

In the following text, substitute  $A$ ,  $B$ ,  $C$ , and  $D$  with numbers that make the paragraph true.  
Note: Assume that  $n$  is an integer that is greater than or equal to 3.

The interior angles of a polygon with  $n$  sides sum to  $180^\circ \times (n - A)$  degrees, and a regular polygon with  $n$  sides have interior angles that are each  $\frac{180^\circ \times (n - A)}{n}$  degrees. However, the sum of the exterior angles is always  $B$  degrees, regardless of  $n$ . The number of diagonals that can be drawn from a single vertex is always  $(n - C)$ , and the total number of diagonals in the entire polygon is given by  $\frac{n(n - C)}{D}$ .

## Solution:

Answer :  $A = 2, B = 360, C = 3, D = 2$ .

Proof: In a polygon with  $n$  sides, drawing all the diagonals from a single vertex will create  $(n - 2)$  triangles inside the polygon. Therefore, the sum of all the interior angles is  $180^\circ \times (n - 2)$  (**A**). To compute the angle of each interior angle in a regular polygon, you can simply divide the sum of the interior angles by the number of angles, which is equivalent to the number of sides  $n$ . The expression used to compute this is:  $\frac{180^\circ \times (n-2)}{n}$  (**A**). The sum of all exterior angles is given by the expression:

$$(180^\circ \times n) - (180^\circ \times (n - 2)) \quad (1)$$

which simplifies to:

$$180^\circ \times n - 180^\circ \times n + 360^\circ = 360^\circ \quad (2)$$

When drawing diagonals from a single vertex in a polygon with  $n$  sides, you connect that single vertex to all other vertices other than itself and its two adjacent vertices. Therefore, the number of diagonals that can be drawn from a single vertex is  $(n - 3)$  (**C**). The expression used to calculate the total number of diagonals in an  $n$  sided polygon is  $\frac{n(n-3)}{2}$  (**D**) . This formula accounts for the fact that each diagonal is counted twice (once from each endpoint), so we divide by 2 to get the correct total.