Department of Operational Research
University of Delhi

Final Practical File

Submitted By
Om Gupta
DUPG00**32347**
Section - A
North Deparment
Master of Operational Research

Submitted To
Dr. Gurjeet Kaur
Department of Operational Research

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1 Practical Questions

1.1 WAP to compute the roots of a quadratic equation.

[21]:
```
a = float(input("Enter the coefficient of x\N{SUPERSCRIPT TWO}: "))
if a==0:
    print("Not a quadratic equation.\nThe coefficient of x\N{SUPERSCRIPT TWO},␣
 ↪needs to be non-zero.")
else:
    b = float(input("Enter the coefficient of x: "))
    c = float(input("Enter the constant term: "))
    # Formatting the equation for maximum readability.
    print(f"Given equation is:\n{a}x\N{SUPERSCRIPT TWO}{"" if b==0 else str(" +␣
 ↪" if b>0 else " - ")+str(abs(b))+"x "}{"" if c==0 else str("+ " if c>0 else␣
 ↪"- ")+str(abs(c))}")
    from math import sqrt
    # Discriminant
    d = b*b-4*a*c
    if d>0:
        d = sqrt(d)
        root1 = (-b+d)/(2*a)
        root2 = (-b-d)/(2*a)
        print(f"Roots are x = {root1:2.2f}, {root2:2.2f}")
    elif d == 0:
        d = sqrt(d)
        root1 = (-b+d)/(2*a)
        print(f"Root is x = {root1:2.2f}")
    else:
        print(f"Since, discriminant ({d}) < 0\nTherefore, no real roots exist.")
```

```
Given equation is:
1.0x² + 2.0x + 1.0
Root is x = -1.00
```

1.2 WAP to play Stone, Paper, Scissors with Computer.

[22]:
```
u = int(input(f"1. Stone\n2. Paper\n3. Scissors\nEnter your choice (1/2/3): "))
if u>3 or u<1:
    print("Incorrect Choice. Please choose from 1/2/3.")
else:
    from random import randint
    c = randint(1,3)
    l = ['Stone', 'Paper', 'Scissors']
    print(f"You Picked -> {l[u-1]}\nComputer Picked -> {l[c-1]}")
    print("\nResult -> ",end="")
    if u==c:
        print("Draw")
    elif (u==1 and c==3) or (u==2 and c==1) or (u==3 and c==2):
```

```
        print("You Won!")
    else:
        print("Computer Won!")
```

```
You Picked -> Paper
Computer Picked -> Stone

Result -> You Won!
```

1.3 Write a program for BMI Calculator with Categorization of underweight, normal weight and overweight.

BMI Categories
Underweight: $BMI < 18.5$
Normal weight: $18.5 <= BMI < 24.9$
Overweight: $25 <= BMI < 29.9$
Obesity: $BMI >= 30$

[23]:
```
# Input: weight (kg) and height (m)
weight = float(input("Enter your weight in kg: "))
height = float(input("Enter your height in meters: "))

print(f"Weight: {weight}kg")
print(f"Height: {height}m")
bmi = weight / (height ** 2)

print(f"Your BMI is: {bmi:.2f}")

# Categorization
if bmi < 18.5:
    print("You are underweight.")
elif 18.5 <= bmi < 24.9:
    print("You have a normal weight.")
elif 25 <= bmi < 29.9:
    print("You are overweight.")
else:
    print("You are obese.")
```

```
Weight: 70.0kg
Height: 169.5m
Your BMI is: 0.00
You are underweight.
```

1.4 WAP to demonstrate exception handling of Zero Division Error.

[24]:
```
a = int(input("Enter Dividend: "))
b = int(input("Enter a Divisor: "))
```

```
try:
    c = a/b
    print(f"{a}/{b} = {c}")
except ZeroDivisionError as e:
    print("Division by 0 is not possible.")
```

```
Division by 0 is not possible.
```

1.5 WAP to demonstrate OOPs using user defined Cuboid Class.

[25]:
```
class Cuboid:
    def __init__(self, l, b, h):
        self.ln = l
        self.br = b
        self.hi = h
    def peri(self):
        """Compute perimeter of the cuboid."""
        return 4*(self.ln+self.br+self.hi)
    def vol(self):
        """Compute volume of the cuboid."""
        return self.ln*self.br*self.hi
c1 = Cuboid(1,2,3)
perimeter = c1.peri()
volume = c1.vol()
print(f'Perimeter is {perimeter}')
print(f'Volume is {volume}')
```

```
Perimeter is 24
Volume is 6
```

1.6 WAP to demonstrate inheritance in OOPs using user defined Rectangle and Cuboid Class.

[26]:
```
class Rectangle:
    def __init__(self, l, b):
        self.ln = l
        self.br = b
    def peri(self):
        """Compute perimeter of the rectangle."""
        return 2*(self.ln+self.br)
    def area(self):
        """Compute area of the rectangle."""
        return self.ln*self.br

class Cuboid(Rectangle):
    def __init__(self, l, b, h):
        super().__init__(l, b)
        self.hi = h
```

```
    def vol(self):
        """Compute volume of the cuboid."""
        return self.area()*self.hi
    def peri(self):
        """Compute perimeter of the cuboid."""
        return 4*(self.ln+self.br+self.hi)

c2 = Cuboid(3,2,3)
perimeter = c2.peri()
volume = c2.vol()
print(f'Perimeter is {perimeter}')
print(f'Volume is {volume}')
```

```
Perimeter is 32
Volume is 18
```

1.7 Write a Program to implement Inheritance. Create a class Employee inherit two classes Manager and Clerk from Employee.

[27]:
```
class Employee:
    def __init__(self, empid, name, age, salary):
        self.empid = empid
        self.name = name
        self.age = age
        self.salary = salary

    def display_info(self):
        print(f"Employee ID: {self.empid}")
        print(f"Name: {self.name}")
        print(f"Age: {self.age}")
        print(f"Salary: {self.salary}")

class Manager(Employee):
    def __init__(self, empid, name, age, salary, department):
        super().__init__(empid, name, age, salary)
        self.department = department

    def display_manager_info(self):
        self.display_info()
        print(f"Department: {self.department}")
        print("Position: Manager")

class Clerk(Employee):
    def __init__(self, empid, name, age, salary, experience):
        super().__init__(empid, name, age, salary)
        self.experience = experience
```

```
    def display_clerk_info(self):
        self.display_info()
        print(f"Experience: {self.experience} years")
        print("Position: Clerk")

manager = Manager(32347 ,"Rahul", 45, 120000, "HR")
clerk = Clerk(12345, "Ashish", 30, 40000, 5)

print("Manager Details:")
manager.display_manager_info()

print("\nClerk Details:")
clerk.display_clerk_info()
```

```
Manager Details:
Employee ID: 32347
Name: Rahul
Age: 45
Salary: 120000
Department: HR
Position: Manager

Clerk Details:
Employee ID: 12345
Name: Ashish
Age: 30
Salary: 40000
Experience: 5 years
Position: Clerk
```

1.8 WAP to demonstrate the demarcation of class variable and instance variable in OOP using Employee Class.

[28]:
```
class Employee:
    # Class variable: shared by all instances
    company_name = "Bajaj Tech"
    emp_count = 0

    def __init__(self, name, age, salary):
        # Instance variables: unique to each instance
        self.name = name
        self.age = age
        self.salary = salary
        Employee.emp_count += 1 # Accessing class variable

    def display_info(self):
        """Display information of the Employee."""
```

```
        print(f"Employee Name: {self.name}")
        print(f"Employee Age: {self.age}")
        print(f"Employee Salary: {self.salary}")
        print(f"Company: {Employee.company_name}")  # Accessing class variable


emp1 = Employee("Rahul", 45, 120000)
emp2 = Employee("Ashish", 30, 40000)

print("Employee 1 Details:")
emp1.display_info()

print("\nEmployee 2 Details:")
emp2.display_info()

# Accessing the class variable directly from the class
print(f"\nNumber of Employees (Accessed via Class): {Employee.emp_count}")

# Modifying the class variable
Employee.company_name = "New Bajaj Tech"

# Display information again after modifying the class variable
print("\nAfter changing the company name for all employees:\n")

print("Employee 1 Details:")
emp1.display_info()

print("\nEmployee 2 Details:")
emp2.display_info()
```

```
Employee 1 Details:
Employee Name: Rahul
Employee Age: 45
Employee Salary: 120000
Company: Bajaj Tech

Employee 2 Details:
Employee Name: Ashish
Employee Age: 30
Employee Salary: 40000
Company: Bajaj Tech

Number of Employees (Accessed via Class): 2

After changing the company name for all employees:

Employee 1 Details:
Employee Name: Rahul
```

```
Employee Age: 45
Employee Salary: 120000
Company: New Bajaj Tech

Employee 2 Details:
Employee Name: Ashish
Employee Age: 30
Employee Salary: 40000
Company: New Bajaj Tech
```

1.9 Write a Program to determine EOQ using various inventory models.

[29]:
```python
from abc import ABC, abstractmethod
from math import sqrt
class DetModels(ABC):
    @abstractmethod
    def get_quantity():
        pass
    @abstractmethod
    def get_total_cost():
        pass
    def get_cycle_time(self, Q, lam):
        return Q/lam

class EOQ(DetModels):
    def get_quantity(self, A, lam, I, C):
        return int(sqrt((2*A*lam)/(I*C)))
    def get_total_cost(self, A, lam, I, C, Q):
        holding_cost = (I * C * (Q / 2))
        ordering_cost = A * (lam / Q)
        total_cost = holding_cost + ordering_cost
        return total_cost

class EPQ(DetModels):
    def get_quantity(self, A, lam, I, C, si):
        return int(sqrt((2*A*lam*si)/(I*C*(si-lam))))
    def get_total_cost(self, A, lam, I, C, Q, si):
        holding_cost = (I * C * Q * (si - lam)) / (2 * si)
        setup_cost = A * (lam / Q)
        total_cost = holding_cost + setup_cost
        return total_cost

class EOQ_Short(DetModels):
    def get_quantity(self, A, lam, I, C, pi):
        return int(sqrt((2*A*lam*(pi + I*C))/(I*C*pi)))
    def get_total_cost(self, A, lam, I, C, Q, pi):
        Q_r = Q * (I * C) / (pi + I * C)
```

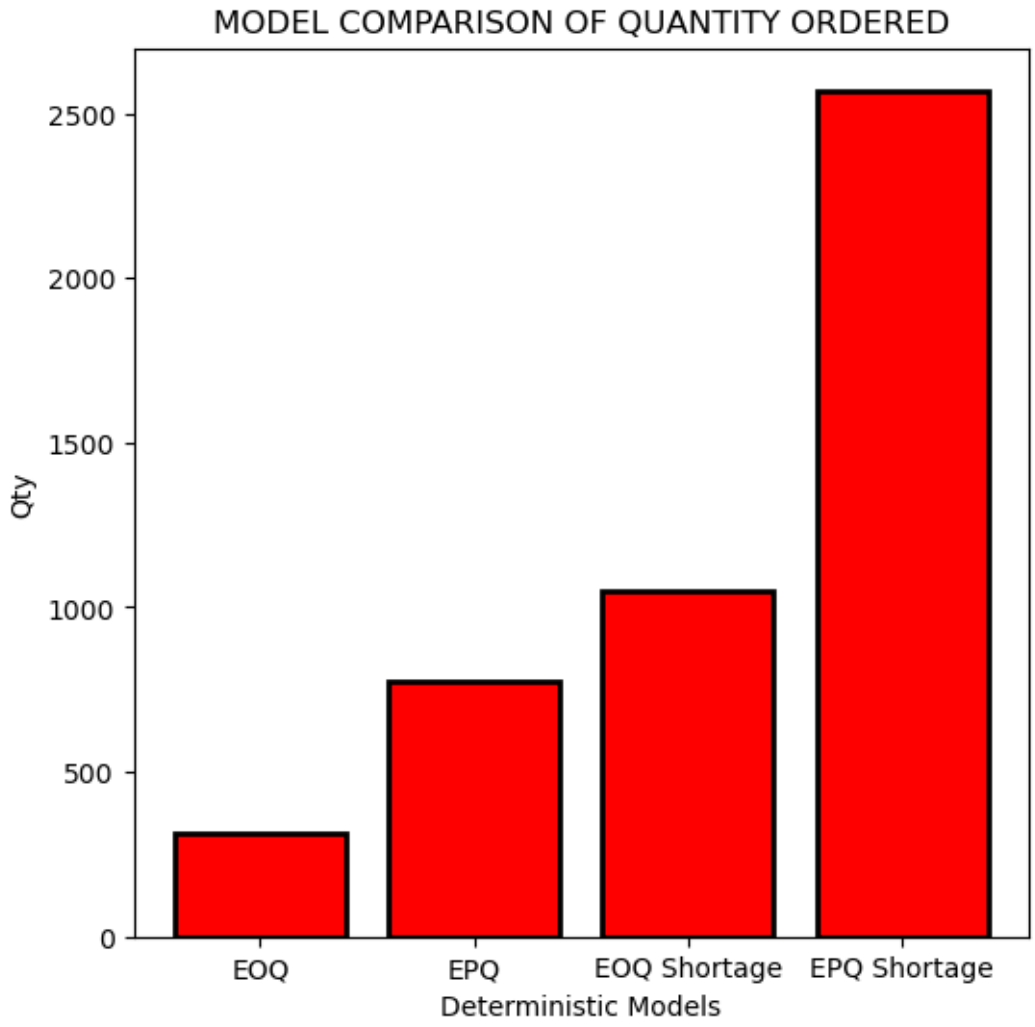
```
        holding_cost = I * C * (Q / 2)
        ordering_cost = A * (lam / Q)
        shortage_cost = pi * (Q - Q_r) / 2
        total_cost = holding_cost + ordering_cost + shortage_cost
        return total_cost

class EPQ_Short(DetModels):
    def get_quantity(self, A, lam, I, C, si, pi):
        return int(sqrt((2*A*lam*(pi + I*C)*si)/(I*C*pi*(si-lam))))
    def get_total_cost(self, A, lam, I, C, Q, si, pi):
        Q_r = Q * (I * C) / (pi + I * C)
        holding_cost = (I * C * Q * (si - lam)) / (2 * si)
        setup_cost = A * (lam / Q)
        shortage_cost = pi * (Q - Q_r) / 2
        total_cost = holding_cost + setup_cost + shortage_cost
        return total_cost
```

[ ]:
```
# Sample Run
A = float(input("Enter ordering cost per order (A): ")) # 100
lam = float(input("Enter demand rate (lambda): ")) # 10000
I = float(input("Enter inventory carrying cost rate (I): ")) # 0.2
C = float(input("Enter unit cost of item (C): ")) # 200

print("\nRunning for EOQ")
my_eoq = EOQ()
Q = my_eoq.get_quantity(A, lam, I, C)
tc = my_eoq.get_total_cost(A, lam, I, C, Q)
T = my_eoq.get_cycle_time(Q, lam)
print(f"Quantity = {Q} units")
print(f"Total Cost = {tc:2.2f}")
print(f"Cycle Time = {T*365:2.2f} days")

si = float(input("Enter production rate (s): ")) # 12000
print("\nRunning for EPQ")
my_epq = EPQ()
Q2 = my_epq.get_quantity(A, lam, I, C, si)
tc = my_epq.get_total_cost(A, lam, I, C, Q, si)
T = my_epq.get_cycle_time(Q, lam)
print(f"Quantity = {Q2} units")
print(f"Total Cost = {tc:2.2f}")
print(f"Cycle Time = {T*365:2.2f} days")

pi = float(input("Enter shortage cost per unit (p): ")) # 2
print("\nRunning for EOQ with Shortage")
my_eoq_short = EOQ_Short()
Q3 = my_eoq_short.get_quantity(A, lam, I, C, pi)
tc = my_eoq_short.get_total_cost(A, lam, I, C, Q, pi)
```

```
T = my_eoq_short.get_cycle_time(Q, lam)
print(f"Quantity = {Q3} units")
print(f"Total Cost =  {tc:2.2f}")
print(f"Cycle Time = {T*365:2.2f} days")

print("\nRunning for EPQ with Shortage")
my_epq_short = EPQ_Short()
Q4 = my_epq_short.get_quantity(A, lam, I, C, si, pi)
tc = my_epq_short.get_total_cost(A, lam, I, C, Q, si, pi)
T = my_epq_short.get_cycle_time(Q, lam)
print(f"Quantity = {Q4} units")
print(f"Total Cost =  {tc:2.2f}")
print(f"Cycle Time = {T*365:2.2f} days")
```

```
Running for EOQ
Quantity = 316 units
Total Cost = $6324.56
Cycle Time = 11.53 days

Running for EPQ
Quantity = 774 units
Total Cost = $3691.22
Cycle Time = 11.53 days

Running for EOQ with Shortage
Quantity = 1048 units
Total Cost = $6353.28
Cycle Time = 11.53 days

Running for EPQ with Shortage
Quantity = 2569 units
Total Cost = $3719.95
Cycle Time = 11.53 days
```

[32]:
```
# Visualising Q for each model
import matplotlib.pyplot as plt

l = [Q, Q2, Q3, Q4]
names = ["EOQ", "EPQ", "EOQ Shortage", "EPQ Shortage"]

plt.figure(figsize=(6,6))
plt.bar(names, l, color = 'r',edgecolor='k',linewidth=2)
plt.ylabel("Qty")
plt.xlabel("Deterministic Models")
plt.title("MODEL COMPARISON OF QUANTITY ORDERED")
plt.show()
```



1.10 Write a Program to determine different characteristics using various Queuing models.

[3]:
```python
from math import factorial

class MM1:
    def __init__(self, lam, mu):
        self.lam = lam  # Arrival rate
        self.mu = mu    # Service rate
        self.rho = lam / mu  # Traffic intensity

    def get_pn(self, n):
        """ Probability of having n customers in the system """
        return (1 - self.rho) * (self.rho ** n)
```

```
    def L(self):
        """ Average number of customers in the system """
        return self.rho / (1 - self.rho)

    def Lq(self):
        """ Average number of customers in the queue """
        return (self.rho ** 2) / (1 - self.rho)

    def W(self):
        """ Average time a customer spends in the system """
        return 1 / (self.mu - self.lam)

    def Wq(self):
        """ Average time a customer spends waiting in the queue """
        return self.rho / (self.mu - self.lam)


class MM1k:
    def __init__(self, lam, mu, k):
        self.lam = lam  # Arrival rate
        self.mu = mu    # Service rate
        self.k = k      # Capacity
        self.rho = lam / mu

    def get_p0(self):
        """ Probability of zero customers in the system """
        if self.rho == 1:
            return 1 / (self.k + 1)
        else:
            return (1 - self.rho) / (1 - self.rho ** (self.k + 1))

    def get_pn(self, n):
        """ Probability of having n customers in the system """
        p0 = self.get_p0()
        return p0 * (self.rho ** n)

    def L(self):
        """ Average number of customers in the system """
        p0 = self.get_p0()
        L = 0
        for n in range(self.k + 1):
            L += n * self.get_pn(n)
        return L

    def Lq(self):
        """ Average number of customers in the queue """
        return self.L() - self.rho
```

```
    def W(self):
        """ Average time a customer spends in the system """
        return self.L() / (self.lam * (1 - self.get_pn(self.k)))

    def Wq(self):
        """ Average time a customer spends waiting in the queue """
        return self.Lq() / (self.lam * (1 - self.get_pn(self.k)))


class MMc:
    def __init__(self, lam, mu, c):
        self.lam = lam  # Arrival rate
        self.mu = mu    # Service rate
        self.c = c      # Number of servers
        self.rho = lam / (c * mu)

    def get_p0(self):
        """ Probability of zero customers in the system """
        summation = sum((self.lam / self.mu) ** n / factorial(n) for n in␣
↪range(self.c))
        last_term = (self.lam / self.mu) ** self.c / (factorial(self.c) * (1 -␣
↪self.rho))
        return 1 / (summation + last_term)

    def get_pn(self, n):
        """ Probability of having n customers in the system """
        p0 = self.get_p0()
        if n < self.c:
            return p0 * (self.lam / self.mu) ** n / factorial(n)
        else:
            return p0 * (self.lam / self.mu) ** n / (factorial(self.c) * self.c␣
↪** (n - self.c))

    def Lq(self):
        """ Average number of customers in the queue """
        p0 = self.get_p0()
        return p0 * (self.rho ** self.c) * self.lam / (factorial(self.c) * (1 -␣
↪self.rho) ** 2)

    def L(self):
        """ Average number of customers in the system """
        return self.Lq() + self.lam / self.mu

    def W(self):
        """ Average time a customer spends in the system """
        return self.L() / self.lam
```

```
    def Wq(self):
        """ Average time a customer spends waiting in the queue """
        return self.Lq() / self.lam


class MMck:
    def __init__(self, lam, mu, c, k):
        self.lam = lam  # Arrival rate
        self.mu = mu    # Service rate
        self.c = c      # Number of servers
        self.k = k      # Capacity
        self.rho = lam / (c * mu)

    def get_p0(self):
        """ Probability of zero customers in the system """
        sum1 = sum((self.lam / self.mu) ** n / factorial(n) for n in range(self.
 ↪c))
        sum2 = ((self.lam / self.mu) ** self.c) / factorial(self.c) * sum(
            (self.lam / (self.c * self.mu)) ** n for n in range(self.k - self.c␣
 ↪+ 1)
        )
        return 1 / (sum1 + sum2)

    def get_pn(self, n):
        """ Probability of having n customers in the system """
        p0 = self.get_p0()
        if n < self.c:
            return p0 * (self.lam / self.mu) ** n / factorial(n)
        else:
            return p0 * (self.lam / self.mu) ** n / (factorial(self.c) * self.c␣
 ↪** (n - self.c))

    def Lq(self):
        """ Average number of customers in the queue """
        p0 = self.get_p0()
        return p0 * (self.rho ** self.c) * self.lam / (factorial(self.c) * (1 -␣
 ↪self.rho) ** 2)

    def L(self):
        """ Average number of customers in the system """
        return self.Lq() + self.lam / self.mu

    def W(self):
        """ Average time a customer spends in the system """
        return self.L() / self.lam
```

```
    def Wq(self):
        """ Average time a customer spends waiting in the queue """
        return self.Lq() / self.lam
```

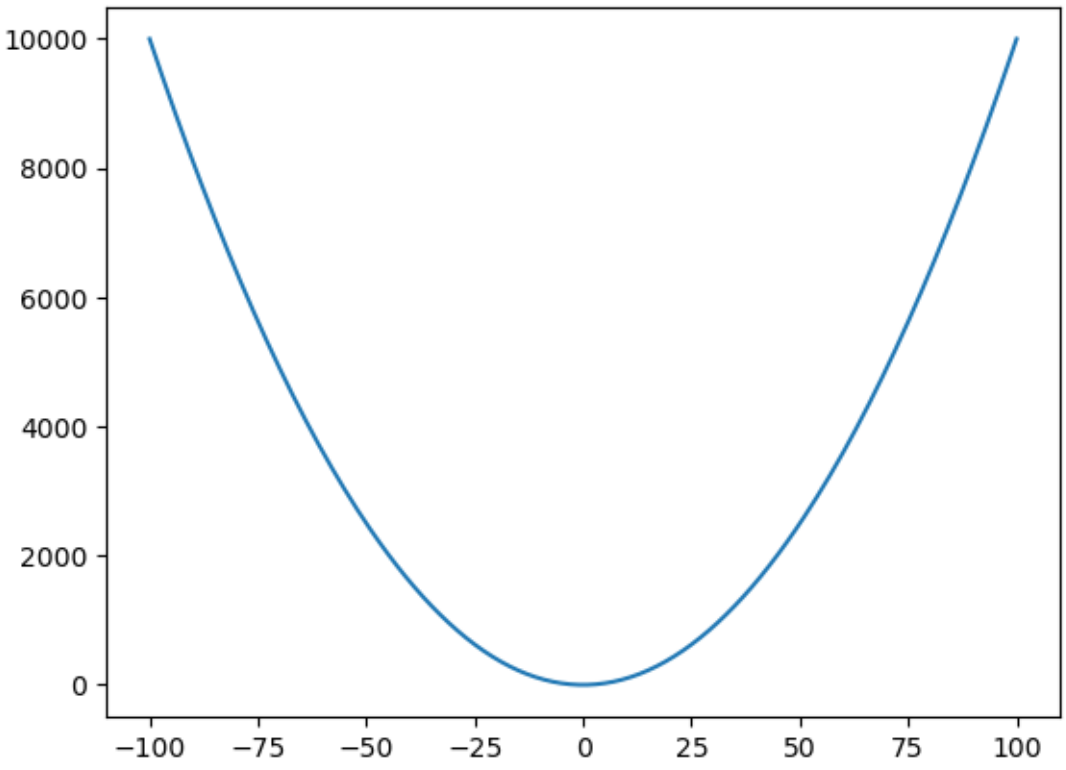
[12]:
```
# Sample Run
mm1 = MM1(lam=2, mu=3)
print("Model: M/M/1")
print("L:", round(mm1.L(),2))
print("Lq:", round(mm1.Lq(),2))
print("W:", round(mm1.W(),2))
print("Wq:", round(mm1.Wq(),2))

mm1k = MM1k(lam=2, mu=3, k=5)
print("\nModel: M/M/1/k")
print("L:", round(mm1k.L(),2))
print("Lq:", round(mm1k.Lq(),2))
print("W:", round(mm1k.W(),2))
print("Wq:", round(mm1k.Wq(),2))

mmc = MMc(lam=5, mu=6, c=3)
print("\nModel: M/M/c")
print("L:", round(mmc.L(),2))
print("Lq:", round(mmc.Lq(),2))
print("W:", round(mmc.W(),2))
print("Wq:", round(mmc.Wq(),2))

mmck = MMck(lam=4, mu=5, c=2, k=10)
print("\nModel: M/M/c/k")
print("L:", round(mmck.L(),2))
print("Lq:", round(mmck.Lq(),2))
print("W:", round(mmck.W(),2))
print("Wq:", round(mmck.Wq(),2))
```

```
Model: M/M/1
L: 2.0
Lq: 1.33
W: 1.0
Wq: 0.67

Model: M/M/1/k
L: 1.42
Lq: 0.76
W: 0.75
Wq: 0.4

Model: M/M/c
L: 0.85
Lq: 0.01
```

```
W: 0.17
Wq: 0.0

Model: M/M/c/k
L: 1.18
Lq: 0.38
W: 0.3
Wq: 0.1
```

1.11 WAP to plot a graph for function $y = x^2$.

[1]:
```
import numpy as np
import matplotlib.pyplot as plt

x = np.arange(-100,101)
y = x**2

plt.plot(x,y)
plt.show()
```



1.12 WAP to fit poisson distribution on a given data.

[ ]:

1.13 Write a python function that calculates the `pierson correlation cofficient` between two lists of numbers.

[ ]:

1.14 Write a python function that calculates `Spareman correlation cofficient`.

[ ]:

1.15 Using matplotlib plot histogram of list of numbers.

[ ]:

1.16 Write a python function that calculates the Z-score for the lists of numbers.

[ ]:

1.17 WAP to test the significance of two sample means.

[ ]:

1.18 WAP to test the goodness of fit of a given dataset on binomial distribution.

[ ]:

1.19 WAP to test significance of two sample variance.

[ ]:

1.20 WAP to implement linear regression in python.

[ ]:

1.21 WAP to plot piechart on consumption of water in daily life.

[ ]:

1.22 WAP to plot bar chart to display result for 10th, 12th, 1st year, 2nd year, 3rd year CGPA.

[ ]:

1.23 WAP to perform various statistical measures using pandas.

[ ]:

1.24 WAP to perform read and write operations with csv files.

[ ]:

1.25 WAP to compute values of $\sin(x)$ using taylor series.

[ ]:

1.26 WAP to display the following pattern

```
    5
   45
  345
 2345
12345
```

[75]:
```
n = int(input("Enter N:"))
for i in range(n,0,-1):
    print('  '*(i-1),end='')
    for j in range(i,n+1):
        print(j,end=' ')
    print()
```

```
      5
    4 5
  3 4 5
2 3 4 5
1 2 3 4 5
```

1.27 WAP to find if a number or string is palindrome or not.

[102]:
```
s = input("Enter a number or a string: ")

def isPalindrome(s):
    return s == s[::-1]

print(f"{s} is {"" if isPalindrome(s) else "NOT "}a palindrome.")
```

```
232 is a palindrome.
```

1.28 WAP to find greatest of number using loop.

[ ]:

1.29 WAP to print fibonacci series.

[ ]:

1.30 WAP to find factorial using recursion.

[ ]:

1.31 WAP to find if a number is armstrong or not.

[ ]:

1.32 Write a menu driven program to find the reverse of a number and sum of digits.

[ ]:
