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All Submissions

Chef and Horcrux

Problem Code: XORTREEH

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russian **Successful Submissions**

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and <u>vietnamese</u>

(http://www.codechef.com/download/translated/OCT17/vietnamese/XORTREEH.pdf) as well.

Once again Harry is out there with his friends Ron and Hermione looking out for Horcruxes. They found out that one of the Horcrux is located at The Lestrange Vault. But You-Know-Who has locked the vault with a dark spell.

Fortunately, the password to the vault can be found out by solving a problem. But they were not able to solve the problem and hence need help from Chef. Since Chef is quite busy, he has delegated this task to you.

You are given an array of **N** elements. **MEX**

(https://en.wikipedia.org/wiki/Mex_(mathematics)) of a set is defined as the minimum non-negative integer that doesn't exist in it. For example, the MEX of the set {0, 2, 4} is 1 and the MEX of the set $\{1, 2, 3\}$ is 0. Note that the MEX of empty set will be 0.

Similar to Expected value (https://en.wikipedia.org/wiki/Expected_value), let's define Cheftated value, C[Y] of a random variable Y as follows:

$$C[Y] = \sum_{i=1}^{a} y_i^{2y_i} * p_i^{3y_i}$$

where Y is a random variable with a finite number of outcomes $y_1,\,y_2,\,....$, y_a occurring with probabilities p_1, p_2, \dots, p_a . Take $0^0 = 1$.

You are given an array **A** consisting of **N** non-negative integers. Your task is to calculate the cheftated value of base **K** xor sum of MEX values of **X** randomly selected subsequences(repetitions allowed) of A.

Cheftated value can always be represented as an irreducible fraction **P/Q** such that gcd(Q, 330301441) = 1, i.e. Q^{-1} (multiplicative inverse

(https://en.wikipedia.org/wiki/Modular_multiplicative_inverse)) modulo 330301441 exists.

You have to print the value P * Q-1 modulo 330301441. Please see the sample explanation for more details.

Also, xor-sum in base **K** (xor_k) can be performed by representing the numbers in base **K** and adding each digit in base K

(https://en.wikipedia.org/wiki/Addition#Addition_in_other_bases)(without carrying

forward), e.g. xorsum of 6 and 9 in base 5 is equal to $11_5 \times 07_5 \times 14_5 = 20_5$, i.e. the number 10.

Input

First line of the input contains an integer **T** denoting number of test cases.

First line of each test case contains three space separated integers N, K and X.

Second line of each test case contains N space separated integers, i-th of which is A_i denoting the ith element of the array.

Output

For each test case, output a line containing single integer representing the value of **P*Q**⁻¹ modulo **330301441**.

Constraints

- 1 ≤ T ≤ 5
- $\bullet \quad 1 \le N \le 10^5$
- 2 ≤ K ≤ 10
- $2 \le X \le 10^{18}$
- $\bullet \quad 0 \le A_i \le 10^5$

Subtasks

• **Subtask #1** (15 points) : **K** ≤ 3

• **Subtask #2** (15 points) : $N \le 10^3$

• **Subtask #3** (70 points) : Original constraints

Example

```
Input:
2
3 2 2
1 0 2
4 4 4
4 0 1 1

Output:
87392358
88861416
```

Explanation

Example case 1: Let's name the sub-sequences as A = [], B = [1], C = [0], D = [2], E = [1, 0], F = [1, 2], G = [0, 2], H = [1, 0, 2].

Possible outcome of xor values after selecting two sub-sequences (repetitions allowed):

- 0 when you select (two from (A, B, D, F)) or (two from (C, G)) or (two from (E)) or (two from (H)) making it 22 ways.
- 1 when you select (one from (A, B, D, F) and one from (C, G)) or (one from (E) and one from (H)) making it 18 ways.
- 2 when you select (one from (A, B, D, F) and one from (E)) or (one from (H) and one from (C, G)) making it 12 ways.
- 3 when you select (one from (A, B, D, F) and one from (H)) or (one from (E) and one from (C, G)) making it 12 ways.

Cheftated value = $0^{2*0} * (22/64)^{3*0} + 1^{2*1} * (18/64)^{3*1} + 2^{2*2} * (12/64)^{3*2} + 3^{2*3} * (12/64)^{3*3} = 70310425195/68719476736.$

Answer to print = $70310425195 * 68719476736^{-1} \mod 330301441 = 87392358$

Author: 7★ adkroxx (/users/adkroxx)

Tester: 7★ alex 2008 (/users/alex 2008)

Date Added: 23-08-2017

Time Limit: 5 secs

Source Limit: 50000 Bytes

Languages: ADA, ASM, BASH, BF, C, C99 strict, CAML, CLOJ, CLPS, CPP

4.3.2, CPP 6.3, CPP14, CS2, D, ERL, FORT, FS, GO, HASK, ICK, ICON, JAVA, JS, LISP clisp, LISP sbcl, LUA, NEM, NICE, NODEJS, PAS fpc, PAS gpc, PERL, PERL6, PHP, PIKE, PRLG, PYPY, PYTH, PYTH 3.5, RUBY, SCALA, SCM chicken, SCM guile, SCM gobi, ST,

TCL, TEXT, WSPC

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CodeChef was created as a platform to help programmers make it big in the world of algorithms, **computer programming** and **programming contests**. At CodeChef we work hard to revive the geek in you by hosting a **programming contest** at the start of the month and another smaller programming challenge in the middle of the month. We also aim to have training sessions and discussions related to **algorithms**, **binary search**, technicalities like **array size** and the likes. Apart from providing a platform for **programming competitions**, CodeChef also has various algorithm tutorials and forum discussions to help those who are new to the world of **computer programming**.

Practice Section (https://www.codechef.com/problems/easy) - A Place to hone your 'Computer Programming Skills'

Try your hand at one of our many practice problems and submit your solution in a language of your choice. Our **programming contest** judge accepts solutions in over 35+ programming languages. Preparing for coding contests were never this much fun! Receive points, and move up through the CodeChef ranks. Use our practice section to better prepare yourself for the multiple **programming challenges** that take place through-out the month on CodeChef.

Compete (https://www.codechef.com/problems/easy) - Monthly Programming Contests and Cook-offs

Here is where you can show off your **computer programming skills**. Take part in our 10 day long monthly coding contest and the shorter format Cook-off **coding contest**. Put yourself up for recognition and win great prizes. Our **programming contests** have prizes worth up to INR 20,000 (for Indian Community), \$700 (for Global Community) and lots more CodeChef goodies up for grabs.

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<u>Contest Hosting (http://www.codechef.com/hostyourcontest)</u>

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Peer (https://www.codechef.com/problems/extcontest)

School (https://www.codechef.com/problems/school)

FAQ's (https://www.codechef.com/wiki/faq)

<u>Initiatives</u>

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<u>Campus Chapters (http://www.codechef.com/campus_chapter/about)</u>

<u>Domain Registration in India (http://www.bigrock.in/)</u> and <u>Web Hosting (http://www.bigrock.com/web-hosting/)</u> powered by BigRock