

Electrical Indicating Instruments: DC

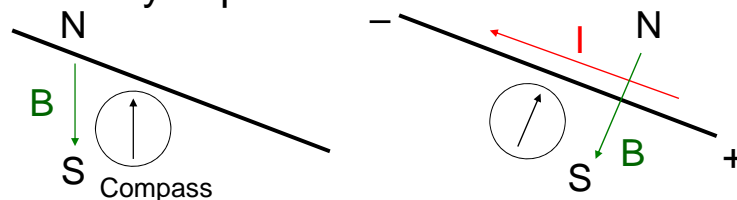


EIE 240 Electrical and Electronic Measurement
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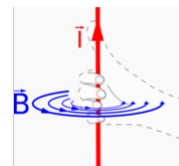
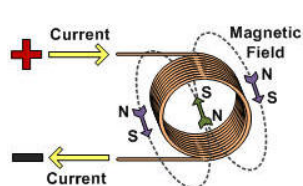
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Analogue Meter's Concept

- Han Oersted, in 1820, noted his finding without any explanation



- Lord Kelvin made more sensitivity to a current

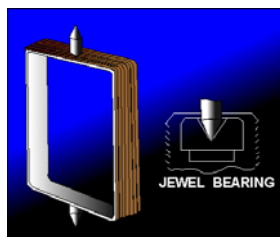


Right-hand Rule

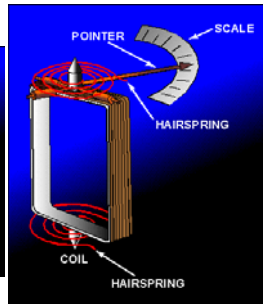
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Direct Current Meters

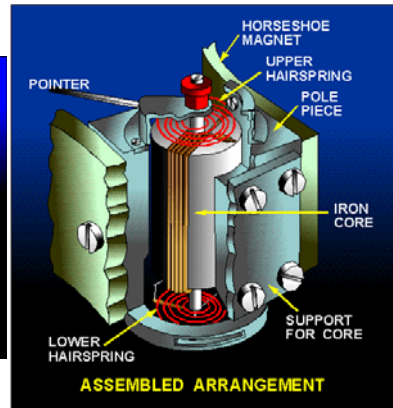
- Permanent-Magnet Moving-Coil (PMMC) developed in 1881



Coil

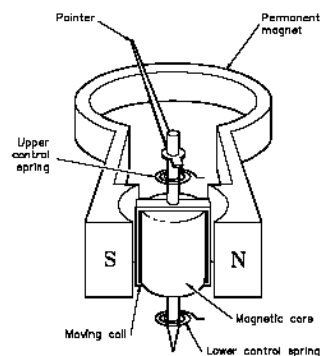


Pointer



Permanent Magnet 3

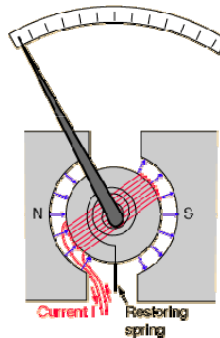
- A wire coil is attached to a shaft that pivots on two jewel bearing.
- The coil can rotate in a space between a cylindrical soft-iron core and two permanent magnetic pole pieces.
- The rotation is opposed by two fine hairsprings.



- Jacques D'Arsonval's Movement (Galvanometer)

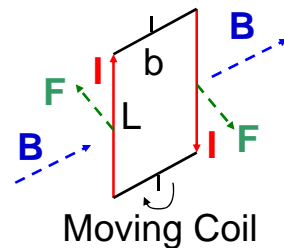
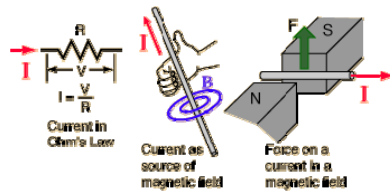
When a current is passed through the coil it rotates, the angle through which it rotates being proportional to the current ($0.0000001 - 1 \mu\text{A}$).

The magnetic field is designed (magnetic pole piece's shape) that it is always at the right angles to the coil sides no matter what angle the coil has rotated through.



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- Electric Current



- Fleming's Left-Hand Rule

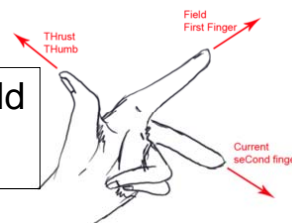
$$\mathbf{F} = \mathbf{L} \times \mathbf{I} \times \mathbf{B}$$

Force
(Newton)

Coil Side
Length
(Metre)

Current
(Ampere)

Magnetic Field
(Tesla)



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- Torque (moment) is an angular force defined by linear force multiplied by a radius.

$$\begin{aligned}\text{Damping Torque in Coil} &= F (b/2) \\ &= B I L b / 2\end{aligned}$$

$$\begin{aligned}\text{Torque}_{\text{total}} &= 2 (B I L b / 2) = B I L b \\ &= B I A \quad , \text{Area } A = Lb\end{aligned}$$

$$\begin{aligned}\text{for } N \text{ coils, } \text{Torque}_{\text{total}} &= N B I A \\ &= K_{\text{coil}} I \quad , K_{\text{coil}} = NBA\end{aligned}$$

- Controlling torque in springs

$$\text{Torque}_{\text{spring}} = K_s \theta$$

- Critical damping or balancing forces (Newton's 3rd Law)

$$\text{Action} = \text{Reaction}$$

$$\text{Torque}_{\text{total}} = \text{Torque}_{\text{spring}}$$

$$K_{\text{coil}} I = K_s \theta$$

$$\theta = (K_{\text{coil}} / K_s) I$$

- If the magnetic field is not uniform throughout the entire region, the scales are nonlinear!

Galvanometer

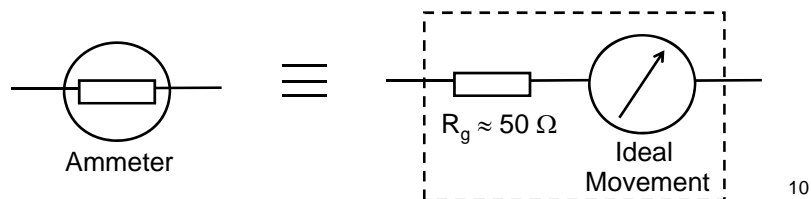
- Galvanometer with a zero at the center of the scale used in DC instruments that can detect current flow in either direction
- Galvanometer with a zero at the left end of the scale indicates an upscale reading only for the proper way of connecting the meter into the circuit



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Equivalent Ammeter Circuit

- The resistance of the meter coil and leads introduces a departure from the ideal ammeter behavior. The model usually used to describe an ammeter in equivalent circuit is a resistance R_g in series with an ideal ammeter (no resistance)

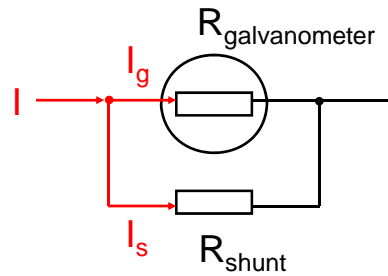


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Full-Scale-Deflection Currents

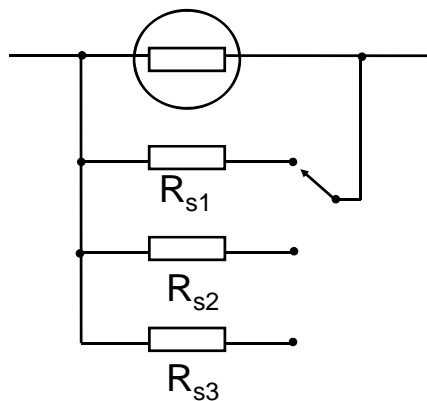
- Current range is 10 μA – 20 mA
- Shunt resistor connected in parallel

$$\begin{aligned}
 V_s &= V_g \\
 (I - I_g)R_s &= I_g R_g \\
 I &= \underbrace{(R_s + R_g)/R_s}_{\text{Scaling factor}} I_g
 \end{aligned}$$



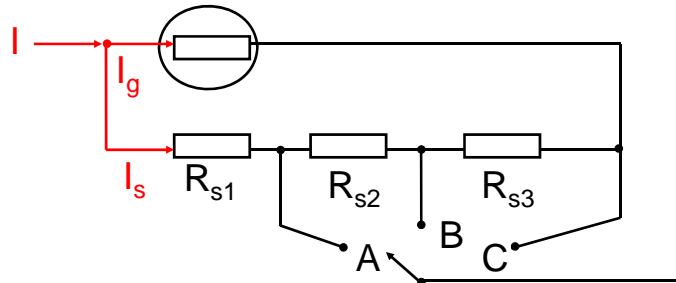
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- Multi-range shunt can be made by switching into a circuit



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- Universal shunt (Ayrton shunt)



A: $(I - I_g)R_{s1} = I_g (R_g + R_{s2} + R_{s3})$

$$I = (R_g + R_{s1} + R_{s2} + R_{s3}) / R_{s1} I_g$$

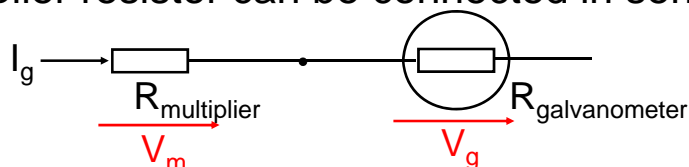
B: $(I - I_g)(R_{s1} + R_{s2}) = I_g (R_g + R_{s3})$

$$I = (R_g + R_{s1} + R_{s2} + R_{s3}) / (R_{s1} + R_{s2}) I_g$$

C: $I = (R_g + R_{s1} + R_{s2} + R_{s3}) / (R_{s1} + R_{s2} + R_{s3}) I_g$

Full-Scale-Deflection Voltages

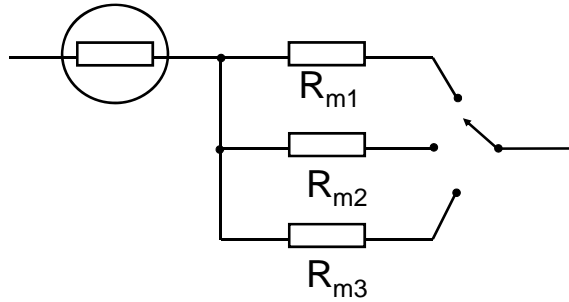
- Since $V = IR$, the response of a moving coil meter responding to a current is also proportional to the potential difference across the meter.
- However, because R_g and I_g are low, it can only be used for low voltages (≈ 0.05 V).
- Multiplier resistor can be connected in series



$$V = I_g R_m + I_g R_g = (R_m + R_g) I_g$$

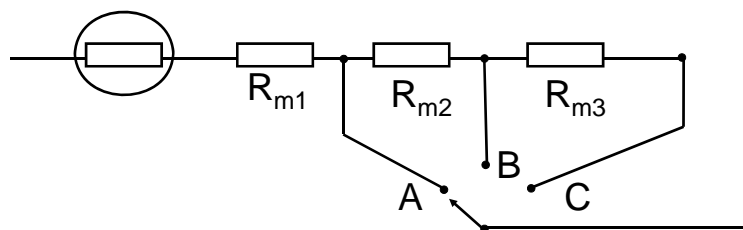
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- Multi-range voltmeter



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- Multi-range voltmeter with a chain arrangement



$$A: V = I_g R_g + I_g R_{m1} = (R_m + R_g) I_g$$

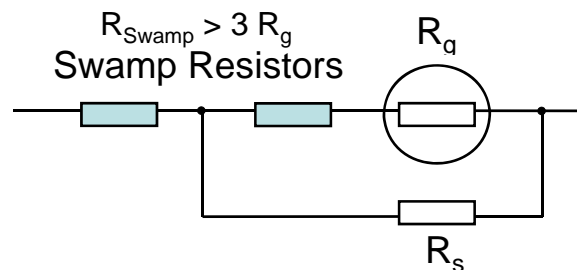
$$B: V = I_g R_g + I_g R_{m1} + I_g R_{m2} = (R_{m1} + R_{m2} + R_g) I_g$$

$$C: V = I_g R_g + I_g R_{m1} + I_g R_{m2} + I_g R_{m3} \\ = (R_{m1} + R_{m2} + R_{m3} + R_g) I_g$$

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Temperature on Moving-Coil Meter

- Higher temperature of coil, higher resistance, lower reading \Rightarrow decrease spring tension
- Measured value is decreased 0.2% for increasing of 1°C temperature.
- Swamp resistor (manganin wire), whose resistance changes slowly with temperature, connected in series
- However, the sensitivity is decreased.



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Sensitivity on Moving-Coil Meter

- Sensitivity = Pointer Change / Input Change

$$S = \theta / I$$

or

$$S = 1 / I_{\text{fsd}}$$

$$= R / V_{\text{fsd}}$$

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Ammeter & Voltmeter Loading

- Systematic Error => Calculation by using Thévenin's theorem in Chapter 3