A^2}{4} E\{\frac{\cos(1800\pi t - 900\pi\tau) + \cos(2200\pi t - 1100\pi\tau)}{2}\} \\ &= \frac{A^2}{8} [\cos 900\pi \tau + \cos 1100\pi\tau] + \frac{A^2}{4} E\{\frac{\cos(1800\pi t - 900\pi\tau) + \cos(2200\pi t - 1100\pi\tau)}{2}\} \\ &= \frac{A^2}{8} [\cos 900\pi \tau + \cos 1100\pi\tau] + \frac{A^2}{4} E\{\frac{\cos(1800\pi t - 900\pi\tau) + \cos(2200\pi t - 1100\pi\tau)}{2}\} \\ &= \frac{A^2}{8} [\cos 900\pi \tau + \cos 1100\pi\tau] + \frac{A^2}{4} E\{\frac{\cos(1800\pi t - 900\pi\tau) + \cos(2200\pi t - 1100\pi\tau)}{2}\} \\ &= \frac{A^2}{8} [\cos 900\pi \tau + \cos 1100\pi\tau] + \frac{A^2}{4} E\{\frac{\cos(1800\pi t - 900\pi\tau) + \cos(2200\pi t - 1100\pi\tau)}{2}\} \\ &= \frac{A^2}{8} [\cos 900\pi \tau + \cos 1100\pi\tau] + \frac{A^2}{4} E\{\frac{\cos(1800\pi t - 900\pi\tau) + \cos(2200\pi t - 1100\pi\tau)}{2}\} \\ &= \frac{A^2}{8} [\cos 900\pi \tau + \cos 1100\pi\tau] + \frac{A^2}{4} E\{\cos(1800\pi t - 900\pi\tau) + \cos(180\pi\tau) + \frac{A^2}{4} E\{\cos(1800\pi t - 900\pi\tau) +$$

3

$$\phi_f(w) = F^{-1} \{ \frac{A^2}{8} [\cos 900\pi\tau + \cos 1100\pi\tau] \} = \frac{\pi A^2}{8} \{ \delta(w - 1100\pi) + \delta(w + 1100\pi) + \delta(w - 900\pi) + \delta(w + 900\pi) \}$$

$$P = \frac{1}{2\pi} \int_{-\infty}^{\infty} P(w) dw = \frac{1}{2\pi} \cdot \frac{\pi A^2}{8} \cdot [1 + 1 + 1 + 1] = \frac{A^2}{4}$$