## MA 573 - Linear Algebra

## Homework 2

**Problem 1** [25pts] Which matrices  $E_{21}$ ,  $E_{31}$  produce zero in the (2,1) respectively (3,1) position of  $E_{21} \cdot A$  respectively  $E_{31} \cdot A$  for

$$A = \left[ \begin{array}{rrr} 2 & 1 & 0 \\ -2 & 0 & 1 \\ 8 & 5 & 3 \end{array} \right]$$

Find the single matrix E that produces both zeros at once and calculate  $E \cdot A$ .

**Problem 2** [25pts] Use the Gauss elimination method in order to find the inverses of the following matrices:

$$A = \begin{bmatrix} 0 & 0 & 0 & 2 \\ 0 & 0 & 3 & 0 \\ 0 & 4 & 0 & 0 \\ 5 & 0 & 0 & 0 \end{bmatrix}, \quad B = \begin{bmatrix} 3 & 2 & 0 & 0 \\ 4 & 3 & 0 & 0 \\ 0 & 0 & 6 & 5 \\ 0 & 0 & 7 & 6 \end{bmatrix}$$

**Problem 3** [25pts] Factor the symmetric matrix  $A = \begin{bmatrix} 2 & -1 & 0 \\ -1 & 2 & -1 \\ 0 & -1 & 2 \end{bmatrix}$  as  $A = LDL^T$ .

**Problem 4** [25pts] For which vectors  $b = \begin{bmatrix} b_1 \\ b_2 \\ b_3 \end{bmatrix}$  the following system of equations has a solution  $\begin{bmatrix} 1 & 1 & 1 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} b_1 \\ b_2 \\ b_3 \end{bmatrix}$ ?