

CSI DEBLY Augustin 2nd year

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State of the art

NDVI-Biomass relationship in microphytobenthic studies : a review

Standardized framework choosen

The non-linear function choosen here has to be asymptotic

$$B_{a,b,c}(NDVI) = \frac{1}{c} \ln \left(\frac{b}{a + b - NDVI} \right) \quad (1)$$

From linear assumptions to the non-linear framework

It's often made the assumption that the relationship between NDVI and biomass is linear such as :

$$B_{\alpha,\beta}(NDVI) = \alpha NDVI + \beta$$

Which is the linearization of the non-linear function around a point, if the NDVI range is small enough.

$$\begin{aligned}
B_{a,b,c}(NDVI) &= \frac{1}{c} \ln \left(\frac{b}{a+b-(x+NDVI_{mean})} \right) \\
&= \frac{1}{c} \left[\ln \left(\frac{b}{a+b-NDVI_{mean}} \right) - \ln \left(1 - \frac{x}{a+b-NDVI_{mean}} \right) \right] \\
&= \frac{1}{c} \left[\ln \left(\frac{b}{a+b-NDVI_{mean}} \right) + \frac{x}{a+b-NDVI_{mean}} \right] \\
&= \frac{1}{c} \left[\ln \left(\frac{b}{a+b-NDVI_{mean}} \right) + \frac{NDVI - NDVI_{mean}}{a+b-NDVI_{mean}} \right] \\
&= \left[\frac{1}{c(a+b-NDVI_{mean})} \right] NDVI \\
&+ \left[\frac{1}{c} \ln \left(\frac{b}{a+b-NDVI_{mean}} \right) - \frac{NDVI_{mean}}{c(a+b-NDVI_{mean})} \right]
\end{aligned} \tag{2}$$

So we have

$$\alpha = \frac{1}{c(a+b-NDVI_{mean})} \tag{3}$$

and

$$\beta = \frac{1}{c} \ln \left(\frac{b}{a+b-NDVI_{mean}} \right) - \frac{NDVI_{mean}}{c(a+b-NDVI_{mean})} \tag{4}$$

To find a, b and c we have 3 unknowns and 2 equations. We must add another constraint :

$$\beta = \frac{1}{c} \ln \left(\frac{b}{a+b} \right) \tag{5}$$

Scaling Bias