Lecture 10: Training Neural Networks (Part 1)

Reminder: A3

• Due Friday, February 11

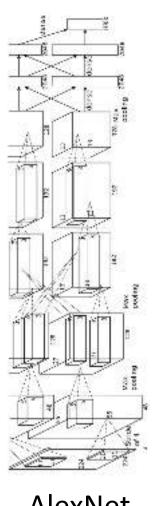
ULCS / Depth

If you are a CSE student:

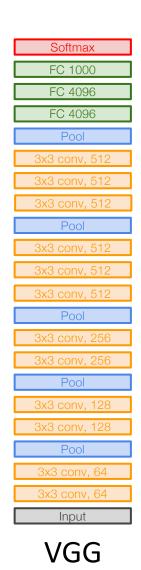
- For undergrads: This course now counts as ULCS (this term only)
- For grad students: This course now counts as technical depth

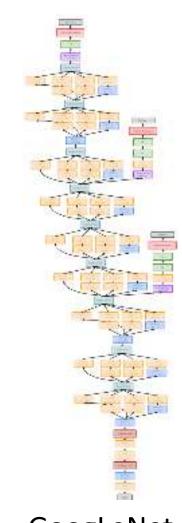
For non-CSE students: Check with your program

Last Time: CNN Architectures

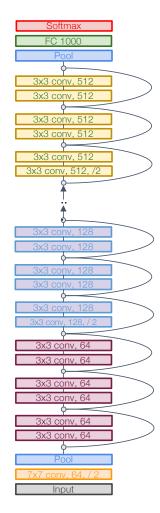


AlexNet





GoogLeNet



ResNet

Justin Johnson February 6, 2022 **Lecture 10 - 4**

Overview

1. One time setup

Activation functions, data preprocessing, weight initialization, regularization

2. Training dynamics

Learning rate schedules; large-batch training; hyperparameter optimization

3. After training

Model ensembles, transfer learning

Overview

1. One time setup

Activation functions, data preprocessing, weight initialization, regularization

2. Training dynamics

Learning rate schedules; large-batch training; hyperparameter optimization

3. After training

Model ensembles, transfer learning

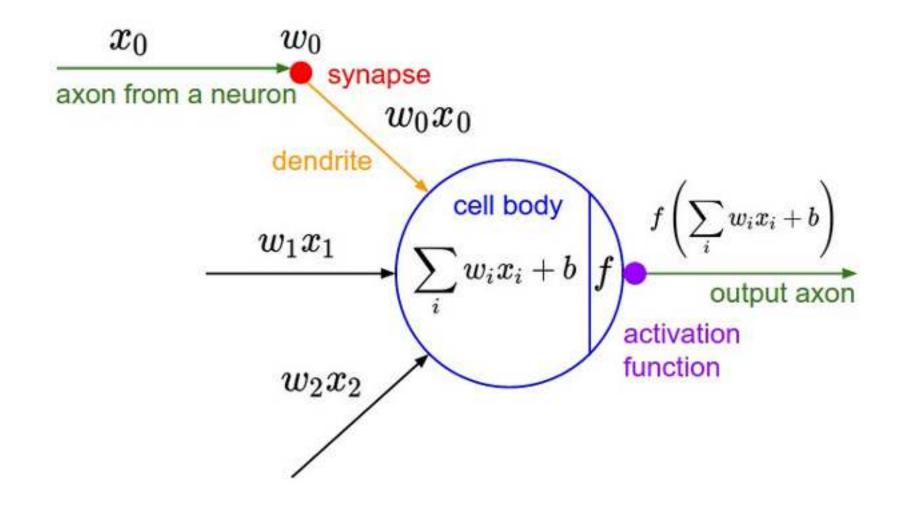
Today

Next time

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Activation Functions

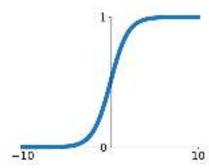
Activation Functions



Activation Functions

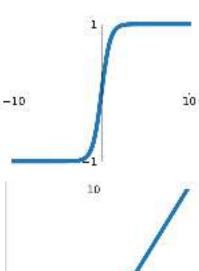
Sigmoid

$$\sigma(x) = \frac{1}{1 + e^{-x}}$$



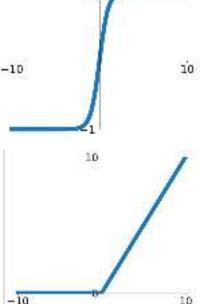
tanh

tanh(x)



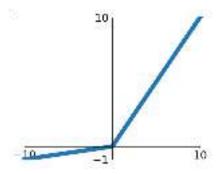
ReLU

 $\max(0,x)$



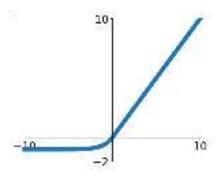
Leaky ReLU

 $\max(0.1x,x)$



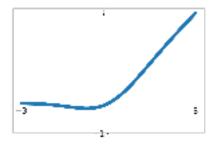
ELU

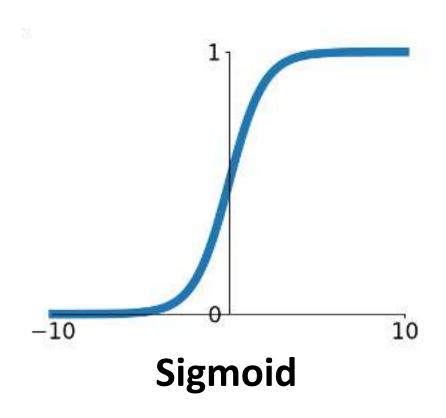
$$\begin{cases} x & x \ge 0 \\ \alpha(e^x - 1) & x < 0 \end{cases}$$



GELU

 $\approx x\sigma(1.702x)$

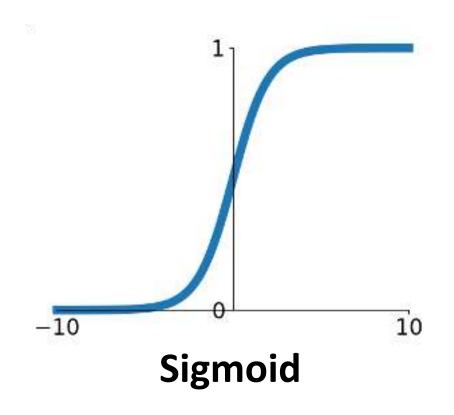




$$\sigma(x) = \frac{1}{1 + e^{-x}}$$

- Squashes numbers to range [0,1]
- Historically popular since they have nice interpretation as a saturating "firing rate" of a neuron

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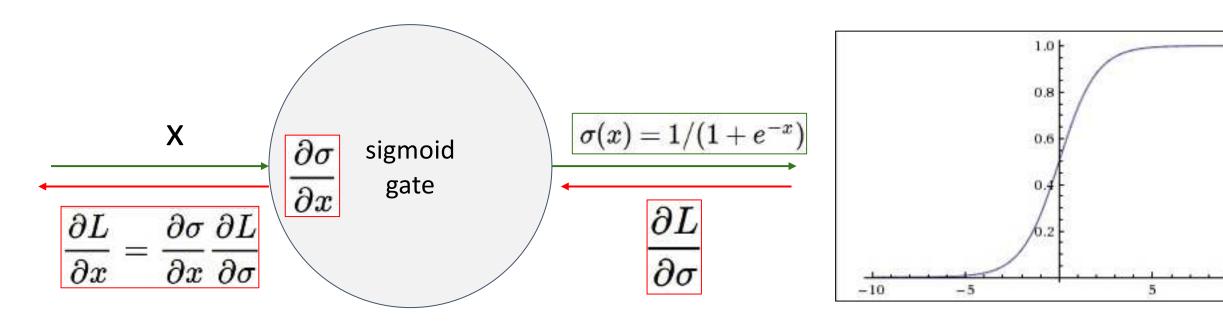
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3 problems:

1. Saturated neurons "kill" the gradients

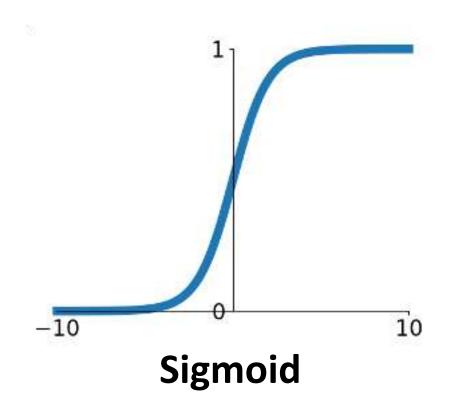
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What happens when x = -10?

What happens when x = 0?

What happens when x = 10?



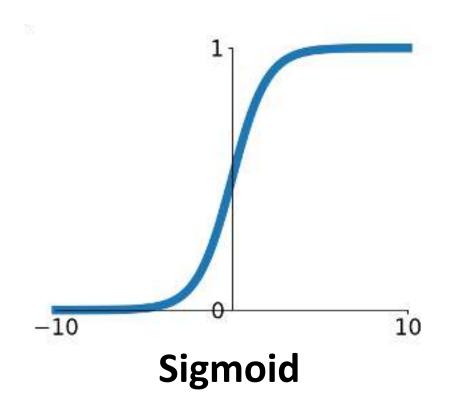
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3 problems:

1. Saturated neurons "kill" the gradients

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$$\sigma(x) = \frac{1}{1 + e^{-x}}$$

- Squashes numbers to range [0,1]
- Historically popular since they have nice interpretation as a saturating "firing rate" of a neuron

3 problems:

- L. Saturated neurons "kill" the gradients
- 2. Sigmoid outputs are not zero-centered

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$$h_i^{(\ell)} = \sum_j w_{i,j}^{(\ell)} \sigma\left(h_j^{(\ell-1)}\right) + b_i^{(\ell)}$$

 $h_i^{(\ell)}$ is the ith element of the hidden layer at layer ℓ (before activation) $w^{(\ell)}$, $b^{(\ell)}$ are the weights and bias of layer ℓ

What can we say about the gradients on $w^{(\ell)}$?

$$h_i^{(\ell)} = \sum_j w_{i,j}^{(\ell)} \sigma\left(h_j^{(\ell-1)}\right) + b_i^{(\ell)}$$

Local Upstream Gradient Gradient

$$\frac{\partial L}{\partial w_{i,j}^{(\ell)}} = \frac{\partial h_i^{(\ell)}}{\partial w_{i,j}} \cdot \frac{\partial L}{\partial h_i^{(\ell)}}$$

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Local Upstream Gradient Gradient

$$\frac{\partial L}{\partial w_{i,j}^{(\ell)}} = \frac{\partial h_i^{(\ell)}}{\partial w_{i,j}} \cdot \frac{\partial L}{\partial h_i^{(\ell)}}$$

$$= \sigma \left(h_j^{(\ell-1)} \right) \cdot \frac{\partial L}{\partial h_i^{(\ell)}}$$

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allowed gradient update directions

allowed gradient update directions

hypothetical optimal w vector

Gradients on rows of w can only point in some directions; needs to "zigzag" to move in other directions

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$$h_i^{(\ell)} = \sum_j w_{i,j}^{(\ell)} \sigma\left(h_j^{(\ell-1)}\right) + b_i^{(\ell)}$$

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allowed gradient update directions

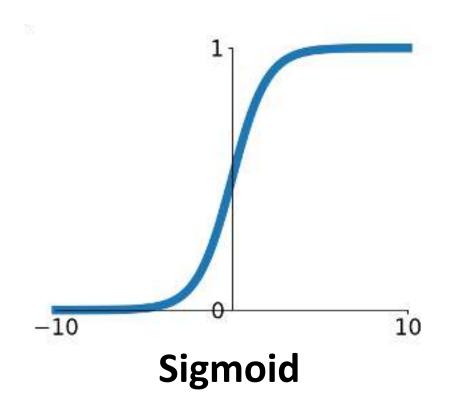
allowed gradient update directions

hypothetical optimal w vector

Not that bad in practice:

- Only true for a single example, minibatches help
- BatchNorm can also avoid this

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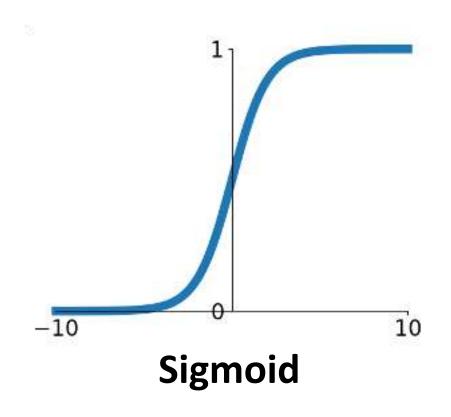
$$\sigma(x) = \frac{1}{1 + e^{-x}}$$

- Squashes numbers to range [0,1]
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3 problems:

- 1. Saturated neurons "kill" the gradients
- 2. Sigmoid outputs are not zero-centered

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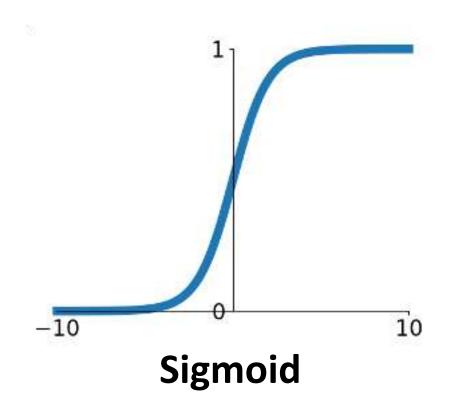
$$\sigma(x) = \frac{1}{1 + e^{-x}}$$

- Squashes numbers to range [0,1]
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3 problems:

- 1. Saturated neurons "kill" the gradients
- 2. Sigmoid outputs are not zero-centered
- exp() is a bit compute expensive

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$$\sigma(x) = \frac{1}{1 + e^{-x}}$$

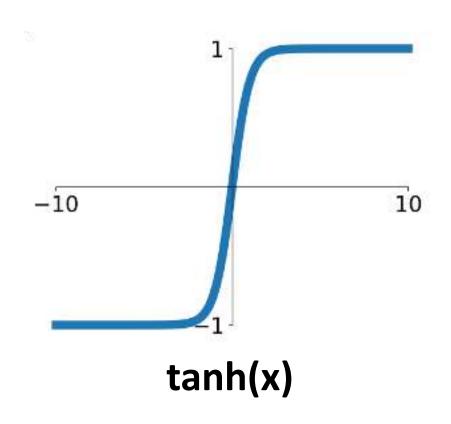
- Squashes numbers to range [0,1]
- Historically popular since they have nice interpretation as a saturating "firing rate" of a neuron

3 problems: Worst problem in practice

- .. Saturated neurons "kill" the gradients
- 2. Sigmoid outputs are not zero-centered
- 3. exp() is a bit compute expensive

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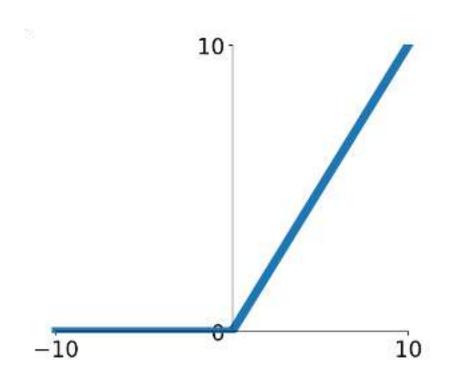
Activation Functions: Tanh



- Squashes numbers to range [-1,1]
- zero centered (nice)
- still kills gradients when saturated :(

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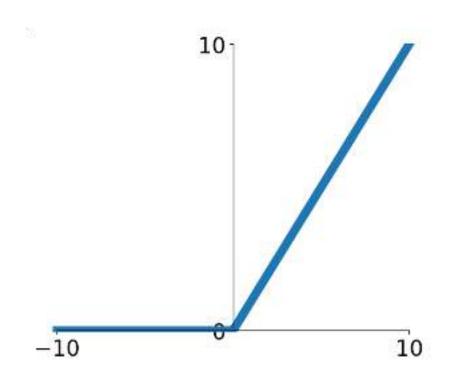
$$f(x) = max(0,x)$$



ReLU (Rectified Linear Unit)

- Does not saturate (in +region)
- Very computationally efficient
- Converges much faster than sigmoid/tanh in practice (e.g. 6x)

$$f(x) = \max(0,x)$$

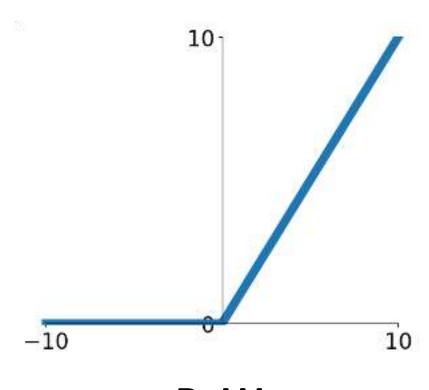


ReLU (Rectified Linear Unit)

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Not zero-centered output

$$f(x) = \max(0,x)$$

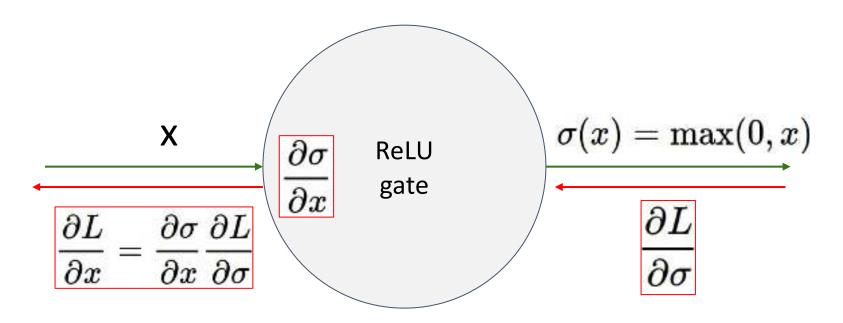


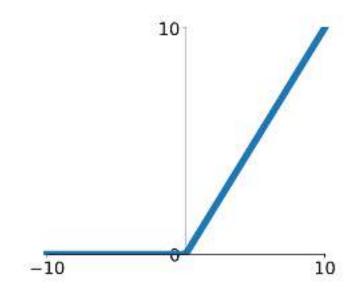
ReLU (Rectified Linear Unit)

- Does not saturate (in +region)
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- Not zero-centered output
- An annoyance:

hint: what is the gradient when x < 0?

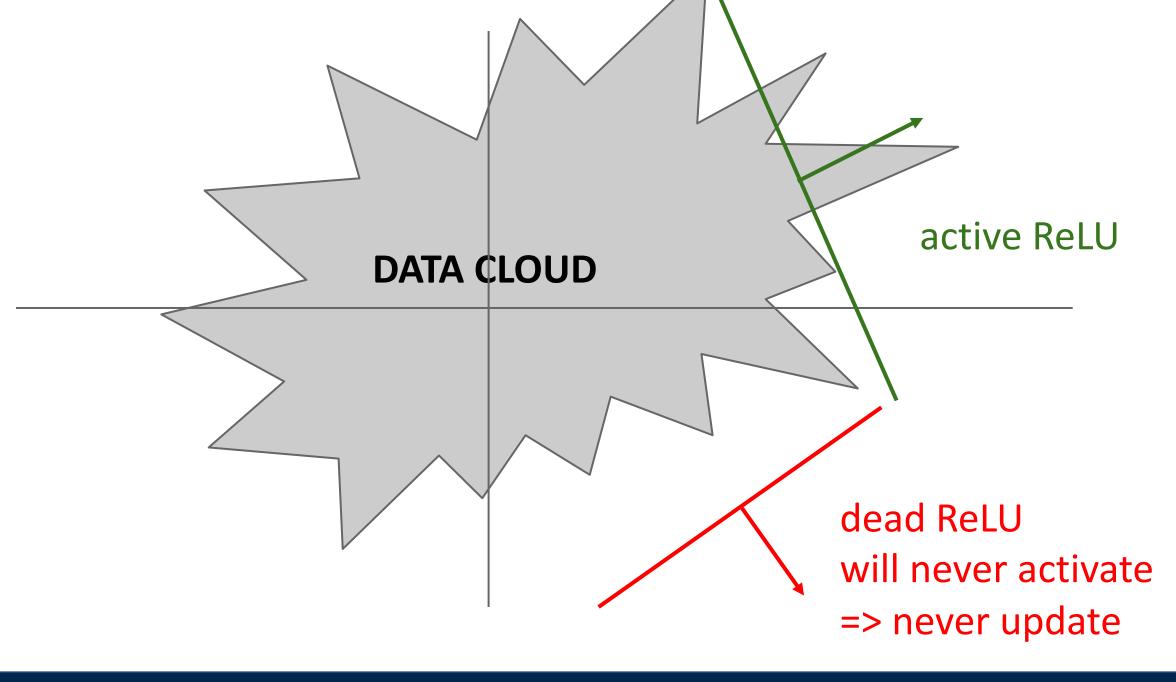




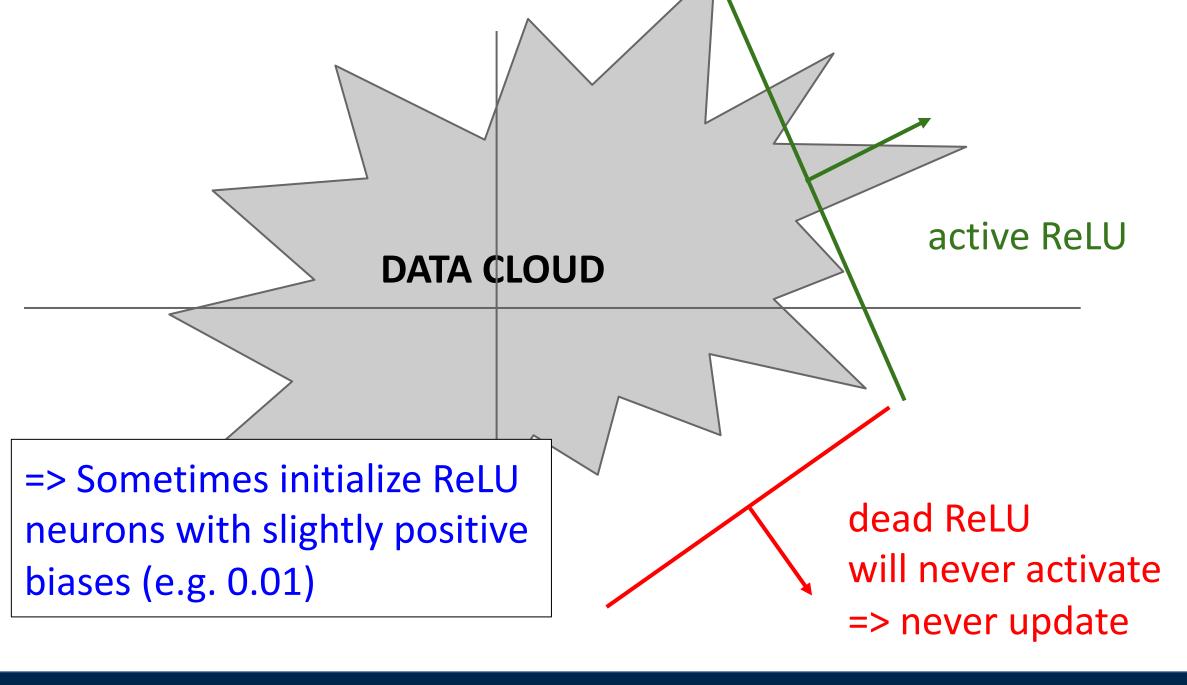
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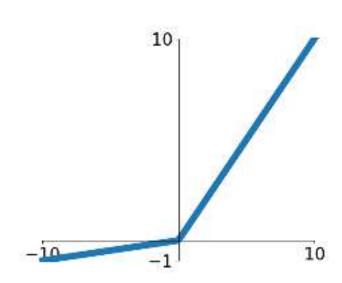


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Activation Functions: Leaky ReLU



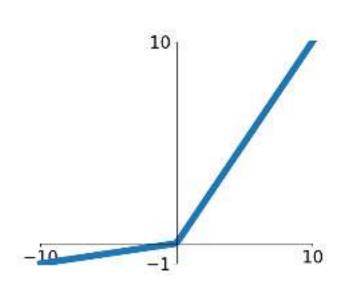
Leaky ReLU

 $f(x) = \max(\alpha x, x)$ α is a hyperparameter, often $\alpha = 0.1$

- Does not saturate
- Computationally efficient
- Converges much faster than sigmoid/tanh in practice! (e.g. 6x)
- will not "die".

Maas et al, "Rectifier Nonlinearities Improve Neural Network Acoustic Models", ICML 2013

Activation Functions: Leaky ReLU



Leaky ReLU

 $f(x) = \max(\alpha x, x)$ α is a hyperparameter, often $\alpha = 0.1$

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- Computationally efficient
- Converges much faster than
 sigmoid/tanh in practice! (e.g. 6x)
- will not "die".

Parametric ReLU (PReLU)

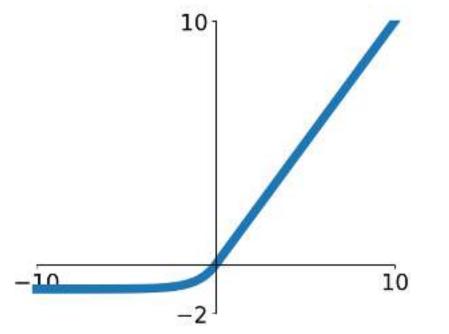
$$f(x) = \max(\alpha x, x)$$

 α is learned via backprop

Maas et al, "Rectifier Nonlinearities Improve Neural Network Acoustic Models", ICML 2013

He et al, "Delving Deep into Rectifiers: Surpassing Human-Level Performance on ImageNet Classification", ICCV 2015

Activation Functions: Exponential Linear Unit (ELU)



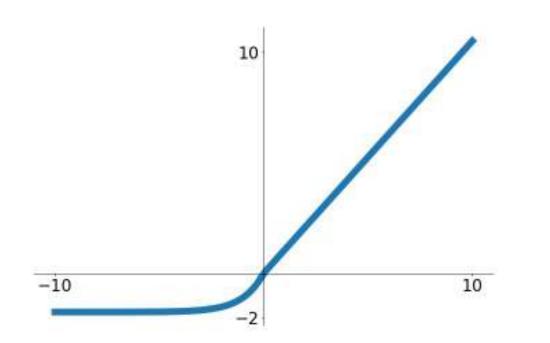
$$f(x) = \begin{cases} x & \text{if } x > 0 \\ \alpha(e^x - 1) & \text{if } x \le 0 \end{cases}$$

(Default alpha=1)

- All benefits of ReLU
- Closer to zero mean outputs
- Negative saturation regime compared with Leaky ReLU adds some robustness to noise

Computation requires exp()

Activation Functions: Scaled Exponential Linear Unit (SELU)



 Scaled version of ELU that works better for deep networks

"Self-Normalizing" property;
 can train deep SELU networks
 without BatchNorm

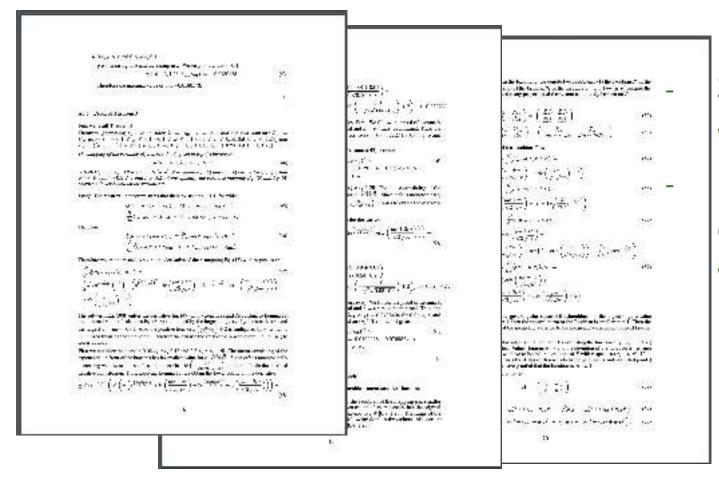
$$selu(x) = \begin{cases} \lambda x & if \ x > 0 \\ \lambda \alpha (e^x - 1) & if \ x \le 0 \end{cases}$$

 $\alpha = 1.6732632423543772848170429916717$

 $\lambda = 1.0507009873554804934193349852946$

Klambauer et al, Self-Normalizing Neural Networks, ICLR 2017

Activation Functions: Scaled Exponential Linear Unit (SELU)



Scaled version of ELU that works better for deep networks "Self-Normalizing" property; can train deep SELU networks without BatchNorm

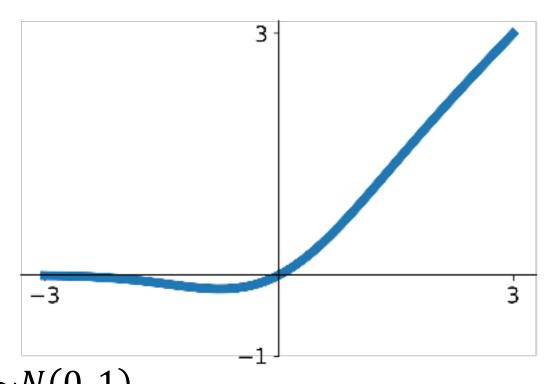
Derivation takes 91 pages of math in appendix...

 $\alpha = 1.6732632423543772848170429916717$

 $\lambda = 1.0507009873554804934193349852946$

Klambauer et al, Self-Normalizing Neural Networks, ICLR 2017

Activation Functions: Gaussian Error Linear Unit (GELU)



$$X \sim N(0, 1)$$

 $gelu(x) = xP(X \le x) = \frac{x}{2} (1 + erf(x/\sqrt{2}))$
 $\approx x\sigma(1.702x)$

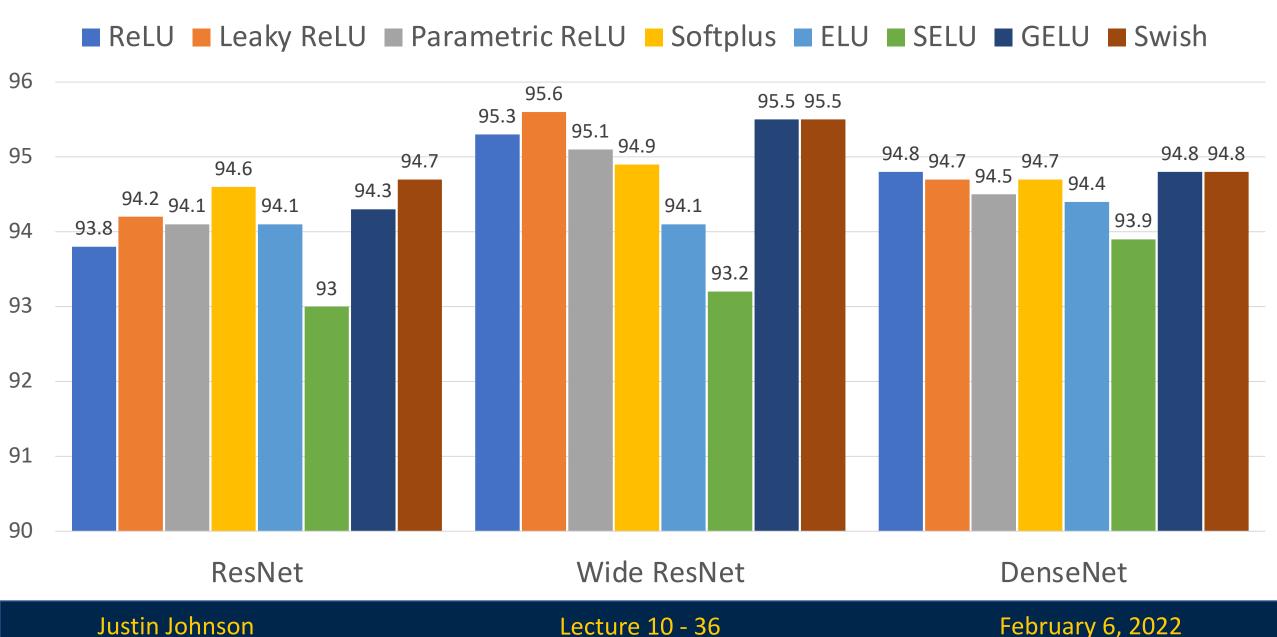
- Idea: Multiply input by 0 or 1 at random; large values more likely to be multiplied by 1, small values more likely to be multiplied by 0 (data-dependent dropout)
- Take expectation over randomness
 - Very common in Transformers (BERT, GPT, ViT)

Hendrycks and Gimpel, Gaussian Error Linear Units (GELUs), 2016

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Accuracy on CIFAR10



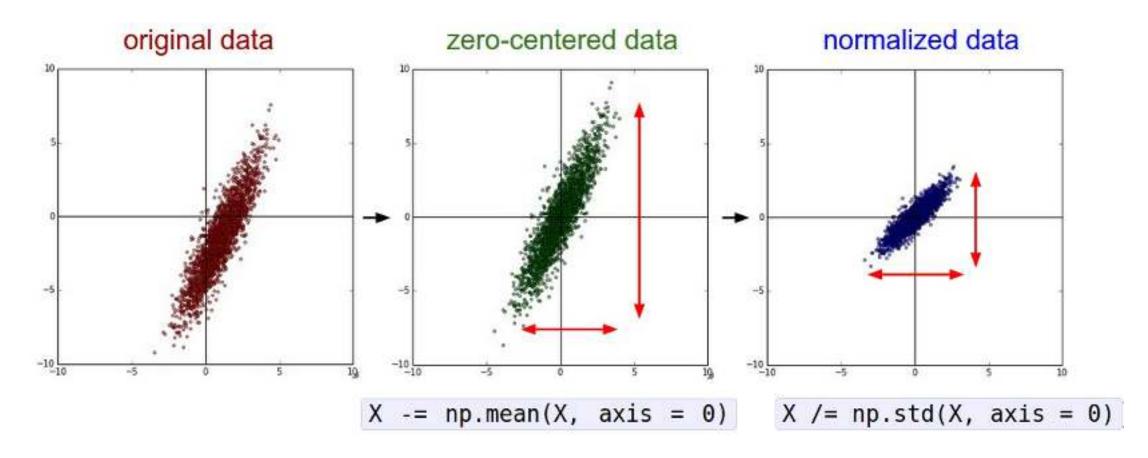
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Activation Functions: Summary

- Don't think too hard. Just use ReLU
- Try out Leaky ReLU / ELU / SELU / GELU if you need to squeeze that last 0.1%
- Don't use sigmoid or tanh

Some (very) recent architectures use GeLU instead of ReLU, but the gains are minimal

Dosovitskiy et al, "An Image is Worth 16x16 Words: Transformers for Image Recognition at Scale", ICLR 2021 Liu et al, "A ConvNet for the 2020s", arXiv 2022



(Assume X [NxD] is data matrix, each example in a row)

Remember: Consider what happens when the input to a neuron is always positive...

$$h_i^{(\ell)} = \sum_j w_{i,j}^{(\ell)} \sigma\left(h_j^{(\ell-1)}\right) + b_i^{(\ell)}$$

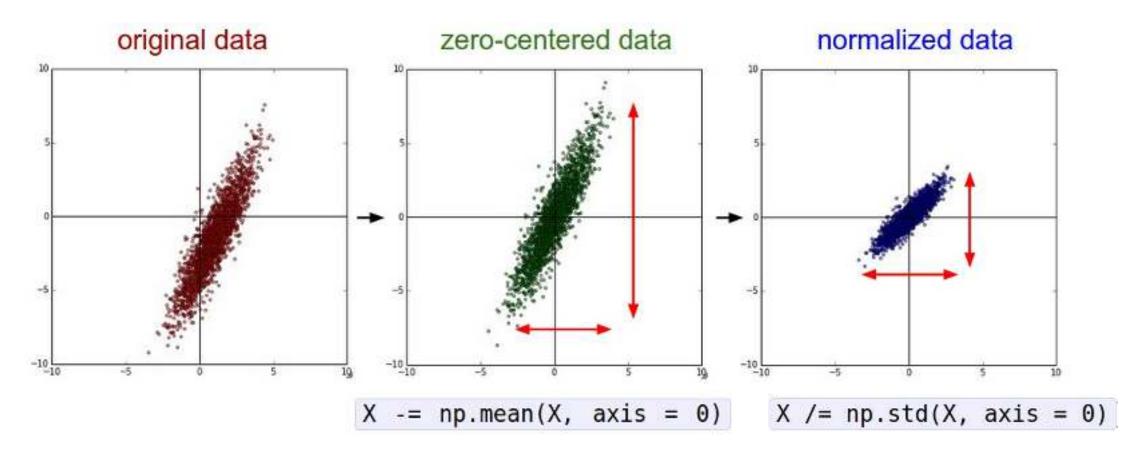
What can we say about the gradients on w? Always all positive or all negative: (
(this is also why you want zero-mean data!)

allowed gradient update directions

allowed gradient update directions

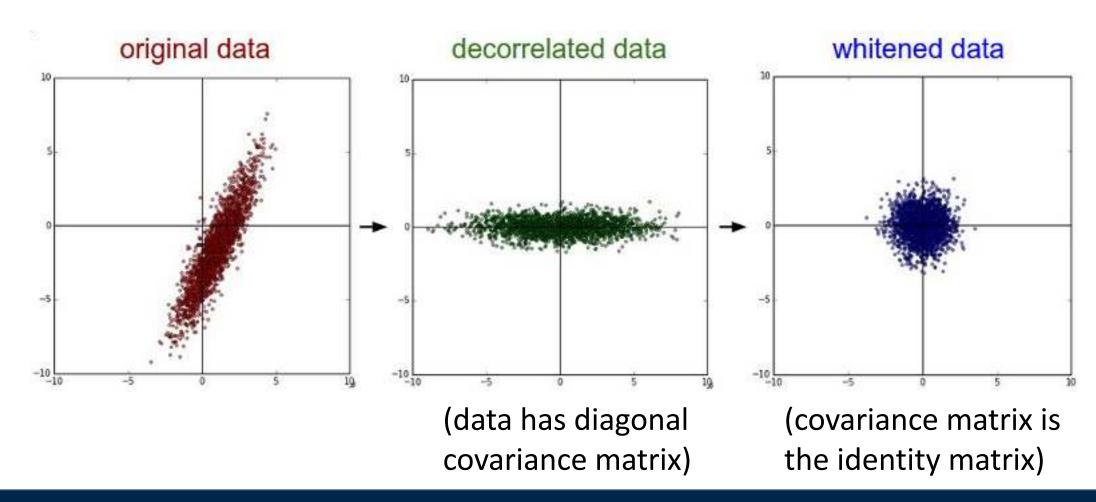
hypothetical optimal w vector

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(Assume X [NxD] is data matrix, each example in a row)

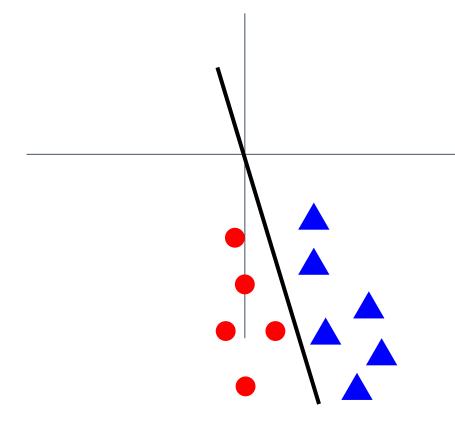
In practice, you may also see PCA and Whitening of the data

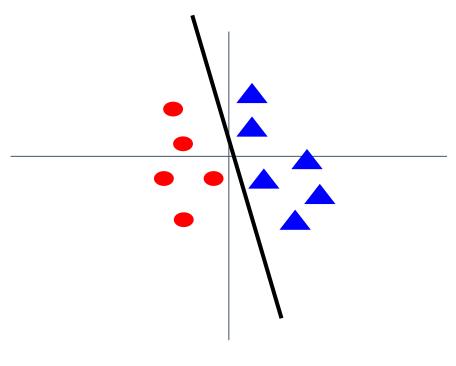


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Before normalization: classification loss very sensitive to changes in weight matrix; hard to optimize

After normalization: less sensitive to small changes in weights; easier to optimize





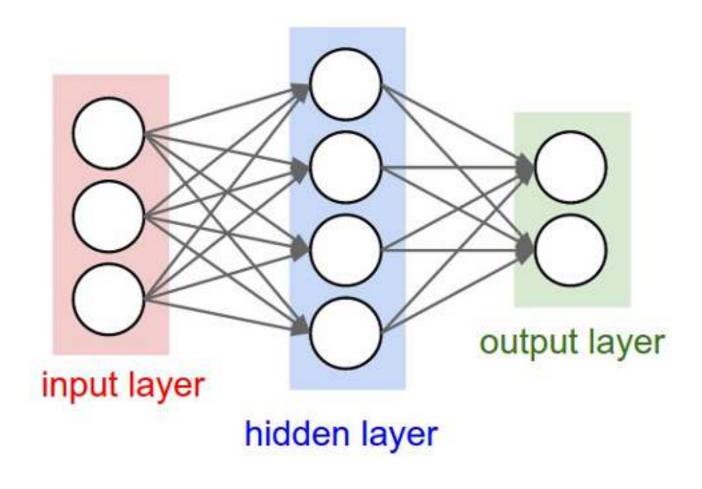
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Data Preprocessing for Images

e.g. consider CIFAR-10 example with [32,32,3] images

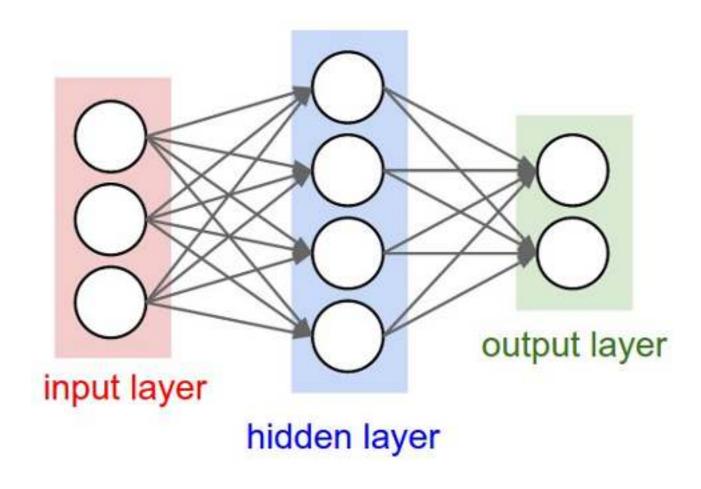
- Subtract the mean image (e.g. AlexNet)
 (mean image = [32,32,3] array)
- Subtract per-channel mean (e.g. VGGNet)
 (mean along each channel = 3 numbers)
- Subtract per-channel mean and
 Divide by per-channel std (e.g. ResNet)
 (mean along each channel = 3 numbers)

Not common to do PCA or whitening



Q: What happens if we initialize all W=0, b=0?

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Q: What happens if we initialize all W=0, b=0?

A: All outputs are 0, all gradients are the same!
No "symmetry breaking"

Next idea: **small random numbers** (Gaussian with zero mean, std=0.01)

W = 0.01 * np.random.randn(Din, Dout)

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Next idea: **small random numbers** (Gaussian with zero mean, std=0.01)

```
W = 0.01 * np.random.randn(Din, Dout)
```

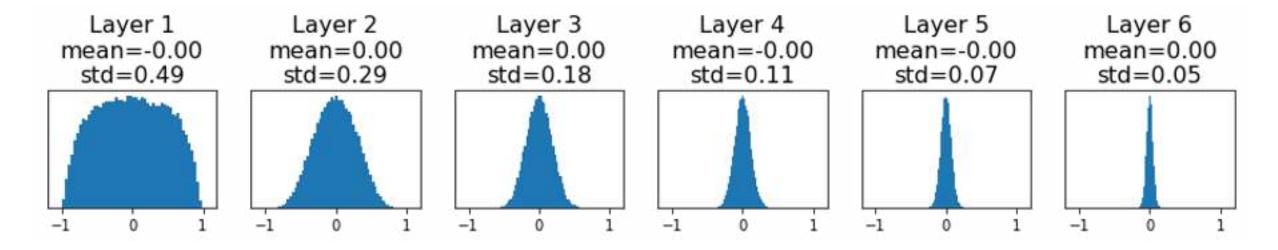
Works ~okay for small networks, but problems with deeper networks.

```
dims = [4096] * 7 Forward pass for a 6-layer
hs = [] net with hidden size 4096
x = np.random.randn(16, dims[0])
for Din, Dout in zip(dims[:-1], dims[1:]):
    W = 0.01 * np.random.randn(Din, Dout)
    x = np.tanh(x.dot(W))
    hs.append(x)
```

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```

All activations tend to zero for deeper network layers

Q: What do the gradients dL/dW look like?



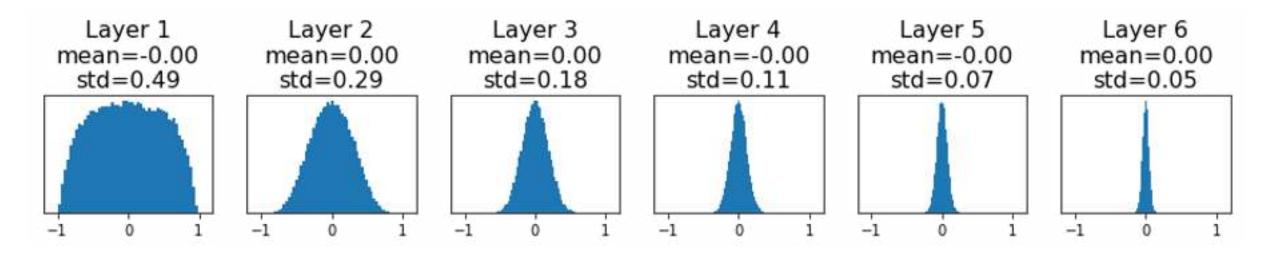
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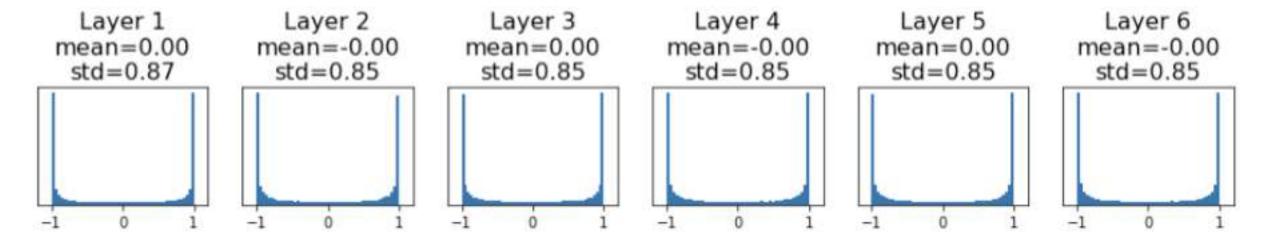
A: All zero, no learning =(



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All activations saturate

Q: What do the gradients look like?

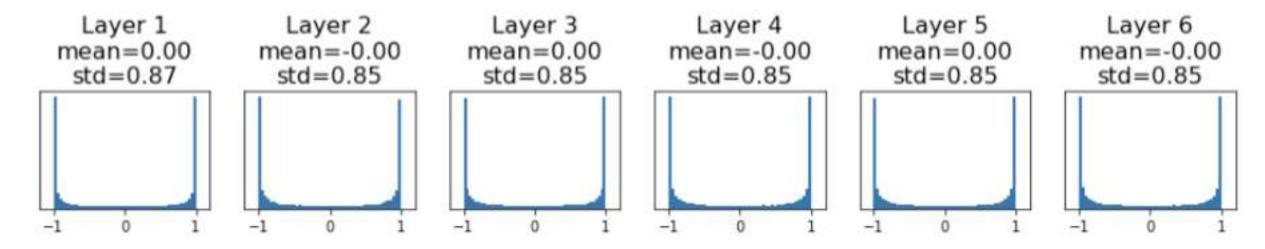


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All activations saturate

Q: What do the gradients look like?

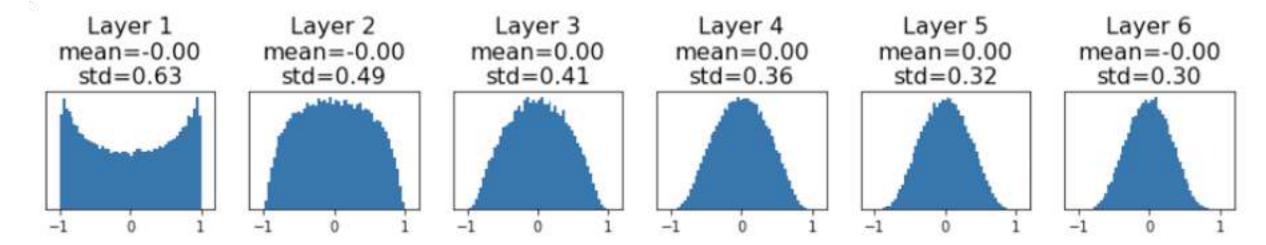
A: Local gradients all zero, no learning =(



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Glorot and Bengio, "Understanding the difficulty of training deep feedforward neural networks", AISTAT 2010

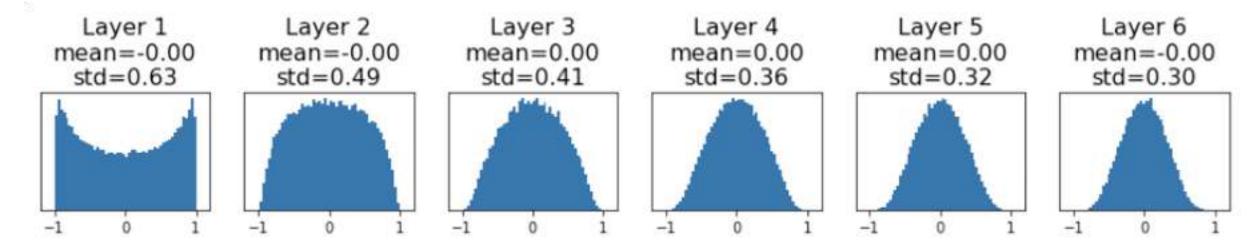
"Just right": Activations are nicely scaled for all layers!



Glorot and Bengio, "Understanding the difficulty of training deep feedforward neural networks", AISTAT 2010

"Just right": Activations are nicely scaled for all layers!

For conv layers, Din is kernel_size² * input_channels



Glorot and Bengio, "Understanding the difficulty of training deep feedforward neural networks", AISTAT 2010

"Xavier" initialization: std = 1/sqrt(Din)

Derivation: Variance of output = Variance of input

$$y = Wx y_i = \sum_{j=1}^{Din} x_j w_j$$

"Xavier" initialization: std = 1/sqrt(Din)

Derivation: Variance of output = Variance of input

$$y = Wx$$

$$y_i = \sum_{j=1}^{Din} x_j w_j$$

$$Var(y_i) = Din * Var(x_i w_i)$$

[Assume x, w are iid]

"Xavier" initialization: std = 1/sqrt(Din)

Derivation: Variance of output = Variance of input

$$y = Wx y_i = \sum_{j=1}^{Din} x_j w_j$$

$$Var(y_i) = Din * Var(x_i w_i)$$
 [Assume x, w are iid]
= $Din * (E[x_i^2]E[w_i^2] - E[x_i]^2 E[w_i]^2)$ [Assume x, w independent]

"Xavier" initialization: std = 1/sqrt(Din)

Derivation: Variance of output = Variance of input

$$y = Wx y_i = \sum_{j=1}^{Din} x_j w_j$$

 $Var(y_i) = Din * Var(x_i w_i)$ [Assume x, w are iid] = $Din * (E[x_i^2]E[w_i^2] - E[x_i]^2 E[w_i]^2)$ [Assume x, w independent] = $Din * Var(x_i) * Var(w_i)$ [Assume x, w are zero-mean]

"Xavier" initialization: std = 1/sqrt(Din)

Derivation: Variance of output = Variance of input

$$y = Wx y_i = \sum_{j=1}^{Din} x_j w_j$$

 $Var(y_i) = Din * Var(x_i w_i)$ [Assume x, w are iid] = $Din * (E[x_i^2]E[w_i^2] - E[x_i]^2 E[w_i]^2)$ [Assume x, w independent] = $Din * Var(x_i) * Var(w_i)$ [Assume x, w are zero-mean]

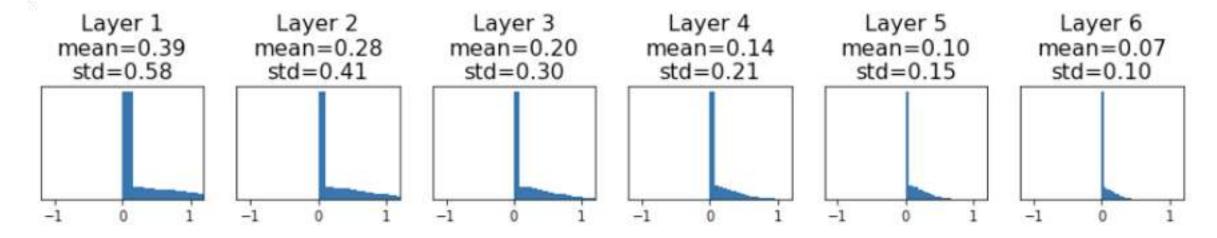
If $Var(w_i) = 1/Din then <math>Var(y_i) = Var(x_i)$

Weight Initialization: What about ReLU?

Weight Initialization: What about ReLU?

Xavier assumes zero centered activation function

Activations collapse to zero again, no learning =(

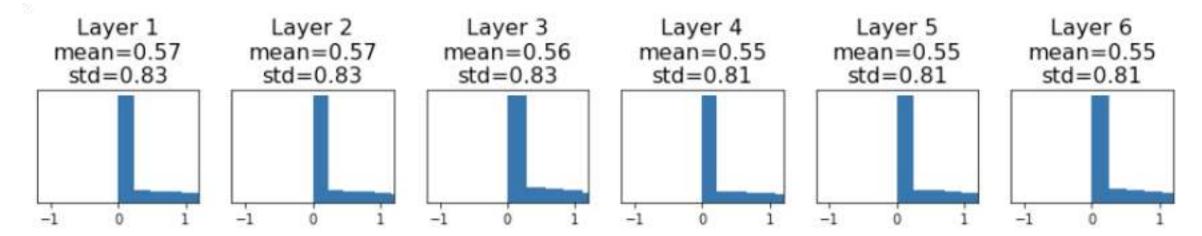


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Weight Initialization: Kaiming / MSRA Initialization

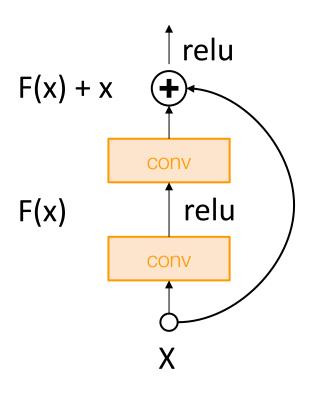
```
dims = [4096] * 7 ReLU correction: std = sqrt(2 / Din)
hs = []
x = np.random.randn(16, dims[0])
for Din, Dout in zip(dims[:-1], dims[1:]):
    W = np.random.randn(Din, Dout) / np.sqrt(Din)
    x = np.maximum(0, x.dot(W))
    hs.append(x)
```

"Just right" – activations nicely scaled for all layers



He et al, "Delving Deep into Rectifiers: Surpassing Human-Level Performance on ImageNet Classification", ICCV 2015

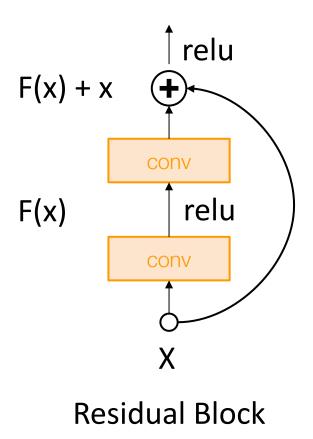
Weight Initialization: Residual Networks



Residual Block

If we initialize with MSRA: then Var(F(x)) = Var(x)But then Var(F(x) + x) > Var(x)variance grows with each block!

Weight Initialization: Residual Networks



If we initialize with MSRA: then Var(F(x)) = Var(x) But then Var(F(x) + x) > Var(x) variance grows with each block!

Solution: Initialize first conv with MSRA, initialize second conv to zero. Then Var(x + F(x)) = Var(x)

Zhang et al, "Fixup Initialization: Residual Learning Without Normalization", ICLR 2019

Proper initialization is an active area of research

Understanding the difficulty of training deep feedforward neural networks by Glorot and Bengio, 2010

Exact solutions to the nonlinear dynamics of learning in deep linear neural networks by Saxe et al, 2013

Random walk initialization for training very deep feedforward networks by Sussillo and Abbott, 2014

Delving deep into rectifiers: Surpassing human-level performance on ImageNet classification by He et al., 2015

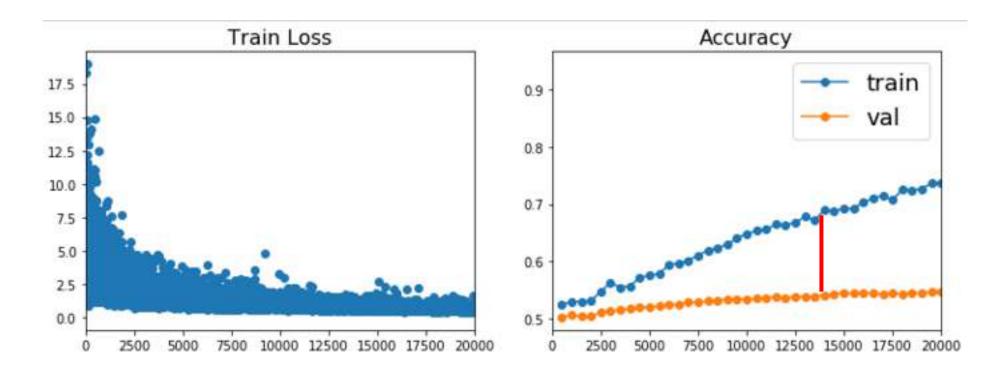
Data-dependent Initializations of Convolutional Neural Networks by Krähenbühl et al., 2015

All you need is a good init, Mishkin and Matas, 2015

Fixup Initialization: Residual Learning Without Normalization, Zhang et al, 2019

The Lottery Ticket Hypothesis: Finding Sparse, Trainable Neural Networks, Frankle and Carbin, 2019

Now your model is training ... but it overfits!



Regularization

Regularization: Add term to the loss

$$L = rac{1}{N} \sum_{i=1}^{N} \sum_{j
eq y_i} \max(0, f(x_i; W)_j - f(x_i; W)_{y_i} + 1) + \lambda R(W)$$

In common use:

L2 regularization

L1 regularization

Elastic net (L1 + L2)

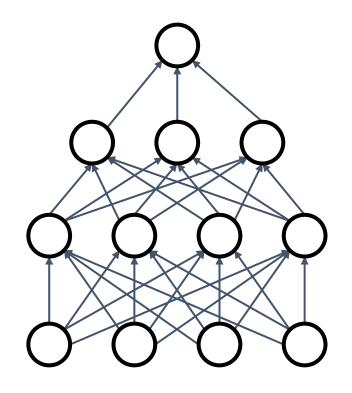
$$R(W) = \sum_k \sum_l W_{k,l}^2$$
 (Weight decay)

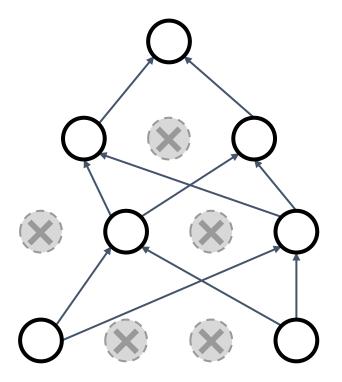
$$R(W) = \sum_k \sum_l |W_{k,l}|$$

$$R(W) = \sum_{k} \sum_{l} \beta W_{k,l}^2 + |W_{k,l}|$$

Regularization: Dropout

In each forward pass, randomly set some neurons to zero Probability of dropping is a hyperparameter; 0.5 is common



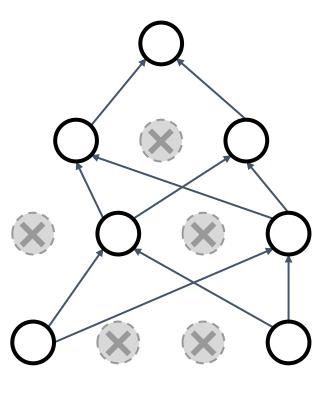


Srivastava et al, "Dropout: A simple way to prevent neural networks from overfitting", JMLR 2014

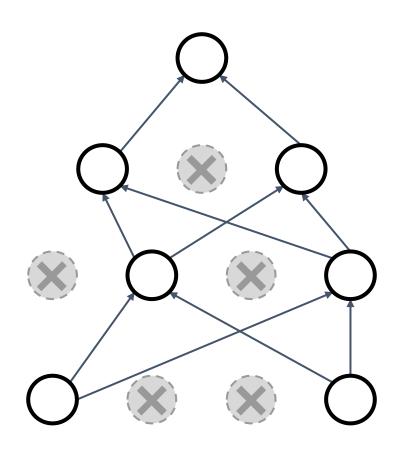
Regularization: Dropout

```
p = 0.5 # probability of keeping a unit active. higher = less dropout
def train_step(X):
  """ X contains the data """
 # forward pass for example 3-layer neural network
 H1 = np.maximum(0, np.dot(W1, X) + b1)
 U1 = np.random.rand(*H1.shape) < p # first dropout mask
 H1 *= U1 # drop!
 H2 = np.maximum(0, np.dot(W2, H1) + b2)
 U2 = np.random.rand(*H2.shape) < p # second dropout mask
 H2 *= U2 # drop!
 out = np.dot(W3, H2) + b3
 # backward pass: compute gradients... (not shown)
 # perform parameter update... (not shown)
```

Example forward pass with a 3-layer network using dropout



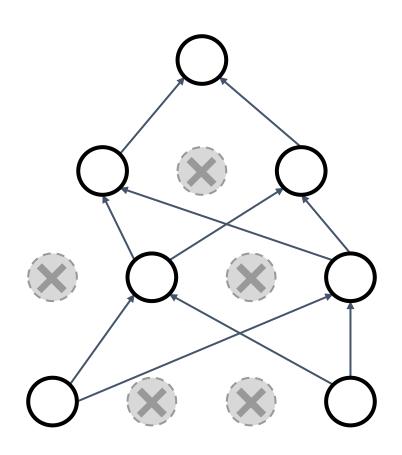
Regularization: Dropout



Forces the network to have a redundant representation; Prevents **co-adaptation** of features



Regularization: Dropout



Another interpretation:

Dropout is training a large **ensemble** of models (that share parameters).

Each binary mask is one model

An FC layer with 4096 units has $2^{4096} \sim 10^{1233}$ possible masks! Only $\sim 10^{82}$ atoms in the universe...

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Output Input (label) (image)

Dropout makes our output random!

$$\mathbf{y} = f_W(\mathbf{x}, \mathbf{z})$$
 Random mask

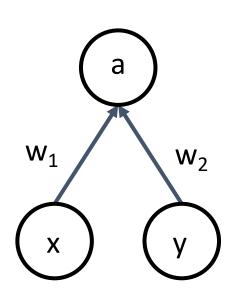
Want to "average out" the randomness at test-time

$$y = f(x) = E_z[f(x,z)] = \int p(z)f(x,z)dz$$

But this integral seems hard ...

Want to approximate the integral

$$y = f(x) = E_z[f(x,z)] = \int p(z)f(x,z)dz$$

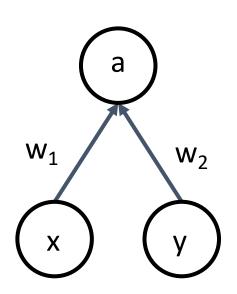


Consider a single neuron:

At test time we have: $E[a] = w_1x + w_2y$

Want to approximate the integral

$$y = f(x) = E_z[f(x,z)] = \int p(z)f(x,z)dz$$

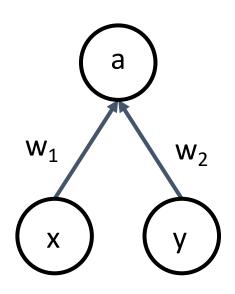


Consider a single neuron:

At test time we have: $E[a] = w_1 x + w_2 y$ During training we have: $E[a] = \frac{1}{4}(w_1 x + w_2 y) + \frac{1}{4}(w_1 x + 0 y) + \frac{1}{4}(0x + 0y) + \frac{1}{4}(0x + w_2 y) + \frac{1}{4}(0x + w_2 y) + \frac{1}{4}(0x + w_2 y)$

Want to approximate the integral

$$y = f(x) = E_z[f(x,z)] = \int p(z)f(x,z)dz$$



Consider a single neuron:

At test time we have: $E[a] = w_1x + w_2y$ During training we have: $E[a] = \frac{1}{4}(w_1x + w_2y) + \frac{1}{4}(w_1x + 0y)$ At test time, drop $+\frac{1}{4}(0x + 0y) + \frac{1}{4}(0x + w_2y)$ nothing and **multiply** $=\frac{1}{2}(w_1x + w_2y)$ by dropout probability

```
def predict(X):
    # ensembled forward pass
H1 = np.maximum(0, np.dot(W1, X) + b1) * p # NOTE: scale the activations
H2 = np.maximum(0, np.dot(W2, H1) + b2) * p # NOTE: scale the activations
out = np.dot(W3, H2) + b3
```

At test time all neurons are active always => We must scale the activations so that for each neuron: output at test time = expected output at training time

Dropout Summary

```
""" Vanilla Dropout: Not recommended implementation (see notes below) """
p = 0.5 # probability of keeping a unit active. higher = less dropout
def train step(X):
  """ X contains the data """
 # forward pass for example 3-layer neural network
 H1 = np.maximum(0, np.dot(W1, X) + b1)
 U1 = np.random.rand(*H1.shape) < p # first dropout mask
 H1 *= U1 # drop!
 H2 = np.maximum(0, np.dot(W2, H1) + b2)
 U2 = np.random.rand(*H2.shape) < p # second dropout mask
 H2 *= U2 # drop!
 out = np.dot(W3, H2) + b3
 # backward pass: compute gradients... (not shown)
 # perform parameter update... (not shown)
def predict(X):
 # ensembled forward pass
 H1 = np.maximum(\theta, np.dot(W1, X) + b1) * p # NOTE: scale the activations
 H2 = np.maximum(0, np.dot(W2, H1) + b2) * p # NOTE: scale the activations
 out = np.dot(W3, H2) + b3
```

drop in forward pass

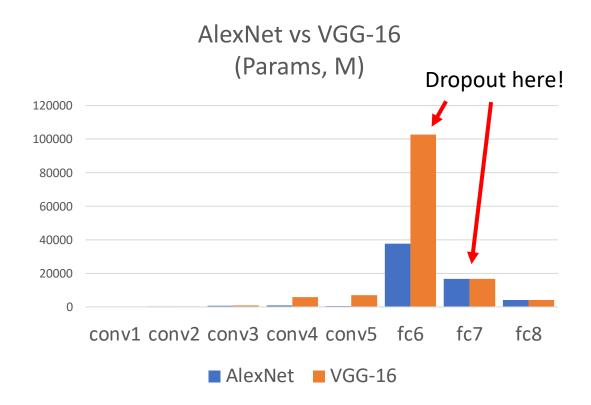
scale at test time

More common: "Inverted dropout"

```
p = 0.5 # probability of keeping a unit active. higher = less dropout
def train step(X):
 # forward pass for example 3-layer neural network
 H1 = np.maximum(0, np.dot(W1, X) + b1)
 U1 = (np.random.rand(*H1.shape) < p) / p # first dropout mask. Notice /p!
                                                                            Drop and scale
 H1 *= U1 # drop!
 H2 = np.maximum(0, np.dot(W2, H1) + b2)
                                                                            during training
 U2 = (np.random.rand(*H2.shape) < p) / p # second dropout mask. Notice /p!
 H2 *= U2 # drop!
 out = np.dot(W3, H2) + b3
 # backward pass: compute gradients... (not shown)
 # perform parameter update... (not shown)
                                                                    test time is unchanged!
def predict(X):
 # ensembled forward pass
 H1 = np.maximum(0, np.dot(W1, X) + b1) # no scaling necessary
 H2 = np.maximum(0, np.dot(W2, H1) + b2)
 out = np.dot(W3, H2) + b3
```

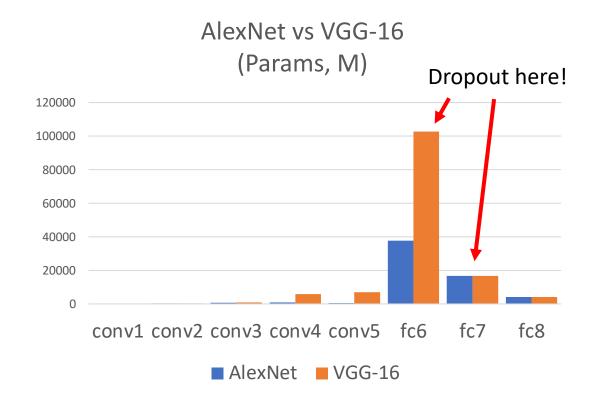
Dropout architectures

Recall AlexNet, VGG have most of their parameters in **fully-connected layers**; usually Dropout is applied there



Dropout architectures

Recall AlexNet, VGG have most of their parameters in **fully-connected layers**; usually Dropout is applied there



Later architectures (GoogLeNet, ResNet, etc) use global average pooling instead of fully-connected layers: they don't use dropout at all!

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Training: Add some kind of randomness

$$y = f_W(x, z)$$

Testing: Average out randomness (sometimes approximate)

$$y = f(x) = E_z[f(x,z)] = \int p(z)f(x,z)dz$$

Training: Add some kind of randomness

$$y = f_W(x, z)$$

Testing: Average out randomness (sometimes approximate)

$$y = f(x) = E_z[f(x,z)] = \int p(z)f(x,z)dz$$

Example: Batch Normalization

Training: Normalize using stats from random minibatches

Testing: Use fixed stats to normalize

Training: Add some kind of randomness

$$y = f_W(x, z)$$

For ResNet and later, often L2 and Batch Normalization are the only regularizers!

Testing: Average out randomness (sometimes approximate)

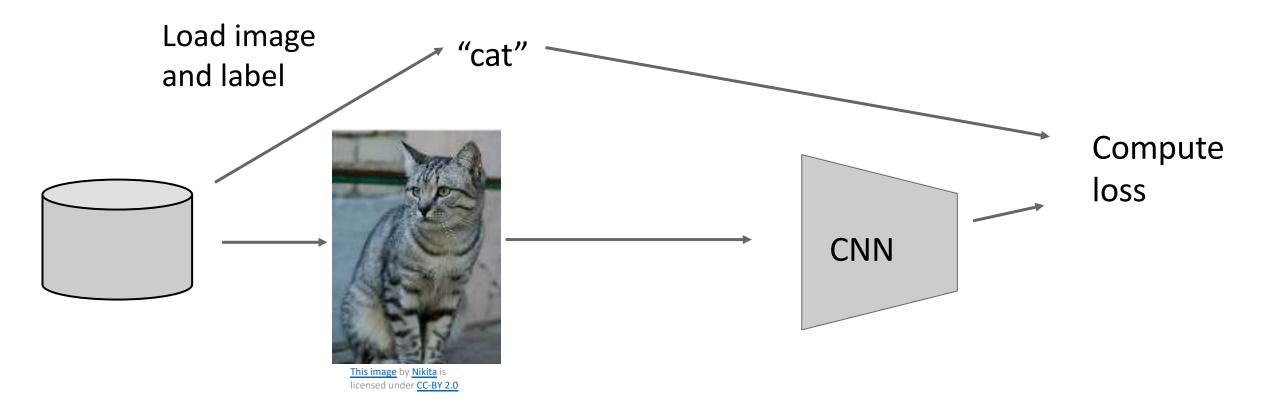
$$y = f(x) = E_z[f(x,z)] = \int p(z)f(x,z)dz$$

Example: Batch Normalization

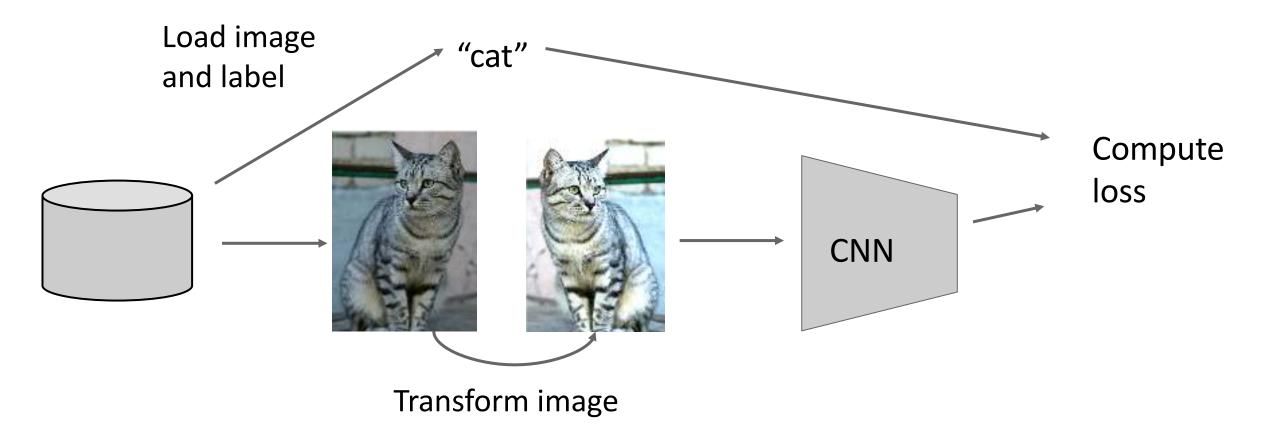
Training: Normalize using stats from random minibatches

Testing: Use fixed stats to normalize

Data Augmentation



Data Augmentation



Data Augmentation: Horizontal Flips





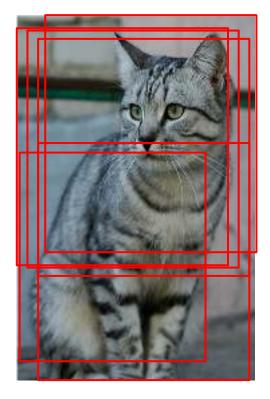


Data Augmentation: Random Crops and Scales

Training: sample random crops / scales

ResNet:

- 1. Pick random L in range [256, 480]
- 2. Resize training image, short side = L
- 3. Sample random 224 x 224 patch



Data Augmentation: Random Crops and Scales

Training: sample random crops / scales

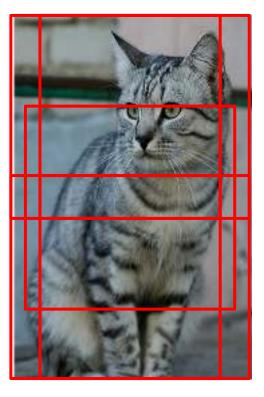
ResNet:

- 1. Pick random L in range [256, 480]
- 2. Resize training image, short side = L
- 3. Sample random 224 x 224 patch



ResNet:

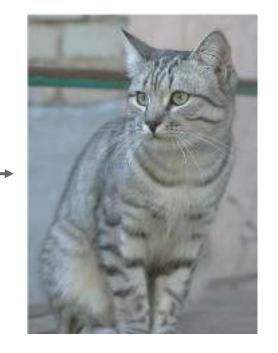
- 1. Resize image at 5 scales: {224, 256, 384, 480, 640}
- 2. For each size, use 10 224 x 224 crops: 4 corners + center, + flips



Data Augmentation: Color Jitter

Simple: Randomize contrast and brightness





More Complex:

- Apply PCA to all [R, G, B] pixels in training set
- Sample a "color offset" along principal component directions
- 3. Add offset to all pixels of a training image

(Used in AlexNet, ResNet, etc)

Data Augmentation: RandAugment

Apply random combinations of transforms:

- **Geometric**: Rotate, translate, shear
- Color: Sharpen, contrast, brightness, solarize, posterize, color

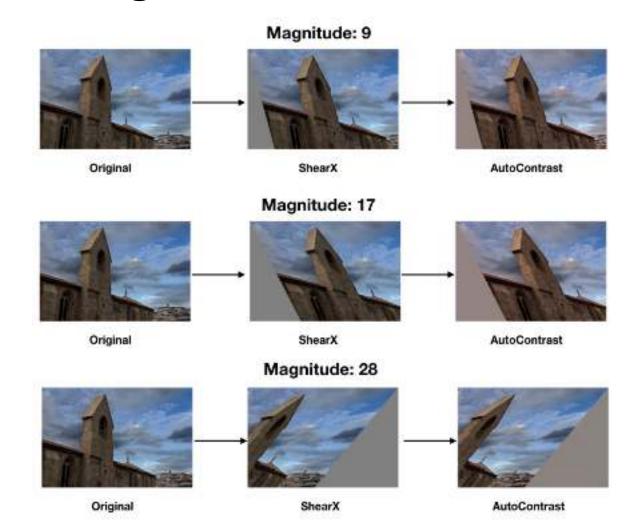
```
transforms = [
'Identity', 'AutoContrast', 'Equalize',
'Rotate', 'Solarize', 'Color', 'Posterize',
'Contrast', 'Brightness', 'Sharpness',
'ShearX', 'ShearY', 'TranslateX', 'TranslateY']
def randaugment (N, M):
"""Generate a set of distortions.
  Args:
   N: Number of augmentation transformations to
        apply sequentially.
   M: Magnitude for all the transformations.
 sampled_ops = np.random.choice(transforms, N)
 return [(op, M) for op in sampled_ops]
```

Cubuk et al, "RandAugment: Practical augmented data augmentation with a reduced search space", NeurIPS 2020

Data Augmentation: RandAugment

Apply random combinations of transforms:

- Geometric: Rotate, translate, shear
- Color: Sharpen, contrast, brightness, solarize, posterize, color



Cubuk et al, "RandAugment: Practical augmented data augmentation with a reduced search space", NeurIPS 2020

Data Augmentation: Get creative for your problem!

Data augmentation encodes invariances in your model

Think for your problem: what changes to the image should **not** change the network output?

May be different for different tasks!

Training: Add some randomness

Testing: Marginalize over randomness

Examples:

Dropout

Batch Normalization

Data Augmentation

Wan et al, "Regularization of Neural Networks using DropConnect", ICML 2013

Regularization: DropConnect

Training: Drop random connections between neurons (set weight=0)

Testing: Use all the connections

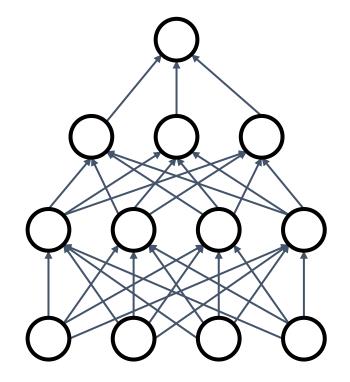
Examples:

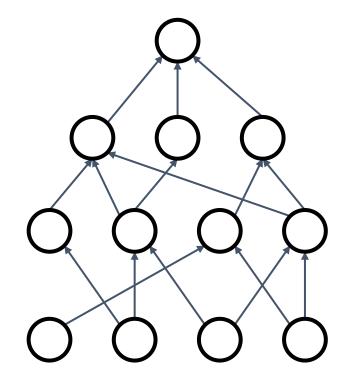
Dropout

Batch Normalization

Data Augmentation

DropConnect





Wan et al, "Regularization of Neural Networks using DropConnect", ICML 2013

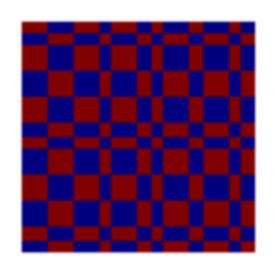
Regularization: Fractional Pooling

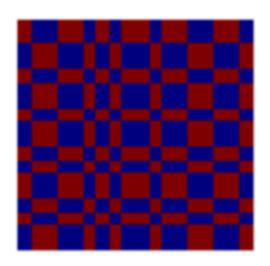
Training: Use randomized pooling regions

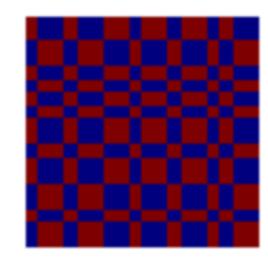
Testing: Average predictions over different samples

Examples:

Dropout
Batch Normalization
Data Augmentation
DropConnect
Fractional Max Pooling







Graham, "Fractional Max Pooling", arXiv 2014

Regularization: Stochastic Depth

Training: Skip some residual blocks in ResNet

Testing: Use the whole network

Examples:

Dropout

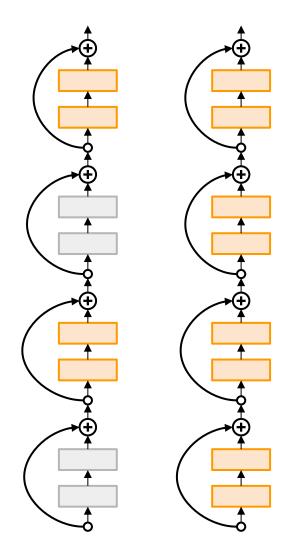
Batch Normalization

Data Augmentation

DropConnect

Fractional Max Pooling

Stochastic Depth



Huang et al, "Deep Networks with Stochastic Depth", ECCV 2016

Regularization: Stochastic Depth

Training: Skip some residual blocks in ResNet

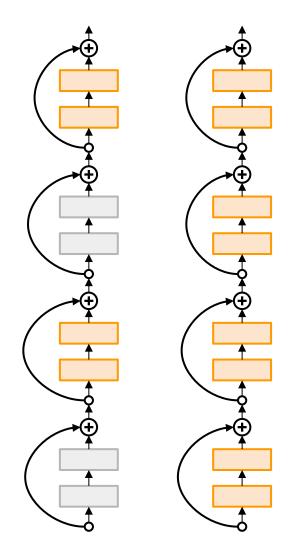
Testing: Use the whole network

Examples:

Dropout
Batch Normalization
Data Augmentation
DropConnect
Fractional Max Pooling
Stochastic Depth

Starting to become common in recent architectures!

- Pham et al, "Very Deep Self-Attention Networks for End-to-End Speech Recognition", INTERSPEECH 2019
- Tan and Le, "EfficientNetV2: Smaller Models and Faster Training", ICML 2021
- Fan et al, "Multiscale Vision Transformers", ICCV 2021
- Bello et al, "Revisiting ResNets: Improved Training and Scaling Strategies", NeurIPS 2021
- Steiner et al, "How to train your ViT? Data, Augmentation, and Regularization in Vision Transformers", arXiv 2021



Huang et al, "Deep Networks with Stochastic Depth", ECCV 2016

Regularization: CutOut

Training: Set random images regions to 0

Testing: Use the whole image

Examples:

Dropout

Batch Normalization

Data Augmentation

DropConnect

Fractional Max Pooling

Stochastic Depth

Cutout / Random Erasing









Replace random regions with mean value or random values

DeVries and Taylor, "Improved Regularization of Convolutional Neural Networks with Cutout", arXiv 2017 Zhong et al, "Random Erasing Data Augmentation", AAAI 2020

Regularization: Mixup

Training: Train on random blends of images

Testing: Use original images

Examples:

Dropout
Batch Normalization
Data Augmentation
DropConnect
Fractional Max Pooling
Stochastic Depth
Cutout / Random Erasing
Mixup







CNN cardo

Target label: cat: 0.4 dog: 0.6

Randomly blend the pixels of pairs of training images, e.g. 40% cat, 60% dog

Zhang et al, "mixup: Beyond Empirical Risk Minimization", ICLR 2018

Regularization: Mixup

Training: Train on random blends of images

Testing: Use original images

1.0 0.8 0.6 0.4 0.2 0.0 0.2 0.4 0.6 0.8 1.0

Sample blend probability from a beta distribution Beta(a, b) with a=b≈0 so blend weights are close to 0/1

Examples:

Dropout
Batch Normalization
Data Augmentation
DropConnect
Fractional Max Pooling
Stochastic Depth
Cutout / Random Erasing
Mixup







Target label: cat: 0.4 dog: 0.6

CNN

Randomly blend the pixels of pairs of training images, e.g. 40% cat, 60% dog

Zhang et al, "mixup: Beyond Empirical Risk Minimization", ICLR 2018

Regularization: CutMix

Training: Train on random blends of images

Testing: Use original images

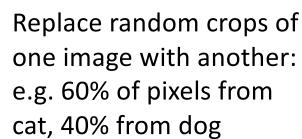
Examples:

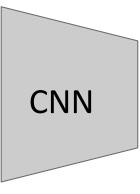
Dropout
Batch Normalization
Data Augmentation
DropConnect
Fractional Max Pooling
Stochastic Depth
Cutout / Random Erasing
Mixup / CutMix











Target label: cat: 0.6 dog: 0.4

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Regularization: Label Smoothing

Training: Train on random blends of images

Testing: Use original images

Examples:

Dropout

Batch Normalization

Data Augmentation

DropConnect

Fractional Max Pooling

Stochastic Depth

Cutout / Random Erasing

Mixup / CutMix

Label Smoothing



Target Distribution

Standard Training Label Smoothing

Cat: 100% Cat: 90%

Dog: 0% Dog: 5%

Fish: 0% Fish: 5%

Set target distribution to be $1-\frac{K-1}{K}\epsilon$ on the correct category and ϵ/K on all other categories, with K categories and $\epsilon\in(0,1)$. Loss is cross-entropy between predicted and target distribution.

Regularization: Summary

Training: Train on random blends of images

Testing: Use original images

Examples:

Dropout

Batch Normalization

Data Augmentation

DropConnect

Fractional Max Pooling

Stochastic Depth

Cutout / Random Erasing

Mixup / CutMix

Label Smoothing

- Use DropOut for large fully-connected layers
- Data augmentation always a good idea
- Use BatchNorm for CNNs (but not ViTs)
- Try Cutout, MixUp, CutMix, Stochastic Depth, Label Smoothing to squeeze out a bit of extra performance

Summary

1. One time setup

Activation functions, data preprocessing, weight initialization, regularization

2. Training dynamics

Learning rate schedules; large-batch training; hyperparameter optimization

3. After training

Model ensembles, transfer learning

Today

Next time

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Next time: Training Neural Networks (part 2)