

STUDY AND TEST A MACHINE LEARNING/NEURAL NETWORK LIBRARY IN C++

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Introduction

- Study mlpack and OpenNN libraries

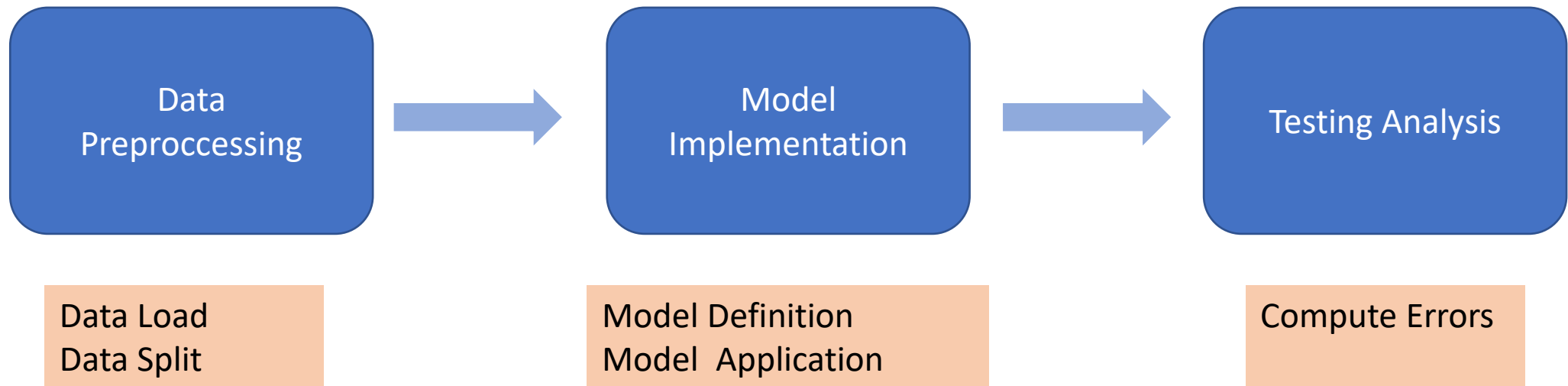


opennn
neural networks

- Compared with Python options: Scikit and Tensorflow



Machine Learning Workflow



Data Preprocessing

Data stored in Armadillo library Matrix and Vector

Provided data class-> Load and save matrices and models
-> Split function

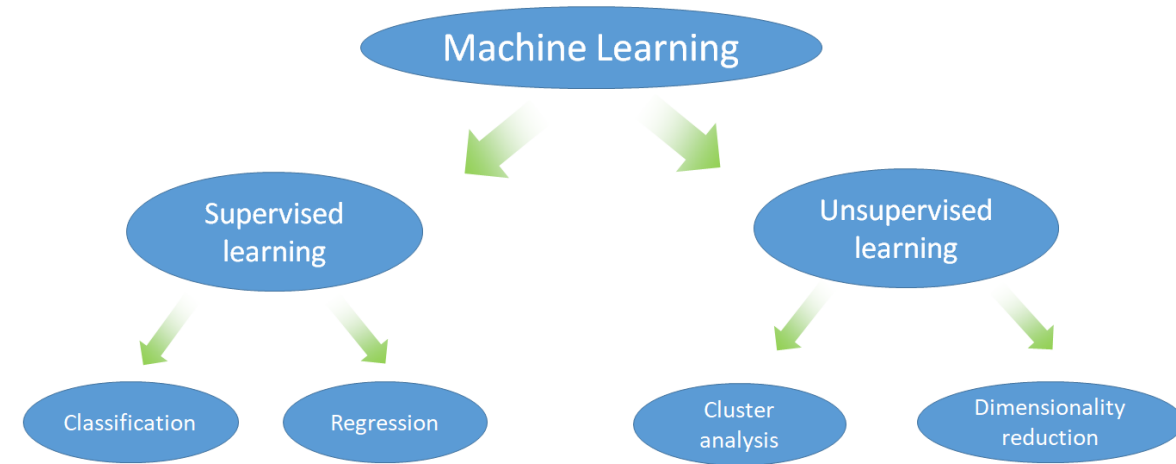
Data Format ->Column-major matrix
->No header data included
->Converts label to one-hot encoding previously



Model Implementation

Each algorithm has associated a class

- >Instant definition
- >Methods to change default parameters
- >Train()
- >Apply()



Test Analysis

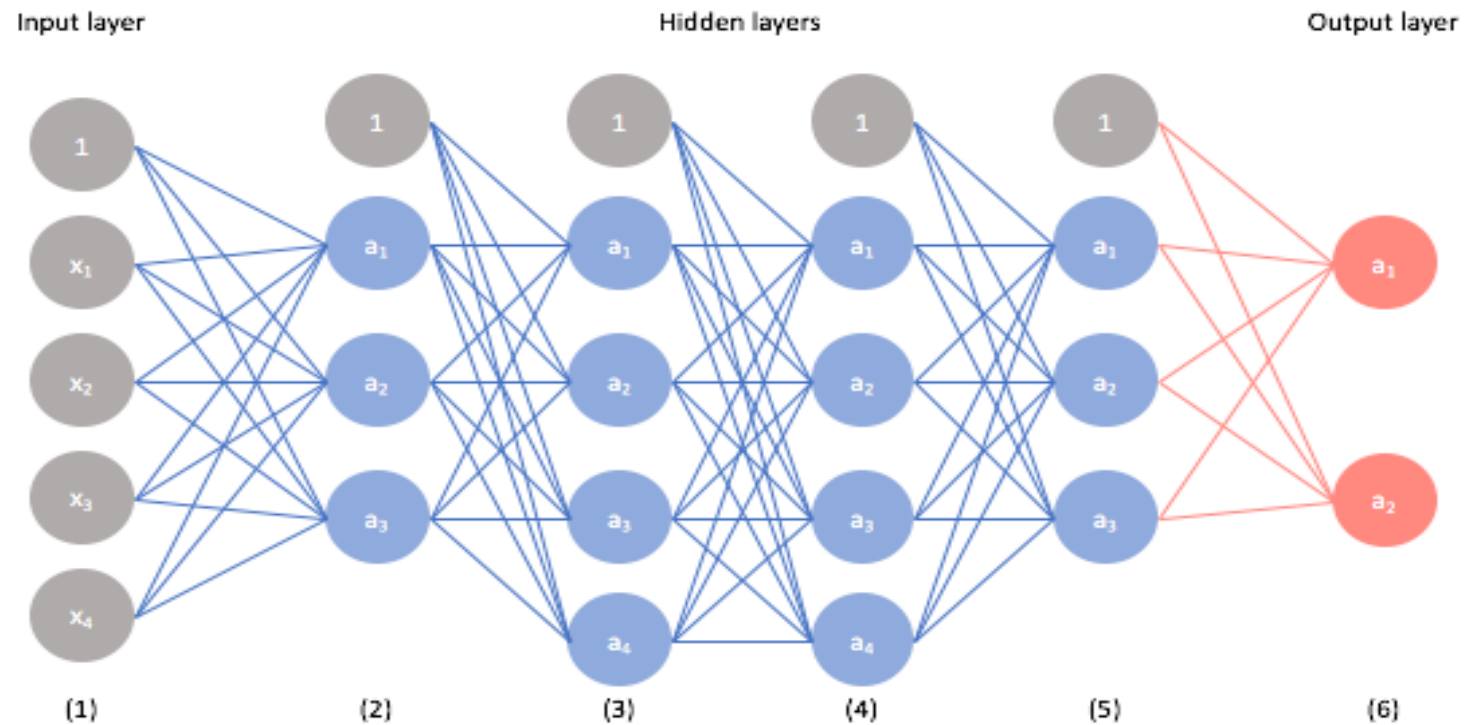
Each algorithm their function -> ComputeError()

->ComputeAccuraccy()

From data class->ConfusionMatrix()



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Data Preprocessing

Data stored in dataset class

- Admits headers
- Specify column uses ->Target,Input or Unused
- Extract scale descriptives-> Mean, Sd, Max and Min
- Split randomly or sequentially->Training,validation and test set

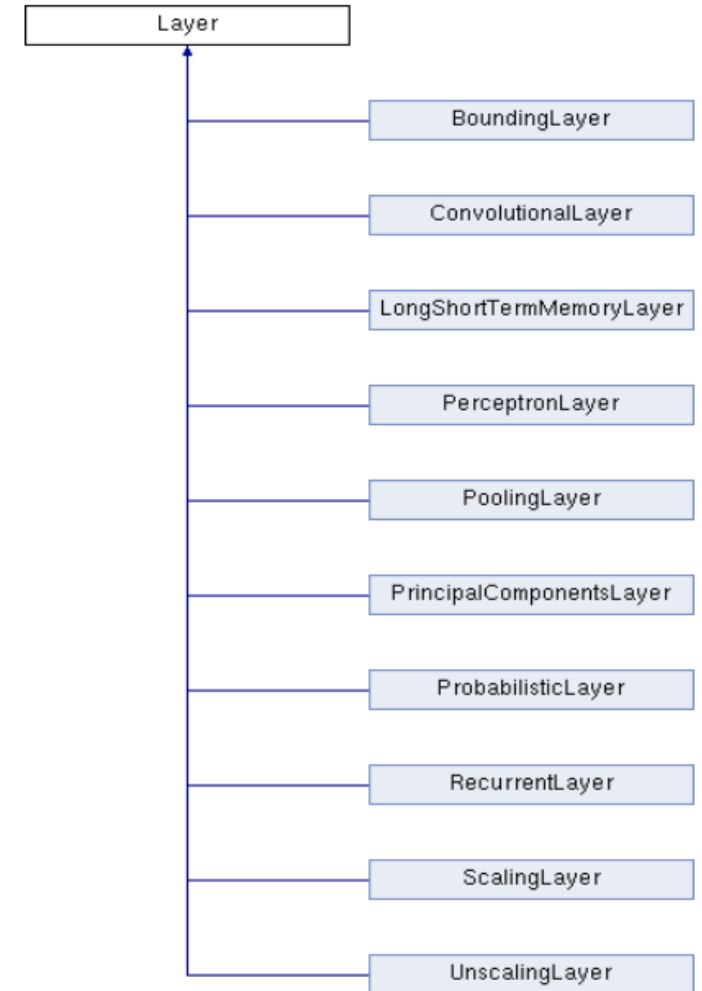
Model Implementation

NeuralNetwork class

Construction by sequential addition of layers

Predefined models

- >Approximation: Perceptron+Linear Activation
- >Classification: Perceptron +Softmax Activation
- >Forecast: LongShortTermMemory



Model Implementation

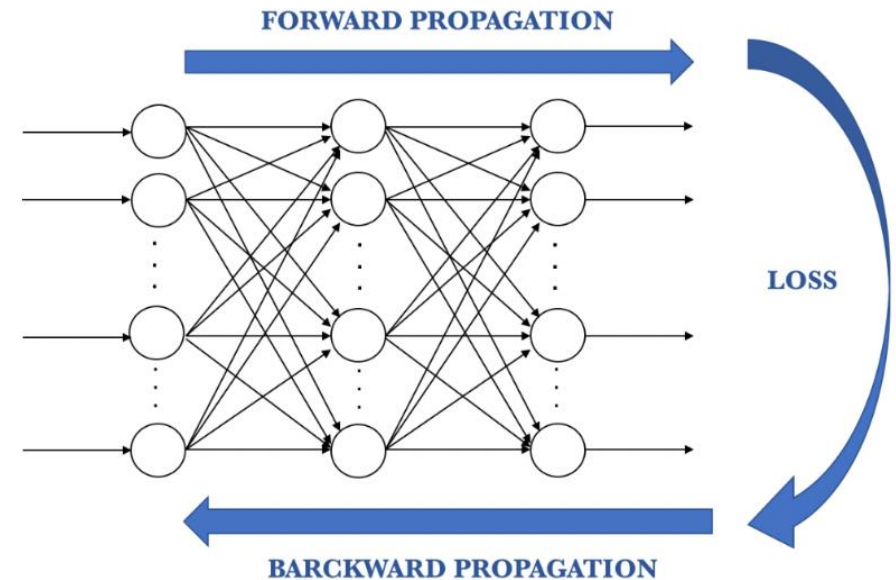
TrainingStrategy class

- LossMethod Class
- OptimizationMethod Class

perform_training()

ModelSelection class

- OrderSelectionMethod->Vary neurons
- InputsSelectionMethod->Vary input subset



Test Analysis

TestingAnalysis class

Perform 4 kinds of Analysis 

Binary classification rates
Kolmogorov-Smirnov analysis
Linear regression análisis
ROC curve analysis

Problem: Defined Results.save() function, but not implemented

Testing



Regression

Linear
Regression



Least-Angle
Regression

Simple regression problem
Swedish Auto Insurance



63 observations

- # Claims
- Total payments

Multivariable regression
Boston House Price



506 observations

Goal: Predict House Price

	CRIM	ZN	INDUS	CHAS	NOX	RM	AGE	DIS	RAD	TAX	PTRATIO	B	LSTAT
0	0.00632	18.0	2.31	0.0	0.538	6.575	65.2	4.0900	1.0	296.0	15.3	396.90	4.98
1	0.02731	0.0	7.07	0.0	0.469	6.421	78.9	4.9671	2.0	242.0	17.8	396.90	9.14
2	0.02729	0.0	7.07	0.0	0.469	7.185	61.1	4.9671	2.0	242.0	17.8	392.83	4.03
3	0.03237	0.0	2.18	0.0	0.458	6.998	45.8	6.0622	3.0	222.0	18.7	394.63	2.94
4	0.06905	0.0	2.18	0.0	0.458	7.147	54.2	6.0622	3.0	222.0	18.7	396.90	5.33

Regression

Linear
Regression



Least-Angle
Regression

- Loading

```
data::Load("../Data/Swedish_auto.txt", predictors);  
responses=arma::conv_to<arma::rowvec>::from( predictors.row(predictors.n_rows-1));  
predictors=predictors(0,arma::span::all);
```

- Splitting

```
double testratio;  
std::cout<<"Introduce the ratio of the Test set ";  
std::cin>>testratio;  
data::Split(predictors,responses,traindata,testdata,trainresponses,testresponses,testratio);  
std::cout<<"Size Train"<<arma::size(traindata)<<" Size Test"<<arma::size(testdata)<<std::endl;
```

- Algorithm definition

Linear Regressor

```
LinearRegression lr(traindata, trainresponses,0.2,true );
```

Least-Angle Regressor

```
LARS lars(traindata, trainresponses);
```

Regression- Results

Linear Regression

Swedish Auto
Insurance

```
Begin linear regression algorithm
Parameters obtained
  22.2037
   3.3262
Be aware that the models includes intercept
Training Regression L2 square error :1324.89
Test Regression L2 square error :957.447
Time required: 1273microseconds
```

Boston House
Price

```
Begin linear regression algorithm
Parameters obtained
 13.6664
 -0.1119
  0.0480
 -0.0217
  0.9489
 -6.2955
  5.0400
 -0.0148
 -1.1969
  0.2322
 -0.0123
 -0.5869
  0.0133
 -0.3947

Be aware that the models includes intercept
Training Regression L2 square error :21.0062
Test Regression L2 square error :33.6281
Time required: 58834microseconds
```

Least-Angle Regression

```
Begin least-angle regression algorithm
Beta obtained
  3.9934
Training Regression L2 square error :1522.84
Test Regression L2 square error :1277.87
Time required: 435microseconds
```

```
Begin least-angle regression algorithm
Beta obtained
 -0.1074
  0.0499
 -0.0341
  0.9554
 -1.0519
  5.8209
 -0.0157
 -1.0028
  0.1792
 -0.0108
 -0.3780
  0.0155
 -0.3538

Training Regression L2 square error :21.9927
Test Regression L2 square error :34.8154
Time required: 61118microseconds
```

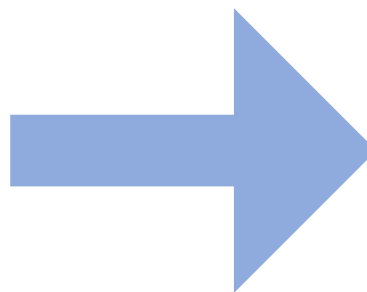
Clustering + Transformation

Iris dataset



150 observations

- Sepal length in cm
- Sepal width in cm
- Petal length in cm
- Petal width in cm



K-Means

```
size_t clusters;  
std::cout<<"Introduce the number of cluster to search ";  
std::cin>>clusters;  
  
arma::Row<size_t> assignments;  
arma::mat centroids;  
  
KMeans<> k;  
k.Cluster(TrainData, clusters, assignments, centroids);
```

PCA

```
PCA<> p;  
p.Apply(InputData, 2);
```


Classification



Logistic
Regression

Banknote
Authentication

1372 observations

Wavelet Transformed image

- Variance
- Skewness
- Kurtosis
- Entropy

Result

```
Parameters obtained
6.8029 -7.1602 -3.9052 -4.8844 -0.6252

Training result
Error : 22.9591
Accuracy : 98.725
Test result
Error : 2.21238
Accuracy : 99.2701
Confusion matrix :
1.4800e+02      0
2.0000e+00 1.2400e+02
Time required: 22287microseconds
```

Perceptron

Iris dataset

```
Perceptron<> model(TrainData,TrainLabel.row(0),classes,1000);
model.Classify(TestData, predictedLabels);
```

Result

```
Introduce the ratio of the Test set 0.2
Introduce the number of classes 3
Confusion Matrix:
7.0000      0      0
0 11.0000      0
0      0 11.0000
Time required: 32433microseconds
```

Classification

Wine
Quality

Adaboost

Perceptron/Decision tree

	fixed acidity	volatile acidity	citric acid	residual sugar	chlorides	free sulfur dioxide	total sulfur dioxide	density	pH	sulphates	alcohol	quality
0	7.4	0.70	0.00	1.9	0.076	11.0	34.0	0.9978	3.51	0.56	9.4	5
1	7.8	0.88	0.00	2.6	0.098	25.0	67.0	0.9968	3.20	0.68	9.8	5
2	7.8	0.76	0.04	2.3	0.092	15.0	54.0	0.9970	3.26	0.65	9.8	5
3	11.2	0.28	0.56	1.9	0.075	17.0	60.0	0.9980	3.16	0.58	9.8	6
4	7.4	0.70	0.00	1.9	0.076	11.0	34.0	0.9978	3.51	0.56	9.4	5

```
Perceptron<> p(TrainData, TrainLabel.row(0), 10);
AdaBoost<> adab(TrainData, TrainLabel.row(0), 10, p);

adab.Classify(TestData, predictions, probabilities);

data::ConfusionMatrix(predictions, TestLabel, Confusion, 7);
```

Result



```
Introduce the ratio of the Test set 0.3
Size Train11x4898 Size Label1x4898
Test result
Confusion matrix :
      0      0      0      0      0      0      0      8.0000e+00
      0      0      0      0      0      0      0      1.0000e+00
      0      0      0      0      0      0      0      0
      0      0      0      0      0      0      0      0
      0      0      0      1.0000e+00  4.0000e+00  3.0000e+00  2.0000e+00
      0      0      0      4.0000e+00  2.8000e+01  2.6200e+02  3.7500e+02
      0      0      0      4.0000e+00  2.3000e+01  1.8500e+02  2.3000e+02
Time required: 129612595microseconds
```

SVM

```
LinearSVM svm(TrainData, TrainLabel, 7);

parameters=svm.Parameters();
std::cout<<"Parameters obtained"<<std::endl;
std::cout<<parameters<<std::endl;

train_accu=svm.ComputeAccuracy(TrainData, TrainLabel);
test_accu=svm.ComputeAccuracy(TestData, TestLabel);
svm.Classify(TestData, predictions);

data::ConfusionMatrix(predictions, TestLabel, Confusion, 7);
```

Result



```
Training result
Accuracy : 0.459556
Test result
Accuracy : 0.405516
Confusion matrix :
      0      0      0      0      0      0      0
      0      0      0      0      0      0      0
      0      0      0      0      0      0      0
      0      0      0      0      0      0      0
      0      0      0      0      0      0      0
      0      0      0      7.0000e+00  4.0000e+01  3.0400e+02  3.9700e+02
Time required: 289209microseconds
```

Comparison



Both are class oriented

Multivariate Regression	Test error	Time elapsed
mlpack	33,63\$	58834ms
Scikit-learn	16,57\$	578ms

Logistic Regression	Test accuracy	Time elapsed	Confusion matrix	
mlpack	99,27%	22287ms	148 2	0 124
Scikit-learn	99,18%	440ms	146 2	2 124

SVM	Test accuracy	Time elapsed
mlpack	40,55%	58834ms
Scikit-learn	45,11%	2138ms

Testing



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neural networks

Multi-variate Regression

Boston House
Price

- Data Preprocessing

```
DataSet data_set("../Data/Boston.csv",',',true);  
data_set.set_columns_uses({"UnusedVariable","Input","Input","Input","Input","Input","Input",  
  
const size_t inputs_number = data_set.get_input_variables_number();  
const size_t outputs_number = data_set.get_target_variables_number();  
const Vector<Descriptives> inputs_descriptives = data_set.scale_inputs_minimum_maximum();  
const Vector<Descriptives> targets_descriptives = data_set.scale_targets_minimum_maximum();  
  
data_set.split_instances_random();
```

Multi-variate Regression

Boston
House Price

- Model

```
NeuralNetwork neural_network;

// Scaling layer

ScalingLayer* scaling_layer = new ScalingLayer(inputs_number);
scaling_layer->set_descriptives(inputs_descriptives);
//scaling_layer_pointer->set_scaling_methods(ScalingLayer::NoScaling);

neural_network.add_layer(scaling_layer);

const size_t scaling_layer_outputs_dimensions = scaling_layer->get_neurons_number();
//Perceptron block

PerceptronLayer* perceptron_layer_1 = new PerceptronLayer(scaling_layer_outputs_dimensions, 64);
perceptron_layer_1->set_activation_function(PerceptronLayer::RectifiedLinear);
neural_network.add_layer(perceptron_layer_1);

const size_t perceptron_layer_1_outputs = perceptron_layer_1->get_neurons_number();

PerceptronLayer* perceptron_layer_2 = new PerceptronLayer(perceptron_layer_1_outputs, 64);
perceptron_layer_2->set_activation_function(PerceptronLayer::RectifiedLinear);
neural_network.add_layer(perceptron_layer_2);

const size_t perceptron_layer_2_outputs = perceptron_layer_2->get_neurons_number();

PerceptronLayer* perceptron_layer_3 = new PerceptronLayer(perceptron_layer_2_outputs, 1);
neural_network.add_layer(perceptron_layer_3);

const size_t perceptron_layer_3_outputs = perceptron_layer_3->get_neurons_number();

UnscalingLayer* unscaling_layer_pointer = new UnscalingLayer(perceptron_layer_3_outputs);
neural_network.add_layer(unscaling_layer_pointer);

neural_network.print_summary();
```

Scaler layer



Perceptron
block



Perceptron
block



Unscaler layer

Multi-variate Regression

Boston House
Price

- Training Strategy

```
// Training strategy
TrainingStrategy training_strategy(&neural_network, &data_set);
training_strategy.set_optimization_method(TrainingStrategy::OptimizationMethod::STOCHASTIC_GRADIENT_DESCENT);
training_strategy.set_loss_method(TrainingStrategy::LossMethod::MEAN_SQUARED_ERROR);
training_strategy.get_loss_index_pointer()->set_regularization_method(LossIndex::RegularizationMethod::NoRegularization);

StochasticGradientDescent* sgd_pointer = training_strategy.get_stochastic_gradient_descent_pointer();

sgd_pointer->set_initial_learning_rate(1.0e-3);
sgd_pointer->set_momentum(0.9);
sgd_pointer->set_minimum_loss_increase(1.0e-6);
sgd_pointer->set_maximum_epochs_number(1000);
sgd_pointer->set_display_period(100);
sgd_pointer->set_maximum_time(1800);

const OptimizationAlgorithm::Results training_strategy_results = training_strategy.perform_training();
```

SGD

Training



```
Training with stochastic gradient descent...
Epoch 0;
Parameters norm: 71.7789
Training loss: 1.62446
Batch size: 1000
Gradient norm: 0.410514
Learning rate: 0.001
Elapsed time: 00:00
Selection error: 1.74567
Epoch 100;
Parameters norm: 71.7788
Training loss: 1.58365
Batch size: 1000
Gradient norm: 0.125481
Learning rate: 0.001
Elapsed time: 00:06
Selection error: 1.72079
Epoch 200;
Parameters norm: 71.7787
Training loss: 1.57907
Batch size: 1000
Gradient norm: 0.127909
Learning rate: 0.001
Elapsed time: 00:12
Selection error: 1.72104
```

Result



```
Epoch 1000: Maximum number of iterations reached.
Parameters norm: 71.7785
Training loss: 1.57135
Batch size: 1000
Gradient norm: 0.000392563
Learning rate: 0.001
Elapsed time: 01:02
Selection error: 1.73463
```

Multi-variate Regression

Boston House
Price

- Testing Analysis

```
// Testing analysis

TestingAnalysis testing_analysis(&neural_network, &data_set);
cout<<endl<<"Testing Analysis"<<endl;
Vector< double > TestError=testing_analysis.calculate_testing_errors();
cout<<"Sum Squared error   : "<<TestError[0]<<endl;
cout<<"Mean Squared error    : "<<TestError[1]<<endl;
cout<<"Root Mean Squared error : "<<TestError[2]<<endl;
cout<<"Normalized Squared error : "<<TestError[3]<<endl;

const TestingAnalysis::LinearRegressionAnalysis linear_regression_results = testing_analysis.perform_linear_regression_analysis()[0];
cout << "Linear Regression analysis"<<endl;
cout<<"Correlation      : " << linear_regression_results.correlation << endl;
```

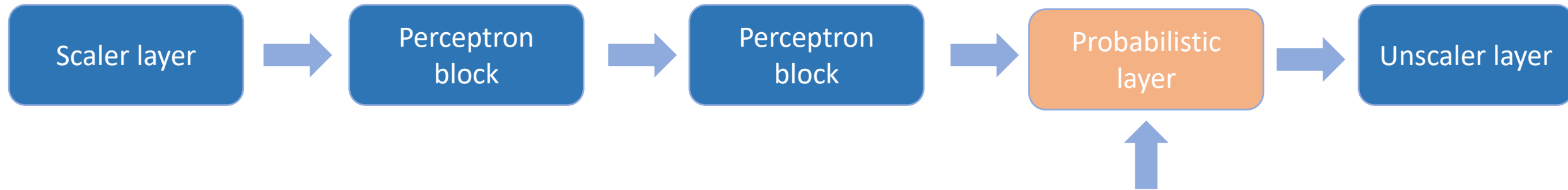


Result

```
Testing Analysis
Sum Squared error   :165.998
Mean Squared error    :1.64354
Root Mean Squared error :1.28201
Normalized Squared error :10.7843
Linear Regression analysis
Correlation      : 1
```


Multi-Classification

Iris dataset



```
ProbabilisticLayer* probabilistic_layer = new ProbabilisticLayer(perceptron_layer_1_outputs, outputs_number);  
probabilistic_layer->set_activation_function(ProbabilisticLayer::ActivationFunction::Softmax);
```

Result

```
Testing Analysis  
Confusion:  
11 0 0  
0 5 4  
0 10 0
```


Binary Classification

Banknote
Authentication

- Pre-Defined Model

```
// Neural network
NeuralNetwork neural_network(NeuralNetwork::Classification, {8, 6, 1});

// Scaling layer

ScalingLayer* scaling_layer_pointer = neural_network.get_scaling_layer_pointer();
scaling_layer_pointer->set_descriptives(inputs_descriptives);
scaling_layer_pointer->set_scaling_methods(ScalingLayer::NoScaling);
```

- ModelSelection Class

```
Performing Incremental neurons selection...
Training with adaptive moment estimator "Adam" ...
Epoch 0;
Training loss: 948.911
Elapsed time: 00:00
Epoch 100;
Training loss: 883.742
Elapsed time: 00:00
Epoch 200;
Training loss: 814.099
Elapsed time: 00:00
Epoch 300;
Training loss: 748.546
Elapsed time: 00:00
Epoch 400;
```

Selection



```
Algorithm finished.
Iteration: 10
Hidden neurons number: 10
Training loss: 59.2315
Selection error: 20.4083
Elapsed time: 01:18

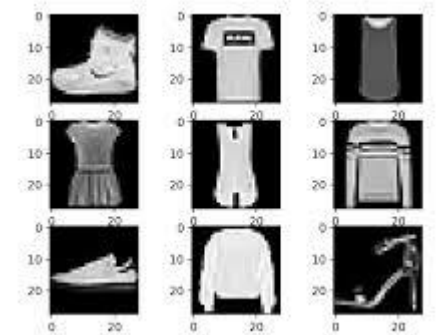
Optimal order: 6
Optimum selection error: 19.1846
Corresponding training loss: 58.6166
```

Result

```
Test Analysis
Confusion:
65 61
2 146
Binary classification tests:
Classification accuracy      : 0.770073
Error rate                   : 0.229927
Sensitivity                   : 0.515873
Specificity                   : 0.986486
Precision                     : 0.970149
Positive likelihood           : 38.1746
Negative likelihood           : 2.03766
F1 score                      : 0.673575
False positive rate           : 0.0135135
False discovery rate          : 0.0298507
False negative rate           : 0.484127
Negative predictive value     : 0.705314
Matthews correlation coefficient: 0.582516
Informedness                  : 0.50236
Markedness                    : 0.956636
```


Image Classification

Fashion
M-NIST



Convolutional block

Fully connected layer

Convolution
layer

Pooling Layer

Perceptron
layer

```
// Convolutional Block
ConvolutionalLayer* convolutional_layer_3 = new ConvolutionalLayer(pooling_layer_2_outputs_dimensions, {2, 3, 3});
neural_network.add_layer(convolutional_layer_3);

const Vector<size_t> convolutional_layer_3_outputs_dimensions = convolutional_layer_3->get_outputs_dimensions();

PoolingLayer* pooling_layer_3 = new PoolingLayer(convolutional_layer_3_outputs_dimensions);
neural_network.add_layer(pooling_layer_3);

const Vector<size_t> pooling_layer_3_outputs_dimensions = pooling_layer_3->get_outputs_dimensions();

// Fully connected layer: Dense layer with number input equal to flatten
PerceptronLayer* perceptron_layer = new PerceptronLayer(pooling_layer_3_outputs_dimensions.calculate_product(), 18);
neural_network.add_layer(perceptron_layer);
```

Result

```
Epoch 11;
Parameters norm: 105.436
Training loss: 1.31657
Batch size: 5
Gradient norm: 0.0465498
Learning rate: 0.001
Elapsed time: 03:31
Selection error: 0.860875
Epoch 12: Maximum number of iterations reached.
Parameters norm: 105.436
Training loss: 1.30501
Batch size: 5
Gradient norm: 0.0285116
Learning rate: 0.001
Elapsed time: 03:49
Selection error: 0.890203
```

Confusion matrix:

```
0 0 0 0 0 0 0 2 0 0
0 0 0 0 0 0 0 0 0 0
0 0 1 0 0 0 0 0 0 0
0 0 0 0 0 0 0 0 0 0
0 0 1 0 0 0 0 1 0 0
0 0 2 0 0 0 0 0 0 0
0 0 2 0 0 0 0 1 0 0
0 0 0 0 0 0 0 0 0 1
0 0 1 0 0 0 0 0 0 0
0 0 0 0 0 0 0 1 0 0
```

Accuracy: 7.69231 %

Problem: Data loading -> Time Consuming

Comparison



OpenNN

data class

NeuralNetwork class
TrainingStrategy class
ModelSelection class

TestingAnalysis class



Tensorflow

Dataset class

model class



model.compile()

model.fit()



It's more complete
(layers, applications...)

Test

Multivariate Regression	Test error/R2 score	Time elapsed
OpenNN	1,64\$/1	62s
Tensorflow	11,85\$/0,87	14,6s

LSTM	R2 score	Time elapsed
OpenNN	44,96%	75s
Tensorflow	<0	71s

Image Classification	Test accuaracy/data used	Reading time elapsed
OpenNN	7,69%/125	Several minutes
Tensorflow	63,11%/60000	3,47s

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