

The right hand side of the equation:

$$\begin{aligned}
& \cosh(b_{\mathcal{V}_1} + W_{\mathcal{V}_{15}} \sigma_5^z + W_{\mathcal{V}_{16}} \sigma_6^z + W_{\mathcal{V}_{16}} \sigma_{16}^z - W_{\mathcal{V}_{11}} \sigma_1^z) \cosh(b_{\mathcal{V}_2} + W_{\mathcal{V}_{27}} \sigma_7^z + W_{\mathcal{V}_{28}} \sigma_8^z + W_{\mathcal{V}_{29}} \sigma_9^z - W_{\mathcal{V}_{22}} \sigma_2^z) \times \\
& \cosh(b_{\mathcal{V}_3} + W_{\mathcal{V}_{310}} \sigma_{10}^z + W_{\mathcal{V}_{311}} \sigma_{11}^z + W_{\mathcal{V}_{312}} \sigma_{12}^z - W_{\mathcal{V}_{33}} \sigma_3^z) \cosh(b_{\mathcal{V}_4} + W_{\mathcal{V}_{413}} \sigma_{13}^z + W_{\mathcal{V}_{414}} \sigma_{14}^z + W_{\mathcal{V}_{415}} \sigma_{15}^z - W_{\mathcal{V}_{44}} \sigma_4^z) \times \\
& \cosh(b_{\mathcal{V}} - W_{\mathcal{V}_1} \sigma_1^z - W_{\mathcal{V}_2} \sigma_2^z - W_{\mathcal{V}_3} \sigma_3^z - W_{\mathcal{V}_4} \sigma_4^z) \cosh\left[i\frac{\pi}{4}(\sigma_{15}^z + \sigma_{16}^z - \sigma_1^z - \sigma_4^z)\right] \times \\
& \cosh\left[i\frac{\pi}{4}(\sigma_7^z + \sigma_8^z - \sigma_1^z - \sigma_2^z)\right] \cosh\left[i\frac{\pi}{4}(\sigma_9^z + \sigma_{10}^z - \sigma_2^z - \sigma_3^z)\right] \cosh\left[i\frac{\pi}{4}(\sigma_{12}^z + \sigma_{13}^z - \sigma_3^z - \sigma_4^z)\right].
\end{aligned} \tag{1}$$

The left hand side of the equation:

$$\begin{aligned}
& \cosh(b_{\mathcal{V}} + W_{\mathcal{V}_1} \sigma_1^z + W_{\mathcal{V}_2} \sigma_2^z + W_{\mathcal{V}_3} \sigma_3^z + W_{\mathcal{V}_4} \sigma_4^z) \cosh(b_{\mathcal{V}_1} + W_{\mathcal{V}_{15}} \sigma_5^z + W_{\mathcal{V}_{16}} \sigma_6^z + W_{\mathcal{V}_{16}} \sigma_{16}^z + W_{\mathcal{V}_{11}} \sigma_1^z) \times \\
& \cosh(b_{\mathcal{V}_2} + W_{\mathcal{V}_{27}} \sigma_7^z + W_{\mathcal{V}_{28}} \sigma_8^z + W_{\mathcal{V}_{29}} \sigma_9^z + W_{\mathcal{V}_{22}} \sigma_2^z) \cosh(b_{\mathcal{V}_3} + W_{\mathcal{V}_{310}} \sigma_{10}^z + W_{\mathcal{V}_{311}} \sigma_{11}^z + W_{\mathcal{V}_{312}} \sigma_{12}^z + W_{\mathcal{V}_{33}} \sigma_3^z) \times \\
& \cosh(b_{\mathcal{V}_4} + W_{\mathcal{V}_{413}} \sigma_{13}^z + W_{\mathcal{V}_{414}} \sigma_{14}^z + W_{\mathcal{V}_{415}} \sigma_{15}^z + W_{\mathcal{V}_{44}} \sigma_4^z) \cosh\left[i\frac{\pi}{4}(\sigma_{15}^z + \sigma_{16}^z + \sigma_1^z + \sigma_4^z)\right] \times \\
& \cosh\left[i\frac{\pi}{4}(\sigma_7^z + \sigma_8^z + \sigma_1^z + \sigma_2^z)\right] \cosh\left[i\frac{\pi}{4}(\sigma_9^z + \sigma_{10}^z + \sigma_2^z + \sigma_3^z)\right] \cosh\left[i\frac{\pi}{4}(\sigma_{12}^z + \sigma_{13}^z + \sigma_3^z + \sigma_4^z)\right].
\end{aligned} \tag{2}$$

$$\sigma_i = \pm 1, \quad i = 1, \dots, 16.$$

The parameters : $b_{\mathcal{V}_\mu}, W_{\mathcal{V}_\mu i}, b'_{\mathcal{V}_\mu}, W'_{\mathcal{V}_\mu i}; \quad \text{for } \mu = 1, \dots, 4.$