

[40] **Homework 5:** *Big O,  $\Omega$ .*

[10] Select the best “big Oh” notation for each expression. Justify by showing the constants  $c$  and  $n_0$ . Note that  $f(n) = O(g(n))$  if there are constants  $c > 0$  and  $n_0 > 0$  so that for all  $n \geq n_0$  we have  $|f(n)| \leq c \cdot g(n)$ .

1.  $95n + 1$ .
2.  $(11n + 1)^6$ .
3.  $4n^4 - 10n^3 - 100$ .
4.  $n^3 + n + n\sqrt{n} + \log n^4$ .

[10] Show the following:

$$\begin{aligned} 10n^3 + \log n &= \Theta(n^3) \\ \frac{6n^2}{\log^3 n + 1} &= O(n^3) \\ 3n^3 + 44n^2 &= \Omega(n^2) \end{aligned}$$

[10] Is  $(\log n)^2 = O(\log n^2)$ ? Justify your answer?

[10] We say that  $f(n) \prec g(n)$  if  $g(n)$  grows faster than  $f(n)$  (e.g.,  $\log n \prec n$ ).

Order the following functions by  $\prec$  from the lowest to the highest:

$$\left(\frac{3}{2}\right)^n, \quad 100, \quad n^3 \log^2 n, \quad 2^{\log_2 n}, \quad \log^4 n, \quad 2^{3 \log_2 n}, \quad 2^n.$$

Justify your answer.