

# Logistic Regression

$$(17) \text{ starting point} = 3.0754 \quad [X \text{ train}]$$

$$\text{Age: } 57 \times \overset{\text{weight}}{(-0.007)} = -0.4$$

$$\text{Sex: } 1 \times (-1.409) = -1.41$$

$$\vdots$$

$$\text{total score } (z) = 3.0754 + (-0.4) + (-1.41) + \dots$$

$$\text{Cost Function} = -y \cdot \ln(\hat{y}) - (1-y) \cdot \ln(1-\hat{y})$$

$$\text{if } y=1, \text{ cost Function} = -\ln(\hat{y})$$

$$y=0, \text{ cost Function} = -\ln(1-\hat{y})$$

$$\text{Initial weight for Age } (w_1) = 0.01$$

$$\text{Initial weight for Sex } (w_2) = 0.5$$

$$\text{Bias } (b) = 0$$

$$z = (w_1 \cdot \text{Age}) + (w_2 \cdot \text{Sex}) + b$$

$$\text{Row (1)}, z = (0.01 \times 63) + (0.5 \times 1) + 0 = 1.13$$

Sigmoid Formula  $\hat{y} = \frac{1}{1 + e^{-1.13}} \approx 0.75$

Row (2),  $\hat{y} \approx 0.70$

Row (3),  $\hat{y} \approx 0.60$

Cost Prediction =  $-\ln(\text{prediction})$

Row 1 Cost  $\approx 0.28$

Row 2 Cost  $\approx 0.35$

Row 3 Cost  $\approx 0.5$

Total Cost Average

$$= \frac{0.28 + 0.35 + 0.5}{3}$$

$$= 0.38$$

Reducing weight (Gradient Descent)

Gradient =  $(\text{Prediction} - \text{Target}) \times$

For row (1), Prediction ( $\hat{y}$ ) = 0.75

Target ( $y$ ) = 1

Error  $(0.75 - 1) = -0.25$

Gradient For age, Error Age =  $(-0.25)(63)$   
 $= -15.75$

Update weight Age ) New weight = Old weight - ( Learning rate  $\times$  Gradient )

$$\text{update } w_1 = 0.01 \text{ (initial weight)} - (0.001 \times -15.75) \text{ Error Age}$$

$$= 0.02575$$

X test come use update weight latest.

$$z = (w_1 \cdot \text{Age}) + (w_2 \cdot \text{Sex}) + b = -1.94225$$

$$\text{sigmoid function} = \hat{y} = \frac{1}{1 + e^{-1.94225}}$$

$$= 87\%$$

Compare with Y test

$$\text{Accuracy} = \frac{\text{No. Correct Prediction}}{\text{total no. Test row}} \times 100\%$$

\* When Learning stop?

(1) The "hard limit" (Epochs)

max — iteration = " "

(2) The Good enough rule (Convergence)

(3) The safety break (Early stopping)

