

MECHANICAL PROPERTIES OF FLUIDS

Pressure: →

→ Fluid: that can flow, like - Gases, liquids

• Pressure: $P_{avg} = \frac{F}{A}$

• Pascal's Law: Pressure is same at all points at the same horizontal level for a fluid at rest.

$$1 \text{ Pa} = 1 \text{ N/m}^2$$

$$1 \text{ Bar} = 10^5 \text{ Pa}$$

$$1 \text{ torr} = 1 \text{ mm of Hg}$$

$$1 \text{ atm} = 1.013 \times 10^5 \text{ Pa}$$

→ At depth h , absolute pressure = $P_0 + \rho gh$

→ Gauge pressure = Absolute pressure - Atmospheric pressure.

→ Pressure applied at any point is transmitted equally in all directions.

Archimedes' Principle: →

Upthrust = Weight of liquid displaced by the body.

$$\text{Upthrust} = V \rho g$$

ρ = density of liquid.

V = Volume of immersed part of the body.

Equation of continuity and Bernoulli's Theorem: →

→ In stream line flow, velocity of particles passing at any point is same at that point.

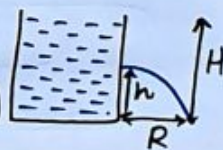
→ Equation of Continuity: $A_1 V_1 = A_2 V_2$ for incompressible fluid. (Using conservation of mass)

→ Bernoulli's Principle: For an incompressible and non-viscous fluid.

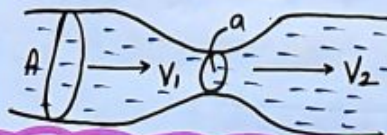
$$P + \frac{1}{2} \rho v^2 + \rho gh = \text{constant using conservation of energy.}$$

→ Toricelli's Law: $V_{efflux} = \sqrt{2gh}$ (when the tank is open).

→ Range of fluid: $R = 2\sqrt{h(H-h)}$, when $h = \frac{H}{2} \Rightarrow R = \text{max}$



→ Venturimeter: $V_1 = \frac{\sqrt{2h\rho mg}}{\sqrt{\rho \left[\frac{A^2}{a^2} - 1 \right]}}$



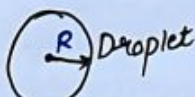
Surface Tension and Capillary Rise: →

* Surface Tension = Force per unit length $T = \frac{F}{L}$

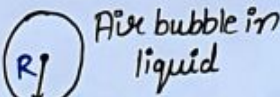
→ Surface Energy: amt. of work to be done to form a surface.
 $E = S \times A$



$$\Delta P = \frac{4T}{R}$$



$$\Delta P = \frac{2T}{R}$$



$$\Delta P = \frac{2T}{R}$$

* Angle of Contact - angle b/w tangent to liquid surface at point of contact and solid surface inside the liquid.

angle of Contact
obtuse liq. will fall in capillary tube.
acute liq. will rise in capillary tube.

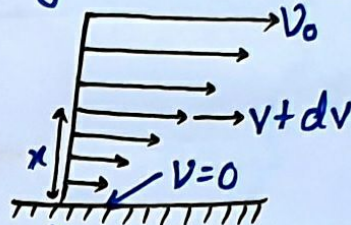
* Capillary Rise: $h = \frac{2 \cdot T \cos \theta}{r \rho g}$

Viscosity and Stoke's Law : →

→ Viscosity : a resistance to fluid motion.

→ Coeff. of Viscosity : $\eta = \frac{\text{Shearing stress}}{\text{Shearing strain}} = \frac{FL}{vA}$

→ Viscous Force : $F = -\eta A \frac{dv}{dx}$
(b/w layers)



* Stoke's Law: Viscous force on a body moving in the fluid is given by—

$$F = 6\pi\eta r v$$

* Terminal Velocity : $V_T = \frac{2r^2(\sigma - \rho)g}{9\eta}$

* Reynold's Number:

$$R_N = \frac{\rho v D}{\eta}$$

→ $R_N < 1000$ → streamline flow
 $1000 < R_N < 2000$ → transition flow
 $R_N > 2000$ → turbulent.



NEET
SLAYER