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POSITION DETERMINATION WITH LORAN-C TRIPLETS AND THE  
HEWLETT-PACKARD HP-41CV PROGRAMMABLE CALCULATOR(U)  
NAVAL POSTGRADUATE SCHOOL MONTEREY CA R H SHUDE

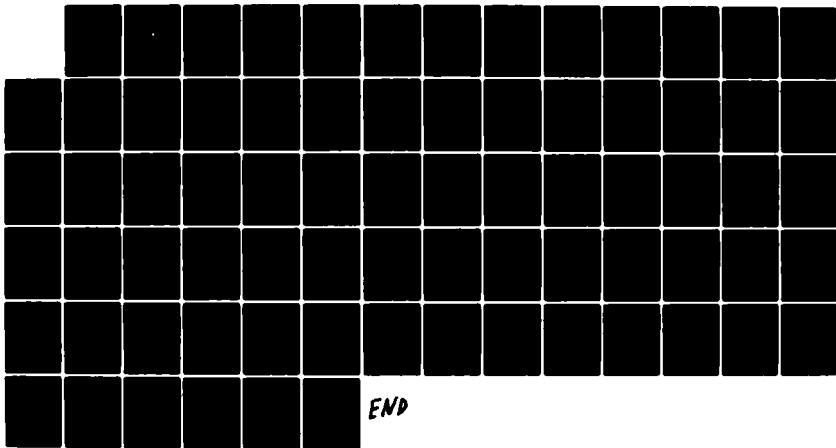
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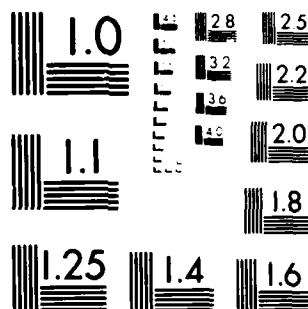
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NPS55-82-022

# NAVAL POSTGRADUATE SCHOOL

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POSITION DETERMINATION WITH  
LORAN-C TRIPLETS AND THE HEWLETT-PACKARD  
HP-41CV PROGRAMMABLE CALCULATOR

by

Rex H. Shudde

September 1982

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Prepared for:  
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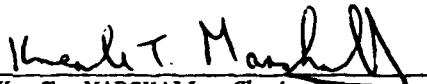
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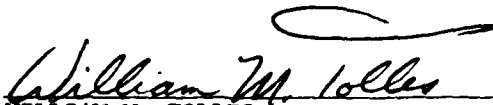
This report was prepared by:

  
REX H. SHUDDE, Associate Professor  
Department of Operations Research

Reviewed by:

Released by:

  
K. T. MARSHALL, Chairman  
Department of Operations Research

  
WILLIAM M. TOLLES  
Dean of Research

### CORRECTION

The coding delay for 7970W, given on page 61 of NPS55-82-022 should be 26000 microseconds.

### ADDENDA

1. On 9 June 1982, the Defense Mapping Agency issued upgraded WGS-72 coordinates for the Loran-C stations. This update includes positions measured to the nearest 0.001", the \*7930 Northwest Pacific Reconfiguration and the addition of the 5970 Commando Lion Chain. The upgraded coordinates are listed on the following page.

2. The HP-41CV program may be modified to display the station coordinates to the nearest 0.001" by changing line 953 to FIX7.

### STATION COVERAGE

<u>Station</u>	<u>No. of Pairs</u>	<u>Location</u>
4990	2	Central Pacific
5930	2	Canadian East Coast
5970	3	Commando Lion
5990	3	Canadian West Coast
7930	3	North Atlantic
*7930	3	Northwest Pacific, Reconfigured
7960	2	Gulf of Alaska
7970	4	Norwegian Sea
7980	4	Southeast U.S.A.
7990	3	Mediterranean Sea
8970	3	Great Lakes
9940	3	West coast, U.S.A.
9960	4	Northeast U.S.A.
9970	4	Northwest Pacific
9990	3	North Pacific

22 November 1982

# LORAN-C STATIONS

ID	CD	MS LAT	MS LON	SS LAT	SS LON
4990X	11000	16.4443950	169.3031200	20.1449160	155.5309700
4990Y	29000	16.4443950	169.3031200	28.2341770	178.1730200
5930X	11000	46.4827199	067.5537713	41.1511930	069.5839090
5930Y	25000	46.4827199	067.5537713	46.4632180	053.1028160
5970W	11000	36.1105797	-129.2027279	42.4437104	-143.4309245
5970X	31000	36.1105797	-129.2027279	35.0223871	-126.3226741
5970Z	42000	36.1105797	-129.2027279	26.3624975	-128.0856445
5990X	11000	51.5758780	122.2202240	55.2620851	131.1519648
5990Y	27000	51.5758780	122.2202240	47.0347990	119.4439530
5990Z	41000	51.5758780	122.2202240	50.3629731	127.2129043
7930W	11000	59.5917270	045.1027470	64.5426580	023.5521750
7930X	21000	59.5917270	045.1027470	62.1759640	007.0426538
7930Z	43000	59.5917270	045.1027470	46.4632180	053.1028160
*7930X	11000	24.1707888	-153.5853232	42.4437104	-143.4309245
*7930Y	30000	24.1707888	-153.5853232	26.3624975	-128.0856445
*7930Z	49000	24.1707888	-153.5853232	09.3245789	-138.0954970
7960X	11000	63.1942814	142.4831900	57.2620210	152.2211225
7960Y	26000	63.1942814	142.4831900	55.2620851	131.1519648
7970W	26000	62.1759640	+007.0426538	54.4829872	-008.1736312
7970X	11000	62.1759640	+007.0426538	68.3806150	-014.2747000
7970Y	46000	62.1759640	+007.0426538	64.5426580	+023.5521750
7970Z	60000	62.1759640	+007.0426538	70.5452610	+008.4358690
7980W	11000	30.5938740	085.1009305	30.4333018	090.4943600
7980X	23000	30.5938740	085.1009305	26.3155006	097.5000093
7980Y	43000	30.5938740	085.1009305	27.0158393	080.0653429
7980Z	59000	30.5938740	085.1009305	34.0346081	077.5446654
7990X	11000	38.5220587	-016.4306159	35.3120787	-012.3130245
7990Y	29000	38.5220587	-016.4306159	40.5820950	-027.5201520
7990Z	47000	38.5220587	-016.4306159	42.0336515	-003.1215512
8970W	11000	39.5107540	087.2912140	30.5938740	085.1009305
8970X	28000	39.5107540	087.2912140	42.4250603	076.4933862
8970Y	44000	39.5107540	087.2912140	48.3649844	094.3318469
9940W	11000	39.3306621	118.4956370	47.0347990	119.4439530
9940X	27000	39.3306621	118.4956370	38.4656990	122.2944529
9940Y	40000	39.3306621	118.4956370	35.1918180	114.4817435
9960W	11000	42.4250603	076.4933862	46.4827199	067.5537713
9960X	25000	42.4250603	076.4933862	41.1511930	069.5839090
9960Y	39000	42.4250603	076.4933862	34.0346081	077.5446654
9960Z	54000	42.4250603	076.4933862	39.5107540	087.2912140
9970W	11000	24.4803597	-141.1930303	24.1707888	-153.5853232
9970X	30000	24.4803597	-141.1930303	42.4437104	-143.4309245
9970Y	55000	24.4803597	-141.1930303	26.3624975	-128.0856445
9970Z	75000	24.4803597	-141.1930303	09.3245789	-138.0954970
9990X	11000	57.0912265	+170.1506789	52.4944040	-173.1048974
9990Y	29000	57.0912265	+170.1506789	65.1440306	+166.5312550
9990Z	43000	57.0912265	+170.1506789	57.2620210	+152.2211225

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REPORT DOCUMENTATION PAGE		READ INSTRUCTIONS BEFORE COMPLETING FORM
1. REPORT NUMBER NPS55-82-022	2. GOVT ACCESSION NO. <b>AD-A222 499</b>	3. RECIPIENT'S CATALOG NUMBER
4. TITLE (and Subtitle) POSITION DETERMINATION WITH LORAN-C TRIPLETS AND THE HEWLETT-PACKARD HP-41CV PROGRAMMABLE CALCULATOR		5. TYPE OF REPORT & PERIOD COVERED Technical
		6. PERFORMING ORG. REPORT NUMBER
7. AUTHOR(s) Rex H. Shudde		8. CONTRACT OR GRANT NUMBER(s)
9. PERFORMING ORGANIZATION NAME AND ADDRESS Naval Postgraduate School Monterey, CA 93940		10. PROGRAM ELEMENT, PROJECT, TASK AREA & WORK UNIT NUMBERS 65155N;R0131 N0001482WR20070
11. CONTROLLING OFFICE NAME AND ADDRESS Chief of Naval Research Arlington, VA 22217		12. REPORT DATE September 1982
		13. NUMBER OF PAGES 71
14. MONITORING AGENCY NAME & ADDRESS (if different from Controlling Office)		15. SECURITY CLASS. (of this report) Unclassified
		15a. DECLASSIFICATION/DOWNGRADING SCHEDULE
16. DISTRIBUTION STATEMENT (of this Report) Approved for public release; distribution unlimited.		
17. DISTRIBUTION STATEMENT (of the abstract entered in Block 20, if different from Report)		
18. SUPPLEMENTARY NOTES		
19. KEY WORDS (Continue on reverse side if necessary and identify by block number)		
Loran	Hyperbolic Fixing	Programmable Calculator
Loran-C	Radio Positioning	HP-41C
Navigation	Geodetics	HP-41CV
Position Determination	Geodetic Distances	
Fixing	Calculator	
20. ABSTRACT (Continue on reverse side if necessary and identify by block number)		
<p>This report presents an algorithm and HP-41CV programs for position determination with Loran-C chains. Additional computational routines include the ability to calibrate Loran station triplet data to a known benchmark and ITD's (Indicated Time Delay's), predict ITD's at given positions, compute the geodesic (similar to great circle) bearing and distance from a fix to the destination and to compute the geodesic bearing and distance from any one location to another. Utility routines allow the user to transfer station pair data between the HP-41CV and magnetic cards, magnetic tape and an extended</p>		

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function/memory module.

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AND THE HEWLETT-PACKARD HP-41CV PROGRAMMABLE CALCULATOR

by

R. H. Shudde

Naval Postgraduate School  
Monterey, California



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September 1982

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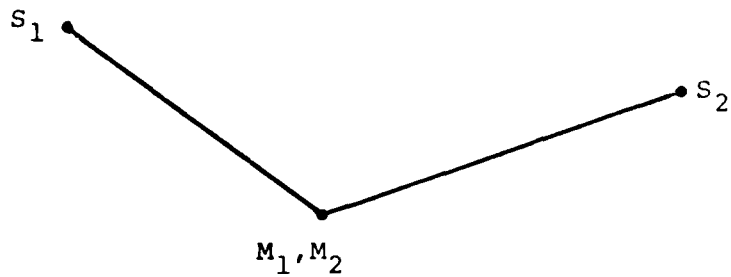
## ABSTRACT

This report presents an algorithm and HP-41CV programs for position determination with Loran-C chains. Additional computational routines include the ability to calibrate Loran station triplet data to a known benchmark and ITD's (Indicated Time Delay's), predict ITD's at given positions, compute the geodesic (similar to great circle) bearing and distance from a fix to the destination and to compute the geodesic bearing and distance from any one location to another. Utility routines allow the user to transfer station pair data between the HP-41CV and magnetic cards, magnetic tape and an extended function/ memory module.

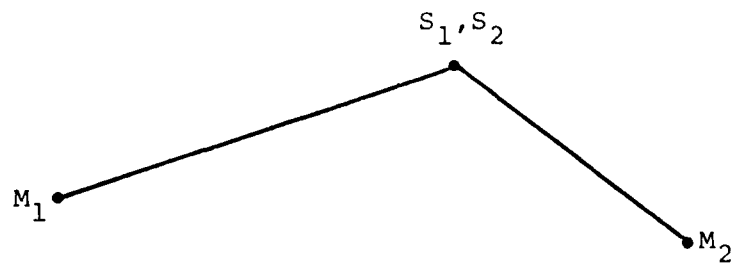
## A. Introduction

The Loran system is a radio aid to navigation which utilizes the principle of hyperbolic fixing. The locus of points for which the difference in arrival time of synchronized signals from a pair of transmitters is constant determines a hyperbolic line of positions. The intersection of two hyperbolic lines of position from two pairs of stations determines position or a hyperbolic fix. That two pairs of stations are required for a fix does not necessarily mean that there are four separate stations, for one station of one pair may be colocated with one station of the other pair forming a Loran triplet (Figure 1). Triplets may be joined "end-to-end" by station colocation to form a Loran chain (Figure 2). Loran chains are common on both the East and West coasts of the North American continent.

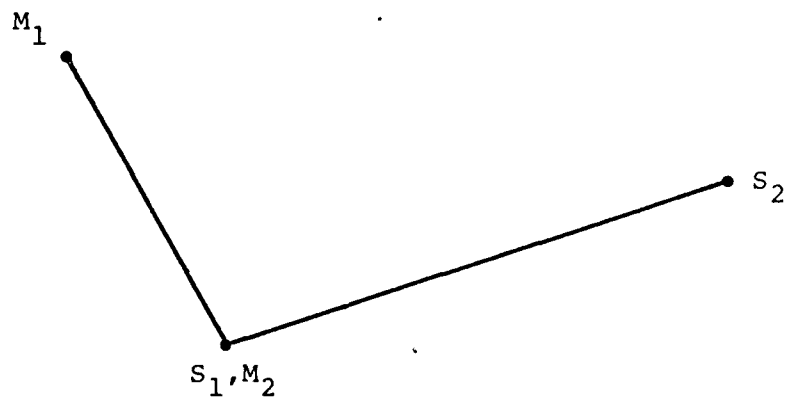
The present day Loran-C operates at 100-kHz and is in use in the Atlantic, Pacific and Mediterranean areas. The computational algorithm and programs described herein can be used for position determination with Loran-C triplets. Further information on the history, development and operation of the Loran systems may be found in References 1 and 2.



(a) Colocated Master Stations



(b) Colocated Slave Stations



(c) Colocated Master and Slave

Figure 1. Loran Triplets.

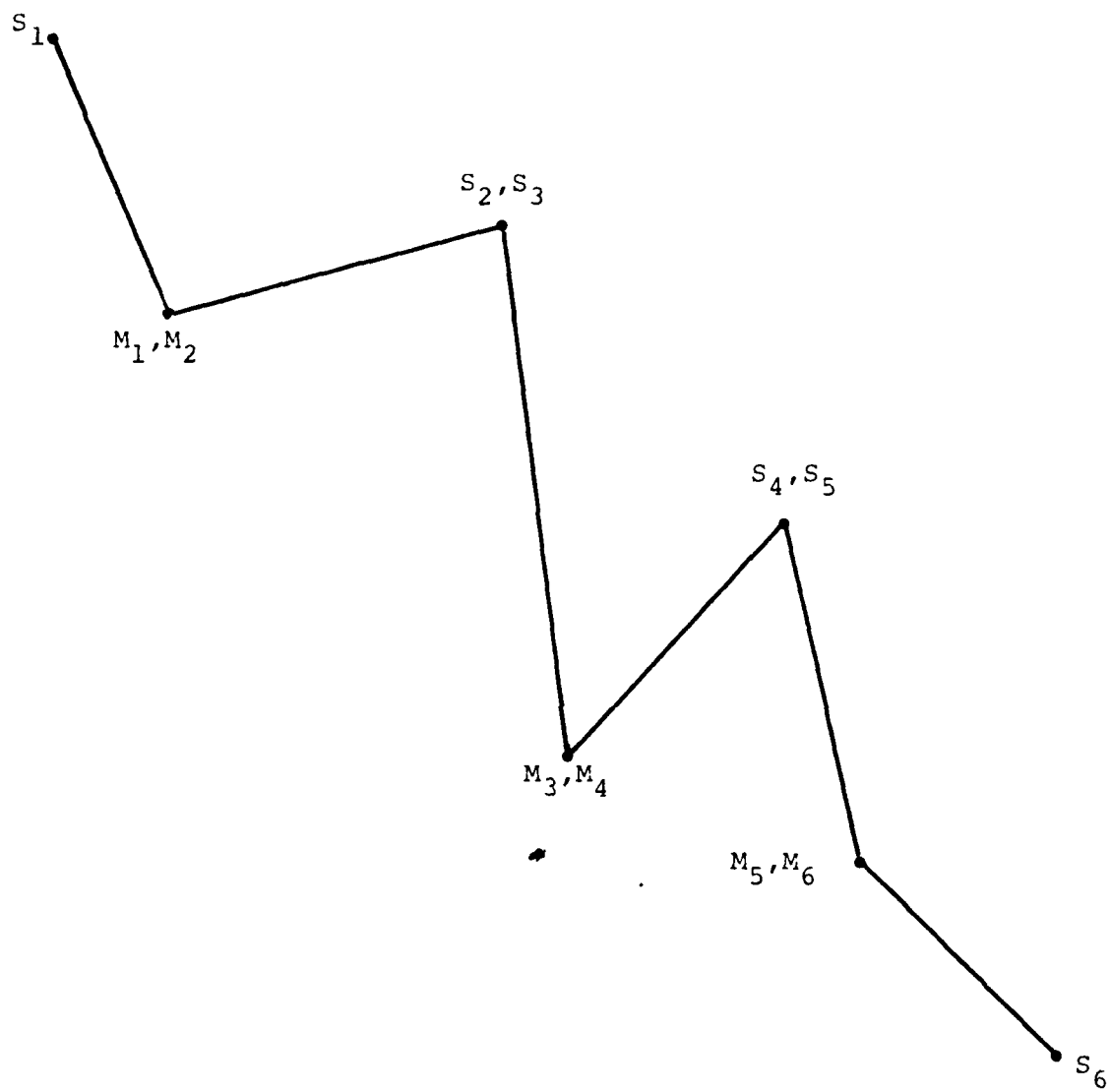


Figure 2. Loran Chain of Five Loran Triplets.

## B. User Routines

### 1. Computational Routines:

- FI - The FIxing routine is the main program for calculating a Loran-C fix from indicated time delays.
- AS - The Alternate Solution routine will allow the second Loran fix solution to be computed. This routine toggles Flag 3 so that on subsequent fixes the FI routine will calculate the alternate solution.
- DN - The DestiNation routine stores the latitude and longitude of a fixed destination.
- HD - Computes the Heading and Distance from the current fix to the destination stored by the DN routine.

### 2. Manual Mode Routines:

- MI - Manual Intput allows station data to be input and stored via the calculator keyboard.
- ED - Echo Data is a utility routine for validating station triplet information stored in the calculator.

### 3. Card Reader Routines:

- CS - Card Store records station data onto magnetic cards.
- CR - Card Read inputs station data from magnetic cards.
- CE - Card Echo is a utility routine for validating station information stored on data cards.

### 4. Extended Memory Routines:

- XS - XMEM Store records station data onto the extended memory module.
- XR - XMEM Recall inputs station data from the extended memory module.



XD - XMEM Delete erases station data from the extended memory module.

5. Tape Cassette Routines:

TS - Tape Store records station data onto the tape cassette.

TR - Tape Recall inputs station data from the tape cassette.

TD - Tape Delete erases station data from the tape cassette.

6. Utility Routines:

DH - This routine is similiar to the HD option except that it computes the heading and distance from any origin to any destination.

PR - PR is used to Predict the station ITD's that will be received at a given latitude and longitude.

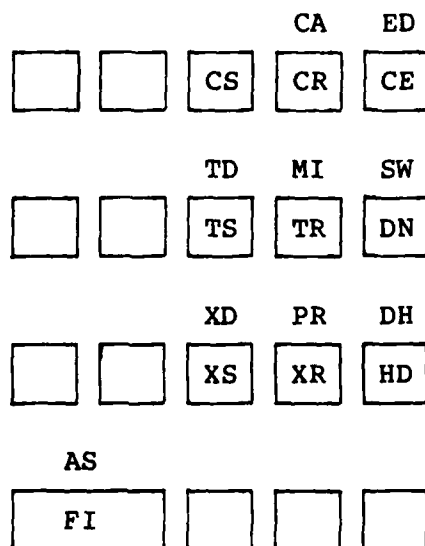
CA - CA is the Calibration option. Given the latitude and longitude of a known position and the indicated time delays from a Loran-C triplet, the stored station data are modified so that the FI routine (or AS) will compute the known position from the same time delays.

SW - SWitch data swaps the data of the two Loran stations stored in memory.

Note: There are no specific routines that relate to HP-41CV printer operations. However, all input and output will be recorded on a printer if one is attached.

### C. Recommended Key Assignments

It is recommended that the following HP-41CV user key assignments be made and recorded onto the program cards if the program is first prepared manually:



The FI function is placed on the ENTER key as a reminder that ENTER should not be used for data entry. To make the user key assignments on the HP-41CV, refer to the ASN function in the HP-41CV Owner's Handbook and Programming Guide.

#### D. User Instructions with Examples

##### 1. Manual Input Routine - MI

This routine can be used to enter station data (Appendix C) to prepare data to be transferred to cards, extended memory, or tape cassette. It can also be used to enter station data manually if alternate data storage media are not available.

Example using 9940W and 9940Y. (Note: The notation <9>, for example, means that you must press the gold shift key and then the 9 key.)

<u>See</u>	<u>Key in</u>	<u>Press</u>
1.	XEQ"MI"	
2. ID?	<9><9><4><0>W	R/S
3. CODE DELAY?	11000	R/S
4. MS LAT?	39.330662	R/S
5. MS LON?	118.495637	R/S
6. SS LAT?	47.034799	R/S
7. SS LON?	119.443953	R/S

If desired, these station parameters can now be transferred to card, extended memory or tape using the CS, XS, or TS routines, respectively. Otherwise, repeat the steps above with the 9940Y station data. These two stations will be used in the remaining examples.

<u>See</u>	<u>Key in</u>	<u>Press</u>
1.	XEQ"MI"	
2. ID?	<9><9><4><0>Y	R/S
3. CODE DELAY?	40000	R/S
4. MS LAT?	39.330662	R/S

5. MS LON?            118.495637            R/S  
6. SS LAT?            35.191818            R/S  
7. SS LON?            114.481743            R/S  
8. NEXT OPTION?

At this point the station data for 9940W and 9940Y are stored in the calculator. The 9940Y data can be transferred to card, extended memory or tape cassette using the CS, XS or TS routines, respectively.

[Advanced User Note: The first action taken in the MI routine is to XEQ"SW". SW is the data swap routine which exchanges to content of R16 - R25 with R26 - R35. The incoming data are then stored in the R16 - R25 registers. The CS, XS and TS routines transfer the content of R16 - R25 to card, extended memory or tape cassette, respectively. If desired, the content of these registers can be swapped once more by using the SW utility routine.]

## 2. Echo Data Routine - ED

This routine allows the user to review the station data resident in the calculator.

Example: Load the station pairs 9940W and 9940Y using either the MI, CR, XR or TR routines.

<u>See</u>	<u>Key in</u>	<u>Press</u>
1.	XEQ"ED"	
2. ID: 9940W		R/S
3. CD: 11000		R/S
4. MLT: 39.330662		R/S
5. MLN: 118.495637		R/S
6. SLT: 47.034799		R/S
7. SLN: 119.443953		R/S
8. BL: 2796.903		R/S
9. ID: 9940Y		R/S
10. CD: 40000		R/S
11. MLT: 39.330662		R/S
12. MLN: 118.495637		R/S
13. SLT: 35.191818		R/S
14. SLN: 114.481743		R/S
15. BL: 1967.302		R/S
16. NEXT OPTION?		

Notation: CD = coding delay, M = master, S = slave, LT = latitude, LN = longitude and BL is the station pair baseline plus the secondary phase correction in microseconds.

### 3a. Card Store Routine - CS

With the card reader attached, station data (in R16 - R25), which has been input using the MI, XR or TR routine, can be transferred to magnetic card using the XEQ"CS" command or by pressing the appropriate user defined key.

Example using 9940W.

- | <u>See</u>      | <u>Key in</u>   | <u>Press</u> |
|-----------------|---|--------------|
| 1.              | XEQ"PD"   |              |
| 2. WRITE: 9940W | (Pass a blank card through the card reader. Label the card track "9940W") |              |
| 3. NEXT OPTION? |   |              |

To proceed with the remaining examples it is recommended that you also prepare a card for the 9940Y station pair.

### 3b. Card Read Routine - CR

With the card reader attached, XEQ"CR" or press the appropriate user defined key. This routine can be used to input the data for two station pairs, which must form a triplet.

Example using 9940W and 9940Y.

- | <u>See</u>      | <u>Key in</u>   | <u>Press</u> |
|-----------------|---|--------------|
| 1.              | XEQ"CR"   |              |
| 2. 1ST CARD     | (Pass the data card for 9940W through the card reader.) |              |
| 3. 2ND CARD     | (Pass the data card for 9940Y through the card reader.) |              |
| 4. NEXT OPTION? |   |              |

### 3c. Card Echo Routine - CE

With the card reader attached, XEQ"CE" or press the appropriate user defined key. This routine is used to validate the content of data cards against the table in Appendix C.

Example using 9940W.

<u>See</u>	<u>Key in</u>	<u>Press</u>
1.	XEQ"CE"	
2. STA. CARD	(Pass one side of a data card [9940W] through the card reader).	
3. ID: 9940W		R/S
4. CD: 11000		R/S
5. MLT: 39.330662		R/S
6. MLN: 118.495637		R/S
7. SLT: 47.034799		R/S
8. SLN: 119.443953		R/S
9. BL: 2796.903		R/S
10. NEXT OPTION?		

Notation: CD = coding delay, M = master, S = slave, LT = latitude, LN = longitude and BL is the station pair baseline plus the secondary phase correction in microseconds.

#### 4a. Store Data in Extended Memory - XS

With the extended memory module in the HP-41CV, station data (in R16 - R25), which has been input using the MI, CR, XR or TR routine, can be transferred to the module using the XEQ"XS" command or by pressing the appropriate user defined key. Example using 9940W.

<u>See</u>	<u>Key in</u>	<u>Press</u>
1.	XEQ"XS"	
2. NEXT OPTION?		

Should the station pair already be in extended memory, the message DUP FL (duplicate file) will be displayed. If needed, the duplicate file may be erased using the XD routine.

To proceed with the remaining examples it is recommended that you also store the 9940Y station pair.

#### 4b. Recall Data from Extended Memory - XR

With the extended memory module installed, XEQ"XR" or press the appropriate user defined key to input the data for a station pair.

Example using 9940W. (Note: The notation <9>, for example, means that you must press the gold shift key and then the 9 key.)

<u>See</u>	<u>Key in</u>	<u>Press</u>
1.	XEQ"XR"	
2. ID?	<9><9><4><0>W	R/S
3. NEXT OPTION?		



4c. Delete Data from Extended Memory - XD

XEQ"XD" or press the appropriate user defined key to delete the specific station pair data from the extended memory module.

Example using 9940W.

	<u>See</u>	<u>Key in</u>	<u>Press</u>
1.		XEQ"XD"	
2. ID?		<9><9><4><0>W	R/S
3. NEXT OPTION?			

The message FL NOT FOUND will be displayed if the file you wish to delete is not in the extended memory.

Note: The extended functions/ memory module will accommodate the data for 11 station pairs. The extended memory module will accommodate the data for an additional 22 station pairs.

#### 5a. Store Data in the Tape Cassette - TS

With the tape cassette attached to the HP-41CV, station data (in R16 - R25), which has been input using the MI, CR, XR or TR routine, can be transferred to the tape using the XEQ"TS" command or by pressing the appropriate user defined key.

Example using 9940W.

<u>See</u>	<u>Key in</u>	<u>Press</u>
1.	XEQ"TS"	
2. NEXT OPTION?		

Should the station pair already be in extended memory, the message DUP FL NAME (duplicate file name) will be displayed. If needed, the duplicate file may be erased using the TD routine.

To proceed with the remaining examples it is recommended that you also store the 9940Y station pair.

#### 5b. Recall Data from the Tape Cassette -TR

With the tape cassette attached, XEQ"TR" or press the appropriate user defined key to input the data for a station pair.

Example using 9940W. (Note: The notation <9>, for example, means that you must press the gold shift key and then the 9 key.)

<u>See</u>	<u>Key in</u>	<u>Press</u>
1.	XEQ"TR"	
2. ID?	<9><9><4><0>W	R/S
3. NEXT OPTION?		

5c. Delete Data from the Tape Cassette - TD

XEQ"TD" or press the appropriate user defined key to delete the specific station pair data from the tape cassette.

Example using 9940W.

<u>See</u>	<u>Key in</u>	<u>Press</u>
1.	XEQ"TD"	
2. ID?	<9><9><4><0>W	R/S
3. NEXT OPTION?		

The message FL NOT FOUND will be displayed if the file to be deleted is not on the tape.

6. Loran-C Fixing Routines FI and AS

Given the indicated time delay (ITD) from two station pairs which form a triplet, a Loran-C fix is obtained.

Example: Load 9940W and 9940Y into the calculator using the MI, CR, XR or TR routine. The ITD on 9940W is 16019 microseconds and the ITD of 9940Y is 42585 microseconds. Where are you?

<u>See</u>	<u>Key in</u>	<u>Press</u>
1.	XEQ"FI"	
2. ITD: 9940W	16019	R/S
3. ITD: 9940Y	42585	R/S
4. LAT: 39.1419		R/S
5. LON: 115.5052		R/S
6. NEXT OPTION?		

Since you are on a boat, you know that you cannot be in central Nevada at 39d14'19" North and 115d50'52" West. Every Loran-C fix has two solutions, so in this case you must use the alternate solution.

<u>See</u>	<u>Key in</u>	<u>Press</u>
7.	XEQ"AS"	
8. LAT: 35.0001		R/S
9. LON: 125.0009		R/S
10. NEXT OPTION?		

This is the proper solution at almost exactly 35 degrees North and 125 degrees West. Note that annunciator 3 (Flag 3) shows in the display indicating the alternate solution. If you should now repeat from Step 1, you will obtain the proper

solution immediately.

The message "E: NO TRIPLET" will appear following Step 1 if the data do not comprise a valid triplet. The latitudes and longitudes of each station pair at the vertex must agree exactly. Should this error occur, use the ED routine to review the resident station data.

The message "E: ITD ERROR" will appear following Step 2 or 3 indicating that the ITD you keyed in is inconsistent with the station parameters. Press R/S to be requeried for the ITD.

7a. Distance and Heading Routines DN and HD

If you know the latitude and longitude of your destination, you may key these in and then see how far your fix is from your destination and what the geodesic heading (similiar to great circle heading) is to your destination.

Example: Your destination is Moss Landing at about 36d48'N and 121d47'W. Your current fix is 35dN and 125dW (see the FI-SA example). First, key in your destination.

<u>See</u>	<u>Key in</u>	<u>Press</u>
1.	XEQ"DN"	
2. DEST LAT?	36.48	R/S
3. DEST LON?	121.47	R/S
4. NEXT OPTION?		R/S

The destination is now stored in the calculator and will remain unchanged until you use either the DN or DH options. Also, the latest fix is stored and will remain unchanged until you use either the FI, AS or DH options. Now, find the distance and bearing from the latest fix (see the FI-AS example) to Moss Landing.

<u>See</u>	<u>Key in</u>	<u>Press</u>
1.	XEQ"HD"	
2. N.MI: 190.38		R/S
3. BRG: 54.3411		R/S
4. NEXT OPTION?		R/S

So the distance to Moss Landing is 190.38 nautical miles at a heading of 54d34'11".

7b. Distance and Heading Routine - DH

Given the latitude and longitude of an origin and destination, this routine will find the distance and heading from one to the other.

Example: How far, and in what direction, is Corvallis, Oregon (44d34'N, 123d16'W) from Cupertino, California (37d19N, 122d02'W)?

<u>See</u>	<u>Key in</u>	<u>Press</u>
1.	XEQ"DH"	
2. ORIG LAT?	37.19	R/S
3. ORIG LON?	122.02	R/S
4. DEST LAT?	44.34	R/S
5. DEST LON?	123.16	R/S
6. N.MI: 438.32		R/S
7. BRG: 353.0259		R/S
8. NEXT OPTION?		

Thus the distance is 438.32 nautical miles and the direction of Corvallis from Cupertino is 353d02'59".

#### 8. ITD Prediction Routine - PR

As an aid to identification, this routine will allow the user to determine what ITD's should be received at a given location.

Example: Suppose that you know you are somewhere near latitude 35 North and longitude 125 West but are not sure what ITD's you should be receiving from 9940W and 9940Y. To determine these ITD's, proceed as follows:

<u>See</u>	<u>Key in</u>	<u>Press</u>
1.	XEQ"PR"	
2. LAT?	35	R/S
3. LON?	125	R/S
4. 9940W: 16019.35		R/S
5. 9940Y: 42584.71		R/S
6. NEXT OPTION?		

You should expect to receive an ITD of 16019.35 from 9940W and an ITD of 42584.71 from 9940Y.



## 9. Calibration Routine - CA

This routine will allow the user to calibrate the Loran data in the calculator to a known position when the indicated time delay (ITD) is known for each station pair.

Example: Suppose you are receiving an ITD of 16308 from 9940W and 42800 from 9940Y. These ITD's would tell you that your location is 36d47'55"N and 121d47'11"W. However, you know that your position is bench marked to be at 36d47'36"N and 121d46'58"W, and you wish to calibrate your calculator so that the ITD's of 16308 and 42800 will give you the latter fix instead of the former. Proceed as follows:

<u>See</u>	<u>Key in</u>	<u>Press</u>
1.	XEQ"CA"	
2. LAT?	36.4736	R/S
3. LON?	121.4658	R/S
4. ITD 9940W:	16308	R/S
5. ITD 9940Y:	42800	R/S
6. NEXT OPTION?		

Entering 16308 and 42800 into the FI routine will now give you a fix at 36d47'35"N and 121d46'59"W. The small discrepancy between this fix and the bench mark is due to assumptions made in the fixing algorithm.

Calibration is achieved by modifying the Master/Slave baseline (BL in the CE and ED routines). See Section F.

10. Switch Data Registers Routine - SW

The SW utility allows the user to swap the station data stored in R16 - R25 with the data stored in R26 - R35. Whenever the MI, XR or TR routine is used, the SW routine is invoked prior to the loading of the data; the incoming data are then placed in R16 - R25. The consequence is that the first station pair data reside in R26 - R35 and the second station pair data reside in R16 - R25.

One user application of SW would be to change the order of the station ID query in the FI routine (this also affects the order of determination of the solution and alternate solution). Another user application would be to output both resident station pairs to card, extended memory or tape cassette using the CS, XS or TS routines, respectively. To accomplish this, first use the CS, XS, or TS routine; then XEQ"SW" (note that the ID of the station data in R16 - R25 appears in the display instead of the NEXT OPTION? prompt); and finally use the CS, XS or TS routine once more.

11a. Recording the Loran-C Program onto Magnetic Cards

- (1) Attach the card reader to the HP-41CV.
- (2) Place the calculator in the USER mode.
- (3) Press the PRGM key to place the calculator in the program mode.
- (4) Pass one side of a blank magnetic card through the card reader. Then follow the display prompts until nine program cards (17 tracks) have been recorded.
- (5) Press the PRGM key once more to leave the program mode.
- (6) To record a status card, XEQ"WSTS". Then pass a blank card through the card reader following the display prompts.

11b. Recording the Loran-C Program onto Magnetic Tape

- (1) Attach the tape cassette to the HP-41CV.
- (2) Place the calculator in the USER mode.
- (3) Press the alpha key, key in the word LORANC, press the alpha key once more, and then XEQ"WRTP".
- (4) To record the program status, press the alpha key, key in the word STATUS, press the alpha key once more, and then XEQ"WRTS".

12a. Loading the Loran-C Program from Magnetic Cards

- (1) Attach the card reader to the HP-41CV.
- (2) Clear program memory: Turn the calculator off, then, while pressing the left arrow (erase) key down, turn the calculator on.
- (3) Place the calculator in the USER mode.
- (4) Read in the STATUS card. The status card will set the calculator to SIZE 42.
- (5) Read in the nine program cards (17 tracks).

12b. Loading the Loran-C program from Tape Cassette

- (1) Attach the tape cassette to the HP-41CV.
- (2) Clear program memory. (See Step 2 above).
- (3) Place the calculator in the USER mode.
- (4) Press the alpha key, key in the word STATUS, press the alpha key once more, and then XEQ"READS". The status file will set the calculator to SIZE 42.
- (5) Press the alpha key, key in the word LORANC, press the alpha key once more, and then XEQ"READP".

#### E. The Loran-C Fixing Algorithm

The principles of Loran lines of position (LOP's) and fixing are adequately covered in Reference 1 and will not be repeated here.

The basic Loran-C equation [Ref. 4] can be written as

$$ITD = [T_S + p(T_S)] - [T_M + p(T_M)] + [T_B + p(T_B)] + \delta \quad (1)$$

where

ITD is the "indicated time difference" in microseconds,

$T_M$  is the distance, in microseconds, from the master  
to the receiver,

$T_S$  is the distance, in microseconds, from the slave to  
the receiver,

$T_B$  is the distance, in microseconds, between the master  
and the slave,

$\delta$  is the assigned station pair coding delay, in micro-  
seconds, and

$p(T)$  is the secondary phase correction, in microseconds,  
for a surface seawater path of length  $T$ .

The quantity

$$\Delta t = T_B + p(T_B) + \delta$$

is a constant for each master/slave pair. The quantity  $T_B$  is computed from the positions of the master and slave using the reverse solution algorithm (Section H) at the time of manual data input (Routine MI).

The following World Geodetic System 1972 (WGS 72) values have been adopted for Loran-C navigation [Ref. 4]:

$v_0 = 299792458$  meters/second is the velocity of light in free space,

$\eta = 1.000338$  is the index of refraction of the surface of the earth for standard atmosphere and 100 kHz electromagnetic waves,

$a_e = 6378135.000$  meters is the equatorial radius of the earth

and  $f = 1/298.26$  is the flattening factor ( $1-b/a_e$ , where  $b$  is the polar radius) of the earth.

Accurate formulas for computing the secondary phase correction  $p(T)$  are contained in Reference 4, but for use in the HP-41CV, the form

$$p(T) = a_0/T + a_1 + a_2T \quad (2)$$

is used, where  $T$  is in microseconds and

1. For  $T \geq 537 \mu\text{sec}$ :

$$a_0 = 129,$$

$$a_1 = -0.408, \text{ and}$$

$$a_2 = 0.0006458.$$

2. For  $T < 537 \mu\text{sec}$ :

$$a_0 = 2.74,$$

$$a_1 = -0.011, \text{ and}$$

$$a_2 = 0.00033.$$

On the surface of a sphere, a hyperbolic line of position (LOP) can be represented by the equation [Ref. 1, page 175]

$$\tan r = \frac{\cos 2a - \cos 2c}{\sin 2c \cos \omega + \zeta \sin 2a} \quad (3)$$

where the origin of the coordinate system is at the prime focus of the spherical hyperbola,  $2c$  is the spherical arc joining the foci,  $2a$  is a constant for any one hyperbola, and  $r$  and  $\omega$  are the spherical coordinates of a point on the hyperbola. If the base line of the coordinate system is the arc joining the foci the  $\omega$  is the spherical polar angle from the baseline to a point  $P$  on the spherical hyperbola and  $r$  is spherical polar distance (or arc) from the prime focus to  $P$ . Using the Loran system we take  $\zeta = +1$  if the prime focus is at a master station and  $\zeta = -1$  if the prime focus is at a slave station.

If we let  $v = v_0/n$  be the velocity of 100kHz electromagnetic radiation at the earth's surface then, for a spherical earth, we can relate the parameters in Equations 1 and 3 as follows:

$$2c = vT_B/a_e ,$$

and

$$2a = v(T_S - T_M)/a_e .$$

Using the spherical approximation for now, we see that  $2c$  is known for any Loran pair. The "indicated time delay" ITD is measured by the receiver at point  $P$ , and to determine a hyperbolic line of position we must determine  $2a$ , but  $T_S - T_M$  cannot be computed from Equations 1 and 2. If  $a_0$  were zero

in Equation 2, then it would be possible to determine  $T_S - T_M$  uniquely. As an approximation we use the following parameters in Equation 2:

$$a_0 = 0 ,$$

$$a_1 = -0.321 ,$$

and

$$a_2 = 0.000635 .$$

These values have been obtained by setting  $a_0 = 0$  and determining  $a_1$  and  $a_2$  by linear regression of the  $T > 537$  values over the interval of  $1000 < T < 8000$ . This approximation is quite good (within  $0.03 \mu s$ ) for distances up to 10,000 microseconds where small changes in the LOP's can cause large position errors. At short distances the error increases from  $0.05 \mu s$  at 1000  $\mu s$  to  $0.58 \mu s$  at 10  $\mu s$ ; although these errors are large for small distances, the LOP's are not as sensitive to these changes as they would be at large distances. When this approximation is substituted into Equation 1, we obtain

$$[T_S + a_1 + a_2 T_S] - [T_M + a_1 + a_2 T_M] = ITD - \Delta t ,$$

or

$$T_S - T_M = (ITD - \Delta t) / (1 + a_2) \quad (4)$$

and hence  $2a = v(T_S - T_M)/a_e$  is determined for use in the spherical approximation.

Consider a Loran-C triplet with the master stations co-located. Let  $\xi_1$  and  $\xi_2$  denote the azimuth angles of slave 1 ( $S_1$ ) and slave 2 ( $S_2$ ), respectively, measured from North toward the East from the master stations (M) (see Figure 3).



Further, let  $\alpha$  and  $r$  be the azimuth and spherical polar arc (distance) of the receiver (R) from M. For this geometry, Equation 3 can be written in the form

$$\tan r_i = \frac{B_i}{C_i \cos(\alpha - \xi_i) + A_i} , \quad (5)$$

where

$$A_i = \zeta_i \sin 2a_i ,$$

$$B_i = \cos 2a_i - \cos 2c_i ,$$

and

$$C_i = \sin 2c_i$$

for the  $i^{\text{th}}$  Loran pair,  $i = 1, 2$ . Since  $r_1 = r_2 = r$ , we can eliminate  $\tan r$  between the two equations. The resulting equation can be rewritten as

$$C \cos \alpha + S \sin \alpha = K , \quad (6)$$

where

$$C = B_1 C_2 \cos \xi_2 - B_2 C_1 \cos \xi_1 ,$$

$$S = B_1 C_2 \sin \xi_2 - B_2 C_1 \sin \xi_1 ,$$

and

$$K = B_2 A_1 - B_1 A_2 .$$

If we define  $\rho > 0$  and  $\gamma$  by the equations

$$\rho \cos \gamma = C , \quad (7)$$

and

$$\rho \sin \gamma = S ,$$

then

$$\rho = \sqrt{C^2 + S^2} ,$$

and

$$\gamma = \text{qatn}(S, C) .$$

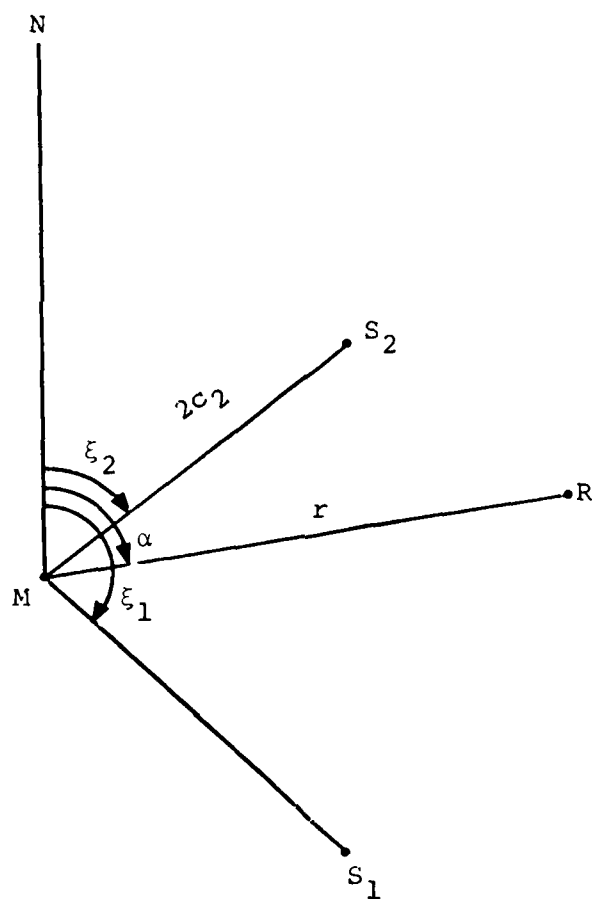


Figure 3. Geometry of a Loran Triplet and a Receiver.

Here the function  $\text{qatn}(y,x)$  is the arctangent of  $y/x$  adjusted for the proper quadrant according to the signs of  $x$  and  $y$ . A compact form of this function is

$$\text{qatn}(y,x) = \tan^{-1} \frac{y}{x + 10^{-9} t(x = 0?)} + \pi t(x < 0?)$$

where  $t(z) = 1$  when  $z$  is true  
and  $t(z) = 0$  when  $z$  is false.

When convenient we will use the notation  $\text{qatn}(y/x)$  interchangeably with  $\text{qatn}(y,x)$ . Now we can substitute Eq. (7) into Eq. (6) and solve for

$$\alpha = \gamma \pm \cos^{-1}(K/\rho) \quad (8)$$

to obtain the azimuth angle  $\alpha$  of the two points of intersection of the spherical hyperbolic LOP's. Finally we can obtain a value for  $r$  by substituting each  $\alpha$  into Eq. (5) for either  $i = 1$  or  $i = 2$ . We find that

$$r = \text{qatn} \left[ \frac{B_i}{C_i \cos(\alpha - \xi_i) + A_i} \right] \text{ for } i = 1 \text{ or } 2. \quad (9)$$

The distance and azimuth from  $M$  or the triplet vertex can be converted into the latitude and longitude of the two possible positions of  $r$ .

The fixing algorithm then uses  $\alpha$  and  $r$  in the direct solution algorithm of spheroidal geodesy (Section G).

## F. The Calibration and ITD Prediction Algorithms

Calibration can be achieved when an ITD is measured at a known bench marked position. From the bench marked position and the known master and slave positions, the quantities  $T_M + p(T_M)$  and  $T_S + p(T_S)$  can be computed using the reverse solution algorithm (Section H) and the accurate secondary phase correction formula (Eq. 2). Equation 1 can then be solved for  $T_B + p(T_B)$  to obtain a modified baseline. This modified baseline is stored and then used instead of the true baseline in subsequent computations. The affect on the accuracy of fixes using this modified baseline with positions far removed from the bench mark has not studied.

The ITD prediction algorithm is a direct application of Equation 1. A known position, together with the known master and slave positions, is used to compute the quantities  $T_M + p(T_M)$  and  $T_S + p(T_S)$ . When these values, along with a computed or calibrated baseline,  $T_B + p(T_B)$ , are substituted into Equation 1, a predicted ITD is obtained.

### G. The Direct Solution Algorithm

This direct solution algorithm is a modification of the second order in flattening ( $f$ ) algorithm given by Thomas [Ref. 5, pp. 7-8]. Thomas' notation has been followed as closely as possible for ease of comparison of the algorithms. The qatn function is defined in a previous section. East longitudes and South latitudes are negative. We are given the point  $P_1(\phi_1, \lambda_1)$  on the spheroid, where  $\phi_1, \lambda_1$  are the geodetic latitude and longitude (geographic coordinates); the forward azimuth  $\alpha_{12}$  and distance  $S$  to a second point  $P_2(\phi_2, \lambda_2)$ ; and from these we are to find the geographic coordinates  $\phi_2, \lambda_2$  and the back azimuth  $\alpha_{21}$ . The given quantities are  $\phi_1, \lambda_1, \alpha_{12}$  and  $S$ . No assumptions about the relative location of  $P_1$  and  $P_2$  are required. The modified direct solution algorithm is:

$$\begin{aligned} \theta_1 &= \tan^{-1}[(1-f)\tan \theta_1], M = -\sin \alpha_{12} \cos \theta_1, \\ C_1 &= fM, C_2 = f(1-M^2)/4, \\ D &= (1-C_2)(1-C_2 - C_1M), P = C_2[1 + (1/2)C_1M]/D, \\ N &= \cos \theta_1 \cos \alpha_{12}, \sigma_1 = \text{qatn}(N, \sin \theta_1), \\ d &= S/(a_e D), u = 2(\sigma_1 - d), W = 1 - 2P \cos u, \\ V &= \cos(u+d), X = C_2^2 \sin d \cos d(2V^2 - 1), \\ Y &= 2PVW \sin d, \Delta\sigma = d + X - Y, \\ K &= [M^2 + (N \cos \Delta\sigma \sin \theta_1 \sin \Delta\sigma)^2]^{1/2}, \\ \theta_2 &= \tan^{-1}[(\sin \theta_1 \cos \Delta\sigma + N \sin \Delta\sigma)/K], \\ \Delta\eta &= \text{qatn}(-\sin \Delta\sigma \sin \alpha_{12}, \cos \theta_1 \cos \Delta\sigma - \sin \theta_1 \sin \Delta\sigma \cos \alpha_{12}), \\ H &= C_1(1-C_2) \Delta\sigma - C_1C_2 \sin \Delta\sigma \cos(2\sigma_1 - \Delta\sigma), \\ \lambda_2 &= \lambda_1 + \Delta\eta - H, \end{aligned}$$

$$\alpha_{21} = \text{qatn}[-M, - (N \cos \Delta\sigma - \sin \theta_1 \sin \Delta\sigma)] ,$$

$$\phi_2 = \tan^{-1}[\tan \theta_2 / (1-f)]$$

Details of the modifications made to Thomas' algorithm are contained in Reference 3. The algorithm above has been further modified so that Eastern longitudes, rather than Western longitudes, are negative.

#### H. The Reverse Solution Algorithm

This reverse solution algorithm is a modification of the second order in flattening (f) algorithm given by Thomas [Ref. 5, pp. 8-10]. Thomas' notation has been followed as closely as possible for ease of comparison of the algorithms. The gathn function is defined in a previous section. East longitudes ( $\lambda$ ) and South latitudes ( $\phi$ ) are negative. We are given the points  $P_1(\phi_1, \lambda_1)$ ,  $P_2(\phi_2, \lambda_2)$  on the spheroid and are to find the distance  $S$  between the points and the forward and back azimuths,  $\alpha_{12}$  and  $\alpha_{21}$ . Given quantities are  $\phi_1$ ,  $\lambda_1$ ,  $\phi_2$  and  $\lambda_2$ . No assumptions about the relative location of  $P_1$  and  $P_2$  are required. The modified reverse solution algorithm is:

$$\begin{aligned}
 \theta_i &= \tan^{-1}[(1-f)\tan \phi_i] , \quad i = 1, 2 , \\
 \Delta\lambda &= \lambda_2 - \lambda_1 , \quad \Delta\theta_m = (\theta_2 - \theta_1)/2 , \quad \theta_m = (\theta_1 + \theta_2)/2 , \\
 H &= \cos^2 \Delta\theta_m - \sin^2 \theta_m , \quad L = \sin^2 \Delta\theta_m + H \sin^2(\Delta\lambda/2) , \\
 d &= 2 \sin^{-1} \sqrt{L} , \quad U = 2 \sin^2 \theta_m \cos^2 \Delta\theta_m / (1-L) , \\
 V &= 2 \sin^2 \Delta\theta_m \cos^2 \theta_m / L , \quad X = U + V , \quad Y = U - V , \\
 T &= d/\sin d , \quad D = 4T^2 , \quad E = 2 \cos d , \quad A = DE , \\
 C &= T - (A-E)/2 , \quad n_1 = X(A+CX) , \\
 B &= 2D , \quad n_2 = Y(B+EY) , \quad n_3 = DXY , \\
 \delta_2 d &= f^2(n_1 - n_2 + n_3)/64 , \quad \delta_1 d = f(TX-Y)/4 , \\
 S/a_e &= (T - \delta_1 d + \delta_2 d) \sin d , \quad M = 32T - (20T-A)X - (B+4)Y , \\
 F &= 2Y - E(4-X) , \quad G = fT/2 + f^2 M/64 , \quad Q = - (FG \tan \Delta\lambda)/4 , \\
 \Delta\lambda_m' &= (\Delta\lambda + Q)/2 ,
 \end{aligned}$$

$$\begin{aligned}
t_1 &= \text{qatn}(\sin \Delta\theta_m \cos \Delta\lambda'_m, \cos \theta_m \sin \Delta\lambda'_m) , \\
t_2 &= \text{qatn}(- \cos \Delta\theta_m \cos \Delta\lambda'_m, \sin \theta_m \sin \Delta\lambda'_m) , \\
\alpha_{12} &= t_1 + t_2 , \quad \alpha_{21} = t_1 - t_2
\end{aligned}$$

Details of the modifications made to Thomas' algorithm are contained in Reference 3. The algorithm above has been further modified so that Eastern longitudes, rather than Western longitudes, are negative.



## I. Program Accuracy

The direct and reverse solution algorithms are equivalent to the second order flattening algorithms given by Thomas (Ref. 5); the parameters of the WGS 1972 spheroid are used. The reverse solution algorithm reproduces the baselines provided by the Defense Mapping Agency for all 40 Loran-C stations to within 0.15 meters (the average deviation is -0.031 meters, DMA minus HP-41CV, with a standard deviation of 0.037 meters) and to within 0.01 microseconds, including the secondary phase correction for an all seawater path. The reverse solution algorithm is also used to generate predicted ITD's; these are presumed to be within 0.01 microseconds, also.

The fixing algorithm uses the direct solution algorithm with the azimuth and distance of the fix from the vertex of the Loran-C triplet computed from Equations 8 and 9 as inputs. Equations 8 and 9 are based upon spherical geometry and include an approximation to the secondary phase correction for an all seawater path. The largest source of error is the assumption that the azimuth and distance to the fix are accurately represented by this spherical approximation. This approximation has not been rigorously tested, however it is possible to use the reverse solution algorithm to predict the ITD's that will be received at a given position and then to enter these ITD's into the fixing algorithm to determine how accurately the fixing algorithm reproduces the original position. The distance between the fix and the original position can be determined using the HD algorithm. Tables 1, 2 and 3 were produced in this manner. Similiar tables with different station

pairs are given in References 3, 6 and 7. It is felt that the results are accurate enough to not warrant the inclusion of an iterative improvement routine. Of the samples in Tables 1, 2 and 3, the largest error, 0.22 n.mi., is the first entry in Table 1. From the chart LCNC-2, it estimated that the angle of intersection of the two hyperbolic lines of position is about 5 degrees and so an error of 0.22 n.mi. should not be unexpected.

Table 1. Colocated Master Stations

Position		Predicted ITD's		HP-41CV Fix		Error n.mi
Lat	Long	9940W	9940X	Lat(N)	Long(W)	
31°	123°	16413.28	27570.93	30°59'47"	123°00'03"	0.22
37°	126°	15610.11	27020.50	36°59'53"	126°00'09"	0.17
42°	129°	13881.78	27285.58	42°00'00"	129°00'00"	0
44°	132°	13180.89	27371.19	44°00'00"	132°00'01"	0.01
48°	135°	12301.25	27552.06	48°00'01"	135°00'03"	0.03
50°	138°	12068.67	27584.22	50°00'01"	138°00'04"	0.05

Table 2. Colocated Slave Stations

Position		Predicted ITD's		HP-41CV Fix		Error n.mi
Lat	Long	9940W	5990Y	Lat(N)	Long(W)	
31°	123°	16413.28	27177.18	31°00'03"	122°59'58"	0.06
37°	126°	15610.11	27403.20	37°00'01"	125°59'59"	0.01
42°	129°	13881.78	27955.45	42°00'00"	129°00'00"	0
44°	132°	13180.89	28512.90	44°00'00"	132°00'00"	0
48°	135°	12301.25	29413.61	48°00'00"	134°59'59"	0.01
50°	138°	12068.67	29816.84	50°00'00"	137°59'59"	0.02

Table 3. Colocated Master and Slave Stations

Position		Predicted ITD's		HP-41CV Fix		Error n.mi
Lat	Long	5930Y	9960W	Lat(N)	Long(W)	
44°	63°	29864.46	11685.15	44°00'00"	63°00'00"	0
41°	66°	30585.61	12946.91	41°00'00"	66°00'00"	0
39°	69°	31020.46	14111.31	39°00'00"	69°00'00"	0
35°	72°	31064.57	15139.48	35°00'00"	72°00'00"	0
30°	75°	31040.82	15610.46	29°59'59"	75°00'01"	0.02
26°	78°	31106.20	15858.46	25°59'57"	78°00'02"	0.05

J. References

1. J. A. Pierce, A. A. McKenzie and R. H. Woodward, editors, LORAN, M.I.T. Radiation Laboratory Series, McGraw-Hill Book Company, Inc., 1948.
2. G. Hefley, The Development of Loran-C Navigation and Timing, National Bureau of Standards Monograph 129, U.S. Department of Commerce, U.S. Government Printing Office, Washington, D.C. 20402, October 1972.
3. R. H. Shudde, "An Algorithm for Position Determination Using Loran-C Triplets with a BASIC Program for the Commodore 2001 Microcomputer", Technical Report NPS55-80-009, March 1980, Naval Postgraduate School, Monterey, CA 93940.
4. General Specifications for Loran-C (20 June 1977) and Loran-C Constants were obtained from the Chief, Navigation Department, Defense Mapping Agency, Hydrographic/Topographic Center, Washington, D.C. 20315.
5. Paul D. Thomas, "Spheroidal Geodesics, Reference Systems, and Local Geometry", PS-138, U.S. Naval Oceanographic Office, Washington, D.C., January 1970.
6. R. H. Shudde, "Position Determination with LORAN-C Triplets and the Hewlett-Packard HP-67/97 Programmable Calculators", Technical Report NPS55-80-010, March 1980, Naval Postgraduate School, Monterey, CA 93940.
7. R. H. Shudde, "Position Determination with LORAN-C Triplets and the Texas Instruments TI-59 Programmable Calculator", Technical Report NPS55-80-020, May 1980, Naval Postgraduate School, Monterey, CA 93940.

Appendix A: Program Storage Allocations, Flag Usage  
and Program Listing

Program Size: 42

Registers:

R00 - R13: Scratch storage

R14: Flattening

<u>2nd Sta. Pair</u>	<u>Variable</u>	<u>1st Sta. Pair</u>
R15:	2a	
R16:	ID	:R26
R17:	$T_B + p(T_B)$	:R27
R18:	2c	:R28
R19:	CD	:R29
R20:	$\theta$ master	:R30
R21:	$\lambda$ master	:R31
R22:	$\alpha$ master-slave	:R32
R23:	$\theta$ slave	:R33
R24:	$\lambda$ slave	:R34
R25:	$\alpha$ slave-master	:R35
	2a	:P36
R37:	$\theta$ fix	
R38:	$\lambda$ fix	
R39:	$\alpha$ fix-dest	
R40:	$\theta$ dest	
R41:	$\lambda$ dest	

Flag Usage:

F00: 1. Requery erroneous ITD at LBL06  
2. Echo two data sets at LBL ED

F01: PR and CA interlock

F03: Set for 2nd solution

F05: Set if slave at vertex of 2nd station pair

F06: Set if slave at vertex of 1st station pair

F07: Set for XMEM functions, clear for tape functions

F08: DN and DH interlock

F09: Set if DMS conversion required

F10: 1. SW and AS interlock  
2. Input interlock in FI vertex check

F14: PR and CA loop control

Q1 • LBL "LON ANC"	DIRECT SOLUTION		
01 • LBL 90	$\theta_1, \lambda_1, \alpha_{12}$ and $S/a_e$ are in		
02 STO 00	the T, Z, Y and X registers		
03 CLX			
04 P-R			
05 STO 01	$\cos \alpha_{12}$		
06 RDN			
07 CHS	$-\sin \alpha_{12}$		
08 STO 02	$\lambda_1$		
09 RDN			
10 STO 03	$\cos \theta_1$		
11 CLX			
12 P-R			
13 STO 04	M		
14 RDN	$\sin \theta_1$		
15 CHS	f		
16 STO 05	$c_1$		
17 CLX			
18 P-R			
19 STO 06	$c_2$		
20 X<>Y			
21 STO 07			
22 X<>Y			
23 RCL 14			
24 * STO 07			
25 P-R			
26 STO 06			
27 X $\uparrow$ 2			
28 -			
29 /			
30 RCL 14			
31 * STO 08			
32 CLX			
33 P-R			
34 STO 08			
35 CHS			
36 -			
37 CHS			





76 STO 13	u	114 RCL 09	N cos Δσ
77 COS		115 +	
78 RCL 10		116 STO 13	
79 *		117 1	
80 ENTER↑		118 P-R	
81 +		119 RCL 11	
82 1		120 *	
83 -		121 X<>Y	
84 CHS	w	122 RCL 05	
85 RCL 13		123 *	
86 RCL 09		124 -	
87 +		125 STO 10	
88 COS		126 X↑2	
89 STO 13	v	127 RCL 06	N cos Δσ - sin θ <sub>1</sub> sin Δσ
90 X↑2		128 X↑2	M <sup>2</sup>
91 ENTER↑		129 +	
92 +		130 SQRT	K
93 1		131 1/X	
94 -	d	132 RCL 13	
95 RCL 09		133 1	
96 1		134 P-R	
97 P-R		135 RCL 05	
98 *		136 *	
99 *	x	137 X<>Y	
100 RCL 08		138 RCL 11	
101 X↑2		139 *	
102 *	v	140 +	
103 X<>Y		141 *	
104 RCL 13		142 ATAN	
105 *	p	143 R-D	
106 RCL 10		144 STO 09	
107 *	d	145 RCL 13	
108 RCL 09		146 SIN	
109 SIN		147 RCL 02	
110 *	y	148 *	
111 ENTER↑		149 RCL 13	
112 +		150 1	
113 -		151 P-R	θ <sub>2</sub>

152 RCL 04	190 R-P	$\Delta\eta$	$\alpha_1, \lambda_2$ and $\theta_2$ are in the Z, Y and X registers
153 * X<>Y	191 CLX 06		REVERSE SOLUTION
155 RCL 05	192 RCL 06		Stack contains $\theta_1, \lambda_1, \theta_2$ and $\lambda_2$ in the T, Z, Y and $\Delta\lambda$ X registers
156 * X<>Y	193 CHS 10		
157 RCL 01	194 RCL 10		
158 *	195 CHS		
159 -	196 R-P		
160 R-P	197 RDN		
161 CLX	198 X<>Y		
162 1	199 RCL 09		
163 RCL 08	200 RTN		
164 -	201 LBL 80		
165 RCL 07	202 X<>Y		
166 * RCL 13	203 RDN		
167 RCL 13	204 -		
168 *	205 CHS		
169 RCL 12	206 STO 00		
170 ENTER↑	207 RDN		
171 + RCL 13	208 -		
172 -	209 LASTX		
173 -	210 X<>Y		
174 COS	211 2		
175 RCL 13	212 /		
176 SIN	213 ENTER↑		
177 * RCL 07	214 ENTER↑		
178 RCL 07	215 1		
179 * RCL 08	216 P-R		
180 RCL 08	217 STO 01		
181 *	218 X12		
182 -	219 RDN		
183 -	220 STO 02		
184 R-D	221 RDN		
185 RCL 03	222 +		
186 +	223 1		
187 DEG	224 P-R		
188 1	225 STO 03		
189 P-R	226 RDN		
	227 STO 04		

$H$	$\Delta\theta_m$	$\cos \Delta\theta_m$	$\sin \Delta\theta_m$	$\cos \theta_m$	$\sin \theta_m$
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$\lambda_2$	
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H	L	d	U	V X
228	X↑2			
229	-			
230	RCL 00			
231	2			
232	/			
233	SIN			
234	X↑2			
235	* RCL 02			
236	RCL 02			
237	X↑2			
238	+ STO 05			
239	STO 05			
240	SQRT			
241	RAD			
242	ASIN			
243	ENTER↑			
244	+ STO 06			
245	STO 06			
246	RCL 04			
247	RCL 01			
248	* ENTER↑			
249	X↑2			
250	ENTER↑			
251	+			
252	1			
253	RCL 05			
254	-			
255	/			
256	STO 07			
257	RCL 02			
258	RCL 03			
259	* X↑2			
260	ENTER↑			
261	+			
262	STO 05			
263	RCL 05			
264	/			
265	ST+ 07			





450 RCL 31 451 - 452 + 453 X=0? 454 RTN 455 SF 05 456 RCL 23 457 RCL 30 458 - 459 RCL 24 460 RCL 31 461 - 462 + 463 X=0? 464 RTN 465 SF 06 466 RCL 23 467 RCL 33 468 - 469 RCL 24 470 RCL 34 471 - 472 + 473 X=0? 474 RTN 475 CF 05 476 RCL 20 477 RCL 33 478 - 479 RCL 21 480 RCL 34 481 - 482 + 483 X=0? 484 RTN 485 TONE 1 486 -E: NO T RIPLET-	Slave 2 and Master 1 Colocated?          Slave 2 and Slave 1 Colocated?          Master 2 and Slave 1 Colocated?          No triplet found	487 AVIEW 488 GT0 50 489 LBL "PR" 490 SF 01 491 GT0 02 492 LBL "CA" 493 CF 01 494 LBL 02 495 FIX 4 496 XEQ 51 497 SF 21 498 SF 14 499 ADV 500 "LAT?" 501 XEQ 99 502 XEQ 14 503 STO 37 504 "LON?" 505 XEQ 99 506 STO 38 507 LBL 66 508 FS? 01 509 GT0 02 510 " " 511 AST0 00 512 BEEP 513 "ITD " 514 ARCL 26 515 ARCL 00 516 XEQ 99 517 STO 39 518 CLX 519 GT0 08 520 LBL 02 521 CLX 522 STO 39 523 LBL 08 524 RCL 37	PREDICT ITD ROUTINE  CALIBRATE ROUTINE CA and PR input routine Flattening Factor Set AVIEW flag Set loop control Input latitude Input longitude Begin loop Transfer if PR input  Input benchmark ITD.  Initialize CA calculation Transfer Initialize PR calculation CA and PR computations
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525 RCL 38 526 RCL 33 527 RCL 34 528 XEQ 00 529 XEQ 03 530 ST- 39 531 RCL 37 532 RCL 38 533 RCL 30 534 RCL 31 535 XEQ 00 536 XEQ 03 537 RCL 39 538 + 539 FS? 01 540 GT0 02 541 RCL 29 542 - 543 ST0 27 544 GT0 08 545 LBL 02 546 CHS 547 RCL 27 548 + 549 RCL 29 550 + 551 " " " 552 AST0 00 553 CLA 554 ARCL 26 555 ARCL 00 556 FIX 2 557 ARCL X 558 BEEP 559 AVIEW 560 LBL 08 561 XEQ -SW- 562 FS?C 14	Load stack.  Reverse solution from Slave. Secondary phase corr.  Load stack.  Reverse solution from Master Secondary phase correction.  Branch for PR  Correct baseline to benchmark  Compute predicted ITD.	563 GT0 66 564 CF 01 565 GT0 50 566 LBL "CS" 567 16.025 568 CF 21 569 "WRITE" " 570 ARCL 16 571 AVIEW 572 XROM 30, 08 573 LBL 50 574 CF 21 575 TONE 6 576 "NEXT OP TION?" 577 AVIEW 578 STOP 579 GT0 50 580 LBL 51 581 DEG 582 298.26 583 1/X 584 ST0 14 585 RTN 586 LBL 44 587 LBL 14 588 TAN 589 1 590 RCL 14 591 - 592 * 593 ATAN 594 RTN 595 LBL 15 596 ADV 597 FIX 0	Loop for second station  Done CARD STORE ROUTINE  Prompt with station ITD  WDATX "NEXT OPTION?"  Query  STORE FLATTENING FACTOR  CONVERT GEOGRAPHIC LATITUDE TO PARAMETRIC LATITUDE  STATION DATA INPUT PROMPTS
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598 SF 21 599 CF 23 600 "ID?" 601 AON 602 PROMPT 603 ASTO X 604 CLA 605 AOFF 606 FC? 23 607 RTN 608 SF 09 609 XEQ 01 610 STO 16 611 -CODE DE LAY? 612 XEQ 00 613 STO 19 614 FIX 6 615 -MS LAT?  616 XEQ 00 617 XEQ 14 618 STO 20 619 -MS LON?  620 XEQ 00 621 STO 21 622 -SS LAT?  623 XEQ 00 624 XEQ 14 625 STO 23 626 -SS LON?  627 XEQ 00 628 STO 24 629 RCL 20 630 RDN	Clear alpha entry flag  Input station ID  Input Coding delay  Input master station latitude.  Convert to Parametric.  Input master station longitude.  Input Slave station latitude.  Convert to parametric.  Input Slave station longitude.	631 XEQ 00 632 STO 18 633 RDN 634 STO 22 635 RDN 636 STO 25 637 RCL 18 638 XEQ 03 639 STO 17 640 RTN 641 LBL 99 642 LBL 00 643 PROMPT 644 LBL 01 645 ARCL X 646 SF 25 647 FS? 55 648 PRA 649 CF 25 650 FC? 09 651 HR 652 RTN 653 LBL 03 654 21282.36 655 * 656 ENTER↑ 657 ENTER↑ 658 537 659 X>Y? 660 GTO 04 661 CLX 662 129 663 X<>Y 664 / 665 LASTX 666 6458 E-7 667 * 668 +	Compute reverse solution to determine baseline and master-slave forward and reverse azimuths.  Add secondary phase correc- tion to baseline.  DATA INPUT PROMPT AND PRINT  Set error ignore flag Print  Clear error ignore flag Convert DMS to DEG if F09 clear.  SECONDARY PHASE CORRECTION $a_e \eta / V_o$  --- T ≥ 537 μS
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743 STO 15 744 LBL 18 745 FS? 10 746 GT0 "FI" 747 XEQ 51 748 RAD 749 RCL 15 750 1 751 P-R 752 X<>Y 753 FS? 05 754 CHS 755 STO 01 756 CLX 757 RCL 18 758 1 759 P-R 760 X<>Y 761 STO 03 762 RDN 763 - 764 STO 02 765 RCL 36 766 1 767 P-R 768 X<>Y 769 FS? 06 770 CHS 771 STO 04 772 CLX 773 RCL 28 774 1 775 P-R 776 X<>Y 777 STO 06 778 RDN 779 - 780 STO 05	Store 2a2 ALTERNATE SOLUTION entry. Input ITD's if vertex interlock set. Regenerate flattening  Station 2 vertex flag A2  C2  B2  Station 1 vertex flag A1  C1  B1	781 RCL 01 782 * 783 RCL 02 784 RCL 04 785 * 786 - 787 STO 07 788 DEG 789 RCL 22 790 FS? 05 791 RCL 25 792 STO 11 793 RCL 05 794 RCL 03 795 * 796 P-R 797 STO 08 798 RDN 799 STO 09 800 RCL 32 801 FS? 06 802 RCL 35 803 RCL 02 804 RCL 06 805 * 806 P-R 807 RCL 08 808 - 809 X<>Y 810 RCL 09 811 - 812 X<>Y 813 R-P 814 RCL 07 815 X<>Y 816 / 817 ACOS 818 FS? 03	K  Station 2 vertex flag  B1C2 cos $\xi_2$ B1C2 sin $\xi_2$ Station 1 vertex flag  C  S  $\rho$ and $\gamma$  $\cos^{-1}(K/\rho)$ Alternate solution?
---	--	---	--

819 CHS 820 + 821 STO 10 822 RCL 11 823 - 824 COS 825 RCL 03 826 * 827 RCL 01 828 + 829 RCL 02 830 X<>Y 831 R-P 832 RDN 833 D-R 834 STO 12 835 RCL 20 836 RCL 21 837 FC? 05 838 GT0 09 839 RCL 23 840 RCL 24 841 LBL 09 842 RCL 10 843 RCL 12 844 XEQ 90 845 STO 37 846 FIX 4 847 XEQ 19 848 SF 21 849 -LAT: - 850 ARCL X 851 BEEP 852 AVIEW 853 RDN 854 STO 38 855 XEQ 20 856 -LON: -	$\alpha = \gamma + \cos^{-1} (K/\rho)$  $C_2 \cos(\alpha - \xi_2) + A_2$  r  Station 2 vertex flag  -----  Compute direct solution $\theta_{fix}$ $\theta_{fix}$ Display latitude  $\lambda_{fix}$	857 ARCL X 858 AVIEW 859 GT0 50 860 LBL 19 861 TAN 862 1 863 RCL 14 864 - 865 / 866 ATAN 867 LBL 20 868 HMS 869 RND 870 0 871 HMS+ 872 RTN 873 LBL "DH" 874 SF 21 875 ADV 876 XEQ 51 877 -ORIG LA T? " 878 XEQ 99 879 XEQ 44 880 STO 37 881 -ORIG L0 N? " 882 XEQ 99 883 STO 38 884 SF 08 885 LBL "DN" 886 SF 21 887 FC? 08 888 ADV 889 XEQ 51 890 -DEST LA T? " 891 XEQ 99	Display longitude  CONVERT PARAMETRIC LATITUDE TO GEOGRAPHIC LATITUDE  DMS ROUNDING ROUTINE  DISTANCE AND HEADING Any origin to any destination Input origin latitude Convert to parametric Input origin longitude  Set F08 to compute STORE DESTINATION  Input destination latitude
---	---	--	---

892 XEQ 44 893 STO 40 894 -DEST LO N? " 895 XEQ 99 896 STO 41 897 FC?C 08 898 GT0 50 899*LBL "HD" 900 RCL 37 901 RCL 38 902 RCL 40 903 RCL 41 904 XEQ 80 905 3443.917 906 * 907 BEEP 908 SF 21 909 "N.MI: " 910 FIX 2 911 ARCL X 912 AVIEW 913 RDN 914 FIX 4 915 360 916 MOD 917 STO 39 918 XEQ 20 919 "BRG: " 920 ARCL X 921 AVIEW 922 GT0 50 923*LBL "AS" 924 FS?C 03 925 GT0 18 926 SF 03 927 GT0 18	Convert to parametric Input destination longitude Return if F08 not set to compute. <u>COMPUTE DISTANCE AND</u> HEADING Compute reverse solution Convert distance to n. mi. Display distance 0° ≤ bearing < 360° Round DMS Display bearing <u>COMPUTE ALTERNATE</u> SOLUTION Toggle F03	928*LBL "ED" 929 SF 00 930 XEQ "SM" 931 XEQ 13 932 XEQ "SM" 933 XEQ 13 934*LBL "CE" 935 CF 21 936 16.025 937 -STA. CA RD" 938 AVIEW 939 XROM 30, 03 940*LBL 13 941 FIX 0 942 XEQ 51 943 SF 21 944 ADV 945 "ID: " 946 ARCL 16 947 AVIEW 948 "CD: " 949 ARCL 19 950 AVIEW 951 "MLT: " 952 RCL 20 953 FIX 6 954 XEQ 19 955 ARCL X 956 AVIEW 957 "MLN: " 958 RCL 21 959 XEQ 20 960 ARCL X 961 AVIEW 962 -SLT: " 963 RCL 23	ECHO DATA ROUTINE  CARD ECHO ROUTINE  RDTAX Data review of R16-R25 Regenerate flattening Display station ID Display coding delay Display master station latitude Display master station longitude
---	--	---	---

964 XEQ 19 965 ARCL X 966 AVIEW " 967 "SLN: " 968 RCL 24 969 XEQ 20 970 ARCL X 971 AVIEW 972 FIX 3 973 "BL: " 974 ARCL 17 975 AVIEW 976 FS?C 00 977 RTN 978 GTO 50 979 LBL "SW" 980 SF 10 981 35.025 982 STO 01 983 25 984 STO 02 985 LBL 12 986 RCL IND 02 987 X<> IND 01 988 STO IND 02 989 DSE 02 990 " 991 DSE 01 992 GTO 12 993 RTN 994 LBL "XR" 995 SF 07 996 GTO 02 997 LBL "TR" 998 CF 07	Display slave station latitude  Display slave station longitude  Display base line in microseconds  SWAP STATION DATA Swaps R16-R25 with R26-R35  Begin loop  Loop to LBL 12  XMEM RECALL  TAPE RECALL	994 LBL 02 1000 XEQ "SW" " 1001 XEQ 60 1002 HSTO 16 1003 XEQ 08 1004 FS? 07 1005 XROM 25 ,21 1006 FC? 07 1007 XROM 28 ,09 1008 GTO 50 1009 LBL "XS" " 1010 SF 07 1011 GTO 02 1012 LBL "TS" " 1013 CF 07 1014 LBL 02 1015 CLA 1016 ARCL 16 1017 9 1018 FS? 07 1019 XROM 25 ,11 1020 FC? 07 1021 XROM 28 ,01 1022 XEQ 08 1023 FS? 07 1024 XROM 25 ,40 1025 FC? 07 1026 XROM 28 ,22 1027 GTO 50	Swap data  ID Prompt Store ID Set pointer  GETRX - Input from XMEM  READRX - Input from tape  XMEM STORE  TAPE STORE -----  Recall ID  CRFLD - XMEM create  CREATE - Tape create  Set pointer & register range SAVERX-Save in XMEM  WRTRX - Save on tape
--	---	---	---

1028*LBL "XD 1029 SF 07 1030 GIO 02 1031*LBL "ID 1032 CF 07 1033*LBL 02 1034 XEQ 60 1035 FS? 07 1036 XROM 25 ,31 1037 FC? 07 1038 XROM 28 ,04 1039 GIO 50 1040*LBL 60 1041 CF 21 1042 "ID? 1043 AON 1044 PROMPT 1045 AOFF 1046 RTN 1047*LBL 08 1048 0 1049 FS? 07 1050 XROM 25 ,43 1051 FC? 07 1052 XROM 28 ,14 1053 17.025 1054 .END.	<p>XMEM DELETE</p> <hr/> <p>TAPE DELETE</p> <hr/> <hr/> <p>PURFL - Purge from XMEM</p> <p>PURGE - Purge from tape</p> <hr/> <p>ID INPUT PROMPT</p> <hr/> <p>SET POINTER</p> <p>SEEKPT - Set XMEM pointer to zero</p> <p>SEEKR - Set tape pointer to zero</p> <p>R17-R25 to be transmitted.</p>
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Appendix B: STATION COVERAGE

<u>Station</u>	<u>No. of Pairs</u>	<u>Location</u>
4990	2	Central Pacific
5930	2	East Coast, Canada
5990	3	West Coast, Canada
7930	3	North Atlantic
7960	2	Gulf of Alaska
7970	4	Norwegian Sea
7980	4	Southeast U.S.A.
7990	3	Mediterranean Sea
8970	3	Great Lakes
9940	3	West coast, U.S.A.
9960	4	Northeast U.S.A.
9970	4	Northwest Pacific
9990	3	North Pacific



### Appendix C: LORAN-C STATION DATA

The following list contains the pertinent parameters for each Loran-C station pair. This list was compiled from the data in Reference 4. Each column contains the following information:

1. The Loran-C station pair designator.
2. The coding delay.
3. The master station latitude.
4. The master station longitude.
5. The slave station latitude.
6. The slave station longitude.

In this list, positive longitudes are West, negative longitudes are East, positive latitudes are North and negative latitudes are South. In columns 3 through 6 the latitudes and longitudes appear to be in decimal form, but the actual format is DDD.MMSSFF (which is compatible with the HP-41CV D.MS or H.MS input mode) where

DDD designates degrees,  
MM designates minutes,  
SS designates seconds, and  
FF designates hundredths of seconds.

ID	CD	MS	AL	SS LAT	SS LON
4990X	11000	16.44400	169.130120	20.144916	155.530970
4990Y	29000	16.44400	169.133120	28.234177	178.173020
5930X	11000	46.463218	067.553771	41.151193	069.583909
5930Y	25000	46.463218	067.553771	46.463218	053.102816
5990X	11000	51.575875	122.220224	55.262085	131.151965
5990Y	27000	51.575875	122.220224	47.034799	119.443953
5990Z	41000	51.575875	122.220224	50.362972	127.212935
7930W	11000	64.542658	045.102747	64.542658	023.552175
7930X	21000	64.542658	045.102747	62.175968	007.042671
7930Z	43000	64.542658	045.102747	46.463218	053.102816
7960X	11000	65.262021	131.151965	57.262021	152.221122
7960Y	26000	65.262021	131.151965	55.262085	131.151965
7970W	36000	68.173020	187.042658	54.462980	-008.173633
7970X	11000	68.173020	187.042658	58.380615	-014.274700
7970Y	46000	68.173020	187.042658	64.542658	+023.552175
7970Z	60000	68.173020	187.042658	70.545261	+008.435869
7980W	11000	80.100930	005.100930	30.433302	090.494360
7980X	23000	80.100930	005.100930	25.315501	097.500009
7980Y	43000	80.100930	005.100930	27.015849	080.065352
7980Z	59000	80.100930	005.100930	34.034604	077.544676
7990X	11000	88.522095	-016.430596	35.312088	-012.312996
7990Y	29000	88.522095	-016.430596	40.582095	-027.520152
7990Z	47000	88.522095	-016.430596	42.033649	-003.121590
8970W	11000	89.510754	087.291214	30.593874	085.100930
8970X	28000	89.510754	087.291214	42.425060	076.493386
8970Y	44000	89.510754	087.291214	48.364984	094.331847
9940W	11000	39.334862	118.495637	47.034799	119.443953
9940X	27000	39.334862	118.495637	38.465699	122.294453
9940Y	40000	39.334862	118.495637	35.191818	114.481743
9960W	11000	42.425060	076.493386	46.482720	067.553771
9960X	25000	42.425060	076.493386	41.151193	069.583909
9960Y	39000	42.425060	076.493386	34.034604	077.544676
9960Z	54000	42.425060	076.493386	39.510754	087.291214
9970W	11000	24.480000	-141.192900	24.170777	-153.58515
9970X	30000	24.480000	-141.192900	12.443700	-143.430906
9970Y	55000	24.480000	-141.192900	26.362499	-128.085621
9970Z	75000	24.480000	-141.192900	09.324566	-138.095523
9990X	11000	57.090988	+170.145981	52.494505	-173.105231
9990Y	29000	57.090988	+170.145981	65.141012	+166.531447
9990Z	43000	57.090988	+170.145981	57.262021	+152.221122

EAST AND SOUTH ARE MINUS '-'

Appendix D: COLOCATED STATIONS

5930 MASTER	- 9960W
5930X	- 9960X
5930Y	- 7930Z
5990X	- 7960Y
5990Y	- 9940W
7930W	- 7970Y
7930X	- 7970 MASTER
7960X	- 9990Z
7980Z	- 9960Y
7980 MASTER	- 8970W
8970X	- 9960 MASTER
8970 MASTER	- 9960Z

Slave stations are denoted with a letter  
suffix. Master stations are so designated.

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