

Q1: Consider augmented matrices:

①

$$A = \left( \begin{array}{cccc|c} 1 & 1 & 2 & 3 & 1 \\ 0 & 0 & 1 & 2 & 1 \\ 0 & 0 & 2 & 4 & 2 \end{array} \right)$$

$$B = \left( \begin{array}{cccc|c} 1 & 1 & 2 & 3 & 1 \\ 0 & 0 & 1 & 2 & 1 \\ 2 & 2 & 4 & 6 & 5 \end{array} \right)$$

Mark each statement True or False regarding each matrix.

C) System with this matrix has no solution

D)  $\begin{pmatrix} -2 \\ 0 \\ 1 \\ 0 \end{pmatrix}$  is a solution for the system with this matrix

E)  $\begin{pmatrix} 0 \\ 0 \\ -1 \\ 1 \end{pmatrix}$  is a solution for the system with this matrix

F) System with this matrix has infinitely many solutions

G) Matrix has pivot position in every row

H) Columns of coefficient matrix span  $\mathbb{R}^3$ .

I) Rows of coefficient matrix span  $\mathbb{R}^2$ .

J)  $\begin{pmatrix} 1 & 1 & 2 & 3 \\ 0 & 0 & 1 & 2 \\ 0 & 0 & 2 & 4 \end{pmatrix} \begin{pmatrix} x \\ y \\ z \\ t \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix}$  has only trivial solution

K) Columns of a matrix are linear independent

L) Rows of a matrix are linear dependant

(For both K & L we consider coefficient mat.)

	C	D	E	F	G	H	I	K	L
A	F	F	T	T	F	F	F	F	T
B	T	F	F	F	F	F	F	F	T

J ☐ F

Q2: Consider coefficient matrices:

②

$$A = \begin{pmatrix} 1 & 2 & 1 \\ 0 & 1 & 1 \\ 0 & 0 & 2 \end{pmatrix}$$

$$B = \begin{pmatrix} 1 & 0 & 2 \\ 0 & 1 & 2 \\ 0 & 0 & 0 \end{pmatrix}$$

Mark each statement True or False regarding each matrix

- C) Equation  $Ax=b$  ( $Bx=b$  respectively) has solution for every  $b$ .
- D) Matrix has row echelon form, but not reduced REF.
- E) Matrix has reduced REF.
- F) Matrix has pivot position in every row.
- G) Columns of a matrix span  $\mathbb{R}^3$ .
- H) Solutions of  $Ax=0$  ( $Bx=0$ , resp.) form a line.
- I)  $Ax=0$  ( $Bx=0$ , resp.) has only trivial solution
- J) Rows of a matrix are linear dependant.

2)

	C	D	E	F	G	H	I	J
A	T	F	T	T	T	F	T	F
B	F	T	F	F	F	T	F	T
		T	F					
		F	T					

Q3. Mark each statement True or False or choose 1 correct answer.

A) T is reflection with respect to  $y = -x$ . Which of following matrices is matrix of T?

1)  $\begin{pmatrix} 2 & 1 \\ 0 & 1 \end{pmatrix}$       2)  $\begin{pmatrix} 1 & 1 \\ 0 & 0 \end{pmatrix}$       3)  $\begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix}$       4)  $\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$

B) T is rotation by  $\pi/4$ . Which of following matrices is matrix of T?

1)  $\begin{pmatrix} 1 & 3 \\ 0 & 1 \end{pmatrix}$       2)  $\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$       3)  $\begin{pmatrix} 3 & 3 \\ 3 & 3 \end{pmatrix}$       4)  $\begin{pmatrix} \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \\ -\frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \end{pmatrix}$

C) Which vector will be transformed into

$\begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix}$  under linear transformation with matrix:

$\begin{pmatrix} \frac{1}{2} & \frac{1}{2} \\ 1 & 0 \\ 0 & 1 \end{pmatrix}$  ?

1)  $\begin{pmatrix} 4 \\ 4 \end{pmatrix}$

3)  $\begin{pmatrix} 1 \\ 1 \end{pmatrix}$

2)  $\begin{pmatrix} 2 \\ 3 \\ 1 \end{pmatrix}$

4)  $\begin{pmatrix} 0 \\ 0 \end{pmatrix}$

D)  $T \begin{pmatrix} x \\ y \\ z \end{pmatrix} = \begin{pmatrix} x^2 + y^2 + z^2 \\ x \\ y \end{pmatrix}$  is linear transformation

E) Linear transformation with matrix  $\begin{bmatrix} 2 & 1 \\ 1 & 3 \end{bmatrix}$  transform  $\begin{pmatrix} 1 \\ 1 \end{pmatrix}$  into  $\begin{pmatrix} 3 \\ 4 \end{pmatrix}$

F) Linear transformation T transform  $\begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix}$  into  $\begin{pmatrix} 1 \\ 1 \\ 2 \end{pmatrix}$ ;  $\begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix}$  into  $\begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix}$  and  $\begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix}$  into  $\begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix}$ .

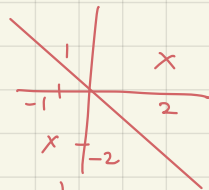
3)

A B C D E F  
3 4 3 F T 3

A) T is reflection with respect to  $y = -x$ . Which of following matrices is matrix of T?

- 1)  $\begin{pmatrix} 2 & 1 \\ 0 & 1 \end{pmatrix}$  2)  $\begin{pmatrix} 1 & 1 \\ 0 & 0 \end{pmatrix}$  3)  $\begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix}$  4)  $\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$

$$\begin{bmatrix} 0 & -1 \\ -1 & 0 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} -y \\ -x \end{bmatrix}$$



from  $(x, y)$  to  $(-y, -x)$

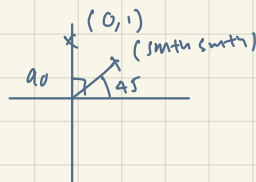
C) Which vector will be transformed into

$\begin{pmatrix} 1 \\ 1 \end{pmatrix}$  under linear transformation with matrix:

- 1)  $\begin{pmatrix} 4 \\ 4 \end{pmatrix}$  2)  $\begin{pmatrix} 2 \\ 3 \end{pmatrix}$  3)  $\begin{pmatrix} 1 \\ 1 \end{pmatrix}$  4)  $\begin{pmatrix} 0 \\ 0 \end{pmatrix}$

B) T is rotation by  $\frac{\pi}{4}$ . Which of following matrices is matrix of T?

- 1)  $\begin{pmatrix} 1 & 3 \\ 0 & 1 \end{pmatrix}$  2)  $\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$  3)  $\begin{pmatrix} 3 & 3 \\ 3 & 3 \end{pmatrix}$  4)  $\begin{pmatrix} \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \\ -\frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \end{pmatrix}$



$$\begin{pmatrix} \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \\ -\frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \end{pmatrix} \begin{pmatrix} 1 \\ 0 \end{pmatrix} = \begin{pmatrix} \frac{1}{\sqrt{2}} \\ -\frac{1}{\sqrt{2}} \end{pmatrix}$$

D)  $T \begin{pmatrix} x \\ y \\ z \end{pmatrix} = \begin{pmatrix} x^2 + y^2 + z^2 \\ x \\ y \end{pmatrix}$  is linear transformation

No



Which matrix will be the matrix of this (4)  
linear transformation?

~~1)~~  $\begin{pmatrix} 1 & 2 & 0 \\ 0 & 1 & 0 \\ 1 & 1 & 1 \end{pmatrix}$ 
 2)  $\begin{pmatrix} 1 & 1 & 2 \\ 1 & 0 & 0 \\ 1 & 0 & 1 \end{pmatrix}$ 
 3)  $\begin{pmatrix} 1 & 1 & 1 \\ 1 & 0 & 0 \\ 2 & 0 & 1 \end{pmatrix}$ 
 4)  $\begin{pmatrix} -1 & -1 & 2 \\ -1 & 0 & 0 \\ -1 & 0 & -1 \end{pmatrix}$

Answers:

Q1:

	C	D	E	F	G	H	I	K	L
A	F	T	T	T	F	F	F	F	T
B	T	F	F	F	F	F	F	F	T

J: False

Q2:

	C	D	E	F	G	H	I	J
A	T	T	F	T	T	F	T	F
B	F	F	T	F	F	T	F	T

Q3:

A	B	C	D	E	F
3)	4)	3)	F	T	3)