

Properties of Tree

- ① There is one and only path between every pair of vertices in a Tree.
- ② If in a graph G , There is one & ----- . Then G is a Tree graph.
- ③ A Tree with n -vertices has $(n-1)$ Edges.

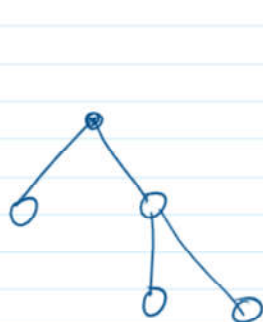
No. of Edges in a Tree = $n-1$ Where n = No. of Vertices.

Minimally Connected graph A Connected graph G is said to be minimally Connected if removal of Any Edge from G , It become disconnected Graph.

Note : A Tree is Minimally Connected graph.

② A graph is a Tree iff it is Minimally Connected.

④ In a non-Trivial Tree, There are atleast Two pendent Vertices.



$$d(a) = d(b) = 1$$

Both a & b are Pendent Vertices

Labeled Tree \mapsto

Definition : A Tree is said to be labeled in which every vertex of Tree has assigned a unique label.

Labeled tree is usually used to construct **expression Tree**. Any **algebraic expression** can be represented with the help of **labeled binary tree**. For this root of tree is labeled with the **central operator** of main expression. The **two offsprings** of root are labeled with central operator of expression for left and right arguments respectively. If either argument is a constant or variable (instead of expression), this is used to label the corresponding offspring vertex. This process continues until expression is exhausted.

Root = Central operator of Main Expression.

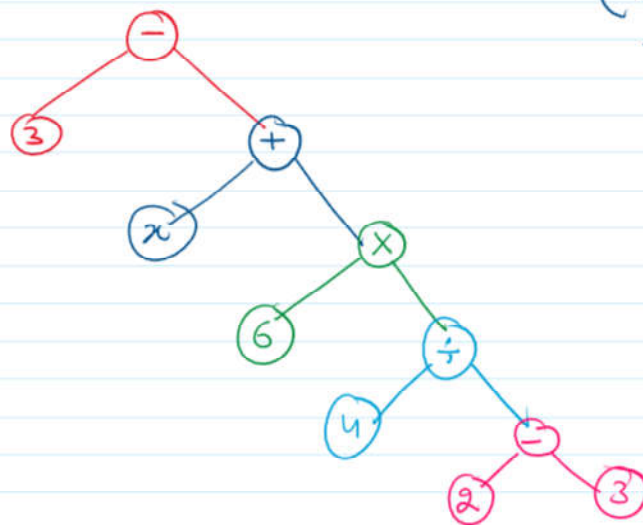
Example 5. Construct the tree of algebraic expression.

$$(i) 3 - (x + (6 \times (4 \div (2-3))))$$

$$\begin{array}{c} 3 \ominus (x + (6 \times (4 \div (2-3)))) \\ \uparrow \quad \uparrow \quad \uparrow \quad \uparrow \quad \uparrow \\ 1 \quad 1 \quad 1 \quad 1 \quad 1 \end{array}$$

$3 - (x + (6 \times (4 \div (2 - 3))))$
 Left Argument Central operator Right Argument

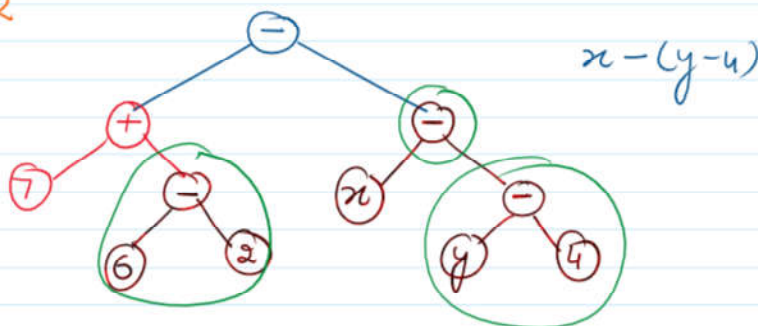
$$(x + (6 \times (4 \div (2 - 3))))$$



$$\begin{array}{l}
 6 \times (\quad) \\
 4 \div (\quad) \\
 (2 - 3)
 \end{array}$$

$(7 + (6 - 2)) - (x - (y - 4))$
 L R

$$7 + (6 - 2)$$



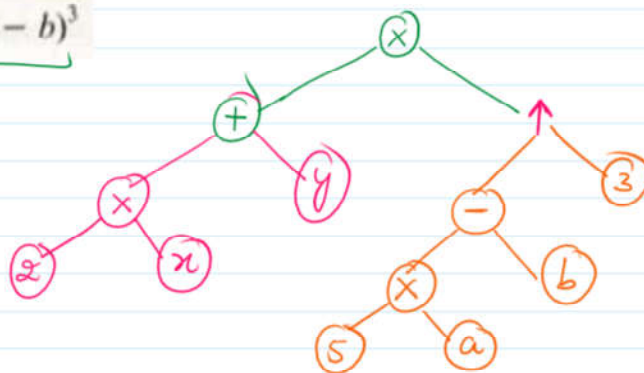
$$x - (y - 4)$$

$$[7 + (6 - 2)] - [x - (y - 4)]$$

Ex.

$((2 \times x) + y) \times ((5 \times a) - b)^3$

$$(2 \times x) + y$$



Traversal of Binary Tree \Rightarrow To Visit each Vertex of Tree Exactly Once.

Preorder :

(1) Process the root R.

(2) Traverse the left subtree of R in preorder.

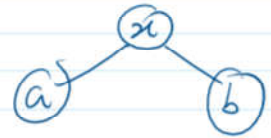
(x)

Preorder : (1) Process the root R.
(2) Traverse the left subtree of R in preorder.
(3) Traverse the right subtree of R in preorder.

Inorder : (1) Traverse the left subtree of R in inorder.
(2) Process the root R.

(3) Traverse the right subtree of R in inorder.
Postorder : (1) Traverse the left subtree of R in postorder.
(2) Traverse the right subtree of R in postorder
(3) Process the root R.

U =



Preorder

x a b

Inorder

a x b

Post order

a b x