

EXAM #3



LIGHT (VOL 3 CHP 1)

- Ray



- light moving as a straight line
- medium (something light travels through)
ex: lens, fluid, mirror, gas
- $c = \text{speed of light} = 2.998 \times 10^8 \text{ m/s}$
(in a vacuum)
- $v = \text{speed of light in medium}$
always $v < c$
- index of refraction (n)

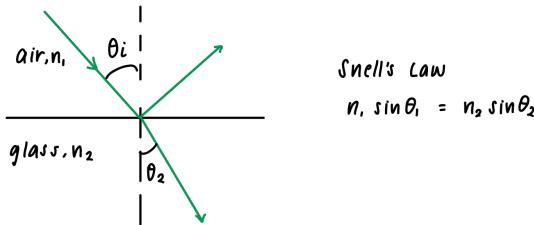
$$n = \frac{c}{v}$$

REFLECTION



$$\theta_i = \theta_R$$

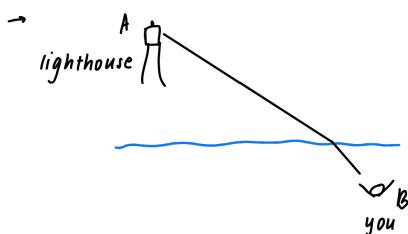
REFRACTION



Snell's Law

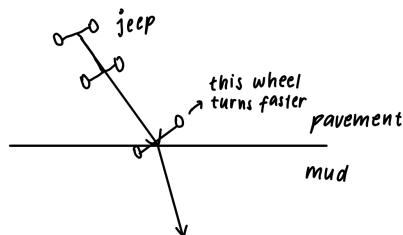
$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

- Why does light change direction?

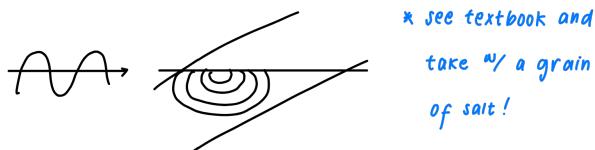


take the path $A \rightarrow B$
that takes the shortest
amount of time.

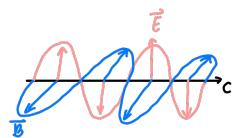
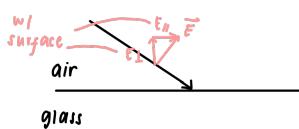
→ another analogy



→ Huygen's Principle



→ [real solution!]



$$\nabla \times \vec{E}_{\text{air}} = - \frac{\partial \vec{B}}{\partial t}$$

$$\epsilon \nabla \vec{E}_{\text{air}} = \rho$$

$$\text{at surface, } \nabla \times \vec{E}_{\text{air}} = \nabla \times \vec{E}_{\text{glass}}$$

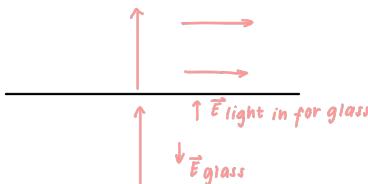
$$E_{\text{air}} \nabla \vec{E}_{\text{air}} = E_{\text{glass}} \nabla \vec{E}_{\text{glass}}$$

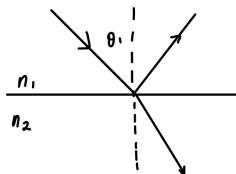
$$E_{\text{glass}||} = E_{\text{air}||}$$

$$E_{\perp \text{glass}} = \frac{E_{\perp \text{air}}}{\epsilon_{\text{glass}}} \quad E_{\perp \text{air}}$$

! Recall PHY-4B ϵ_0 = permittivity of free space (vacuum)

ϵ = permittivity of material, measure of how well a material holds energy from an electric field

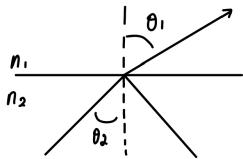




$$n_1 < n_2$$

$$\theta_2 < \theta_1$$

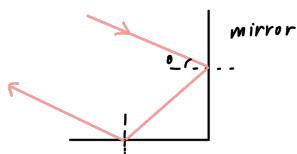
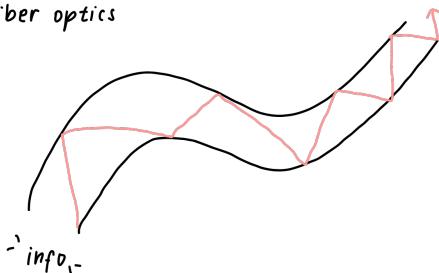
* light bends toward normal
as it passes into higher index
material



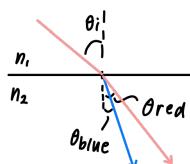
when $\theta_1 = 90^\circ$, $\theta_2 = \theta_{\text{critical angle}}$
↳ total internal reflection

* bends away from normal going
into lower index.

- fiber optics

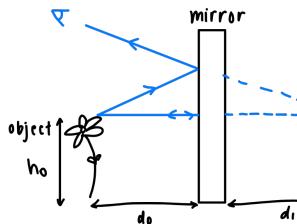


what if n is wavelength dependent?
(for a specific medium)
 $n \uparrow$ as $\lambda \downarrow$ very slightly



GEOMETRIC OPTICS

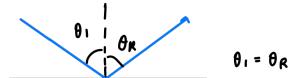
(Vol 2 Chp 2)



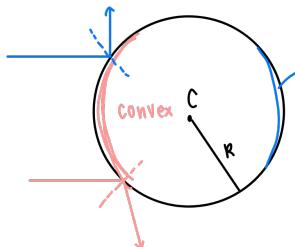
virtual image
--- lens

- appears at the intersection of
means it's where
the ray looks like
it's coming from, but
no actual light is there.

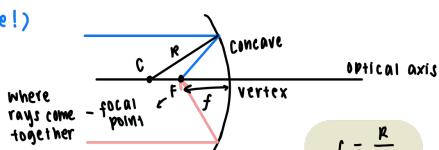
RECALL! LAW OF reflection



CURVED MIRRORS



convex (! like a cave!)



$$f = \frac{R}{2}$$

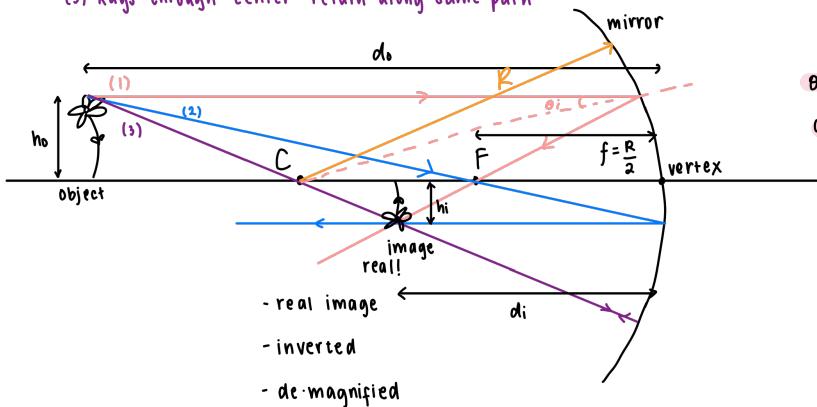
F - focal point

f - focal length

rule: (1) parallel ray goes through focus

(2) Rays through focus go parallel

(3) Rays through center return along same path



$\theta_i \rightarrow$ incident

θ through center
always normal!

mirror equation \rightarrow

$$\frac{1}{d_o} + \frac{1}{d_i} = \frac{1}{f}$$

- Why does mirror reflect light?

The moving electric charge (electrons) makes moving electric field, when light comes in, it vibrates the photon w/ the same speed it comes in & reflect it w/ the same amount & speed of the photon that comes in.

- Why use metal / glass?

It is smooth & protects the reflection.

- $\frac{1}{f} = \frac{1}{d_o} + \frac{1}{d_i}$

Proof for flat mirror!

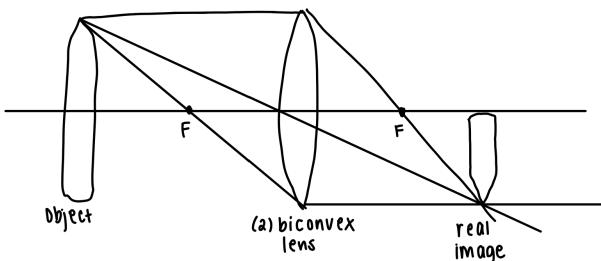
$$f = \frac{R}{2} \text{ and } R \text{ of flat mirror is } \infty$$

which means

$$\begin{aligned} f &= \frac{\infty}{2} = \infty \\ \frac{1}{f} &= \frac{1}{\infty} = 0 \\ \frac{1}{d_o} &= -\frac{1}{d_i} \quad \checkmark \end{aligned}$$

- difference between lens & mirror :

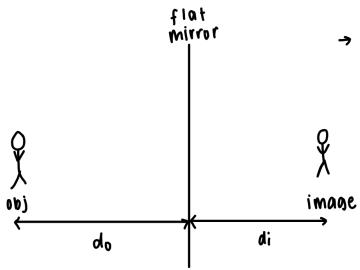
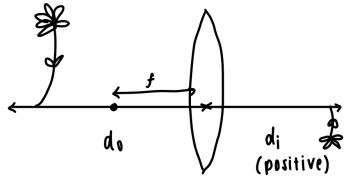
 light goes through → light bounces off.



→ When u put object @ focal point, the lines are parallel.

————— " ————— really close to the lens, u would see the virtual image
(w/in focal length of a lens) behind the object (ex: magnifying glass)
→ lines diverge

THIN LENS

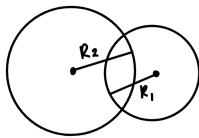


→ images to the right of the mirror d_i is negative (-)

→ for lenses, the material MATTERS A LOT!

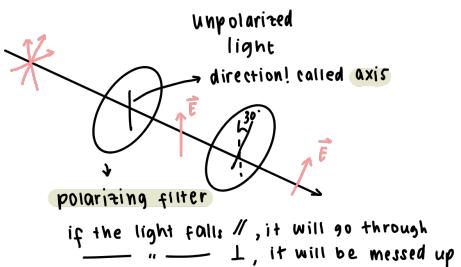
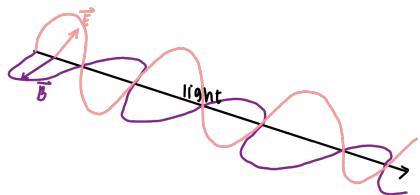
→ if index of refraction is higher, focal length (f) is closer. it bends more
(the ray trace)

→ Lens maker's equation: $\frac{1}{f} = \left(\frac{n_2}{n_1} - 1 \right) \left(\frac{1}{R_1} - \frac{1}{R_2} \right)$

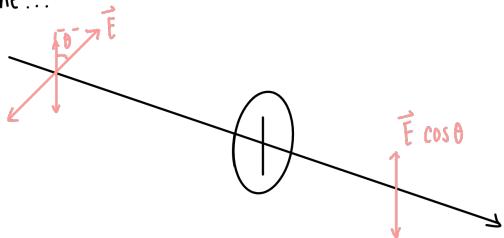


→ our eyes are tuned to be n_2 (eye), n_1 (air) perfect ratio to be able to see w/ air surrounding. that's why we can't really see well underwater & need goggles bcs there are air inside.

POLARIZATION



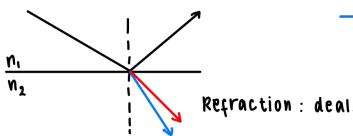
imagine...



→ if u put 2 polarizers, 90° to each other, light cannot come through

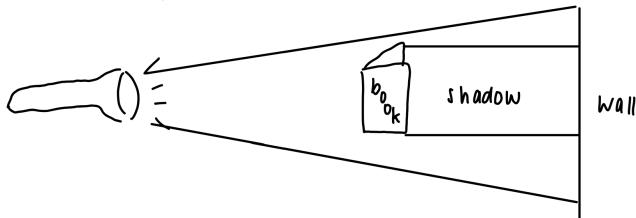
→ if u add another polarizer, 90° , light will still not come through but if u put it in between & angle it, L.G.T.

WAVE NATURE OF LIGHT



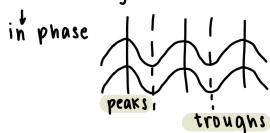
— blue light bends more

Refraction : deals w/ light changing medium

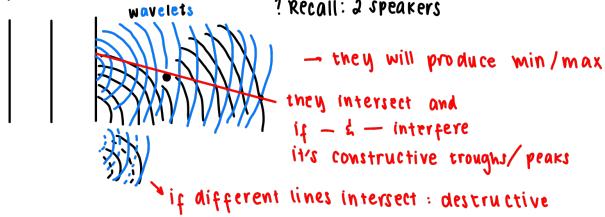


! treat light as a particle

- laser HAS the same wavelength as a strand of hair.

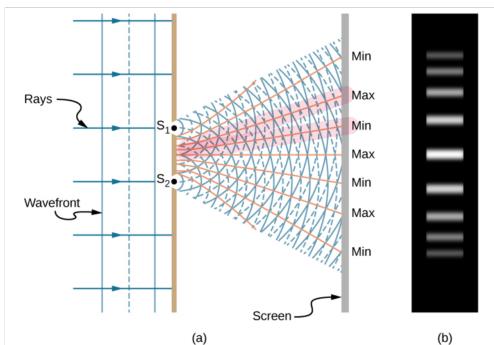


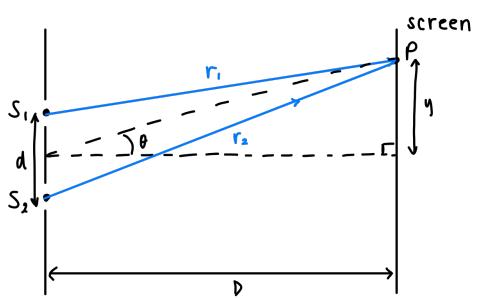
- Huygen's Principle



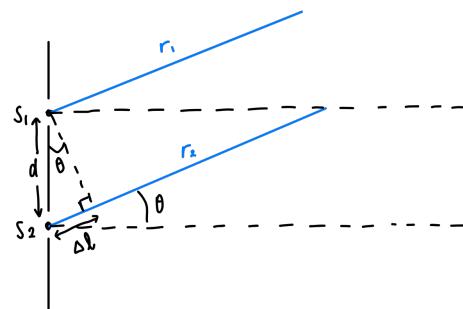
max - all — or all -----

min - — + ---



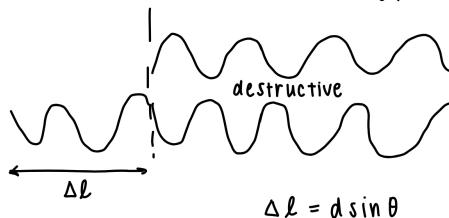


approximate
 $D \gg d$

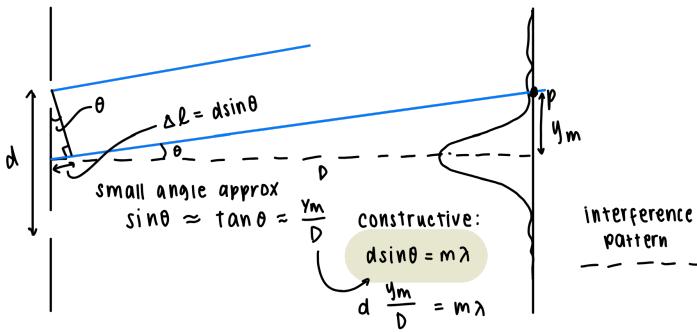


$$\Delta l = m\lambda \text{ constructive}$$

$$\Delta l = \left(m + \frac{1}{2}\right)\lambda \text{ destructive}$$



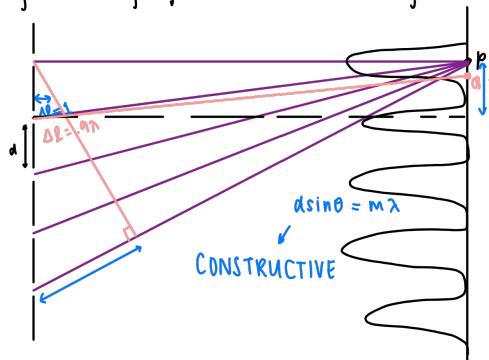
$$\Delta l = d \sin \theta$$



$$d = \frac{m\lambda D}{y_m}$$

- ray will always go \perp to the wavelength

MULTIPLE SLIT



constructive interference
* sharper peaks

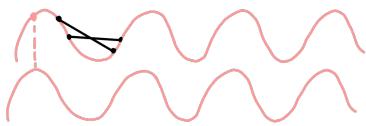
the more slits u have,
the finer the light will become

At point P : constructive



→ when you pass monochromatic light through a diffraction = ??

at point A



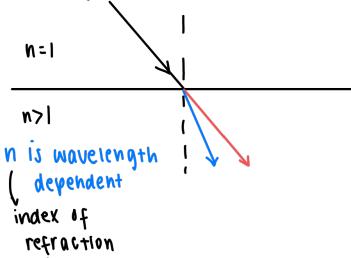
→ when you pass white light through a diffraction = multiple colors come out.

Diffraction

- light interferes as it passes through slits

Refraction

- light changes direction as it passes through a substance



index of refraction

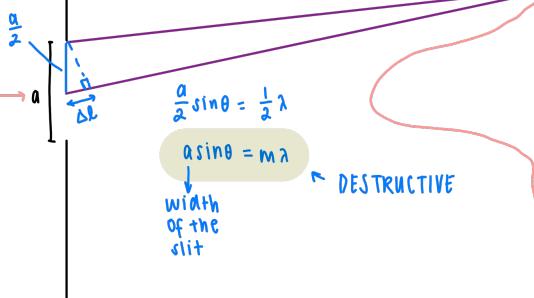
$m=2$

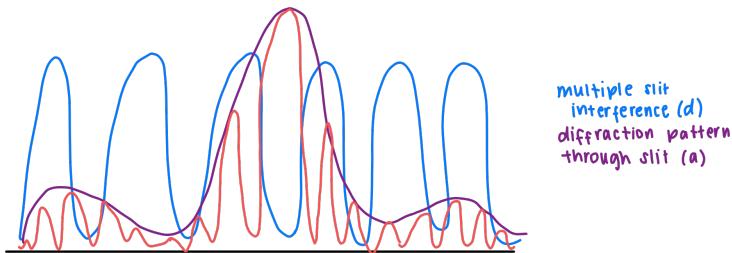
m is the "order" of the destructive interference

as it passes through single slit, there will be infinite little sources of destructive interference.

→ find where they are destructive interfering

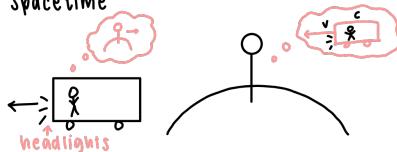
SINGLE SLIT





RELATIVITY

→ spacetime



who's moving?

disagree: they say the other ones moving

agree:

- relative speed

- feel stationary because

NO acceleration

- the laws of physics apply

→ "WRT": with respect to

→ measure c (speed of light) = $3 \times 10^8 \text{ m/s}$

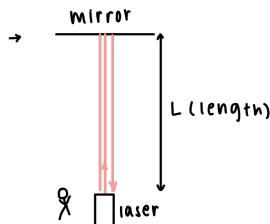
→ Newton says $c+v$ is possible

→ NOW, we have the technology to measure $c = \underline{3 \times 10^8 \text{ m/s}}$

constant, everyone agrees

$$\rightarrow \text{in E&M, } c = \frac{1}{\sqrt{\mu_0 \epsilon_0}} \quad \left[\text{speed} = \frac{\text{distance}}{\text{time}} \right]$$

→ reference frame: in the ex/ , it is the box where the people feel stationary.



for person who is stationary.

$$\Delta t' = \frac{2L}{c}$$

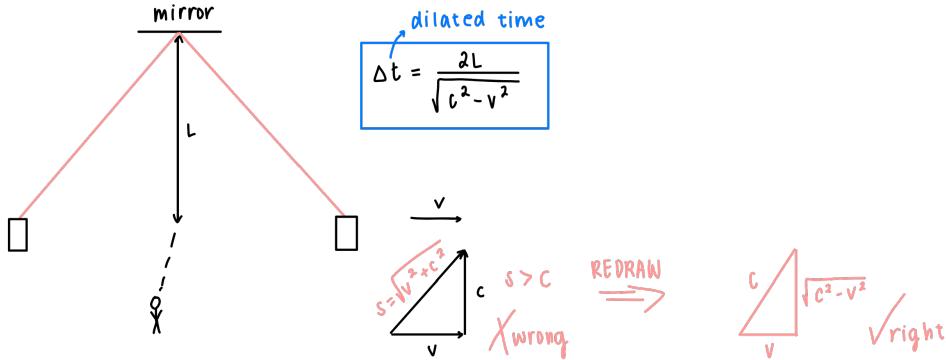
↓ (proper time)

time light travels, measured
by observer stationary WRT laser

[Δt : proper time]

→ time interval between events
that occur in same location

→ if moving (*e.g.*: train moving)



$$\rightarrow c \Delta t = 2L = \Delta t \sqrt{c^2 - v^2}$$

$$\Delta t = \frac{c \Delta t}{\sqrt{c^2 - v^2}} = \frac{\cancel{c} \Delta t}{\cancel{c} \sqrt{1 - \frac{v^2}{c^2}}}$$

$$\Delta t = \frac{\Delta t}{\sqrt{1 - v^2/c^2}}$$

$$\Delta t = \Delta \tau \gamma$$

define Lorentz Factor

$$\gamma = \frac{1}{\sqrt{1 - v^2/c^2}}$$

→ as $\gamma \uparrow$, the Δt has to \downarrow

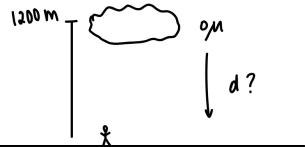
so, the person stationary outside watching the whole experiment happen, sees the other person in the train moves in slow-mo.

→ as you approach speed of light ($\gamma \uparrow$), $\Delta t \downarrow$ longer

↳ people will view you moving so slow

you will see the people moving slow as well.

→ *e.g.*: muon $\mu = \mu_0$ mon



$$\approx 2.2 \mu s$$

$$\text{assume: } v = c = 3 \times 10^8 \frac{m}{s}$$

$$d = vt \quad \text{classical mechanics}$$

$$= (3 \times 10^8 \frac{m}{s})(2.2 \times 10^{-6} s) = 660 m$$

$\Delta t =$ proper time

$\Delta t =$ dilated time

L_0 = proper length

→ distance measured by an observer at rest WRT both end points.

→ assume: $v = 0.9c$

$$\gamma = \frac{1}{\sqrt{1 - 0.9^2}} = 2.29$$

outside observer (stationary) will see time dilated by a ratio of 2.29

dilated time $\Delta t = \gamma \Delta \tau$
 how long does lifetime of mon, WRT the mon itself
 observer on Earth see the mon live?
 $= (2.29)(2.2 \times 10^{-6} \text{ s}) = 5 \times 10^{-6} \text{ s}$

∴ the travel time of the mon is longer (what the observer sees)

↓ events in the reference frame

mon aging (life expectancy) longer

the mon still feels the same v & time

$$d = v \Delta t = (0.9)(3 \times 10^8 \text{ m/s})(5 \times 10^{-6} \text{ s}) \\ = 1350 \text{ m}$$

→ ex:

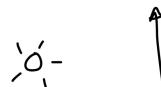


P_1 → $v = 0.9c$
 fly 2 years
 2 sec 1 aging in slow-mo



go back 2 years
 $0.9c$ ← P_1

1 sec 2 very much older



analysis doesn't work until acceleration is done

since acceleration is not in the stationary reference frame

[continuation of the analysis]

mon's POV

$$\Delta \tau = 2.2 \times 10^{-6} \text{ s} \quad (\text{proper time})$$

$$v = 0.9c$$

$$L = v \Delta \tau$$

$$= (0.9)(3 \times 10^8 \text{ m/s})(2.2 \times 10^{-6} \text{ s})$$

$$= 594 \text{ m}$$

∴ mon sees the Earth is compressed, distance it travels get compressed & the person gets shorter

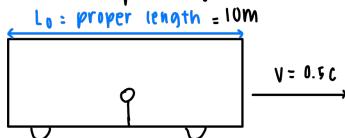
→ they have to agree in v (speed), so since $v = \frac{\text{distance}}{\text{time}}$, needs to change if one change

→ the closer you are to the speed of light, then what's gonna happen to you is like the you.

→ you see people shorter since they are condensed.

→ people see you go in slow-mo.

[another example ...]



* both people agree on V

$$V = \frac{L_0}{\Delta t} = \frac{L}{\Delta \tau}$$

[recall $\Delta t = \gamma \Delta \tau$]

$$\frac{L_0}{\gamma \Delta \tau} = \frac{L}{\Delta \tau}$$



$$L = (10\text{m}) \sqrt{1 - (0.5)^2} < 10\text{m}$$

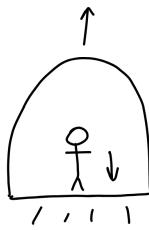
the person sees the train
squished, shorter

$$L = \frac{L_0}{\gamma} \quad [\text{recall } \gamma = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}}]$$

$$L = L_0 \sqrt{1 - \frac{v^2}{c^2}}$$

length of the
object in moving frame

EQUIVALENCE PRINCIPLE



both persons are
experiencing the same
laws of physics,
but the CAUSE is
different!

→ acceleration due to gravity is equivalent to acceleration due to motion.

$$90^\circ = \overbrace{\quad\quad\quad}^{\text{dashed}}$$



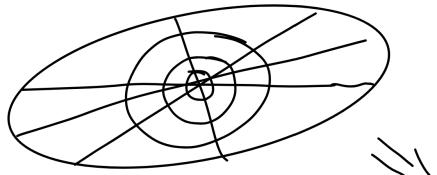
why does the mass
know to fall to the
moon/gravitational source?

think of trampoline base

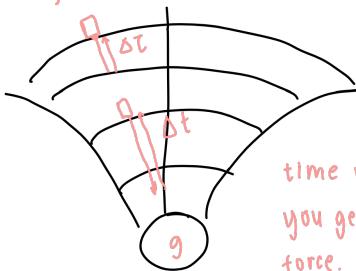


if we put mass

the ball will want to go straight
but it is attracted to the dip
and continue to go around it



if we put laser



$$\Delta t > \Delta T$$

time is slower when
you get to gravitational
force.
faster, further away.