

L-8 Inference

Tuesday, February 8, 2022 9:56 AM

Rules of Inference :-

TABLE 1 Rules of Inference.		
Rule of Inference	Tautology	Name
$\frac{p \quad p \rightarrow q}{\therefore q}$	$(p \wedge (p \rightarrow q)) \rightarrow q$	Modus ponens
$\frac{\neg q \quad p \rightarrow q}{\therefore \neg p}$	$(\neg q \wedge (p \rightarrow q)) \rightarrow \neg p$	Modus tollens
$\frac{p \rightarrow q \quad q \rightarrow r}{\therefore p \rightarrow r}$	$((p \rightarrow q) \wedge (q \rightarrow r)) \rightarrow (p \rightarrow r)$	Hypothetical syllogism
$\frac{p \vee q \quad \neg p}{\therefore q}$	$((p \vee q) \wedge \neg p) \rightarrow q$	Disjunctive syllogism
$\frac{p}{\therefore p \vee q}$	$p \rightarrow (p \vee q)$	Addition
$\frac{p \wedge q}{\therefore p}$	$(p \wedge q) \rightarrow p$	Simplification
$\frac{p \quad q}{\therefore p \wedge q}$	$((p) \wedge (q)) \rightarrow (p \wedge q)$	Conjunction
$\frac{p \vee q \quad \neg p \vee r}{\therefore q \vee r}$	$((p \vee q) \wedge (\neg p \vee r)) \rightarrow (q \vee r)$	Resolution

Law of Detachment

$$S_1: p \quad S_2: p \rightarrow q$$

$$\therefore q$$

$$\frac{p \quad p \rightarrow q}{\therefore q}$$

Law of Denying

$$S_1: \neg q \quad S_2: p \rightarrow q$$

$$\therefore \neg p$$

$$S_1: q \quad S_2: p \rightarrow \neg q$$

$$\therefore \neg p$$

$$\frac{p \rightarrow q \quad q \rightarrow r}{p \rightarrow r}$$

$$S_1: p \quad S_2: q$$

$$p \text{ and } q$$

$$\frac{p \vee q \quad \neg p \vee r}{q \vee r}$$

$$p \vee q \quad \neg p \vee r \quad q \vee r \quad q \vee r$$

$$x + y + 2 - 3 + 7$$

$$x + y + (2 - 3) + 7$$

$$x + y + (-1) + 7$$

$$x + y + 6$$

State which rule of inference is the basis of the following argument: "It is below freezing now. Therefore, it is either below freezing or raining now."

One statement premise

$$\frac{p \quad p \vee q}{p \vee q}$$

$$S_1: p \quad C: p \vee q$$

$$\frac{p \quad p \vee q}{p \vee q} \rightarrow \text{Addition}$$

State which rule of inference is the basis of the following argument: "It is below freezing and raining now. Therefore, it is below freezing now."

If it rains today, then we will not have a barbecue today. If we do not have a barbecue today, then we will have a barbecue tomorrow. Therefore, if it rains today, then we will have a barbecue tomorrow.

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$\frac{p}{p \rightarrow q}$ $\therefore q$	$(p \wedge (p \rightarrow q)) \rightarrow q$	Modus ponens
$\frac{\neg q}{p \rightarrow q}$ $\therefore \neg p$	$(\neg q \wedge (p \rightarrow q)) \rightarrow \neg p$	Modus tollens
$\frac{p \rightarrow q}{q \rightarrow r}$ $\therefore p \rightarrow r$	$((p \rightarrow q) \wedge (q \rightarrow r)) \rightarrow (p \rightarrow r)$	Hypothetical syllogism
$\frac{p \vee q}{\neg p}$ $\therefore q$	$((p \vee q) \wedge \neg p) \rightarrow q$	Disjunctive syllogism
$\frac{p}{\therefore p \vee q}$	$p \rightarrow (p \vee q)$	Addition
$\frac{p \wedge q}{\therefore p}$	$(p \wedge q) \rightarrow p$	Simplification
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- Ⓐ Hypothetical
- Ⓑ Modus Tollens
- Ⓒ Disjunctive
- Ⓓ Resolution

If p then q $p \rightarrow q$
 If q then r $q \rightarrow r$
 $p \rightarrow q$ and $q \rightarrow r$
 $p \rightarrow r$

Let p: You read the newspaper every day. q: You will be informed. Which of the following is logical expression for "If you read the newspaper every day, you will be informed, and conversely"?

- (A) $q \rightarrow p$ (B) $p \wedge q$ (C) $p \rightarrow q$ (D) $p \leftrightarrow q$

If p then q and Conversely
 $p \rightarrow q$ & $q \rightarrow p$
 $p \leftrightarrow q$