

```
typedef struct Tno {
    struct Tno* ant;
    int char;
```

```
struct Tno prox; } Tno;
```

// Inicializa

```
init(Tno* ptcab,
    (*ptcab) = (Tno*) malloc(sizeof(Tno))
    (*ptcab) -> prox = (*ptcab) -> ant =
    (*ptcab)
```

```
Tno* ptcab,
init(&ptcab)
```

```
init2(Tno* &ptcab,
ptcab = malloc(...);
ptcab -> prox = ptcab -> ant = ptcab
```

// Algoritmo de busca que
retorna pt!

```
busca(ptcab, x)
```

```
pt = ptcab -> prox;
```

Enquanto pt != ptcab e pt -> char < x

```
pt = pt -> prox
return pt;
```

// Algoritmo que insere!

```
Insere(ptcab, x)
```

```
pt = busca(ptcab, x);
```

```
ant = pt -> ant
```

Se pt != ptcab e pt -> char == x
ok, já tem

```
novo = malloc(...)
```

Se novo == null

erro - acabou a memória
retorna null

```
novo -> char = x
```

```
novo -> prox = pt
```

```
novo -> ant = ant
```

```
ant -> prox = novo
```

```
pt -> ant = novo return novo
```

A função busca
retorna o ponteiro
para o elemento
que está próximo
da chave inserida.

A função Insere()
retorna nula em
caso de erro, ou
o endereço do novo
elemento inserido.

QUESTÃO 2:

2.1

Calcular(T_{no}^{xx} no, int ant)

(segundo)
ant \rightarrow anterior
esq \rightarrow esquerda
dir \rightarrow direita

Se no == nulo
retorna 0

Se no.esq \neq nulo

no.poma - prefixo = no.chave + Calcular(no.esq, ant)

Se não

no.poma - prefixo = no.chave + ant

Total = no.poma - prefixo

Se no.dir

Total = Calcular(no.dir, Total)

retorna Total;

2.2

Não pode estar certo. A análise $O(h)$ em circunstâncias mais normais leva em conta o pior caso. Se inserirmos uma chave que seja menor que todos as chaves da árvore, não precisamos atualizar poma - prefixo para todos os nós. Sendo assim, como tem-se que percorrer todos os n nós da árvore, o algoritmo deveria ser $O(n)$.

QUESTÃO 3

3.1

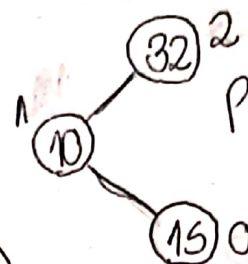
Inserindo 32



Inserindo 10

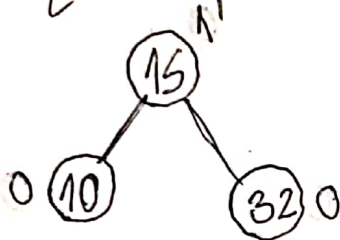


Inserindo 15

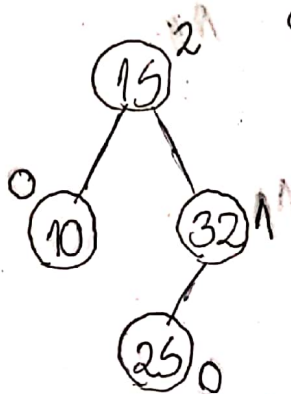


Problema encontrado
Não é AVL.

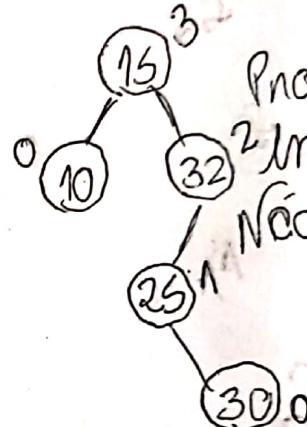
Realizando uma
rotação dupla direita



Inserindo 25

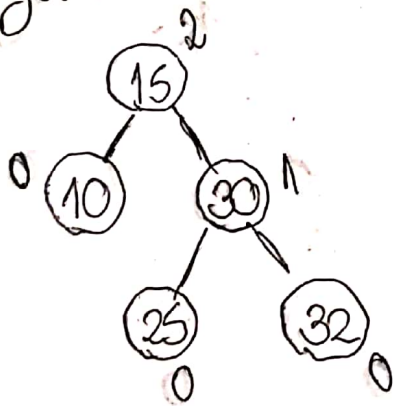


Inserindo 30



Problema
encontrado
Não é AVL

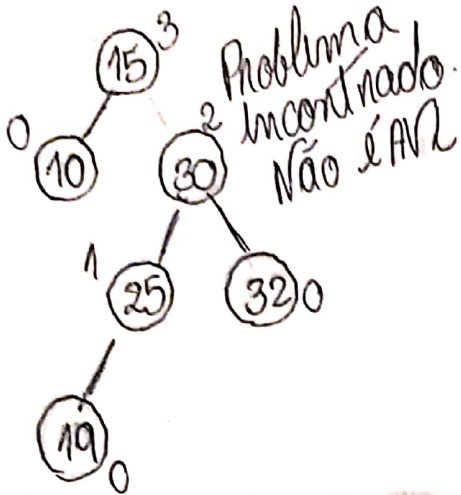
Realizando uma rotação dupla esquerda.



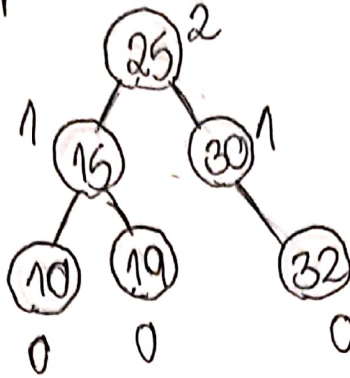
FINAL!

3.2°

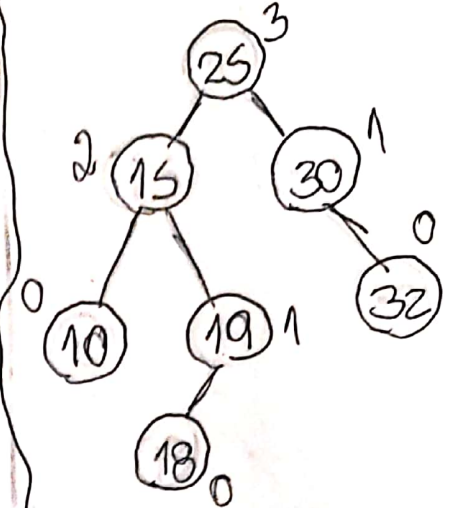
Inserindo 19



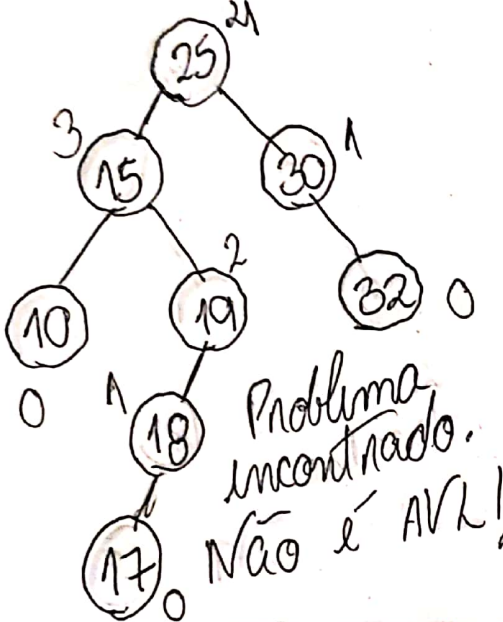
Realizando rotação dupla Esquerda



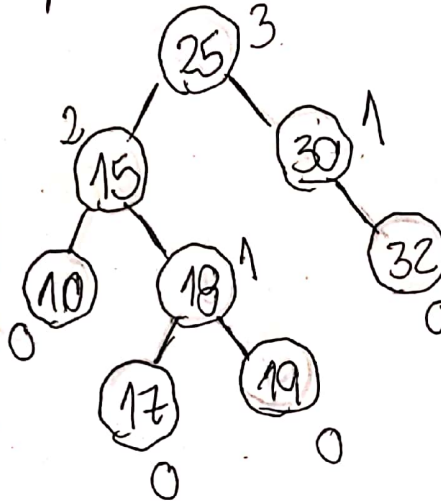
Inserindo 18



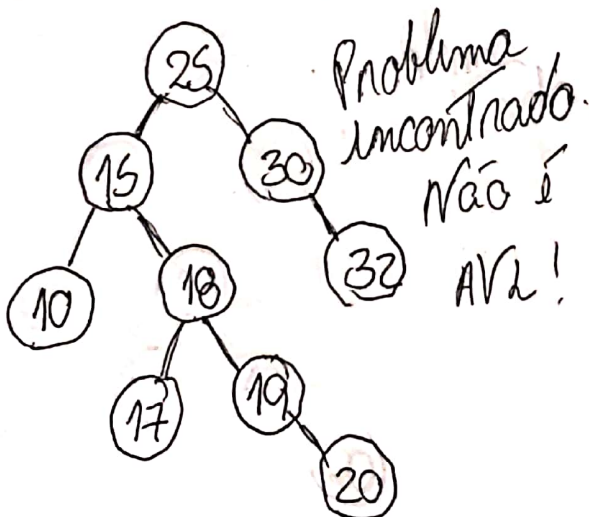
Inserindo 17



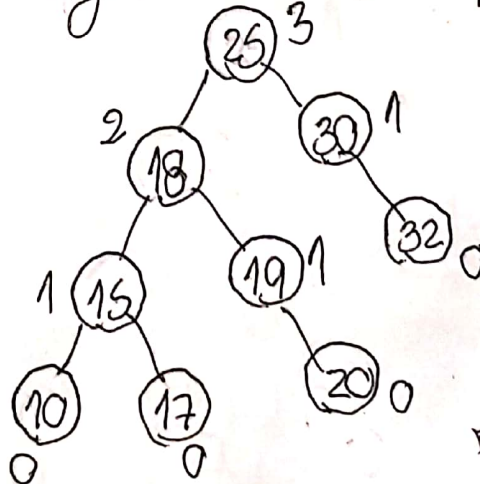
Realizando rotação dupla Direita



Inserindo 20



Realizando rotação simples



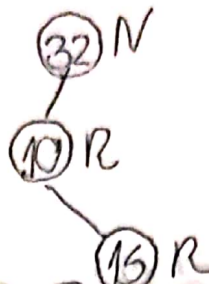
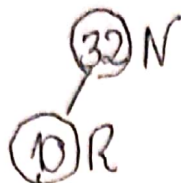
FINAL!

QUESTÃO 4:

32/10/15/25/30

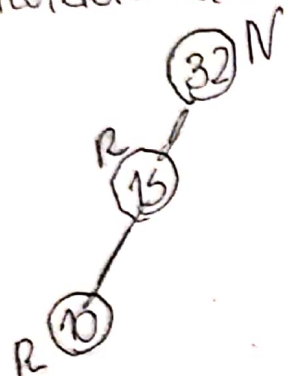
4.1

Inserir 32, Inserir 10, Inserir 15

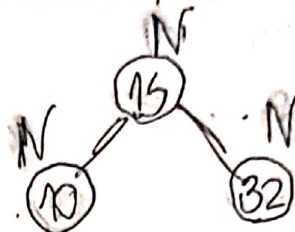


Problema Inconhecido
2 RUBROS!

Rotaciona 10 à esquerda?

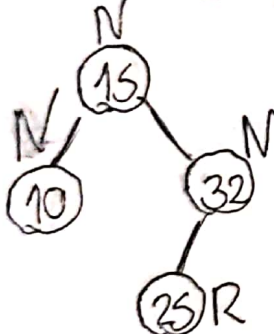


Rotaciona 32 à direita e

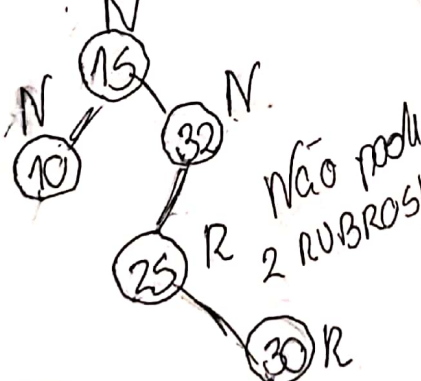


troca cor com 15
raiz fica negra.

Inserir 25

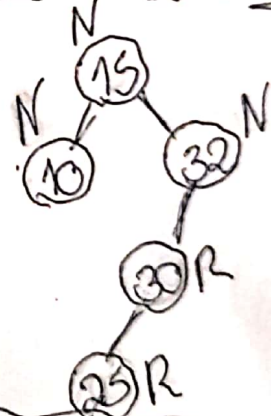


Inserir 30

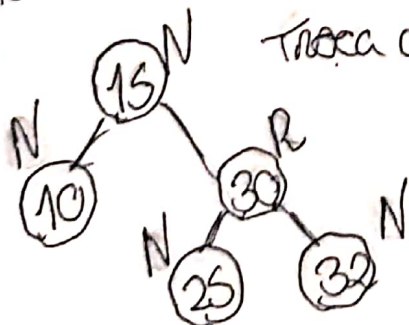


Não pode
2 RUBROS!

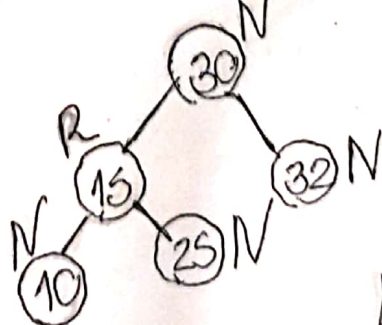
Rotaciona à esquerda



Rotaciona à direita e troca cor!



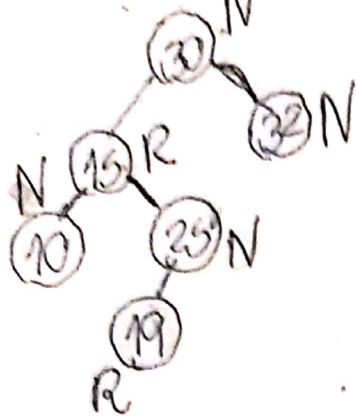
Rotaciona



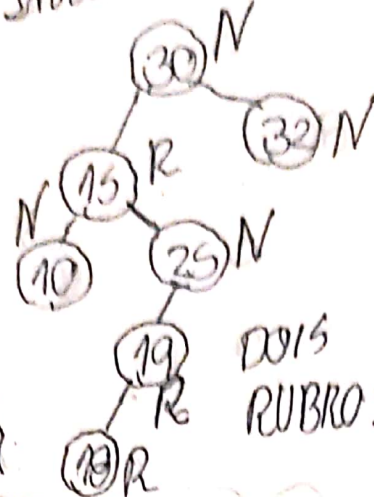
RESPOSTA FINAL

4.2

Inserir 19

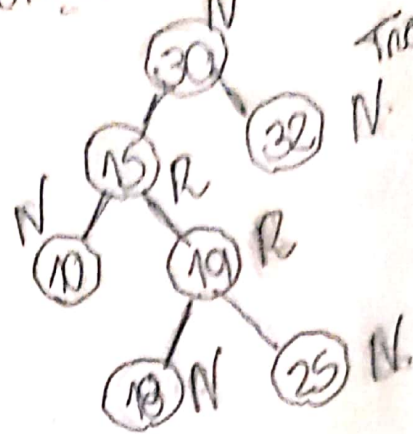


Inserir 18

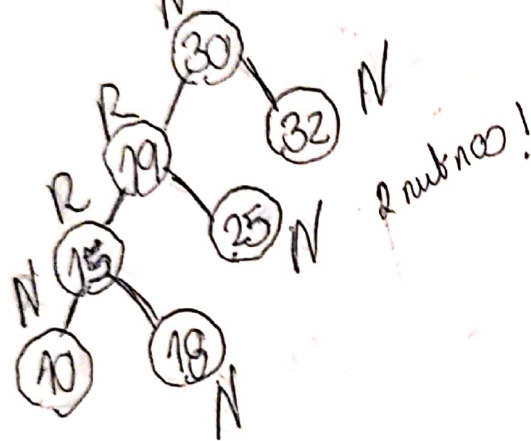


DOIS RUBROS!

Rotacao a direita e troca a cor



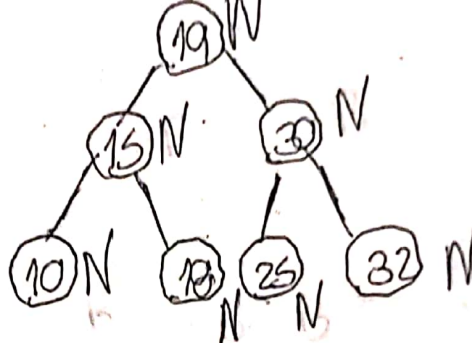
Rotacao a esquerda



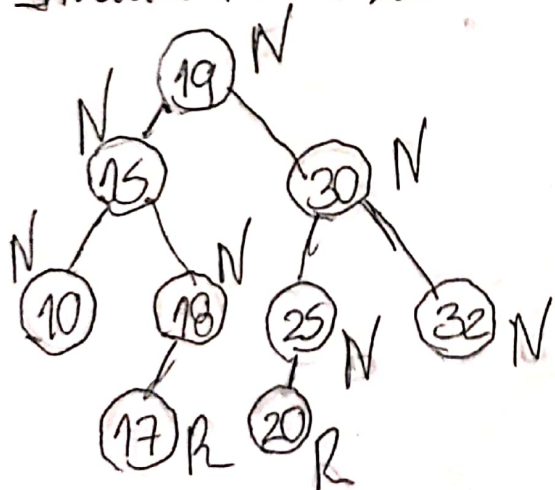
2 rubros!

Rotacao para direita

e troca a cor!



Inserir 17 e 20

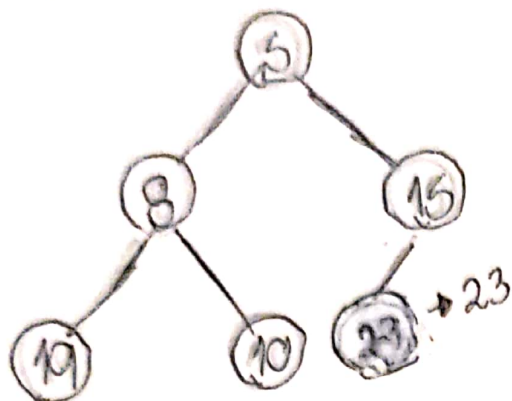


RESPOSTA FINAL.

5. QUESTÃO

5 | 8 | 15 | 19 | 10 | 23 | | | | |

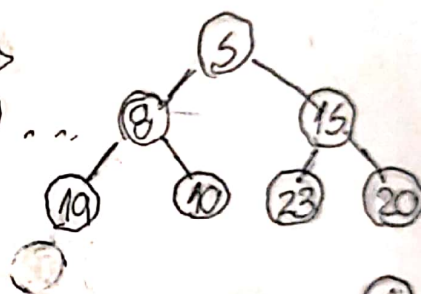
5.1



5.2 Inserir uma map as chaves 20, 7, 11, 18:

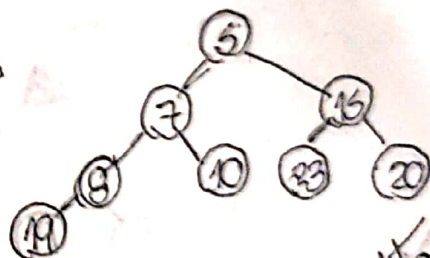
→ 20

5 | 8 | 15 | 19 | 10 | 23 | 20



→ 7

5 | 7 | 15 | 8 | 10 | 23 | 20 | 19



→ 11

5 | 7 | 15 | 8 | 10 | 23 | 20 | 19 | 11

→ 18

5 | 7 | 15 | 8 | 10 | 23 | 20 | 19 | 11 | 18

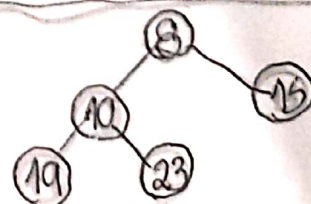
Resultado

5.3 Remover chave mínima 5.1

→ 23 | 8 | 15 | 19 | 10 |

→ 8 | 23 | 15 | 19 | 10 |

→ 8 | 10 | 15 | 19 | 23



Depois de remover a chave mínima