

Aughdon Breslin, MA331 Assignment 1, Professor Rossi, 7/21/21

2) Construct a 99% confidence interval for the mean daily intake of dairy products

$$n = 50 \geq 30 \rightarrow CLT \rightarrow \sigma \cong s$$

$$\alpha = 1 - 0.99 = .01 \rightarrow z = 2.58 \text{ where } z = z_{\alpha/2}$$

$$SE = \sigma/\sqrt{n} \rightarrow s/\sqrt{n} = 35/\sqrt{50} \cong 4.95$$

$$99\%CI = \bar{x} \pm z * SE = 756 \pm 2.58 * 4.95 = [743.229, 768.771]$$

4) Estimating Difference Between Two Binomial Distributions

$$n_1 = 50, n_2 = 100,$$

$$p_1 = .76, q_1 = 1 - .76 = .24, p_2 = .65, q_2 = 1 - .65 = .35$$

1) Estimate the difference in the true proportions favoring the bond proposal with a 99% confidence interval.

$$\alpha = 1 - 0.99 = .01 \rightarrow z = 2.58$$

$$(p_1 - p_2) \pm \sqrt{(p_1 q_1 / n_1) + (p_2 q_2 / n_2)} = (.76 - .65) \pm \sqrt{((.76)(.24)/50) + ((.65)(.35)/100)} = .1 \pm .033 = [0.033, 0.187]$$

2) If both samples were pooled into one sample of size $n = 150$, with 103 in favor of the proposal, provide a point estimate of the proportion of city residents who will vote for the bond proposal. What is the margin of error?

$$p = 103/150 = .687$$

$$99\%CI \text{ means } z = 2.58$$

$$ME = z * \sqrt{pq/n} = 2.58 * \sqrt{(0.687)(.313)/150} = .038$$

5) $n = 40$, mean = 10.3% = .103, stdev = .31% = .0031, Find 95% upper confidence bound where $z = z_{\alpha}$

$$\alpha = 1 - 0.95 = .05 \rightarrow z_{.05} = 1.64$$

$$SE = \sigma/\sqrt{n} = .0031/\sqrt{40} \cong 0.0005$$

$$UCB = \text{mean} + z * SE = .103 + 1.64 * .0005 = 0.10382$$