

WAVES mind map

Wave Equation

• Mechanical Waves:

\longleftrightarrow Longitudinal Waves
 \updownarrow Transverse Waves

• Wave function and eq.ⁿ

Wave function: $y = f(x \pm vt)$

Wave equation of a wave travelling +ve x direction \rightarrow

$$y = A \sin(\omega t - Kx)$$

Standing Waves

• Superposition of Waves:

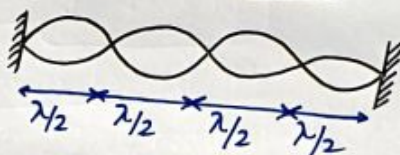
$$y = A \sin(\omega t + \phi)$$

\rightarrow If $\phi = 2n\pi \rightarrow$ Constructive interference.

\rightarrow If $\phi = (2n-1)\pi \rightarrow$ Destructive interference.

• On a stretched string:

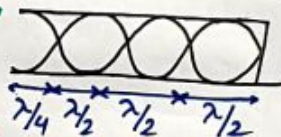
$$\lambda = \frac{2L}{n} \Rightarrow f = \frac{nv}{2L} \quad n = n^{\text{th}} \text{ harmonic} = 1, 2, 3, \dots$$



• Closed Organ pipe:

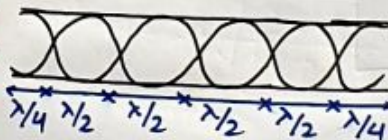
$$\lambda = \frac{4L}{(2n+1)} \Rightarrow f = \frac{(2n+1)v}{4L}$$

$n = n^{\text{th}} \text{ overtone} = 0, 1, 2, 3, \dots$



• Open Organ pipe:

$$\lambda = \frac{2L}{n} \Rightarrow f = \frac{nv}{2L} \quad n = n^{\text{th}} \text{ harmonic} = 1, 2, 3, \dots$$



• Beats:

$$\text{Beat frequency} = f_1 - f_2$$

Transverse Wave

• Velocity of a Wave on a string:

$$v = \sqrt{\frac{T}{\mu}} \quad T = \text{Tension in string.}$$

$\mu = \text{mass/length.}$

• Power: $P_{av} = \frac{1}{2} \mu \omega^2 A^2 v$

$$\text{Intensity: } I_{av} = \frac{1}{2} \rho \omega^2 A^2 v$$

\rightarrow phase difference $= \frac{2\pi}{\lambda} \times \text{path difference.}$

Sound

• Speed of Sound: $v = \sqrt{\frac{B}{\rho}}$

$B \rightarrow$ Bulk modulus

$\rho \rightarrow$ Density of med.

\rightarrow Acc.ⁿ to Newton:

$$v = \sqrt{\frac{P}{\rho}}$$

$$\text{Laplace Correction: } v = \sqrt{\frac{\gamma P}{\rho}}$$

• Loudness of Sound:

$$L = 10 \log_{10} \left[\frac{I}{I_0} \right] \quad \begin{matrix} \text{intensity of sound} \\ \text{Threshold of hearing} \end{matrix}$$

$$= 10^{-12} \frac{W}{m^2}$$

Doppler's Effects

• Source moving, Observer stationary:

$$f = f_0 \left[1 - \frac{v_s}{v} \right] \quad \begin{matrix} O \rightarrow v_o = 0 \\ S \rightarrow v_s \neq 0 \end{matrix}$$

$$f = f_0 \left[1 + \frac{v_s}{v} \right] \quad \begin{matrix} O \rightarrow v_o = 0 \\ S \leftarrow v_s \neq 0 \end{matrix}$$

• Observer moving, Source stationary:

$$f = f_0 \left[1 + \frac{v_o}{v} \right] \quad \begin{matrix} O \rightarrow v_o \neq 0 \\ S \rightarrow v_s = 0 \end{matrix}$$

$$f = f_0 \left[1 - \frac{v_o}{v} \right] \quad \begin{matrix} O \leftarrow v_o \neq 0 \\ S \rightarrow v_s = 0 \end{matrix}$$

• Both Source and Observer moving:

$$f = f_0 \left[\frac{v + v_o}{v - v_s} \right]$$

$$f = f_0 \left[\frac{v - v_o}{v + v_s} \right]$$



NEET
SLAYER