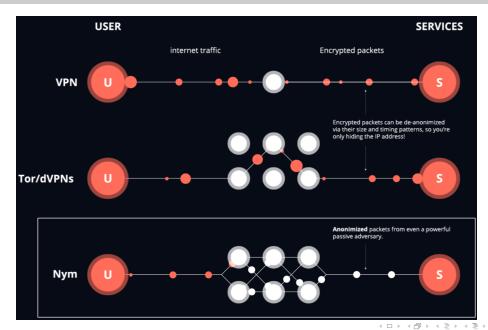
Sphinx Packets

Decentralized Header Construction

Aurélien Chassagne

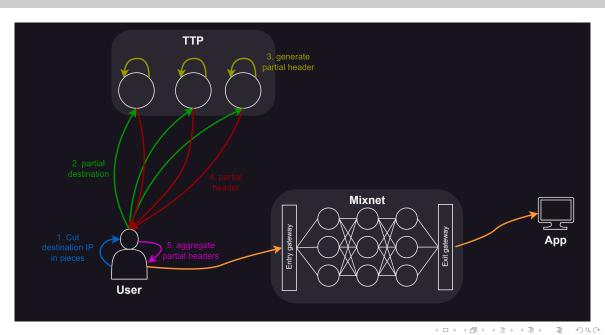
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Schema overview



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Desired properties

Generic properties

- Correctness: schema works without adversary
- Compactness: Minimal overhead
- **Efficiency**: Easy and fast to compute (e.g. XOR, hash, exponentiation,...)

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- Depends on the mixnode
 - Forward / reply Undistinguishibility: Cannot distinguish forward from reply packet
 - Replay attack resistant:: Cannot reused previous packet

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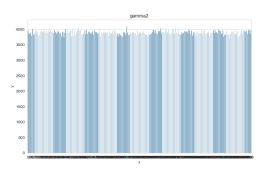
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Desired properties

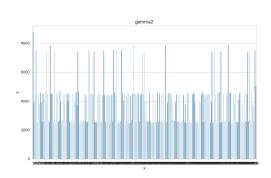
- Generic properties
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 - Forward / reply Undistinguishibility: Cannot distinguish forward from reply packet
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- Depends on the header
 - **Integrity**: Maximum size path
 - Wrap-resistance: Unable to increase the intial path
 - Unlinkability: Cannot link incoming and outgoing packet from a mixnode

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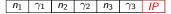
Original schema

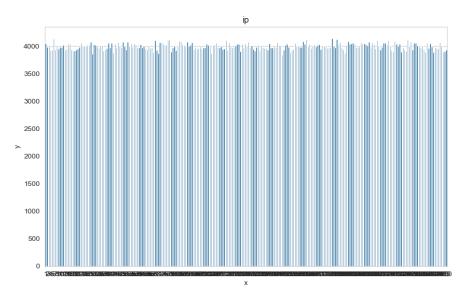


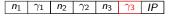
My schema

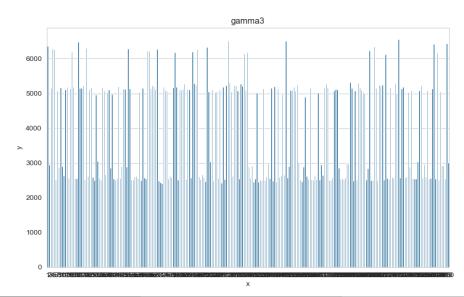


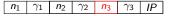
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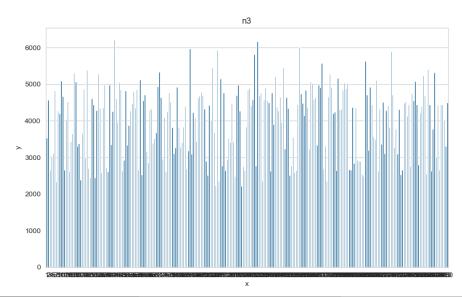


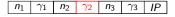


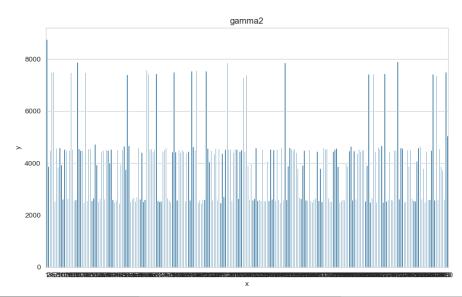


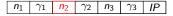


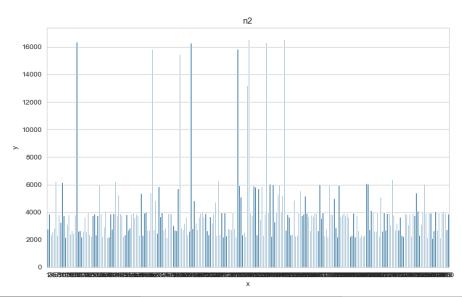


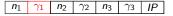


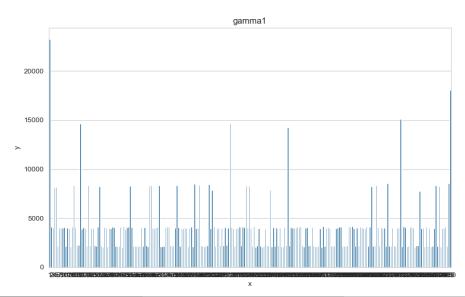




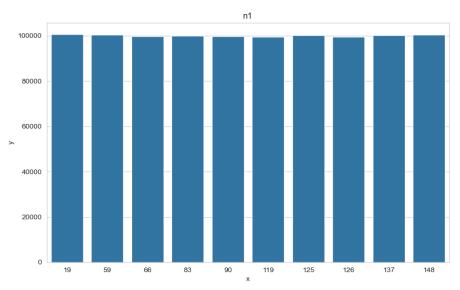






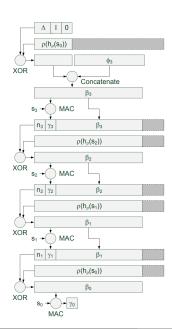


 n_1 γ_1 n_2 γ_2 n_3 γ_3 IP

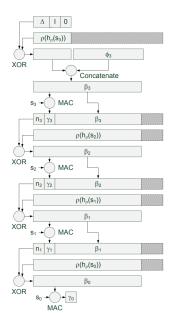


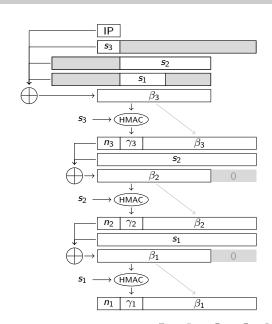
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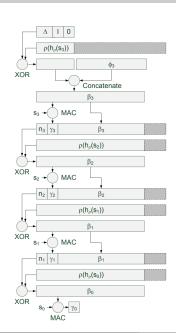
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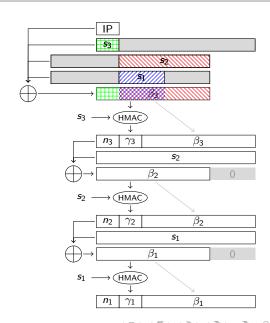


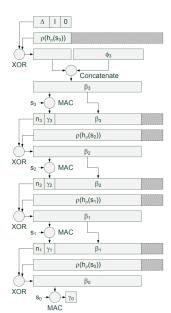
Aurélien Chassagne Sphinx Packets February 18, 2025 13/16

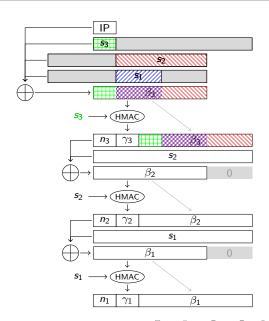


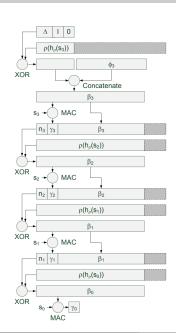


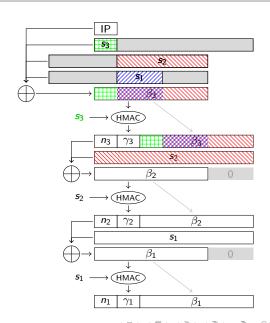


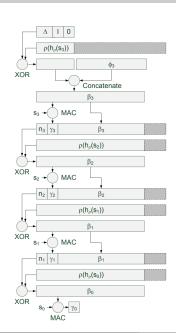


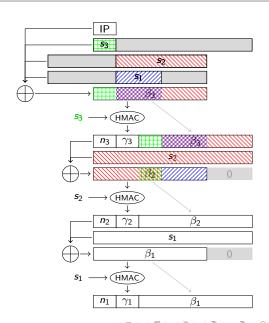


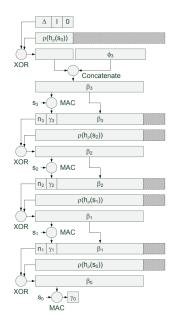


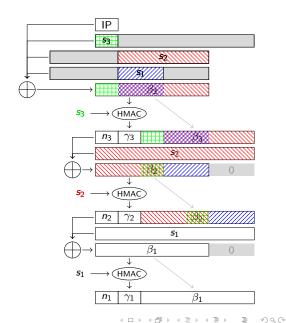


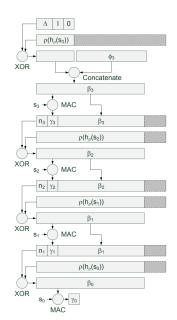


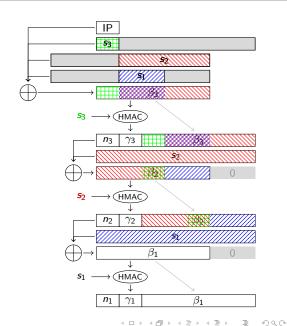


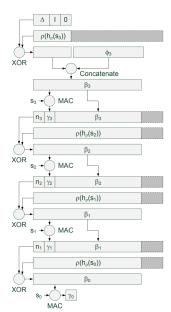


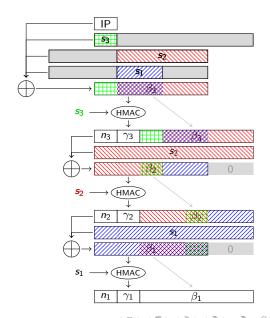


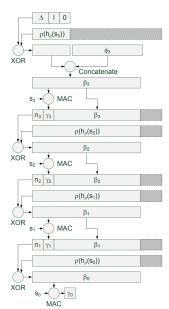


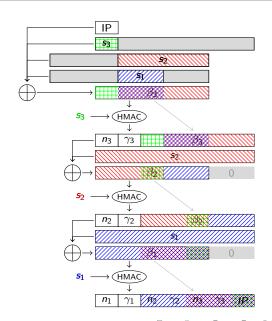


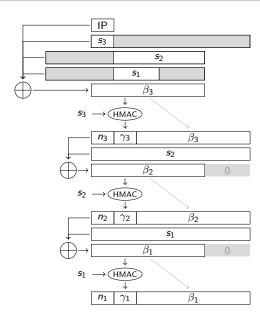




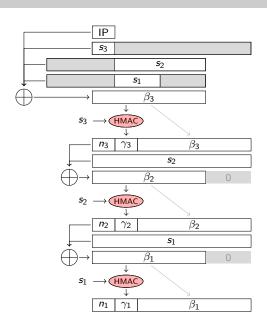






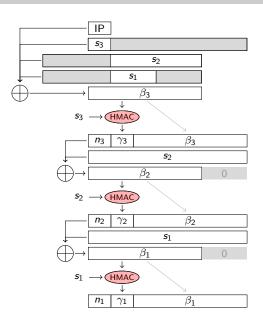


Main problem: Decentralizing a Hash?



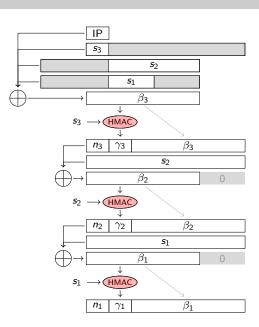
Main problem: Decentralizing a Hash?

 Need homomorphic properties to split computation and aggregate results.



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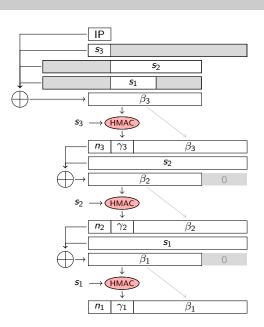
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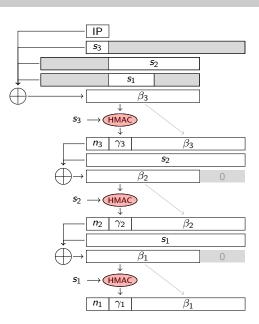
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 - ② ElGamal
 - 3 Paillier



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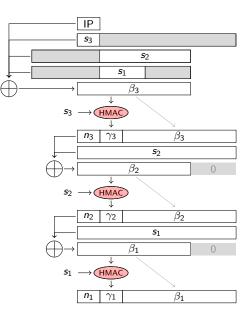
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$$\mathcal{E}(m_1) \cdot \mathcal{E}(m_2) = (g^{m_1} r_1^n) (g^{m_2} r_2^n) \mod n^2$$

$$= g^{m_1 + m_2} (r_1 r_2)^n \mod n^2$$

$$= \mathcal{E}(m_1 + m_2).$$

Problem: Mix of different operations... order matters!



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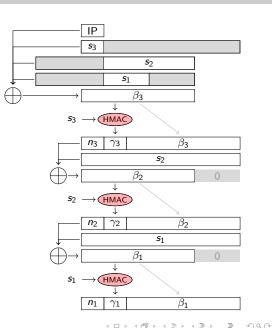
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$$\mathcal{E}(m_1) \cdot \mathcal{E}(m_2) = (g^{r_1}, m_1 \cdot h^{r_1})(g^{r_2}, m_2 \cdot h^{r_2})$$
$$= (g^{r_1 + r_2}, (m_1 \cdot m_2)h^{r_1 + r_2})$$
$$= \mathcal{E}(m_1 \cdot m_2)$$

3 Paillier

Limitation: Increase ciphertext size...



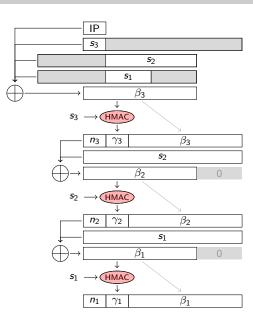
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$$\mathcal{E}(m_1) \cdot \mathcal{E}(m_2) = m_1^e m_2^e \mod n$$

= $(m_1 m_2)^e \mod n$
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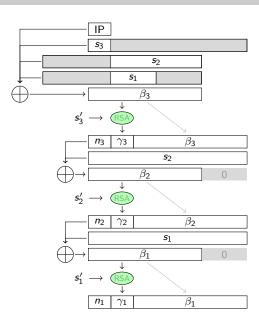


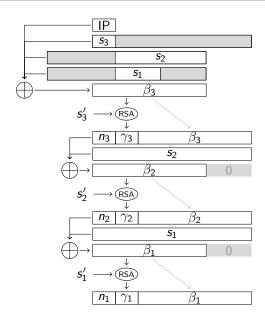
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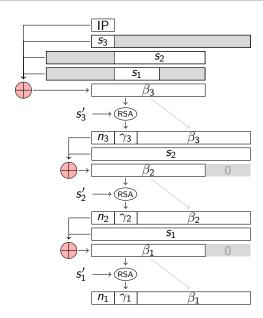
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Selected solution: RSA for integrity tag

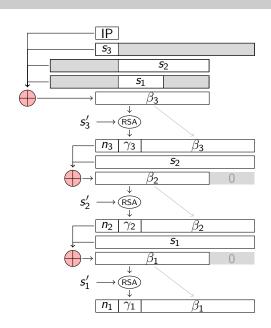
NB: s_i is different for each TTP but RSA required the same e... Thus, create a new shared secret s_i' common to all TTP







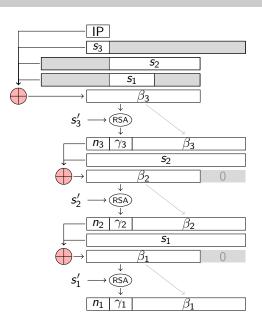
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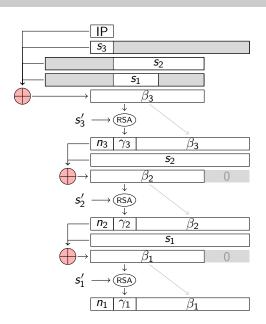
Since we use **RSA** for integrity tag γ_i

$$\mathcal{E}(m_1) \cdot \mathcal{E}(m_2) = m_1^e m_2^e \mod n$$

$$= (m_1 m_2)^e \mod n$$

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Modular multiplication of integrity tags gives integrity tag of headers' modular product.



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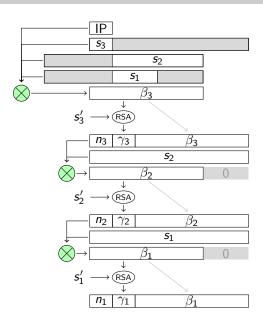
$$\mathcal{E}(m_1) \cdot \mathcal{E}(m_2) = m_1^e m_2^e \mod n$$

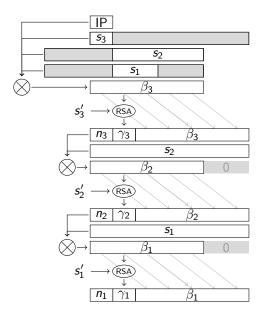
$$= (m_1 m_2)^e \mod n$$

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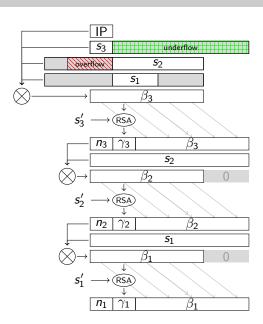
Modular multiplication of integrity tags gives integrity tag of headers' modular product.

Thus, header elements must be combined via modular multiplication rather than XOR.

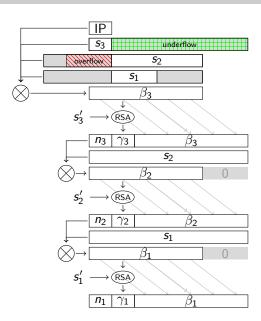




• Current Challenge: Overflow issues



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- Handling these issues is challenging.
 It may lead to information loss
 (further research is required).



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- Current Challenge: Overflow issues
- Handling these issues is challenging.
 It may lead to information loss
 (further research is required).
- Proposed solution: Simplify by dividing data into small chunks and processing each chunk modulo its size.

