

作业

一. 如果存在 $\text{Halt}(P, i)$, 构造

① $\text{void Evil}(i) \{$

② $\text{if}(\neg \text{Halt}(\text{Evil}, i)) \text{return};$

③ $\text{else while}(1);$

若 ② $\neg \text{Halt}(\text{Evil}, i)$ 为假 $\text{Halt}(\text{Evil}, i)$ 为真
则进入 ③ 死循环

若 ② $\text{Halt}(\text{Evil}, i)$ 为假, 在 ② 返回, 矛盾
故不存在 $\text{Halt}(P, i)$

二. 定义 α , $\alpha(i) = \begin{cases} \text{自}, & i \geq 0 \wedge i \in \mathbb{Z} \\ \text{负}, & i < 0 \wedge i \in \mathbb{Z} \end{cases}$

加法 $\alpha(a) \oplus \alpha(b) = \begin{cases} \text{自}, & \alpha(a) = \text{自}, \alpha(b) = \text{自} \\ \text{负}, & \alpha(a) = \text{负}, \alpha(b) = \text{负} \\ \text{未}, & \text{其它} \end{cases}$

除法 $\alpha(a) \oslash \alpha(b) = \begin{cases} \text{自}, & (\alpha(a) = \text{自} \wedge \alpha(b) = \text{自} \wedge b \neq 0 \wedge a \bmod b = 0) \\ & \vee (\alpha(a) = \text{负} \wedge \alpha(b) = \text{负} \wedge a \bmod b = 0) \\ \text{负}, & (\alpha(a) = \text{自} \wedge \alpha(b) = \text{负} \wedge a \neq 0 \wedge a \bmod b = 0) \\ & \vee (\alpha(a) = \text{负} \wedge \alpha(b) = \text{自} \wedge b \neq 0 \wedge a \bmod b = 0) \\ \text{未}, & \text{其它} \end{cases}$

$$2 + (2 \div (-1)) = 0$$

$$\alpha(2) + (\alpha(2) \oslash \alpha(-1)) = \text{自} \oplus \text{负} = \text{未}$$