## King Mongkut's University of Technology Thonburi Midterm Examination 1/2014

CPE 214 Signals and Systems Date: September 26, 2014

Computer Engineering Department

Time: 1:00 - 4:00 p.m.

## Instructions:

Violation of examination rules and regulations will not be tolerated. Serious violator could face dismissal charge.

- 1. Only one calculator is allowed in the examination room.
- 2. Books, documents, and notes are not allowed in the examination room.
- Carefully read the explanation in each problem and then answer each question.
- 4. Do not take the examination sheets out of the examination room.
- 5. Write your answers on the examination booklet(s).
- 6. This examination has 3 pages (7 problems, 60 points).
- 1. Determine the fundamental frequency  $\omega_0$  and the Fourier series coefficients  $a_k$  of the following signals. (7 points)
  - a)  $x(t) = 2 + \cos\left(\frac{2\pi}{3}t\right) + 4\sin\left(\frac{5\pi}{3}t\right)$ b)  $x[n] = (-1)^n$

(2 points)

(3 points)

c)  $x[n] = 1 + \sin(\frac{3\pi}{8}n + \frac{\pi}{4})$ 

(2 points)

2. Determine the Fourier transform, the magnitude, and phase of Fourier transform of the following signals (6 points)

a) 
$$x(t) = \delta(t+1) + \delta(t-1)$$

(3 points)

b) 
$$x(t) = e^{-2(t+1)}u(t-1)$$

(3 points)

3. Consider a causal LTI system with frequency response

$$H(jw) = \frac{1}{j\omega + 3}$$

For a particular input x(t) this system is observed to produce the output  $y(t) = e^{-3t}u(t) - e^{-4t}u(t)$ 

Determine:

(7 points)

- a) Magnitude and phase of frequency response.
- b) The input x(t).

(2 points) (3 points)

c) Impulse response of this system.

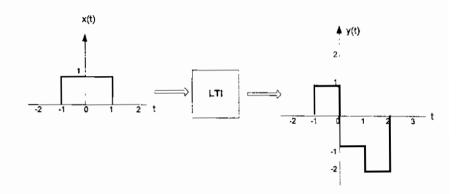
(2 points)

4. Consider an LTI system that is characterized by the difference equation y[n] - 0.5y[n-1] = x[n]

Determine:

- (8 points) a) Frequency response of this system (2 points)
- b) Impulse response of this system. Is this system a causal system?

- c) The response of this system to the input  $x_1[n] = \delta[n-1] + \delta[n+2]$ (3 points)
- 5. Given input-output pair of an LTI system as following:



Determine:

(9 points)

a) The impulse response (h(t)) of this system.

- (5 points)
- b) The response of this system when the input is  $x_1(t) = u(t)$ (2 points)
- c) The magnitude and phase of Frequency response of this system. (2 points)
- 6. The frequency response of an LTI system is

(8 points)

$$H(e^{j\omega}) = \frac{-12 + 5e^{-j\omega}}{12 - 7e^{-j\omega} + e^{-j2\omega}}$$

- a) Determine the difference equation of this system.
- (3 points)
- b) Determine the response of this system to the input  $x[n] = (\frac{1}{2})^n u[n]$

(4 points)

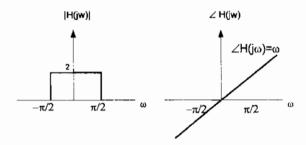
c) Is this system a causal system?

(1 point)

7. Magnitude and phase of frequency response for an LTI system is shown in the figure below. Determine the output of the system when input is (15 points)

a) 
$$x1(t) = e^{j\frac{\pi t}{4}}$$
 (7 points)

b) 
$$x2(t) = \cos\left(\frac{3\pi}{2}t\right) + \cos\left(\frac{\pi}{2}t\right)$$
 (8 points)



## Note:

Fourier Transform:

$$X(j\omega) = \int\limits_{-\infty}^{\infty} x(t) e^{-j\omega t} dt \hspace{1cm} \text{and} \hspace{1cm} x(t) = \frac{1}{2\pi} \int\limits_{-\infty}^{\infty} X(j\omega) e^{j\omega t} d\omega$$

Discrete-Time Fourier Transform:

$$X(e^{j\omega}) = \sum_{-\infty}^{\infty} x[n]e^{-j\omega n}$$
 and  $x[n] = \frac{1}{2\pi} \int_{-\pi}^{\pi} X(e^{j\omega})e^{j\omega n} d\omega$ 

Laplace Transform:

$$X(s) = \int_{-\infty}^{\infty} x(t)e^{-st}dt \qquad \text{and} \qquad x(t) = \frac{1}{2\pi i} \int_{\sigma - j\infty}^{\sigma + j\infty} X(s)e^{st}d\omega$$

z - Transform:

$$X(z) = \sum_{-\infty}^{\infty} x[n]z^{-n} \qquad \text{and} \qquad x[n] = \frac{1}{2\pi i} \iint X[z]z^{n-1} dz$$

**Summation Formulas** 

$$\sum_{k=0}^{n} a^{k} = \frac{1-a^{n+1}}{1-a} \quad a \neq 1$$

$$\sum_{k=0}^{n} ka^{k} = \frac{a[1-(n+1)a^{n}+na^{n+1}]}{(1-a)^{2}}$$

$$\sum_{k=0}^{\infty} ka^{k} = \frac{a}{(1-a)^{2}} \quad |a| < 1$$

$$\sum_{k=0}^{\infty} a^{k} = \frac{1}{1-a} \quad |a| < 1$$

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