

NumPy (4.1)

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References

1. Refer guidelines: Ch4: 4.1-4.2, Usage of rand(), randn() and randint() functions of NumPy
2. <https://numpy.org/doc/stable/user/quickstart.html>
(<https://numpy.org/doc/stable/user/quickstart.html>).
3. W3Schools tutorial: https://www.w3schools.com/python/numpy/numpy_intro.asp
(https://www.w3schools.com/python/numpy/numpy_intro.asp).

- homogeneous multidimensional array
- It is a table of elements (usually numbers), all of the same type, indexed by a tuple of non-negative integers.
- In NumPy dimensions are called axes.

For example:

- the array for the coordinates of a point in 3D space, [1, 2, 1], has one axis.
- this axis has 3 elements in it, so we say it has a length of 3.

In [2]: `import numpy as np`

numpy.array function

- Can create an array from a regular Python list or tuple using the array function.
- The type of the resulting array is deduced from the type of the elements in the sequences.

In [3]: `# 1-D array
arr1=np.array([1,2,3,4,5]) #create using a list
print(arr1)`

[1 2 3 4 5]

```
# 1-D array  
arr1=np.array((1,2,3,4,5)) #create using a tuple  
print(arr1)
```

In [4]: *# ERROR: calling array with multiple arguments, rather than providing a single sequence as an argument*
`arr1=np.array(1,2,3,4,5)`

```
-----
--
TypeError                                Traceback (most recent call last)
C:\Users\MONAAD~1\AppData\Local\Temp\ipykernel_33432\2955937289.py in <module>
      1 # ERROR: calling array with multiple arguments, rather than providing a single sequence as an argument
----> 2 arr1=np.array(1,2,3,4,5)

TypeError: array() takes from 1 to 2 positional arguments but 5 were given
```

In [5]: *# 0-D array*
`arr0=np.array(56)`
`print(arr0)`
`arr0.dtype`

56

Out[5]: `dtype('int32')`

The array below has 2 axes
 The first axis has a length of 2, the second axis has a length of 5.

In [6]: *# 2-D array*
transforms sequences of sequences into two-dimensional arrays,
`arr2=np.array([[1,2,3,4,5],[6,7,8,9,10]])`
`print(arr2)`

```
[[ 1  2  3  4  5]
 [ 6  7  8  9 10]]
```

In [7]: *# 3-D array*
`arr3=np.array([[[1,2,3,4,5],[6,7,8,9,10],[11,12,13,15,16]]])`
`print(arr3)`
`print(arr3.shape)`

```
[[[ 1  2  3  4  5]
   [ 6  7  8  9 10]
   [11 12 13 15 16]]]
(1, 3, 5)
```

Data types in Numpy

https://www.w3schools.com/python/numpy/numpy_data_types.asp
https://www.w3schools.com/python/numpy/numpy_data_types.asp

Below is a list of all data types in NumPy and the characters used to represent them.

```
i - integer
b - boolean
u - unsigned integer
f - float
c - complex float
m - timedelta
M - datetime
O - object
S - string
U - unicode string
V - fixed chunk of memory for other type ( void )
```

ndarray.ndim

ndarray.ndim:
- the number of axes (dimensions) of the array

```
In [90]: arr2.ndim
```

```
Out[90]: 2
```

ndarray.size

ndarray.size:
- the total number of elements of the array.
- This is equal to the product of the elements of shape.

```
In [8]: print(arr2)
print(arr2.size)
```

```
[[ 1  2  3  4  5]
 [ 6  7  8  9 10]]
10
```

ndarray.dtype

ndarray.dtype:
- an object describing the type of the elements in the array.
- One can create or specify dtype's using standard Python types.
- Additionally NumPy provides types of its own
- e.g. `numpy.int32`, `numpy.int16`, and `numpy.float64`, etc.

```
In [92]: arr2.dtype
```

```
Out[92]: dtype('int32')
```

In [12]: *#The type of the array can also be explicitly specified at creation time:*
`c = np.array([[1, 2], [3, 4]], dtype=complex)`
`print(c)`
`print(c.dtype)`

```
[[1.+0.j 2.+0.j]
 [3.+0.j 4.+0.j]]
complex128
```

ValueError: In Python ValueError is raised when the type of passed argument to a function is unexpected/incorrect.

In [94]: `arrE = np.array(['a', '2', '3'], dtype='i')`

```
-----
--
ValueError                                Traceback (most recent call last)
C:\Users\MONAAD~1\AppData\Local\Temp\ipykernel_34036\242163293.py in <module>
----> 1 arrE = np.array(['a', '2', '3'], dtype='i')

ValueError: invalid literal for int() with base 10: 'a'
```

ndarray.shape

ndarray.shape

- This is a tuple of integers indicating the size of the array in each dimension.
- For a matrix with n rows and m columns, shape will be (n,m).
- The length of the shape tuple is therefore the number of axes, ndim.

In [13]: `print(arr2)`
`arr2.shape`

```
[[ 1  2  3  4  5]
 [ 6  7  8  9 10]]
```

Out[13]: (2, 5)

```
In [16]: print(arr0)
print("dimension =", arr0.ndim) # number of axes
print("shape =", arr0.shape) #tuple of integers indicating the size of the
print("size =", arr0.size) # total number of elements
print("type =", arr0.dtype)
type(arr0)
```

```
56
dimension = 0
shape = ()
size = 1
type = int32
```

Out[16]: numpy.ndarray

```
In [97]: print(arr2)
print("dimension =", arr2.ndim) # number of axes
print("shape =", arr2.shape) #tuple of integers indicating the size of the
print("size =", arr2.size) # total number of elements
```

```
[[ 1  2  3  4  5]
 [ 6  7  8  9 10]]
dimension = 2
shape = (2, 5)
size = 10
```

numpy.arange() function

numpy.arange() function

- used to generate an array with evenly spaced values within a specified interval
- function returns a one-dimensional array of type numpy.ndarray.

SYNTAX: numpy.arange([start,]stop, [step,]dtype=None)

```
In [98]: my_arr = np.arange(10) # returns an ndarray
print(type(my_arr))
print(my_arr)
print(my_arr.dtype)
```

```
<class 'numpy.ndarray'>
[0 1 2 3 4 5 6 7 8 9]
int32
```

```
In [99]: a = np.arange(10.0)
print(a)
print(a.dtype)
```

```
[0. 1. 2. 3. 4. 5. 6. 7. 8. 9.]
float64
```

```
In [100]: np.arange(5,9)
```

```
Out[100]: array([5, 6, 7, 8])
```

```
In [17]: print(np.arange(5,9))
```

```
[5 6 7 8]
```

```
In [ ]:
```

```
In [101]: my_list = list(range(10))  
print(my_arr)
```

```
[0 1 2 3 4 5 6 7 8 9]
```

```
In [102]: my_list[6]
```

```
Out[102]: 6
```

numpy.random.randn()

If positive int_like arguments are provided, randn generates an array of shape (d0, d1, ..., dn), filled with random floats sampled from a univariate “normal” (Gaussian) distribution of mean 0 and variance 1. A single float randomly sampled from the distribution is returned if no argument is provided.

```
In [103]: data1 = np.random.randn() # no argument is passed  
data1
```

```
Out[103]: -2.3331363347462255
```

```
In [104]: data1 = np.random.randn(4)  
print(data1)  
print("dimension =", data1.ndim)  
print("shape =", data1.shape)  
print("size =", data1.size)
```

```
[-0.60375642 -1.04366194  1.36811314  1.5368956 ]  
dimension = 1  
shape = (4,)  
size = 4
```

```
In [105]: data1 = np.random.randn(4,)  
data2 = np.random.randn(4,)
```

```
In [106]: data1
```

```
Out[106]: array([-2.0208327 , -0.93259063,  0.929466   ,  0.77663329])
```

```
In [107]: print(data1)
```

```
[-2.0208327 -0.93259063  0.929466   0.77663329]
```

```
In [108]: data2
```

```
Out[108]: array([ 0.39618175,  1.19276609, -1.05046029,  0.58576348])
```

```
In [109]: data2D = np.random.randn(4,2)
print(data2D)
print("dimension =", data2D.ndim)
print("shape =", data2D.shape)
print("size =", data2D.size)
```

```
[[ 1.21823406  1.74074758]
 [-1.11434085 -0.39568197]
 [ 0.02095032  1.15207729]
 [ 0.60003254 -0.17979428]]
dimension = 2
shape = (4, 2)
size = 8
```

```
In [110]: data3D = np.random.randn(2,3,4)
print(data3D)
print("dimension =", data3D.ndim)
print("shape =", data3D.shape)
print("size =", data3D.size)
```

```
[[[ 0.37512274  0.89138773 -1.17377731  0.86390354]
  [-0.36918698  0.05444447 -0.18040142  0.65471241]
  [ 3.21813828 -0.25451469  1.09110046 -0.3128593 ]]

 [[ 1.18999283  0.41274646  0.13751601 -1.41654525]
  [-1.23578612  0.4592293  -0.62813189  0.07130364]
  [-0.28327309  1.46181478  0.85717345  0.84205929]]]
dimension = 3
shape = (2, 3, 4)
size = 24
```

```
In [ ]:
```

```
In [111]: 3 + data1 *10
```

```
Out[111]: array([-17.20832704, -6.32590627, 12.29466001, 10.76633287])
```

```
In [112]: data1
```

```
Out[112]: array([-2.0208327 , -0.93259063,  0.929466  ,  0.77663329])
```

```
In [113]: data1 + data2
```

```
Out[113]: array([-1.62465096,  0.26017546, -0.12099429,  1.36239677])
```

```
In [114]: data3 = np.random.randn(4,3)
```

```
In [115]: data3.shape
```

```
Out[115]: (4, 3)
```

```
In [116]: data1.shape
```

```
Out[116]: (4,)
```

```
In [117]: data1.dtype
```

```
Out[117]: dtype('float64')
```

```
In [19]: lst1 = [6,5,0.3,-1]
arr1 = np.array(lst1)
print(type(arr1), arr1.dtype)
```

```
<class 'numpy.ndarray'> float64
```

```
In [20]: print(arr1)
```

```
[ 6.  5.  0.3 -1. ]
```

```
In [120]: lst2 = [6,5,3,-1]
arr2 = np.array(lst2)
print(type(arr2), arr2.dtype, arr2, sep="....")
```

```
<class 'numpy.ndarray'>....int32....[ 6  5  3 -1]
```

```
In [25]: lst3 = [[6,5,3,-1],[2,3,4,8]] #2-d list
arr3 = np.array(lst3)
print(type(arr3), arr3.dtype, sep="....")
print(arr3)
```

```
<class 'numpy.ndarray'>....int32
[[ 6  5  3 -1]
 [ 2  3  4  8]]
```



```
In [26]: arr3.ndim
```

```
Out[26]: 2
```

```
In [27]: arr3.shape
```

```
Out[27]: (2, 4)
```

```
In [28]: tup1 = (16,15,13,-11)
arr4 = np.array(tup1)
print(type(arr4), arr4.dtype, arr4, sep="....")
```

```
<class 'numpy.ndarray'>....int32....[ 16  15  13 -11]
```

```
In [29]: arr5 = np.array((16,15,13,-11))
arr5
```

```
Out[29]: array([ 16,  15,  13, -11])
```

```
In [22]: np.zeros(3) # creates an array of zeros
```

```
Out[22]: array([0., 0., 0.])
```

```
In [23]: np.zeros(3).dtype
```

```
Out[23]: dtype('float64')
```

```
In [31]: np.zeros((2,3)) # creates an array of zeros, tuple passed for the shape
```

```
Out[31]: array([[0., 0., 0.],
               [0., 0., 0.]])
```

```
In [24]: np.zeros((2,3,4))
```

```
Out[24]: array([[[0., 0., 0., 0.],
                 [0., 0., 0., 0.],
                 [0., 0., 0., 0.]],
               [[0., 0., 0., 0.],
                 [0., 0., 0., 0.],
                 [0., 0., 0., 0.]])
```

```
In [6]: #creates an array without initializing its value to any particular value
np.empty((2,3))
```

```
Out[6]: array([[ -6.95222783e-310,  6.43418863e-235,  1.29217778e-311],
               [ 1.29217778e-311,  1.97626258e-323,  5.43472210e-323]])
```

Table 4-1. Array creation functions

Function	Description
<code>array</code>	Convert input data (list, tuple, array, or other sequence type) to an ndarray either by inferring a dtype or explicitly specifying a dtype; copies the input data by default
<code>asarray</code>	Convert input to ndarray, but do not copy if the input is already an ndarray
<code>arange</code>	Like the built-in <code>range</code> but returns an ndarray instead of a list
<code>ones</code> , <code>ones_like</code>	Produce an array of all 1s with the given shape and dtype; <code>ones_like</code> takes another array and produces a ones array of the same shape and dtype
<code>zeros</code> , <code>zeros_like</code>	Like <code>ones</code> and <code>ones_like</code> but producing arrays of 0s instead
<code>empty</code> , <code>empty_like</code>	Create new arrays by allocating new memory, but do not populate with any values like <code>ones</code> and <code>zeros</code>
<code>full</code> , <code>full_like</code>	Produce an array of the given shape and dtype with all values set to the indicated “fill value”; <code>full_like</code> takes another array and produces a filled array of the same shape and dtype
<code>eye</code> , <code>identity</code>	Create a square $N \times N$ identity matrix (1s on the diagonal and 0s elsewhere)

Table 4-2. NumPy data types

Type	Type code	Description
<code>int8</code> , <code>uint8</code>	<code>i1</code> , <code>u1</code>	Signed and unsigned 8-bit (1 byte) integer types
<code>int16</code> , <code>uint16</code>	<code>i2</code> , <code>u2</code>	Signed and unsigned 16-bit integer types
<code>int32</code> , <code>uint32</code>	<code>i4</code> , <code>u4</code>	Signed and unsigned 32-bit integer types
<code>int64</code> , <code>uint64</code>	<code>i8</code> , <code>u8</code>	Signed and unsigned 64-bit integer types
<code>float16</code>	<code>f2</code>	Half-precision floating point
<code>float32</code>	<code>f4</code> or <code>f</code>	Standard single-precision floating point; compatible with C float
<code>float64</code>	<code>f8</code> or <code>d</code>	Standard double-precision floating point; compatible with C double and Python float object
<code>float128</code>	<code>f16</code> or <code>g</code>	Extended-precision floating point
<code>complex64</code> , <code>complex128</code> , <code>complex256</code>	<code>c8</code> , <code>c16</code> , <code>c32</code>	Complex numbers represented by two 32, 64, or 128 floats, respectively
<code>bool</code>	<code>?</code>	Boolean type storing True and False values
<code>object</code>	<code>0</code>	Python object type; a value can be any Python object
<code>string_</code>	<code>S</code>	Fixed-length ASCII string type (1 byte per character); for example, to create a string dtype with length 10, use <code>'S10'</code>
<code>unicode_</code>	<code>U</code>	Fixed-length Unicode type (number of bytes platform specific); same specification semantics as <code>string_</code> (e.g., <code>'U10'</code>)

```
In [7]: x=3
        type(x)
```

```
Out[7]: int
```

```
In [8]: a1 = np.array([1,2,3])
        a1.dtype
```

```
Out[8]: dtype('int32')
```

```
In [9]: a2 = np.array([1,2,3], dtype = np.float64)
a2.dtype
```

```
Out[9]: dtype('float64')
```

```
In [10]: a2
```

```
Out[10]: array([1., 2., 3.])
```

```
In [12]: farr1 = a1.astype(np.float64)
print(farr1)
print(a1.dtype, farr1.dtype)
```

```
[1. 2. 3.]
int32 float64
```

```
In [37]: a1
```

```
Out[37]: array([1, 2, 3])
```

```
In [38]: farr1
```

```
Out[38]: array([1., 2., 3.])
```

```
In [39]: a2
```

```
Out[39]: array([1., 2., 3.])
```

```
In [13]: a3 = np.array([1.5, 2.6, 3.1])
print(a3, a3.dtype)
iarr1 = a3.astype(np.int32)
print(iarr1)
print(a3.dtype, iarr1.dtype)
```

```
[1.5 2.6 3.1] float64
[1 2 3]
float64 int32
```

```
In [16]: a=1.6
b=int(a)
print(a,b)
```

```
1.6 1
```

astype()

Given array of strings representing numbers, can use astype to convert them to numeric form

```
In [27]: numeric_strings = np.array(['1.25', '-9.6d', '42'], dtype=np.string_)
print(numeric_strings.dtype)
numeric_strings.astype(float)
```

```
|S5
```

```
-----
--
ValueError                                Traceback (most recent call last)
C:\Users\MONAAD~1\AppData\Local\Temp\ipykernel_33432\3555613002.py in <module>
      1 numeric_strings = np.array(['1.25', '-9.6d', '42'], dtype=np.string_)
      2 print(numeric_strings.dtype)
----> 3 numeric_strings.astype(float)

ValueError: could not convert string to float: b'-9.6d'
```

```
In [29]: numeric_strings = np.array(['1.25', '-9.6', '42'], dtype=np.string_)
print(numeric_strings.dtype)
nArr=numeric_strings.astype(float) # same as float64
print(numeric_strings, numeric_strings.dtype)
print(nArr, nArr.dtype)
```

```
|S4
[b'1.25' b'-9.6' b'42'] |S4
[ 1.25 -9.6  42. ] float64
```

Can use another array's dtype attribute to create an array of that data type

```
In [17]: int_array = np.arange(10)
print(int_array, int_array.dtype)
calibers = np.array([.22, .270, .357, .380, .44, .50], dtype=np.float64)
print(calibers, calibers.dtype)
a = int_array.astype(calibers.dtype) #int_array.astype(float64)
a
```

```
[0 1 2 3 4 5 6 7 8 9] int32
[0.22  0.27  0.357 0.38  0.44  0.5   ] float64
```

```
Out[17]: array([0., 1., 2., 3., 4., 5., 6., 7., 8., 9.])
```

```
In [32]: int_array
```

```
Out[32]: array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
```

Calling `astype` always creates a new array (copy of the data), even if the new dtype is the same as the old dtype

In []:

Arithmetic operations with scalars propagate the scalar argument to each element in the array

```
In [37]: arr = np.array([[1., 2., 3.], [4., 5., 6.]])  
print(arr)
```

```
[[1. 2. 3.]  
 [4. 5. 6.]]
```

```
In [38]: a2 = 1 / arr
```

```
In [39]: print(arr)  
print(a2)
```

```
[[1. 2. 3.]  
 [4. 5. 6.]]  
[[1.         0.5         0.33333333]  
 [0.25       0.2        0.16666667]]
```

```
In [40]: arr ** 0.5
```

```
Out[40]: array([[1.         , 1.41421356, 1.73205081],  
               [2.         , 2.23606798, 2.44948974]])
```

Comparisons between arrays of the same size yield boolean arrays

```
In [41]: arr
```

```
Out[41]: array([[1., 2., 3.],  
               [4., 5., 6.]])
```

```
In [42]: arr2 = np.array([[0., 4., 1.], [7., 4., 12.]])  
arr2
```

```
Out[42]: array([[ 0.,  4.,  1.],  
               [ 7.,  4., 12.]])
```

```
In [44]: arr+arr2
```

```
Out[44]: array([[ 1.,  6.,  4.],  
               [11.,  9., 18.]])
```

```
In [43]: arr2 >= arr
```

```
Out[43]: array([[False,  True, False],  
               [ True, False,  True]])
```

```
In [45]: arr1
```

```
Out[45]: array([ 6. ,  5. ,  0.3, -1. ])
```

```
In [ ]: @@@@#####BROADCASTING#####
```

Operations between differently sized arrays is called broadcasting
Discussed in more detail in Appendix A.

Basic Indexing and Slicing

```
In [50]: arr = np.arange(11,20)
arr
```

```
Out[50]: array([11, 12, 13, 14, 15, 16, 17, 18, 19])
```

```
In [51]: arr[5] #indexing
```

```
Out[51]: 16
```

```
In [52]: arr[5:8] #slicing
```

```
Out[52]: array([16, 17, 18])
```

If you assign a scalar value to a slice, the value is propagated (or broadcasted henceforth) to the entire selection

```
In [18]: #assign a scalar value to a slice -
arr = np.arange(11,20)
print(arr)
print(arr[5:8])
arr[5:8] = 888
print(arr)
```

```
[11 12 13 14 15 16 17 18 19]
[16 17 18]
[ 11  12  13  14  15 888 888 888 19]
```

Numpy arrays differ from Python's built-in lists:

- array slices are views on the original array=> This means that the data is not copied, and any modifications to the view will be reflected in the source array

```
In [19]: #1. create a slice of arr
arr = np.arange(11,20)
arr_slice = arr[5:8]
arr_slice
```

```
Out[19]: array([16, 17, 18])
```

```
In [20]: # 2a. change values in arr_slice, the mutations are reflected in the origin
print(arr)
arr_slice[1] = 777
print(arr)
```

```
[11 12 13 14 15 16 17 18 19]
[ 11  12  13  14  15  16 777  18  19]
```

```
In [21]: # 2b. "bare" slice [:] will assign to all values in an array
print(arr)
print(arr_slice)
arr_slice[:] = 64
print(arr)
```

```
[ 11  12  13  14  15  16 777  18  19]
[ 16 777  18]
[11 12 13 14 15 64 64 64 19]
```

copy()

If you want a copy of a slice of an ndarray instead of a view, you will need to explicitly copy the array

```
In [22]: arr = np.arange(10)
arr_slice = arr[5:8].copy()
print(arr_slice)
print(arr)
```

```
[5 6 7]
[0 1 2 3 4 5 6 7 8 9]
```

```
In [23]: arr_slice[1] = 909
print(arr_slice)
print(arr)
```

```
[ 5 909  7]
[0 1 2 3 4 5 6 7 8 9]
```

Higher dimensional arrays

Two-dimensional array

- the elements at each index are no longer scalars but rather one-dimensional arrays

		axis 1		
		0	1	2
axis 0	0	0,0	0,1	0,2
	1	1,0	1,1	1,2
	2	2,0	2,1	2,2

Figure 4-1. Indexing elements in a NumPy array

```
In [24]: arr2d = np.array([[1, 2, 3], [4, 5, 6], [7, 8, 9]])
print(arr2d)
arr2d[2]
```

```
[[1 2 3]
 [4 5 6]
 [7 8 9]]
```

```
Out[24]: array([7, 8, 9])
```

```
In [123]: # accessing individual elements
```

```
In [124]: arr2d[0][2] #individual elements accessed recursively
```

```
Out[124]: 3
```

```
In [125]: arr2d[0, 2] # pass a comma-separated list of indices to select individual elements
```

```
Out[125]: 3
```

```
In [126]: arr2d[0]
```

```
Out[126]: array([1, 2, 3])
```

```
In [127]: arr2[0]
```

```
Out[127]: array([0., 4., 1.])
```


In multidimensional arrays, if you omit later indices, the returned object will be a lower dimensional ndarray consisting of all the data along the higher dimensions.

```
In [3]: # the 2 x 2 x 3 array, arr3d, arr3d[0] is a 2 x 3 array
arr3d = np.array([[[1, 2, 3], [4, 5, 6]], [[7, 8, 9], [10, 11, 12]]])
print(arr3d.ndim)
print(arr3d.shape)
arr3d
```

```
3
(2, 2, 3)
```

```
Out[3]: array([[[ 1,  2,  3],
                [ 4,  5,  6]],

               [[ 7,  8,  9],
                [10, 11, 12]]])
```

```
In [4]: arr3d[0][0][0] #arr3d[0,0,0]
```

```
Out[4]: 1
```

```
In [5]: arr3d[1][1] #arr3d[1,1]
```

```
Out[5]: array([10, 11, 12])
```

```
In [7]: arr3d[0] # 2d array returned
```

```
Out[7]: array([[1, 2, 3],
               [4, 5, 6]])
```

```
In [8]: print(arr3d)
old_values = arr3d[0].copy()
arr3d[0] = 42
arr3d
```

```
[[[ 1  2  3]
  [ 4  5  6]]

 [[ 7  8  9]
  [10 11 12]]]
```

```
Out[8]: array([[[42, 42, 42],
                [42, 42, 42]],

               [[ 7,  8,  9],
                [10, 11, 12]]])
```

```
In [9]: old_values
```

```
Out[9]: array([[1, 2, 3],
               [4, 5, 6]])
```

```
In [10]: arr3d[0] = old_values
arr3d
```

```
Out[10]: array([[[ 1,  2,  3],
                 [ 4,  5,  6]],

                [[ 7,  8,  9],
                 [10, 11, 12]]])
```

```
In [11]: #arr3d[1, 0] gives all of the values whose indices start with (1, 0), form
arr3d[1, 0]
```

```
Out[11]: array([7, 8, 9])
```

```
In [12]: # Alternatively, indexed in two steps
# Step 1
x = arr3d[1]
print(x)
# Step 2
x[0]
```

```
[[ 7  8  9]
 [10 11 12]]
```

```
Out[12]: array([7, 8, 9])
```

Indexing with slices

```
In [70]: arr = np.arange(10)
arr
```

```
Out[70]: array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
```

```
In [71]: # ndarrays can be sliced
arr[5:8]
```

```
Out[71]: array([5, 6, 7])
```

```
In [14]: # 2-D Array
arr2d = np.array([[1, 2, 3], [4, 5, 6], [7, 8, 9]])
arr2d
```

```
Out[14]: array([[1, 2, 3],
                [4, 5, 6],
                [7, 8, 9]])
```

```
In [15]: arr2d[:2] # selects the first two rows of arr2d
```

```
Out[15]: array([[1, 2, 3],
                [4, 5, 6]])
```

pass multiple slices

- obtain array views of the same number of dimensions.
- By mixing integer indexes and slices, get lower dimensional slices

```
In [22]: arr2d
```

```
Out[22]: array([[1, 2, 3],
               [4, 5, 6],
               [7, 8, 9]])
```

```
In [23]: arr2d[:2, 1:]
```

```
Out[23]: array([[2, 3],
               [5, 6]])
```

```
In [24]: arr2d[:1, 2:] # result is a 2d array
```

```
Out[24]: array([[3]])
```

```
In [25]: arr2d[:1, 2:][0] # result is a 1d array
```

```
Out[25]: array([3])
```

```
In [26]: arr2d[:1, 2:][0][0] # result is a 0d array
```

```
Out[26]: 3
```

```
In [35]: a = arr2d[:1, 2:]
         print(a,a.ndim)
         print(a[0],a[0].ndim)
         print(a[0][0],a[0][0].ndim)
```

```
[[0]] 2
[0] 1
0 0
```

```
In [36]: arr2d
```

```
Out[36]: array([[1, 0, 0],
               [4, 0, 0],
               [7, 8, 9]])
```

```
In [37]: #select the second row but only the first two columns
         arr2d[1, :2]
```

```
Out[37]: array([4, 0])
```

```
In [38]: #select the third column but only the first two rows *****
         arr2d[:2, 2]
```

```
Out[38]: array([0, 0])
```

In []:

```
In [39]: #colon by itself means to take the entire axis   *****  
arr2d[:, :1]
```

```
Out[39]: array([[1],  
               [4],  
               [7]])
```

```
In [40]: arr2d[:, 1:]
```

```
Out[40]: array([[0, 0],  
               [0, 0]])
```

Assigning to a slice expression assigns to the whole selection:

```
In [41]: arr2d[:, 1:] = 0
```

```
In [42]: arr2d
```

```
Out[42]: array([[1, 0, 0],  
               [4, 0, 0],  
               [7, 8, 9]])
```

In []:

Boolean Indexing

This is a type of advanced indexing which is used when the resultant object is meant to be the result of Boolean operations, such as comparison operators.

Example 1

```
In [43]: # Example 1: items greater than 5  
x = np.array([[ 0,  1,  2],[ 3,  4,  5],[ 6,  7,  8],[ 9, 10, 11]])  
x
```

```
Out[43]: array([[ 0,  1,  2],  
               [ 3,  4,  5],  
               [ 6,  7,  8],  
               [ 9, 10, 11]])
```

```
In [46]: a = x>5 # a is a boolean array
print(a)
# This boolean array is passed when indexing the array x
x[a]
```

```
[[False False False]
 [False False False]
 [ True  True  True]
 [ True  True  True]]
```

```
Out[46]: array([ 6,  7,  8,  9, 10, 11])
```

```
In [48]: # Alternatively, in single step
x[x > 5]
```

```
Out[48]: array([ 6,  7,  8,  9, 10, 11])
```

Example 2

Suppose each name corresponds to a row in the data array and we wanted to select all the rows with corresponding name 'Bob' (i.e. rows with index 0 and 3)

Like arithmetic operations, comparisons (such as ==) with arrays are also vectorized.
Thus, comparing names with the string 'Bob' yields a boolean array

```
In [51]: # array of names with duplicates
names = np.array(['Bob', 'Joe', 'Will', 'Bob', 'Will', 'Joe', 'Joe'])
names
```

```
Out[51]: array(['Bob', 'Joe', 'Will', 'Bob', 'Will', 'Joe', 'Joe'], dtype='<U4')
```

```
In [52]: # generating an array using randn function generate an array of random normal
data = np.random.randn(7, 4)
data
```

```
Out[52]: array([[ 0.73306676,  1.63158556, -0.43868445, -0.43539892],
 [ 0.35252711, -0.87424822,  0.07827878,  0.52866901],
 [-0.74617094,  0.14910413,  0.09339057, -1.2405628 ],
 [-0.4073256 ,  0.39018441, -1.04150493, -1.09103013],
 [-1.1602655 ,  0.0171261 , -1.30286833, -0.09872869],
 [ 0.42608207, -1.06788264, -0.16000847, -1.07645539],
 [-0.1165941 ,  0.01132781, -0.94498526, -0.25123313]])
```

```
In [55]: names
```

```
Out[55]: array(['Bob', 'Joe', 'Will', 'Bob', 'Will', 'Joe', 'Joe'], dtype='<U4')
```

```
In [56]: names == "Bob" # True at index 0,3
```

```
Out[56]: array([ True, False, False,  True, False, False, False])
```

```
In [61]: #This boolean array can be passed when indexing the array  
data[names == 'Bob'] # returns row 0 and 3 of data
```

```
Out[61]: array([[ 0.73306676,  1.63158556, -0.43868445, -0.43539892],  
               [-0.4073256 ,  0.39018441, -1.04150493, -1.09103013]])
```

- The boolean array must be of the same length as the array axis it's indexing

- Boolean selection will fail if the boolean array is not the correct length, it is recommend care when using this feature.

```
In [62]: data[names == 'Bob', 2:]
```

```
Out[62]: array([[ -0.43868445, -0.43539892],  
               [-1.04150493, -1.09103013]])
```

```
In [63]: data[names == 'Bob', 3]
```

```
Out[63]: array([-0.43539892, -1.09103013])
```

Example 2b

```
In [ ]: # select data for all others, except Bob
```

```
In [149]: names != 'Bob'
```

```
Out[149]: array([False,  True,  True, False,  True,  True,  True])
```

```
In [152]: data[names != 'Bob'] # using != operator
```

```
Out[152]: array([[ 0.04148935,  2.65756412,  1.9097909 , -0.66803221],  
               [-0.10932864,  0.45910202, -0.52826133,  0.13182746],  
               [ 0.59031437, -0.18722703, -0.21928411, -0.92838616],  
               [-0.00928052, -0.70175191,  1.28834738,  0.98356384],  
               [-0.15833311,  0.68302444, -2.49969158, -2.40368797]])
```

```
In [153]: data[~(names == 'Bob')] # using ~ operator
```

```
Out[153]: array([[ 0.04148935,  2.65756412,  1.9097909 , -0.66803221],  
               [-0.10932864,  0.45910202, -0.52826133,  0.13182746],  
               [ 0.59031437, -0.18722703, -0.21928411, -0.92838616],  
               [-0.00928052, -0.70175191,  1.28834738,  0.98356384],  
               [-0.15833311,  0.68302444, -2.49969158, -2.40368797]])
```

```
In [69]: x = np.array([[2,4],[5,1]])
w1=np.eye(2)
print(w1)
w=np.eye(2)*x
print(w)
```

```
[[1. 0.]
 [0. 1.]]
[[2. 0.]
 [0. 1.]]
```

```
In [70]: z=np.ones_like(x)
print(z)
```

```
[[1 1]
 [1 1]]
```

```
In [72]: a = np.ones((3,2))
print(a)
```

```
[[1. 1.]
 [1. 1.]
 [1. 1.]]
```

```
In [75]: a1 = np.ones(9)
print(a1)
```

```
[1. 1. 1. 1. 1. 1. 1. 1. 1.]
```

```
In [ ]: aaa
```

The ~ operator can be useful when you want to invert a general condition

```
In [154]: cond = names == 'Bob'
data[~cond]
```

```
Out[154]: array([[ 0.04148935,  2.65756412,  1.9097909 , -0.66803221],
                 [-0.10932864,  0.45910202, -0.52826133,  0.13182746],
                 [ 0.59031437, -0.18722703, -0.21928411, -0.92838616],
                 [-0.00928052, -0.70175191,  1.28834738,  0.98356384],
                 [-0.15833311,  0.68302444, -2.49969158, -2.40368797]])
```

- The Python keywords and and or do not work with boolean arrays. Use & (and) and | (or) instead
- Selecting two of the three names to combine multiple boolean conditions, use boolean arithmetic operators like & (and) and | (or)

```
In [14]: names
```

```
Out[14]: array(['Bob', 'Joe', 'Will', 'Bob', 'Will', 'Joe', 'Joe'], dtype='<U4')
```

```
In [155]: mask = (names == 'Bob') | (names == 'Will')
mask
```

```
Out[155]: array([ True, False,  True,  True,  True, False, False])
```

```
In [156]: data[mask]
```

```
Out[156]: array([[ 0.27415301,  1.01906259,  1.47708284, -0.47090873],
                 [-0.10932864,  0.45910202, -0.52826133,  0.13182746],
                 [ 0.04107582,  1.38307928,  0.59278498,  1.49310956],
                 [ 0.59031437, -0.18722703, -0.21928411, -0.92838616]])
```

Selecting data from an array by boolean indexing always creates a copy of the data, even if the returned array is unchanged (as in all above examples).

```
In [15]: data = np.random.randn(7, 4)
data
```

```
Out[15]: array([[ 1.9841926 ,  0.02490136, -1.05969915,  0.20543926],
                 [ 0.76459831,  1.13837446, -0.02112344,  0.75179457],
                 [ 2.55381686,  1.46109436,  1.55227011,  0.09925178],
                 [ 0.11516685, -0.364902  , -1.0657805 , -0.87011183],
                 [-0.19506677,  0.0107136 , -0.34065633, -0.74752875],
                 [-0.16355998,  0.87912877,  0.21827526, -0.15869218],
                 [ 2.08183192,  0.76867047, -0.25807129, -1.39484498]])
```

```
In [16]: # Setting values with boolean arrays
```

```
data[data < 0] = 0
data
```

```
Out[16]: array([[1.9841926 , 0.02490136, 0.          , 0.20543926],
                 [0.76459831, 1.13837446, 0.          , 0.75179457],
                 [2.55381686, 1.46109436, 1.55227011, 0.09925178],
                 [0.11516685, 0.          , 0.          , 0.          ],
                 [0.          , 0.0107136 , 0.          , 0.          ],
                 [0.          , 0.87912877, 0.21827526, 0.          ],
                 [2.08183192, 0.76867047, 0.          , 0.          ]])
```

```
In [17]: names
```

```
Out[17]: array(['Bob', 'Joe', 'Will', 'Bob', 'Will', 'Joe', 'Joe'], dtype='<U4')
```



```
In [162]: # Setting whole rows or columns using a one-dimensional boolean array  
data[names != 'Joe'] = 7  
data
```

```
Out[162]: array([[7.          , 7.          , 7.          , 7.          ],  
                [1.64672438, 0.87290525, 0.51320328, 0.          ],  
                [7.          , 7.          , 7.          , 7.          ],  
                [7.          , 7.          , 7.          , 7.          ],  
                [7.          , 7.          , 7.          , 7.          ],  
                [0.          , 0.92021892, 0.55098641, 0.          ],  
                [0.          , 0.04456924, 0.8647162 , 0.          ]])
```

Fancy Indexing

Fancy indexing is a term adopted by NumPy to describe indexing using integer arrays

```
In [19]: arr = np.empty((8, 4))
```

```
In [20]: for i in range(8):  
         arr[i] = i
```

```
In [28]: arr
```

```
Out[28]: array([[ 0,  1,  2,  3],  
                [ 4,  5,  6,  7],  
                [ 8,  9, 10, 11],  
                [12, 13, 14, 15],  
                [16, 17, 18, 19],  
                [20, 21, 22, 23],  
                [24, 25, 26, 27],  
                [28, 29, 30, 31]])
```

To select out a subset of the rows in a particular order, you can simply pass a list or ndarray of integers specifying the desired order

```
In [30]: arr[2]
```

```
Out[30]: array([ 8,  9, 10, 11])
```

```
In [26]: arr[4, 3, 0, 6]
```

```
-----
--
IndexError                                Traceback (most recent call last)
C:\Users\MONAAD~1\AppData\Local\Temp\ipykernel_2536\2175898046.py in <module>
----> 1 arr[4, 3, 0, 6]

IndexError: too many indices for array: array is 2-dimensional, but 4 were indexed
```

```
In [168]: arr[[4, 3, 0, 6]]
```

```
Out[168]: array([[4., 4., 4., 4.],
                 [3., 3., 3., 3.],
                 [0., 0., 0., 0.],
                 [6., 6., 6., 6.]])
```

```
In [22]: arr
```

```
Out[22]: array([[0., 0., 0., 0.],
                 [1., 1., 1., 1.],
                 [2., 2., 2., 2.],
                 [3., 3., 3., 3.],
                 [4., 4., 4., 4.],
                 [5., 5., 5., 5.],
                 [6., 6., 6., 6.],
                 [7., 7., 7., 7.]])
```

```
In [170]: arr[[-3, -5, -7]] #negative indices selects rows from the end
```

```
Out[170]: array([[5., 5., 5., 5.],
                 [3., 3., 3., 3.],
                 [1., 1., 1., 1.]])
```

```
In [23]: arr = np.arange(32)
arr
```

```
Out[23]: array([ 0,  1,  2,  3,  4,  5,  6,  7,  8,  9, 10, 11, 12, 13, 14, 15, 16,
                17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31])
```

```
In [25]: arr = np.arange(32).reshape((8, 4))
```

```
In [172]: arr
```

```
Out[172]: array([[ 0,  1,  2,  3],
                 [ 4,  5,  6,  7],
                 [ 8,  9, 10, 11],
                 [12, 13, 14, 15],
                 [16, 17, 18, 19],
                 [20, 21, 22, 23],
                 [24, 25, 26, 27],
                 [28, 29, 30, 31]])
```

Passing multiple index arrays - selects a one-dimensional array of elements corresponding to each tuple of indices

```
In [175]: arr[[1, 5, 7, 2]]
```

```
Out[175]: array([[ 4,  5,  6,  7],
                 [20, 21, 22, 23],
                 [28, 29, 30, 31],
                 [ 8,  9, 10, 11]])
```

```
In [174]: arr[[1, 5, 7, 2], [0, 3, 1, 2]] # elements (1, 0), (5, 3), (7, 1), and (2,
```

```
Out[174]: array([ 4, 23, 29, 10])
```

```
In [ ]: #####
```

```
In [31]: arr
```

```
Out[31]: array([[ 0,  1,  2,  3],
                 [ 4,  5,  6,  7],
                 [ 8,  9, 10, 11],
                 [12, 13, 14, 15],
                 [16, 17, 18, 19],
                 [20, 21, 22, 23],
                 [24, 25, 26, 27],
                 [28, 29, 30, 31]])
```

```
In [32]: arr[[1, 5, 7, 2]]
```

```
Out[32]: array([[ 4,  5,  6,  7],
                 [20, 21, 22, 23],
                 [28, 29, 30, 31],
                 [ 8,  9, 10, 11]])
```

```
In [178]: arr[[1, 5, 7, 2]][:, [0, 3, 1, 2]] #*****
```

```
Out[178]: array([[ 4,  7,  5,  6],
                 [20, 23, 21, 22],
                 [28, 31, 29, 30],
                 [ 8, 11,  9, 10]])
```

In []:

Transposing Arrays and Swapping Axes

Transposing is a special form of reshaping that similarly returns a view on the underlying data without copying anything. Arrays have the transpose method and also the special T attribute

```
In [2]: arr = np.arange(15).reshape((3, 5))
arr
```

```
Out[2]: array([[ 0,  1,  2,  3,  4],
               [ 5,  6,  7,  8,  9],
               [10, 11, 12, 13, 14]])
```

```
In [3]: arr.shape
```

```
Out[3]: (3, 5)
```

In []:

```
In [4]: arr.T # view is returned
```

```
Out[4]: array([[ 0,  5, 10],
               [ 1,  6, 11],
               [ 2,  7, 12],
               [ 3,  8, 13],
               [ 4,  9, 14]])
```

```
In [5]: arr.shape # original array, no change
```

```
Out[5]: (3, 5)
```

```
In [6]: arr
```

```
Out[6]: array([[ 0,  1,  2,  3,  4],
               [ 5,  6,  7,  8,  9],
               [10, 11, 12, 13, 14]])
```

inner matrix product using np.dot

```
In [7]: arr = np.random.randn(6, 3)
arr
```

```
Out[7]: array([[ 1.33947136,  0.12996198, -0.45386506],
 [ 0.28790223,  1.1020587 , -0.5691221 ],
 [-1.28681354,  1.28491604,  1.08099913],
 [-0.65904142, -0.99329287,  1.98409826],
 [ 0.38152898,  0.88826111, -1.10257725],
 [ 0.64084846,  0.21869393, -0.82499963]])
```

```
In [8]: np.dot(arr.T, arr) # 3x5 5x3 #@@@@@@@@#
```

```
Out[8]: array([[ 4.52354699, -0.02841369, -4.41980293],
 [-0.02841369,  4.70589829, -2.42778759],
 [-4.41980293, -2.42778759,  7.53139946]])
```

transpose()

<https://www.geeksforgeeks.org/python-numpy-numpy-transpose/>

numpy.transpose()

- It can transpose the 2-D numpy arrays
- it has no effect on 1-D arrays

Parameter: only pass (0, 1) or (1, 0)

Eg.array of shape (2, 3) to change it (3, 2) you should pass (1, 0) where 1 as 3 and 0 as 2.

Returns: ndarray

```
In [77]: arr = np.arange(15).reshape((3, 5))
arr
```

```
Out[77]: array([[ 0,  1,  2,  3,  4],
 [ 5,  6,  7,  8,  9],
 [10, 11, 12, 13, 14]])
```

```
In [78]: arr.shape
```

```
Out[78]: (3, 5)
```

```
In [79]: arr.transpose(1,0) # returns transposed array
```

```
Out[79]: array([[ 0,  5, 10],
 [ 1,  6, 11],
 [ 2,  7, 12],
 [ 3,  8, 13],
 [ 4,  9, 14]])
```

```
In [80]: arr.transpose(0,1) # returns original array
```

```
Out[80]: array([[ 0,  1,  2,  3,  4],
 [ 5,  6,  7,  8,  9],
 [10, 11, 12, 13, 14]])
```

```
In [81]: # 3-D array
arr3D = np.arange(16).reshape((2, 2, 4))
arr3D
```

```
Out[81]: array([[[ 0,  1,  2,  3],
                  [ 4,  5,  6,  7]],

                [[ 8,  9, 10, 11],
                 [12, 13, 14, 15]]])
```

```
In [82]: # the axes have been reordered with the second axis first, the first axis s
# and the last axis unchanged
arr3D.transpose((1, 0, 2))
```

```
Out[82]: array([[[ 0,  1,  2,  3],
                  [ 8,  9, 10, 11]],

                [[ 4,  5,  6,  7],
                 [12, 13, 14, 15]]])
```

swapaxes()

<https://www.geeksforgeeks.org/numpy-swapaxes-function-python/>

numpy.swapaxes() function interchange two axes of an array.

arr : [array_like] input array.

axis1 : [int] First axis.

axis2 : [int] Second axis.

Return : [ndarray] In earlier NumPy versions, a view of arr is returned only if the order of the axes is changed, otherwise the input array is returned. For NumPy >= 1.10.0, if arr is an ndarray, then a view of arr is returned; otherwise a new array is created

```
In [83]: arr3D
```

```
Out[83]: array([[[ 0,  1,  2,  3],
                  [ 4,  5,  6,  7]],

                [[ 8,  9, 10, 11],
                 [12, 13, 14, 15]]])
```

```
In [84]: arr3D.swapaxes(1,2)
```

```
Out[84]: array([[[ 0,  4],
                  [ 1,  5],
                  [ 2,  6],
                  [ 3,  7]],

                [[ 8, 12],
                 [ 9, 13],
                 [10, 14],
                 [11, 15]]])
```

```
In [85]: arr3D.swapaxes(1,0)
```

```
Out[85]: array([[[ 0,  1,  2,  3],
                  [ 8,  9, 10, 11]],

                [[ 4,  5,  6,  7],
                 [12, 13, 14, 15]]])
```

```
In [86]: arr3D # original array unchanged
```

```
Out[86]: array([[[ 0,  1,  2,  3],
                  [ 4,  5,  6,  7]],

                [[ 8,  9, 10, 11],
                 [12, 13, 14, 15]]])
```