

# Logistic Regression

$$(1) \text{ starting point} = 3.0754 \quad [x_{\text{train}}]$$

$$\text{Age: } 57 \times \underset{\text{weight}}{0.007} = -0.4$$

$$\text{Sex: } 1 \times (-1.409) = -1.41$$

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$$\text{total score (z)} = 3.0754 + (-0.4) + (-1.41) + \dots$$

$$\text{Cost Function} = -y \cdot \ln(\hat{y}) - (1-y) \cdot \ln(1-\hat{y})$$

$$\text{If } y=1, \text{ cost Function} = -\ln(\hat{y})$$

$$\text{If } y=0, \text{ cost Function} = -\ln(1-\hat{y})$$

$$\text{Initial weight for Age } (\omega_1) = 0.01$$

$$\text{Initial weight for Sex } (\omega_2) = 0.5$$

$$\text{Initial weight for Bias } (b) = 0$$

$$\text{Bias } (b) = 0$$

$$z = (\omega_1 \cdot \text{Age}) + (\omega_2 \cdot \text{Sex}) + b$$

$$\text{Row}(1), z = (0.1 \times 63) + (0.5 \times 1) + b = 1.13$$

Sigmoid formula  $\hat{y} = \frac{1}{1 + e^{-1.13}} \approx 0.75$

Row(2),  $\hat{y} \approx 0.70$

Row(3),  $\hat{y} \approx 0.60$

Cost Prediction =  $-\ln(\text{prediction})$

Row 1 Cost  $\approx 0.28$

Total Cost Average

$$= \frac{0.28 + 0.35 + 0.51}{3}$$

Row 2 Cost  $\approx 0.35$

$$= 0.38$$

Row 3 Cost  $\approx 0.51$

(Gradient Descent)

Reducing weight

Gradient =  $(\text{Prediction} - \text{Target}) \times$

For row(1), prediction ( $\hat{y}$ ) = 0.75

Target ( $y$ ) = 1

$$(0.75 - 1) = -0.25$$

Error

Gradient for age, Error Age =  $(-0.25) (63)$   
 $= -15.75$

Update weight ) New weight = Old weight - (Learning rate  
Age x Gradient)

$$\text{update } w_1 = \frac{\text{initial weight}}{0.01} - \frac{(L.R)}{\text{Error Age}}$$

$$= 0.02575$$

$\times$  Test come use update weight latest.

$$z = (w_1 \cdot \text{Age}) + (w_2 \cdot \text{Sex}) + b = -1.9422$$

$$\text{Sigmoid function} \Rightarrow \hat{y} = \frac{1}{1 + e^{-1.9422}}$$

$$= 0.7 - 1.$$

↓  
Compare with  $y_{\text{test}}$

$$\text{Accuracy} = \frac{\text{No. Correct Prediction}}{\text{Total no. Test row}} \times 100\%$$

\* When Learning Stop?

(1) The "hard limit" (Epochs)

Max - iteration =

n n (Convergence)

(2) The good enough rule (Early stopping)

(3) The safety break (Early stopping)

