

In the following text, substitute A , B , C , and D with numbers that make the paragraph true.
Note: Assume that n is an integer that is greater than or equal to 3.

The interior angles of a polygon with n sides sum to $180^\circ \times (n - \mathbf{A})$ degrees, and a regular polygon with n sides have interior angles that are each $\frac{180^\circ \times (n - \mathbf{A})}{n}$ degrees. However, the sum of the exterior angles is always \mathbf{B} degrees, regardless of n . The number of diagonals that can be drawn from a single vertex is always $(n - \mathbf{C})$, and the total number of diagonals in the entire polygon is given by $\frac{n(n - \mathbf{C})}{\mathbf{D}}$.

Solution:

Answer : $A = 2, B = 360, C = 3, D = 2$.

Proof: In a polygon with n sides, drawing all the diagonals from a single vertex will create $(n - 2)$ triangles inside the polygon. Therefore, the sum of all the interior angles is $180^\circ \times (n - 2)$ (**A**). To compute the angle of each interior angle in a regular polygon, you can simply divide the sum of the interior angles by the number of angles, which is equivalent to the number of sides n . The expression used to compute this is: $\frac{180^\circ \times (n - 2)}{n}$ (**A**). The sum of all exterior angles is given by the expression:

$$(180^\circ \times n) - (180^\circ \times (n - 2)) \quad (1)$$

which simplifies to:

$$180^\circ \times n - 180^\circ \times n + 360^\circ = \mathbf{360}(\mathbf{B}) \quad (2)$$

When drawing diagonals from a single vertex in a polygon with n sides, you connect that single vertex to all other vertices other than itself and its two adjacent vertices. Therefore, the number of diagonals that can be drawn from a single vertex is $(n - 3)$ (**C**). The expression used to calculate the total number of diagonals in an n sided polygon is $\frac{n(n-3)}{2}$ (**D**). This formula accounts for the fact that each diagonal is counted twice (once from each endpoint), so we divide by 2 to get the correct total.