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Assignment: Home Work 3

Problem-1:

Denoise the image (Img-1) using Butterworth Notch Reject filter of order 4. Show the noisy image, clean image, and the noise pattern (by taking IDFT of the filtered out frequencies) in juxtaposition. Note: Use appropriate values of cutoff frequencies taking guidance from the DFT spectrum of the image.

Noisy Image:

```
I2 = imread('Img-1.tif');
I = im2double(I2)
%subplot(4,4,1);
figure(1);
imshow(I)
title('Noisy Image');
```



Spectrum:

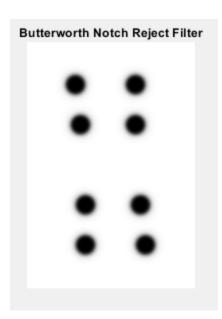
```
F = fft2(I);
Fsh = fftshift(F);
S2 = log(1+abs(Fsh));
figure(2);
%subplot(4,4,2);
imshow(S2,[])
title('Fourier Transformed Spectrum')
```

Fourier Transformed Spectrum

ButterWorth Notch Reject Filter:

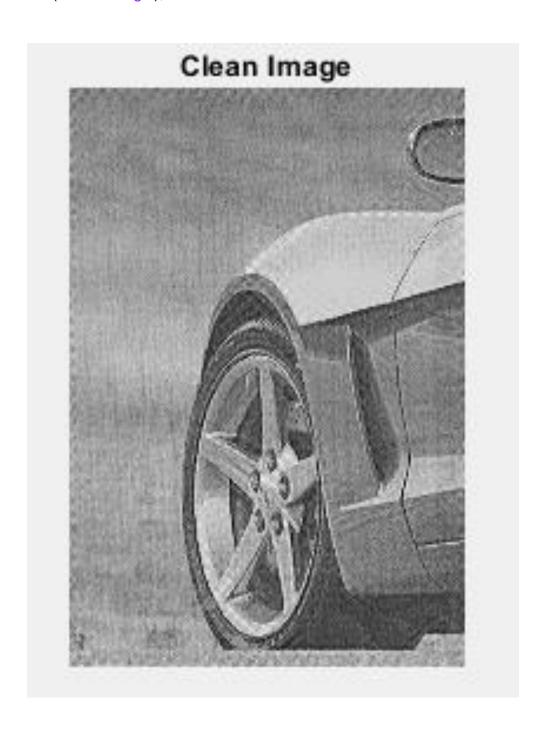
```
sz = size(I)
D0 = 10; %Changed
%h=figure;
%datacursormode(S2, 'on')
%h=figure;
HNR1 = ones(sz(1), sz(2));
HNRplus1 = ones(sz(1), sz(2));
HNRneg1 = ones(sz(1), sz(2));
for u = 1:sz(1)
           for v = 1:sz(2)
                      D1 = sqrt((u-sz(1)/2-80)^2 + ((v-sz(2)/2)-35)^2); + sqrt((u-sz(1)/2-80)^2)
55)^2 + ((v-sz(2)/2)-86)^2;
                      Dnv1 = sqrt((u-sz(1)/2+80)^2 + ((v-sz(2)/2)+35)^2); % + sqrt((u-sz(1)/2+80)^2) + ((v-sz(2)/2)+35)^2); % + sqrt((u-sz(1)/2+80)^2) + ((v-sz(2)/2)+35)^2) + ((v-sz(2)/2)+35)^2 + ((v-sz(2)/
sz(1)/2+55)^2 + ((v-sz(2)/2)+86)^2;
                      HNRplus1(u, v) = 1/(1+(D0/D1)^8); Changed
                      HNRneg1(u,v) = 1/(1+(D0/Dnv1)^8); Changed
           end
end
HNR1 = HNRplus1.*HNRneg1;
HNR2 = ones(sz(1), sz(1));
HNRplus2 = ones(sz(1), sz(2));
HNRneg2 = ones(sz(1), sz(2));
for u = 1:sz(1)
           for v = 1:sz(2)
                      D2 = sqrt(((u-sz(1)/2)-40)^2 + (((v-sz(2)/2)-30)^2));
                      Dnv2 = sqrt(((u-sz(1)/2)+40)^2 + (((v-sz(2)/2)+30)^2));
                      HNRplus2(u,v) = 1/(1+(D0/D2)^8); Changed
                      HNRneg2(u,v) = 1/(1+(D0/Dnv2)^8); Changed
           end
end
HNR2 = HNRplus2.*HNRneg2;
HNR3 = ones(sz(1), sz(2));
HNRplus3 = ones(sz(1), sz(2));
HNRneg3 = ones(sz(1), sz(2));
for u = 1:sz(1)
           for v = 1:sz(2)
                      D3 = sqrt((u-sz(1)/2-(40))^2 + ((v-sz(2)/2)-(-25))^2);
                      Dnv3 = sqrt((u-sz(1)/2+(40))^2 + ((v-sz(2)/2)+(-25))^2);
                      HNRplus3(u,v) = 1/(1+(D0/D3)^8); Changed
                      HNRneg3(u,v) = 1/(1+(D0/Dnv3)^8); Changed
           end
end
```

```
HNR3 = HNRplus3.*HNRneg3;
HNR4 = ones(sz(1), sz(2));
HNRplus4 = ones(sz(1), sz(2));
HNRneg4 = ones(sz(1), sz(2));
for u = 1:sz(1)
    for v = 1:sz(2)
        D4 = sqrt((u-sz(1)/2-80)^2 + ((v-sz(2)/2)-(-25))^2);
        Dnv4 = sqrt((u-sz(1)/2+80)^2 + ((v-sz(2)/2)+(-25))^2);
        HNRplus4(u,v) = 1/(1+(D0/D4)^8); Changed
        HNRneg4(u,v) = 1/(1+(D0/Dnv4)^8); Changed
    end
end
HNR4 = HNRplus4.*HNRneg4;
%HNR1234 = HNR1.*HNR2.*HNR3.*HNR4;
HNR1234 = HNR1.*HNR2.*HNR3.*HNR4;
%figure(3);imshow(HNR1,[])
%figure(3);imshow(HNR1,[])
%title('Butterworth Notch Reject Filter');
figure(3);imshow(HNR1234,[])
%figure(3);imshow(HNR1,[])
title('Butterworth Notch Reject Filter');
```



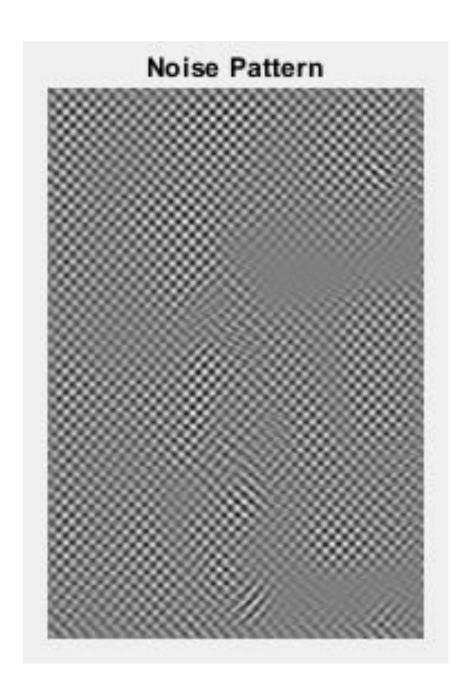
Clean Image:

lbSs = real(ifft2(ifftshift(M)));%Changed
figure(5);imshow(lbSs,[])
title('Clean Image');



Noise Pattern through Notch Pass Filter:

G = (1-HNR1234).*Fsh; NP = real(ifft2(ifftshift(G))) figure(6); imshow(NP,[]) title('Noise Pattern');

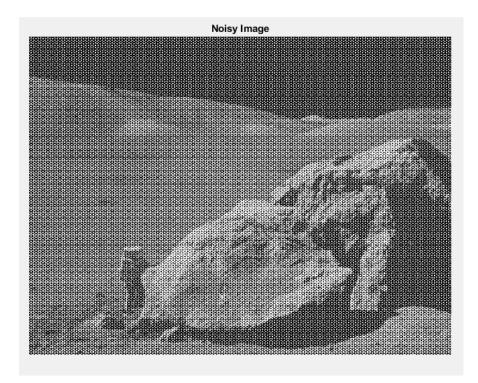


Problem-2:

Denoise the image (Img-2) using Butterworth Band Reject filter of order 4. Show the noisy image, clean image, and the noise pattern (by taking IDFT of the filtered out frequencies) in juxtaposition. Note: Use appropriate values of cutoff frequency and the band width taking guidance from the DFT spectrum of the image.

Noisy Image:

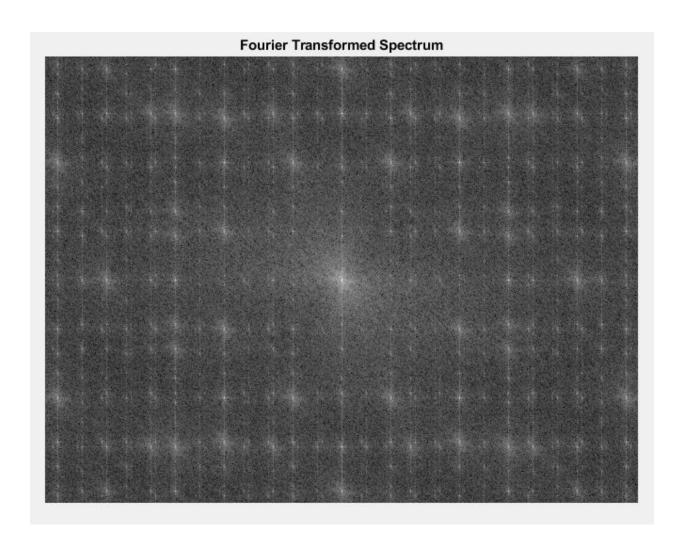
```
I2 = imread('Img-2.tif');
I = im2double(I2)
%subplot(4,4,1);
figure(1);
imshow(I)
title('Noisy Image');
```



Fourier Transformation:

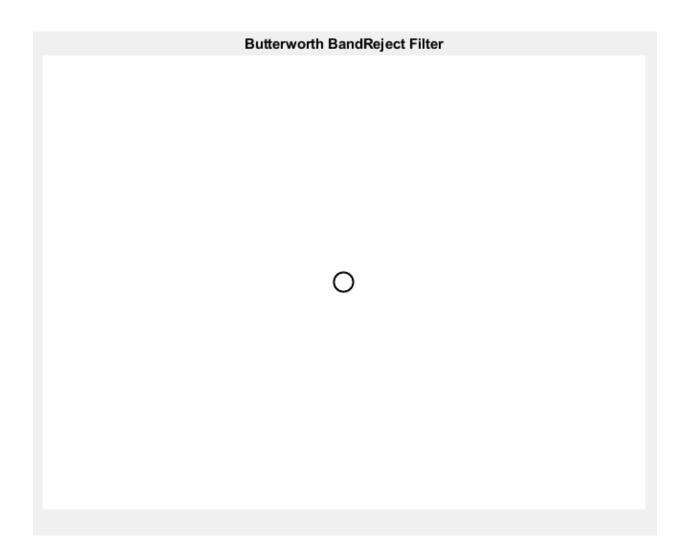
```
F = fft2(I);

%S = abs(F);
Fsh = fftshift(F);
S2 = log(1+abs(Fsh));
figure(2);
%subplot(4,4,2);
imshow(S2,[])
title('Fourier Transformed Spectrum')
impixelinfo(figure(2));
```



ButterWorth Band Reject Filter:

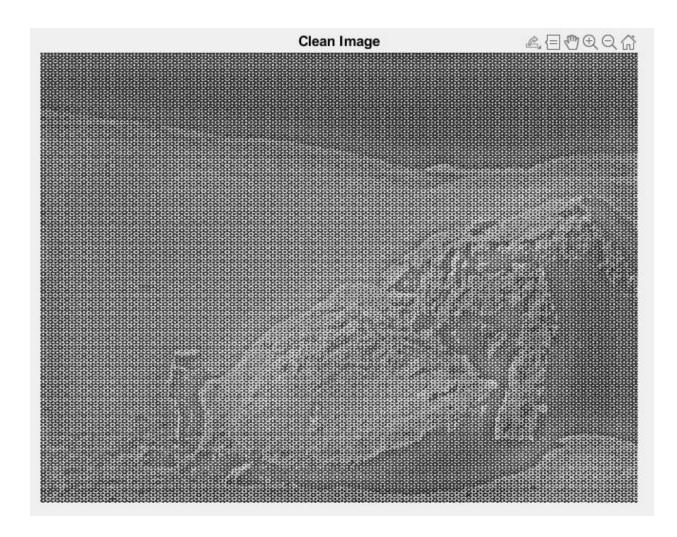
```
\begin{split} sz &= size(I); \\ D0 &= 10; \, W = 2; \\ HBW &= ones(sz(1),sz(2)); \\ for \, u &= 1:sz(1) \\ for \, v &= 1:sz(2) \\ D &= sqrt((u-sz(1)/2)^2 + (v-sz(2)/2)^2); \\ HBW(u,v) &= 1/(1 + ((D^*W/(D^2-D0^2))^4)); \\ end \\ end \\ figure(3); \\ imshow(HBW,[]); \, title('Butterworth \, BandReject \, Filter'); \end{split}
```



Clean Image:

lbS = ifftshift(BR);
lbSs = ifft2(lbS);
figure(5);imshow(lbSs,[])

title('Clean Image');



Noise Pattern through Band Pass Filter:

G = (1-HBW).*Fsh; NP = real(ifft2(ifftshift(G))) figure(6); imshow(NP,[]) title('Noise Pattern');

