ECE 252: Systems Programming and Concurrency	Spring 2021
Lecture 20 — Advanced Concurrency Problems	
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Get a Pizza This!

Let's consider a more advanced concurrency problem. In [Dow08] it's called the "Cigarette Smokers Problem", but smoking is bad for you so it's going to be the "Pizza Makers Problem". Pizza, while not exactly health food, is amazing. Delicious, delicious pizza.

A new show to be hosted by some famous TV chef personality is being pitched, and you're going to write a simulation of it. The show is about making pizza. A pizza requires three ingredients: dough, sauce, and cheese. All three ingredients are necessary to make a pizza (otherwise it does not meet the definition of a pizza).

Each contestant has an unlimited supply of one ingredient. Contestant A has an unlimited supply of dough, Contestant B has an unlimited supply of sauce, and Contestant C has an unlimited supply of cheese. Each contestant needs to get the two ingredients they do not have and then can make a pizza. They will continue to (try to) make pizza in a loop until time is up. At the beginning of the episode, the host places two different random ingredients out. Contestants can signal the host to ask for more ingredients, but they should not do so unless they actually need some. Each time the host is woken up (signalled), he again places two different random ingredients out. When an ingredient is placed on the table, the host posts on the associated semaphore. For example, if the host puts out cheese and sauce, then the host posts on both cheese and sauce.

In this scenario, there are resources provided by some external system and the contestants are processes that want resources. But we shouldn't be wasteful: resources should only be requested when they are needed and processes should take only what they need. Applications should only wake up if they can do something useful.

There are some restrictions, though, and they could make the problem either impossible or trivial. In the impossible version, you can't modify what the host does (which is sensible, because you don't control the other system) but you also cannot use conditional (if) statements, which is pretty ridiculous. In the trivial version, the host tells which contestants whose turn it is, which is boring but also unrealistic, because again it requires the host system to know too much about the contestants. The interesting version has just the restriction that we can't control the host behaviour [Dow08]. And he is a TV chef personality, after all, they do wacky things.

Consider the following solution. All semaphores start at 0, except for host which starts as 1 (so the host will run the first time). Does this work?

Contestant A	Contestant B	Contestant C
<pre>wait(sauce) get_sauce() wait(cheese) get_cheese() make_pizza() post(host)</pre>	<pre>wait(dough) get_dough() wait(cheese) get_cheese() make_pizza() post(host)</pre>	<pre>wait(sauce) get_sauce() wait(dough) get_dough() make_pizza() post(host)</pre>

No. Deadlock can easily occur. Suppose the host puts out sauce and dough. If contestant B takes the dough and contestant A takes the sauce, then both of them are blocked and nobody can proceed and nobody gets pizza.

Part of the problem here is that a contestant doesn't have a good way to assess what the ingredients are before going up there. And once there, if it finds that the ingredients match someone else's needs, we don't call that contestant over. That would be clever, but to make this work we would need a way to "check" what ingredients are

there and semaphores don't let us do that. If we want to do that, we'd have to break the rule about not modifying the host's behaviour. Can we work with what we have?

Imagine now that each contestant gets a helper. The job of the helper is to, well, help their contestant to make pizza by figuring out whose turn it is. For this there are boolean variables dough_present, sauce_present, and cheese_present that are all initialized to false. They are protected by a semaphore (called mutex). The helpers update that variable, and based on the information available, signal which contestant should come up to the table and take ingredients. Each contestant now has a semaphore (such as contestantA for contestantA) which the helpers will post on. Contestants are still responsible for telling the host to put out more ingredients.

Helper 1

wait(sauce) wait(mutex) if dough_present dough_present = false; post(contestantC) else if cheese_present cheese_present = false; post(contestantA) else sauce_present = true; end if post(mutex)

Helper 2

```
wait( dough )
wait( mutex )
if sauce_present
  sauce_present = false;
  post( contestantC )
else if cheese_present
  cheese_present = false;
  post( contestantB )
else
  dough_present = true;
end if
post( mutex )
```

Helper 3

```
wait( cheese )
wait( mutex )
if dough_present
  dough_present = false;
  post( contestantB )
else if sauce_present
  sauce_present = false;
  post( contestantA )
else
  cheese_present = true;
end if
post( mutex )
```

So let's analyze Helper 1. Each of the other helpers does the same thing but for a different ingredient. In this case, the helper is woken up when sauce is placed on the table. It then locks the mutex so that it can manipulate the shared variables of what ingredients are present. Now we decide what to do here. If the current helper is the first one to run, then all the variables will be false, so we'll end up at the else block and just set sauce_present to true and then let the next helper run. If dough_present is true, then Helper 2 has already run and we know that dough is present on the table. With both sauce and dough present, we know that the ingredients present match the needs of Contestant C. If cheese_present is true then Helper 3 has already run and the ingredients present match the needs of Contestant A.

Obviously, each of the other helpers will signal the appropriate contestant based on its assessment of the state of the ingredients.

Contestant A

wait(contestantA)
get_sauce()	
get_cheese()	
<pre>make_pizza()</pre>	
post(host)	

Contestant B

wait(c	ontestantB)
get_dou	gh()	
get_che	ese()	
make_pi	zza()	
post(h	ost)	

Contestant C

```
wait( contestantC )
get_sauce()
get_dough()
make_pizza( )
post( host )
```

The contestant code is pretty much trivial now: wait until a helper signals, then go take your ingredients and make a pizza. Once the pizza is in the oven, indicate that you are ready for more ingredients.

The generalized version of the problem is what happens when the host puts out ingredients periodically, without a need to be signalled to ask for more. How do we modify the solution to deal with that?

Obviously if there is no longer a need for the contestants to signal that they want more resources then the post (host) statements in the contestant code has to be removed. But what about the helpers?

Instead of boolean variables to indicate the presence or absence of an ingredient what we need instead is an integer counter to know how many there are. So let's call them num_dough, num_sauce, and num_cheese, and they all start as zero.

Helper 1

```
wait( sauce )
wait( mutex )
if num_dough > 0
   num_dough--
   post( contestantC )
else if num_cheese > 0
   num_cheese--
   post( contestantA )
else
   num_sauce++
end if
post( mutex )
```

Helper 2

```
wait( dough )
wait( mutex )
if num_sauce > 0
   num_sauce--
   post( contestantC )
else if num_cheese > 0
   num_cheese--
   post( contestantB )
else
   num_dough++
end if
post( mutex )
```

Helper 3

```
wait( cheese )
wait( mutex )
if num_dough > 0
   num_dough--
   post( contestantB )
else if num_sauce > 0
   num_sauce--
   post( contestantA )
else
   num_cheese++
end if
post( mutex )
```

Now instead of setting the variables to true and false, the variables tracking the ingredients are incremented and decremented. Otherwise not much has changed. This pattern is referred to as the "scoreboard" [Dow08] – there are variables keeping track of the state of the system which are viewable from all threads. As threads go about their actions, they take a look at the current state (the scoreboard) and decide how to act based on that.

The Barbershop Problem

Consider the "Barbershop Problem", originally proposed by Dijkstra. A variant of this appears in [SGG13]. A barbershop is a place where customers get their hair cut. A barbershop consists of a waiting area with n chairs, and a barber chair.

If there are no customers to be served, the barber goes to sleep. If a customer enters the barbershop and all chairs are occupied, then the customer leaves the shop. If the barber is busy, but chairs are available, then the customer sits in one of the free chairs. If the barber is asleep, the customer wakes up the barber.

Customer threads should call get_hair_cut() when it is their turn. If the shop is full, the customer should return (exit/leave). The barber thread will call cut_hair. The barber can cut only one person's hair at a time, so there should be exactly one thread calling get_hair_cut() concurrently. You can assume that external forces cause customers to appear and the barber to keep working (so you do not need to write any loops). Assume n is initialized to an appropriate value.

We need an integer counter for customers waiting called customers that starts at 0. We will also have a mutex for controlling access to customers called mutex (it obviously starts at 1). Finally, two semaphores, customer and barber that both start at 0.

As for the solution:

Customer

```
wait( mutex )
if customers == n+1
    signal( mutex )
    return
end if
customers++
signal( mutex )

signal( customer )
wait( barber )
get_hair_cut()

wait( mutex )
customers--
signal( mutex )
```

Barber

wait(customer)
signal(barber)
cut_hair()

The barber code is much simpler, so let's start there. The barber waits for there to be a customer. When there is

one, the barber calls the customer forward by signalling on barber, and then cuts hair. Simple enough.

As for the customer, customers is shared data, so its access should be protected by mutex. If we find that the number of customers is already n – that is, the waiting area is full, the customer should leave. But not without unlocking mutex! If the customer forgot to do that then no more customers could enter. That's a problem. Otherwise the count of customers is increased and the customer signals the semaphore customer. This will wake up the barber, if the barber is sleeping, but also indicates the number of customers waiting. Then the customer must wait for the barber. When the customer gets called forward by the barber, the customer can get their hair cut. Finally, when leaving, the customer decrements the number of customers counter.

Let's look over this for a risk of deadlock. We don't see anywhere, really, the nested-waits pattern that usually indicates trouble. There isn't really any scenario where a customer can get blocked waiting for another customer or the barber, and the barber code is very simple.

As for starvation, it also won't happen. Assuming there are actually customers, the barber will have work to do. And the customers will wait for a finite period before they get their hair cut. The size of the waiting area is limited so we expect that a customer doesn't get delayed indefinitely. It is possible for them to wait quite a while, though, but they will eventually get a turn.

We can maybe say that customers who give up in frustration are disappointed but that's better than making them wait forever. If they are told they won't get service today, they can go to a different barbershop or come again some other time. That's why there's the limit on the waiting area at all. In the scenario, the barber is only human and can only cut so many people's hair in a day. The exact number will vary based on how long each hair cut takes, which depends on the person whose hair is being cut. But there is a limit of some sort: at some point the barber will go home. And only so many people can fit into the waiting room anyway: if there are too many, then nobody can move around (and this violates fire code!).

This is actually a good lesson for services in general. They have a certain capacity, and when things are overloaded it's helpful to tell clients that they are unable to take any more requests right now. Clients can then choose what to do (and it's usually either "wait a while and try again" or "go to a different service"). And you can! If the game that you want to play requires a server and all servers are busy, you can play a different game (or go outside, or who knows what!).

Escape from Hoth and Chemistry: Building H₂O

Where we want to go with this is the building H_2O problem. But for right now, we need to take a slight detour to the ice planet of Hoth! The chemistry problem is somewhat complicated, so the best way to approach it is by starting with an easier variant and then moving on.

The Rebel Alliance is trying desperately to escape the ice planet Hoth before Darth Vader can put an end to the rebellion once and for all. The rebels want to evacuate the base with transports; transports are escorted by a pair of X-Wing fighters. Transports have no hope of surviving if they are not escorted, so the fighters must stay with their assigned transport. Normally, central command would tell the fighters and transports when to launch, but the base is under assault. Thus, the transports and fighters must organize themselves. Only one group of fighters and transports can launch at a time. In this problem, a pair of fighters is a single unit.

If a transport is ready, but fighters are not, the transport has to wait for the next fighters. If the fighters are ready but the transport is not, then the fighters have to wait for the next transport. When the fighters and transport are ready, they can both use the launch() function and they are off! The transport is the slower one to launch, so the next group should not proceed until the transport has finished the launch() process.

Assume there are an appropriate number of fighters and transports so that nobody is left behind. The setup and creation of each kind of thread is something we will assume is handled externally and we can just focus on the behaviour of each kind of thread.

We will need an integer counter for the number of ready fighters, called fighters, an integer counter for the number of ready transports called transports, and three semaphores: mutex, fighter_queue, transport_queue.

Initial values: mutex = 1 and fighter_queue = 0 and transport_queue = 0.

```
Fighters
                                                Transport
                                                wait( mutex )
                                                if fighters > 0
wait( mutex )
if transports > 0
                                                   fighters--
  transports--
                                                   signal( fighter_queue )
  post( transport_queue )
                                                else
else
                                                   transports++
  fighters++
                                                   post( mutex )
                                                  wait( transport_queue )
  post( mutex )
  wait( fighter_queue )
                                                end if
end if
                                                launch()
launch()
                                                post( mutex )
```

Let's start with the fighters. As you might have guessed, this is also a scoreboard kind of problem. When the fighters arrive, if transports is greater than 0, then post on the queue for transports and let's launch. Otherwise, increment the number of fighters, post on the mutex, and wait in the queue to get called by a transport. Whether they proceeded directly or waited for a transport, they launch.

It is a little strange that the fighters don't post on mutex if there is a transport ready. Isn't this a problem? It turns out no, because the transport threads post on it unconditionally. The mutex does two jobs here, really; it will prevent concurrent modification of the fighters and transports variables, but it also makes sure that only one group can call launch() concurrently.

The transport code is pretty straightforward with that in mind: wait on the mutex, check if fighters is greater than 0, and if so decrement the count and tell the fighters to proceed; otherwise increment the number of transports, wait on the transport queue. Either way, the transport launches and then posts on mutex.

Is there a risk of deadlock here? For one thing, there are no nested waits; each kind of thread is careful to post on mutex before waiting on their associated queue semaphore. So nothing there. The only way fighters can get blocked is if no transports are presently ready (and more will soon arrive); the only way that transports can get blocked is if no fighters are ready (and they will also be ready soon).

How about starvation? As long as there are an appropriate number of fighters and transports, they will successfully match up with one another and can eventually launch.

On to the Chemistry... There are two kinds of thread, oxygen() and hydrogen(). As you will recall from basic chemistry, water, H_2O , requires two hydrogen modules and one oxygen module. To assemble the desired molecule (water) a group rendezvous pattern is needed to make each thread wait until all ingredients are present in the correct amounts. As each thread passes the barrier, it should call the function bond() which makes the water. Our solution must function so that all threads for one molecule invoke bond() before any of the threads from the next molecule do.

To clarify, if an oxygen thread arrives at the barrier when no hydrogen threads are present, it has to wait for two hydrogen threads to arrive. If a hydrogen thread arrives a the barrier when no other threads are waiting, it has to wait for an oxygen thread and another hydrogen thread. It is not necessary for the threads to know what other threads they are matched with, as long as the correct elements are present in the correct proportions.

In the example, we'll assume the oxygen and hydrogen threads are created and started correctly and in the correct proportions. The code for the creation of those two types of threads is not shown for space reasons. The reusable two-phase barrier from earlier has also been converted into C code.

The oxygen queue and hydrogen queue start as "locked" so we'll only signal the threads when they are going to proceed. Before that we have a scoreboard pattern, where threads take a look at the state of the system and decide what to do.

```
int oxygen;
                                                           int main( void ) {
int hydrogen;
                                                             oxygen = 0;
pthread_mutex_t barrier_mutex;
                                                             hydrogen = 0;
sem t turnstile:
                                                             barrier_count = 0;
int barrier_count;
                                                             barrier_N = 3;
int barrier_N;
                                                             pthread_mutex_init( &barrier_mutex, NULL );
sem_t bond:
sem_t oxygen_queue;
                                                             sem_init( &barrier_turnstile, 0, 0 );
sem_t hydrogen_queue;
                                                             sem_init( &bond, 0, 1 );
void barrier_enter( ) {
                                                             sem_init( &oxygen_queue, 0, 0 );
 pthread_mutex_lock( &barrier_mutex );
                                                             sem_init( &hydrogen_queue, 0, 0 );
 barrier_count++;
 if ( barrier_count == barrier_N ) {
                                                             /* Creation of oxygen and hydrogen threads
    sem_post( &turnstile );
                                                              not shown for space reasons */
 pthread_mutex_unlock( &barrier_mutex );
                                                             pthread_mutex_destroy( &barrier_mutex );
 sem_wait( &turnstile );
                                                             sem_destroy( &barrier_turnstile );
  sem_post( &turnstile );
                                                             sem_destroy( &bond );
                                                             sem_destroy( &oxygen_queue );
                                                             sem_destroy( &hydrogen_queue );
void barrier_exit( ) {
  pthread_mutex_lock( &barrier_mutex );
                                                             pthread_exit( 0 );
 barrier_count--:
 if ( barrier_count == 0 ) {
    sem_wait( &turnstile );
 pthread_mutex_unlock( &barrier_mutex );
void* oxygen( void* ignore ) {
                                                           void* hvdrogen( void* ignore ) {
  sem_wait( &bond );
                                                             sem_wait( &bond );
                                                             hydrogen++;
 oxvaen++:
 if( hydrogen >= 2 ){
                                                             if( hydrogen >= 2 && oxygen >= 1 )
    sem_post( &hydrogen_queue );
                                                               sem_post( &hydrogen_queue );
    sem_post( &hydrogen_queue );
                                                               sem_post( &hydrogen_queue );
   hvdrogen -= 2:
                                                               hvdrogen -= 2:
    sem_post( &oxygen_queue );
                                                               sem_post( &oxygen_queue );
    oxygen--;
                                                               oxygen--;
 } else {
                                                             } else {
    sem_post( &bond );
                                                               sem_post( &bond );
 sem_wait( &oxygen_queue );
                                                             sem_wait( &hydrogen_queue );
 bond():
                                                             bond():
 barrier_enter();
                                                             barrier_enter();
 barrier_exit();
                                                             barrier_exit();
  sem_post( &bond );
                                                             pthread_exit( NULL )
 pthread_exit( NULL )
```

Let's analyze the solution then, starting with oxygen threads. When it enters, it waits on the bond semaphore, which in this case is used somewhat like a mutex. If there are at least two hydrogen threads waiting, then, we can unblock two of them, signal the oxygen queue, and update the counters. If there are not two hydrogens waiting, then we just signal bond so that the next thread will arrive. Then the thread can get in line at the oxygen queue.

The hydrogen code is more or less the same, but the if-condition is different since it's not enough for 1 hydrogen to be present (we need at least two). If we have what we need, signal the queues to release the needed molecules, and we are ready to go. If not, get in line.

When threads are released from the oxygen queue and hydrogen queue respectively, they proceed forward to the bond() step, and afterwards there is a barrier enter followed by exit to wait for all of them to be finished. All

we really need is for all three threads to be done with bond() before they can exit so the barrier enter and exit happen one after the other.

Now it may be that when a thread arrives it unblocks some thread ahead of it in line. So if the oxygen that arrives is the 2nd oxygen and there is already one waiting ahead of it, that first one proceeds. That's okay – one molecule of water is as good as any other so we don't really care which oxygen ends up in its composition.

Why does only the Oxygen thread post on bond but hydrogen threads do not? Same idea as the fighters. When a thread arrives but the water molecule cannot be formed, whether it is oxygen or hydrogen, a post on bond takes place. If, however, the thread arriving is the last one necessary for bonding to take place, then one oxygen and two hydrogen proceed. Whoever waited on bond does not matter, as long as one of the threads that went into the water molecule posts on it before leaving. As the chemical composition of water has one oxygen, the job is assigned to this molecule. If we put it in hydrogen we might post on it twice.

These are by no means all the concurrency problems in the world. There are many more in [Dow08] that could be considered. But for now we will leave it here, before we get into really obscure problems...

References

[Dow08] Allen B. Downey. The Little Book of Semaphores (2nd Edition). Green Tea Press, 2008.

[SGG13] Abraham Silberschatz, Peter Baer Galvin, and Greg Gagne. *Operating System Concepts (9th Edition)*. John Wiley & Sons, 2013.