



# CS396: Security, Privacy & Society

Fall 2022

Lecture 10: MACs & Hashing

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# Outline

- ◆ Message authentication
  - ◆ Message Integrity
  - ◆ Message Authentication Codes (MACs)
  - ◆ MAC constructions



# **Message authentication**



# Recall: Integrity

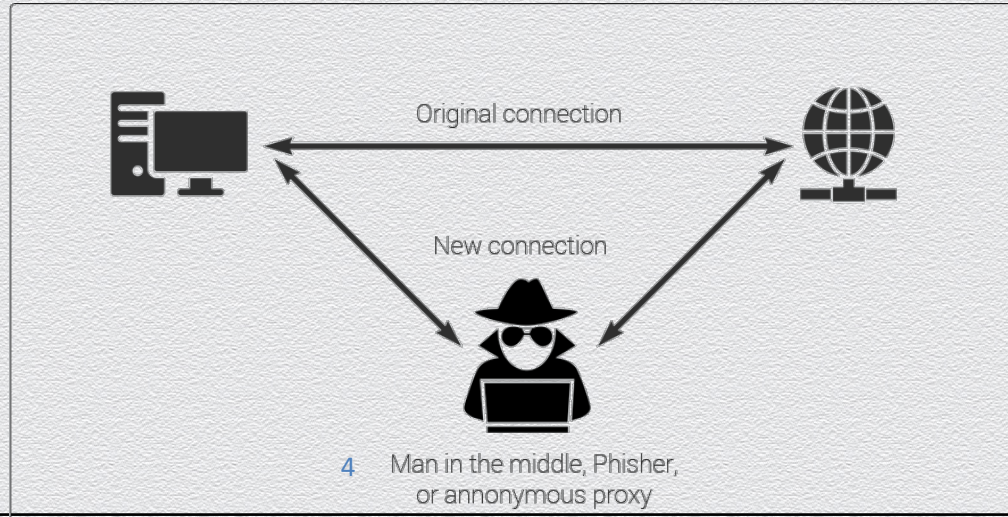
Fundamental security property

- ◆ **an asset is modified only by authorized parties**
- ◆ “I” in the CIA triad

*“computer security seeks to prevent **unauthorized** viewing (confidentiality) or **modification (integrity)** of **data** while preserving access (availability)”*

## Alteration

- ◆ main threat against integrity of **in-transit** data
- ◆ e.g., MITM attack





# Security problems studied by modern cryptography

- ◆ Classical cryptography: **message encryption**
  - ◆ early crypto schemes tried to provide **secrecy / confidentiality**
- ◆ Modern cryptography: **wide variety** of security problems
  - ◆ today we need to study a large set of **security properties** beyond secrecy
- ◆ The sibling of message encryption: **message authentication**
  - ◆ another cornerstone of any secure system aiming to provide **authenticity & integrity**



# Message authentication: Motivation

Information has **value**, but only when it is **correct**

- ◆ random, incorrect, inaccurate or maliciously altered data is **useless** or **harmful**
  - ◆ **message authentication = message integrity + authenticity**
    - ◆ while in transit (or at rest), no message should be **modified** by an outsider
    - ◆ no outsider can **impersonate** the stated message sender (or owner)
- ◆ it is often necessary / worth to protect critical / valuable data
  - ◆ **message encryption**
    - ◆ while in transit (or at rest), no message should be **leaked** to an outsider



# Example 1

## Secure electronic banking

- ◆ a bank receives an electronic request to transfer \$1,000 from Alice to Bob

## Concerns

- ◆ who ordered the transfer, Alice or an attacker (e.g., Bob)?
- ◆ is the amount the intended one or was maliciously modified while in transit?
  - ◆ adversarial Vs. random message-transmission errors
    - ◆ standard error-correction is not sufficient to address this concern



## Example 2

### Web browser cookies

- ◆ a user is performing an online purchase at Amazon
- ◆ a “cookie” contains session-related info, as client-server HTTP traffic is stateless
  - ◆ stored at the client, included in messages sent to server
  - ◆ contains client-specific info that affects the transaction
    - ◆ e.g., the user’s shopping cart along with a discount due to a coupon

### Concern

- ◆ was such state maliciously altered by the client (possibly harming the server)?



# Integrity of communications / computations

Highly important

- ◆ any unprotected system cannot be assumed to be trustworthy w.r.t.
  - ◆ origin/source of information (due to impersonation attacks, phishing, etc.)
  - ◆ contents of information (due to man-in-the-middle attacks, email spam, etc.)
  - ◆ overall system functionality

Prevention Vs. detection

- ◆ unless system is “closed,” adversarial tampering with its integrity **cannot be avoided!**
- ◆ goal: identify system components that are not trustworthy
  - ◆ **detect tampering** or **prevent undetected tampering**
    - ◆ e.g., avoid “consuming” falsified information



# Encryption does not imply authentication

## A common misconception

“since ciphertext  $c$  hides message  $m$ , Mallory cannot meaningfully modify  $m$  via  $c$ ”

## Why is this incorrect?

- ◆ all encryption schemes (seen so far) are based on one-time pad, i.e., masking via XOR
- ◆ consider flipping a single bit of ciphertext  $c$ ; what happens to plaintext  $m$ ?
  - ◆ such property of one-time pad does not contradict the secrecy definitions

Generally, secrecy and integrity are distinct properties

- ◆ encrypted traffic generally provides **no integrity** guarantees



## **Message authentication codes (MACs)**



# Problem setting: Reliable communication

Two parties wish to communicate over a channel

- ◆ Alice (sender/source) wants to send a message  $m$  to Bob (recipient/destination)

Underlying channel is unprotected

- ◆ attacker (Mallory / adversary) can manipulate any sent messages
- ◆ e.g., message transmission via a compromised router

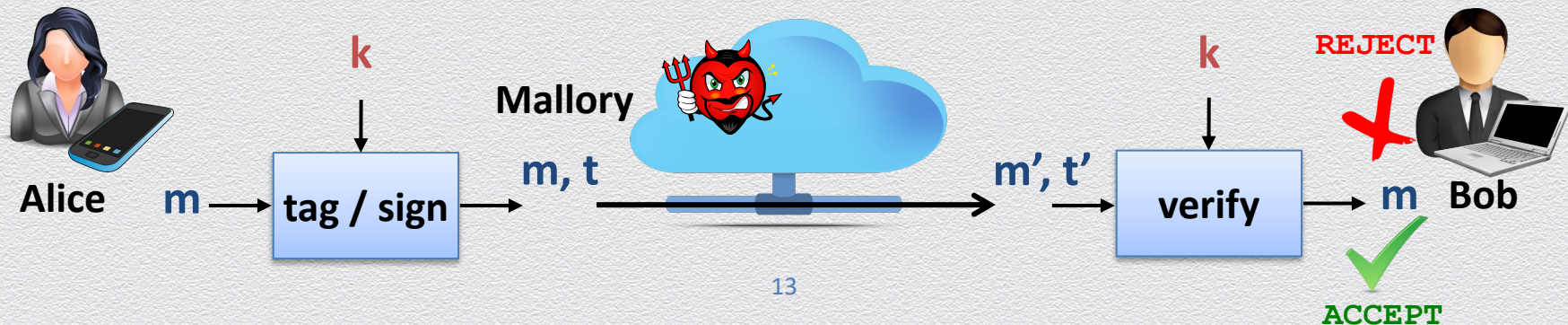




# Solution concept: Symmetric-key message authentication

## Main idea

- ◆ secretly annotate or “sign” message so that it is **unforgeable** while in transit
  - ◆ Alice **tags** her message  $m$  with **tag**  $t$ , which is sent **along** with **plaintext**  $m$
  - ◆ Bob **verifies** authenticity of received message using tag  $t$
  - ◆ Mallory can manipulate  $m, t$  but “**cannot forge**” a fake verifiable pair  $m', t'$
  - ◆ Alice and Bob share a **secret key**  $k$  that is used for both operations





# Security tool: Symmetric Message Authentication Code

- ◆ The tag is computed using a **tag-generation algorithm** (**Mac**)

$$t \leftarrow \text{Mac}_k(m)$$

- ◆ **verification algorithm** (**Vrfy**)

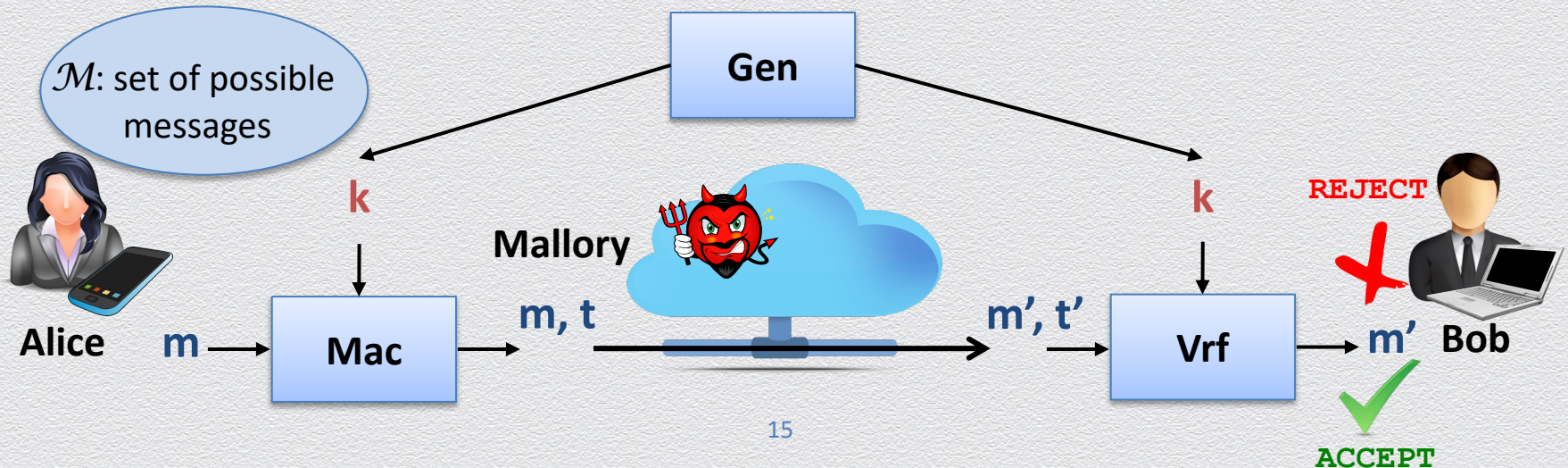
$$b := \text{Vrf}_k(m, t)$$



# Security tool: Symmetric Message Authentication Code

Abstract cryptographic primitive, a.k.a. **MAC**, defined by

- ◆ a **message space**  $\mathcal{M}$ ; and
- ◆ a triplet of algorithms **(Gen, Mac, Vrf)**
  - ◆ Gen, Mac are probabilistic algorithms, whereas Vrf is deterministic

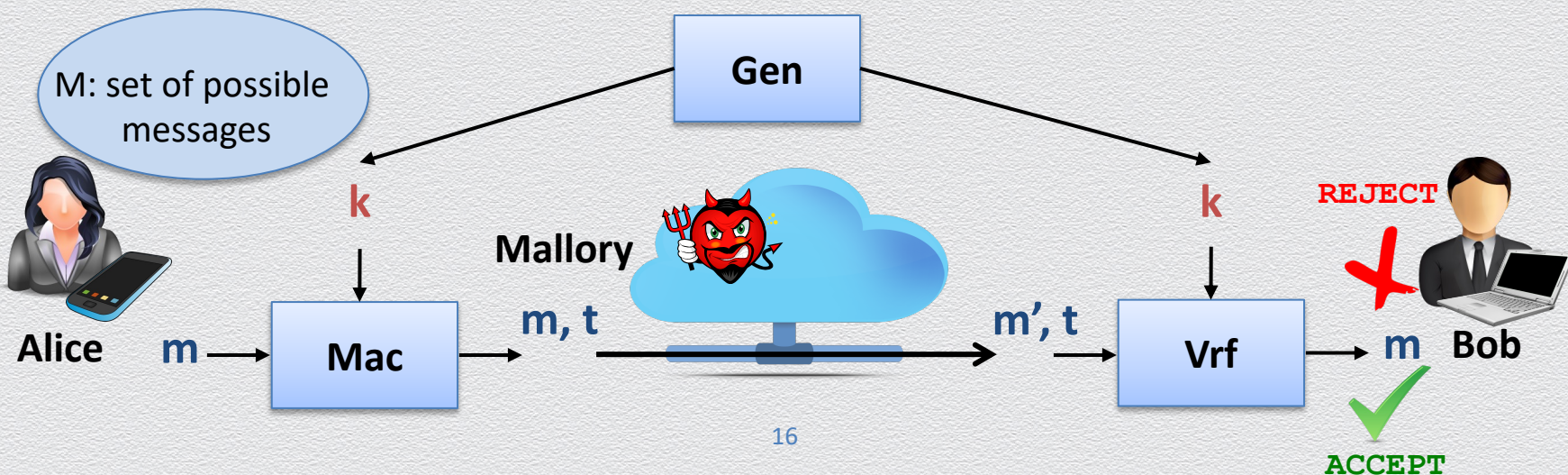




# Desired properties for MACs

By design, any MAC should satisfy the following

- ◆ **efficiency:** key generation & message transformations “are fast”
- ◆ **correctness:** for all  $m$  and  $k$ , it holds that  $\text{Vrf}_k(m, \text{Mac}_k(m)) = \text{ACCEPT}$
- ◆ **security:** one “cannot forge” a fake verifiable pair  $m', t'$





# Main application areas

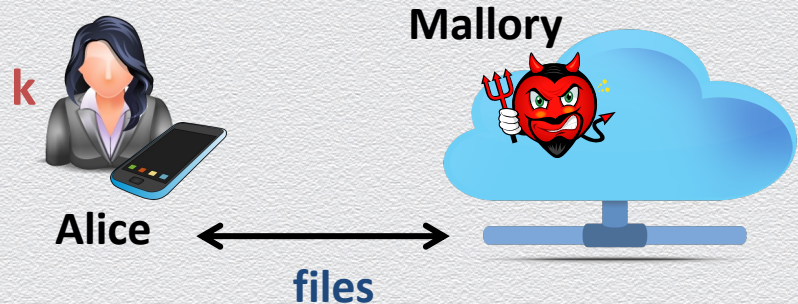
## Secure communication

- ◆ **verify authenticity of messages** sent among parties
- ◆ assumption
  - ◆ Alice and Bob **securely generate, distribute and store shared key  $k$**
  - ◆ attacker does not learn key  $k$



## Secure storage

- ◆ **verify authenticity of files** outsourced to the cloud
- ◆ assumption
  - ◆ Alice **securely generates and stores key  $k$**
  - ◆ attacker does not learn key  $k$





# Conventions

## Random key selection

- ◆ typically, Gen selects key  $k$  **uniformly at random** from the key space  $\mathcal{K}$

## Canonical verification

- ◆ when Mac is deterministic, Vrf typically amounts to re-computing the tag  $t$ 
  - ◆  $\text{Vrf}_k(m, t)$ : 1.  $t' := \text{Mac}_k(m)$  2. if  $t = t'$ , output `ACCEPT` else output `REJECT`
- ◆ but conceptually the following operations are distinct
  - ◆ authenticating  $m$  (i.e., running Mac) Vs. verifying authenticity of  $m$  (i.e., running Vrf)



# MAC security

MAC scheme  
(Gen, Mac, Vrf)



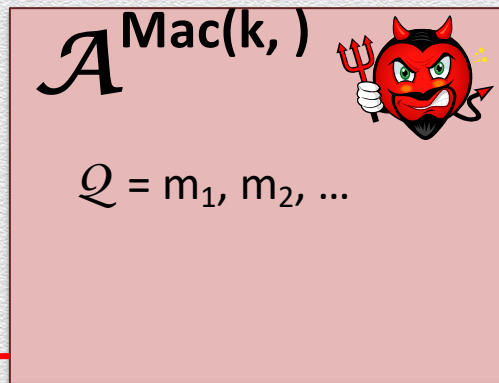
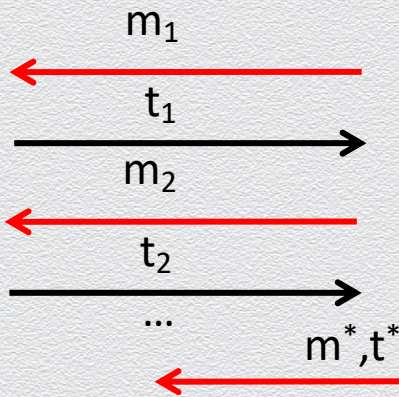
$\mathcal{T}$

Gen  $\rightarrow$  k

Mac<sub>k</sub>(m<sub>i</sub>)  $\rightarrow$  t<sub>i</sub>

Attacker **wins** the game if

1. Vrf<sub>k</sub>(m\*, t\*) = ACCEPT &
2. m\* not in  $\mathcal{Q}$



The MAC scheme is **secure** if any PPT  $\mathcal{A}$  wins the game only negligibly often.



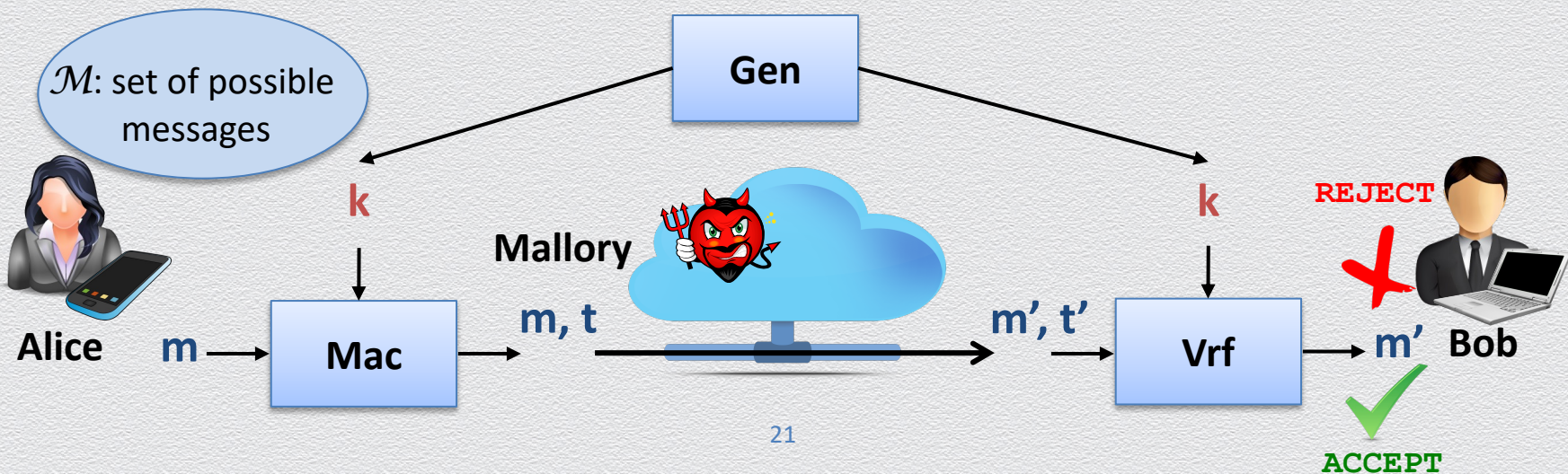
# Replay attacks



# Recall: MAC

Abstract cryptographic primitive, a.k.a. **MAC**, defined by

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# Recall: MAC security

MAC scheme  
(Gen, Mac, Vrf)



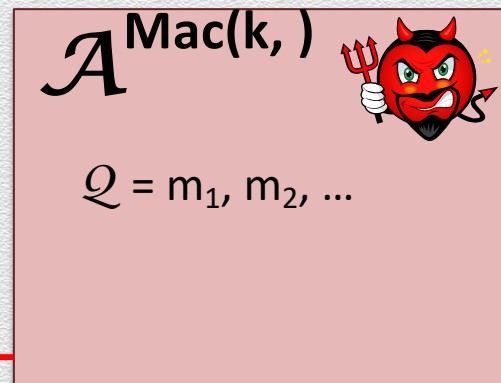
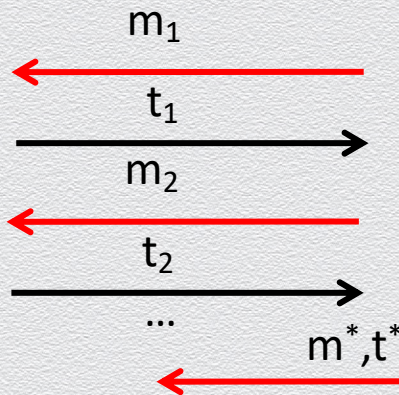
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# Real-life attacker

In practice, an attacker may

- ◆ observe a traffic of authenticated (and successfully verified) messages
- ◆ manipulate (or often also partially influences) traffic
  - ◆ aims at inserting an invalid but verifiable message  $m^*, t^*$  into the traffic
    - ◆ interesting case: forged message is a new (unseen) one
    - ◆ trivial case: forged message is a previously observed one, a.k.a. a **replay attack**
- ◆ launch a **brute-force attack** (given that  $\text{Mac}_k(m) \rightarrow t$  is publicly known)
  - ◆ given any observed pair  $m, t$ , exhaustively search key space to find the used key  $k$



# Threat model

In the security game, Mallory is an adversary  $\mathcal{A}$  who is

- ◆ “active” (on the wire)
  - ◆ we allow  $\mathcal{A}$  to **observe** and **manipulate** sent messages
- ◆ “well-informed”
  - ◆ we allow  $\mathcal{A}$  to **request MAC tags** of messages of **its choice**
- ◆ “replay-attack safe”
  - ◆ we restrict  $\mathcal{A}$  to **forge only new** messages
- ◆ “PPT”
  - ◆ we restrict  $\mathcal{A}$  to be **computationally bounded**
  - ◆ new messages may be forged undetectably only negligibly often



# Notes on security definition

Is it a rather strong security definition?

- ◆ we allow  $\mathcal{A}$  to **query MAC tags for any message**
  - ◆ but real-world senders will authenticate only “meaningful” messages
- ◆ we allow  $\mathcal{A}$  to break the scheme by **forging any new message**
  - ◆ but real-world attackers will forge only “meaningful” messages

Yes, it is the right approach...

- ◆ message “meaningfulness” **depends on higher-level application**
  - ◆ text messaging apps require authentication of English-text messages
  - ◆ other apps may require authentication of binary files
  - ◆ security definition should better be **agnostic** of the specific higher application



# Notes on security definition (II)

Are replay attacks important in practice?

- ◆ absolutely yes: a **very realistic & serious threat!**
  - ◆ e.g., what if a money transfer order is “replayed”?

Yet, a “replay-attack safe” security definition is preferable

- ◆ again, whether replayed messages are valid depends on higher-level app
- ◆ better to delegate to this app the specification of such details
  - ◆ e.g., semantics on traffic or validity checks on messages before they’re “consumed”

Eliminating replay attacks

- ◆ use of counters (i.e., common shared state) between sender & receiver
- ◆ use of timestamps along with a (relaxed) authentication window for validation



# MAC constructions



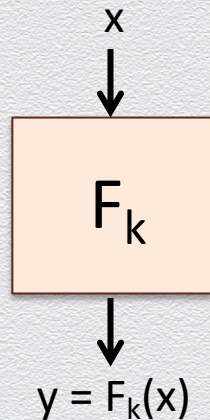
# Three generic MAC constructions

- ◆ fixed-length MAC
  - ◆ direct application of a PRF for tagging
  - ◆ limited applicability
- ◆ domain extension for MACs
  - ◆ straightforward secure extension of fix-length MAC
  - ◆ inefficient
- ◆ CBC-MAC
  - ◆ resembles CBC-mode encryption
  - ◆ efficient



# 1. Fixed-length MAC

- ◆ based on use of a PRF
  - ◆ employ a PRF  $F_k$  in the obvious way to compute and canonically verify tags
  - ◆ set tag  $t$  to be the pseudorandom string derived by evaluating  $F_k$  on message  $m$
- ◆ secure, provided that  $F_k$  is a secure PRF



## MAC scheme $\Pi$

$\text{Gen}(1^n): \{0,1\}^n \rightarrow k$

$\text{Mac}_k(m): \text{set } t = F_k(m)$

$\text{Vrfy}_k(m,t): \text{return } 1 \text{ iff } t = F_k(m)$

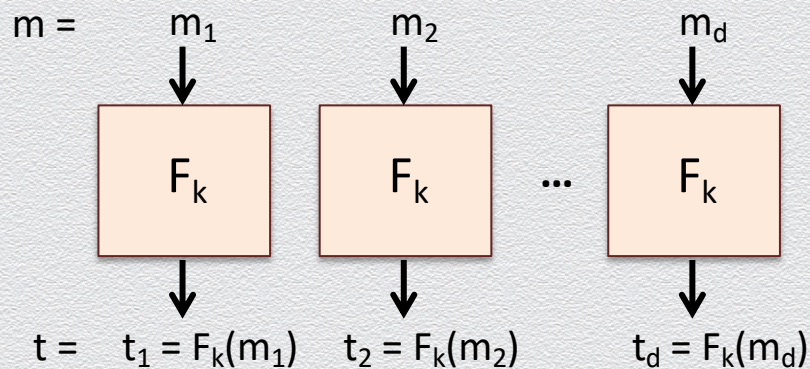


## 2. Domain extension for MACs (I)

- ◆ suppose we have the previous fix-length MAC scheme
- ◆ how can we authenticate a message  $m$  of arbitrary length?

- ◆ naïve approach

- ◆ pad  $m$  and view it as  $d$  blocks  $m_1, m_2, \dots, m_d$
- ◆ separately apply MAC to block  $m_i$



- ◆ security issues

- ◆ reordering attack; verify block index,  $t = F_k(m_i || i)$
- ◆ truncation attack; verify message length  $\delta = |m|$ ,  $t = F_k(m_i || i || \delta)$
- ◆ mix-and-match attack; randomize tags (using message-specific fresh nonce)



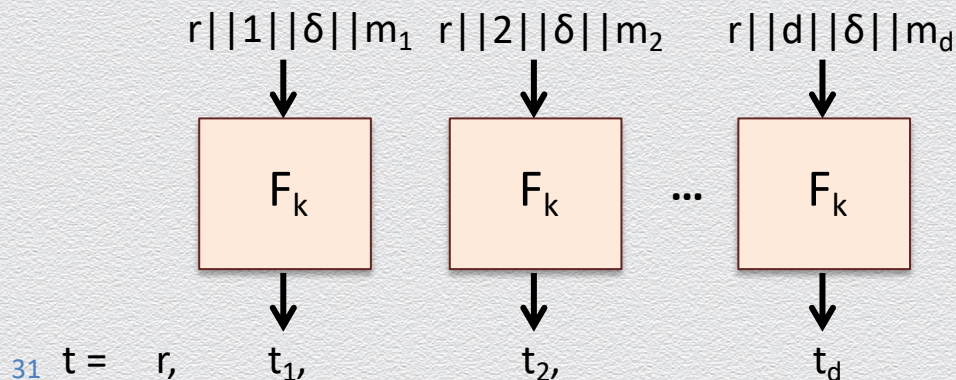
## 2. Domain extension for MACs (II)

### Final scheme

- ◆ assumes a secure MAC scheme for messages of size  $n$
- ◆ set tag of message  $m$  of size  $\delta$  at most  $2^{n/4}$  as follows
  - ◆ choose fresh random nonce  $r$  of size  $n/4$ ; view  $m$  as  $d$  blocks of size  $n/4$  each
  - ◆ separately apply MAC on each block, authenticating also its index,  $\delta$  and nonce  $r$

### Security

- ◆ extension is secure, if  $F_k$  is a secure PRF





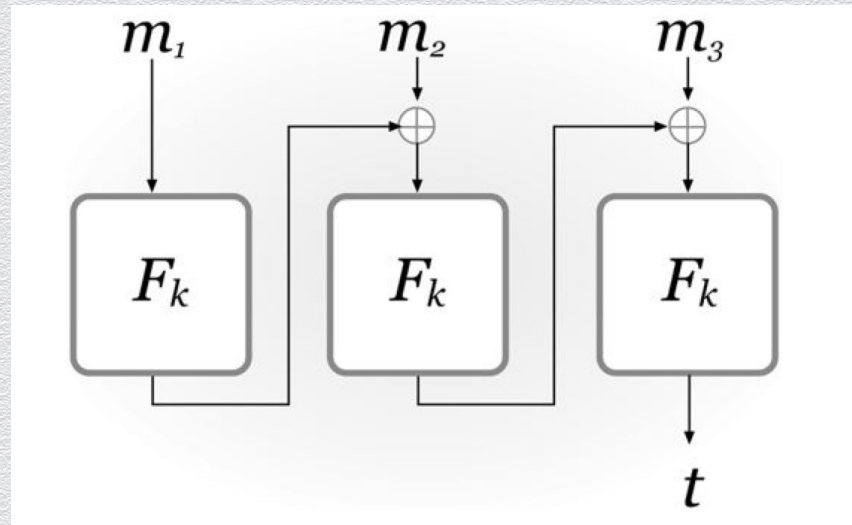
### 3. CBC-MAC

#### Idea

- ◆ employ a PRF in a manner similar to CBC-mode encryption

#### Security

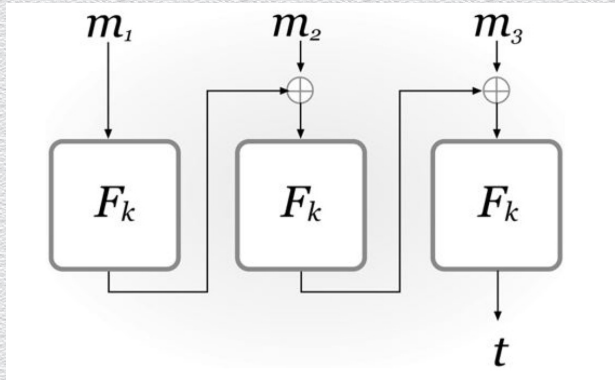
- ◆ extension is secure, if
  - ◆  $F_k$  is a secure PRF; and
  - ◆ only **fixed-length** messages are authenticated
- ◆ messages of length equal to any multiple of  $n$  can be authenticated
  - ◆ but this length need be fixed in advance
  - ◆ insecure, otherwise





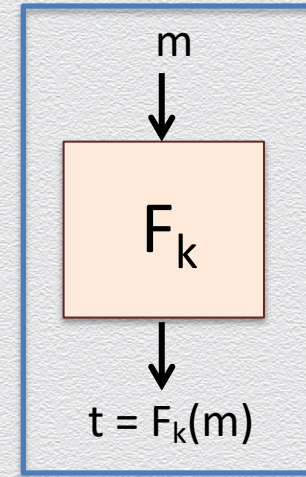
### 3. CBC-MAC Vs. previous schemes

- ◆ can authenticate longer messages than basic PRF-based scheme (1)

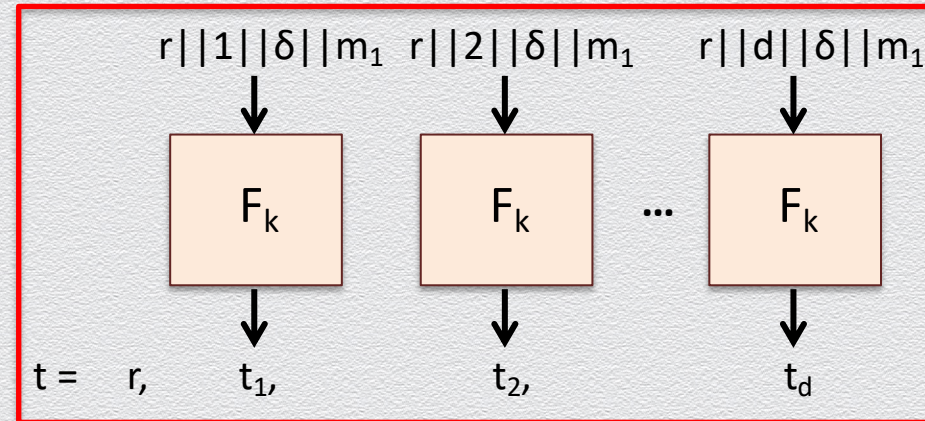


- ◆ more efficient than domain-extension MAC scheme (2)

Scheme (1)



Scheme (2)

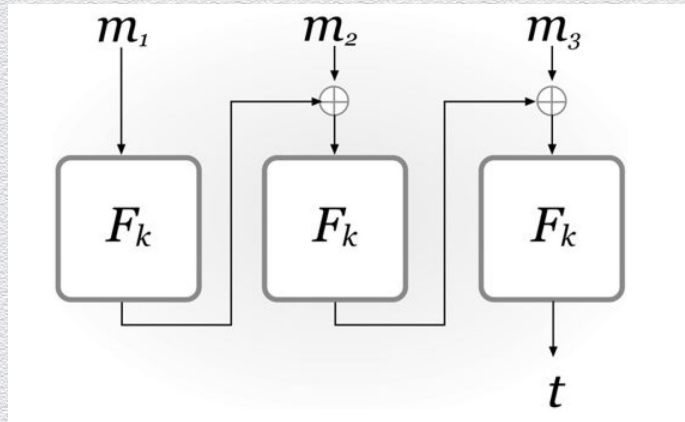




### 3. CBC-MAC Vs. CBC-mode encryption

- ◆ crucially for their security
  - ◆ CBC-MAC uses **no IV** (or uses an IV set to 0) and only the **last PRF output**
  - ◆ CBC-mode encryption uses a **random IV** and **all PRF outputs**
  - ◆ “simple”, innocent modification can be catastrophic...

**CBC-MAC**



**CBC-mode encryption**

